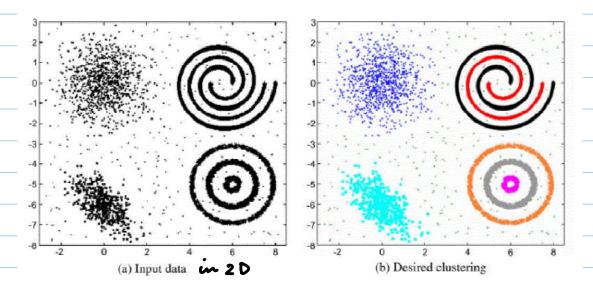
Clustering = Unsupervied Learning LECTURE 19 & unlabeled data

Note Title

* Why Data Clustering?



From: A.K. Jain, "Data clustering: 50 years beyond K-means,"

<u>Pattern Recognition Letters</u>, vol. 31, pp. 651-666, 2010.

· Underlying structure: to gain insight into data, generate hypotheses, detect anomalies, and identify salient features.

· Natural classification: to identify the degree of similarity among forms or organisms (phylogenetic relationship).

· Compression: as a method for organizing the data and summarizing it through cluster prototypes.

* The K-Means Algorithm

- Most popular
- Simplest
- Still being used after all these years and after hundreds of clustering algorithms were proposed.
- Est up

 Let X = { X 1, ..., X n },

 X j ∈ IR^d, 1 ≤ j ≤ n

 Suppose we want to cluster (group)

 Them into a set of K clusters,

 C = { C 1, ..., C K }, 1 < K ≪ n.

 Each C j contains some data vectors

 in X.
- · K-means algorithm finds a partition s.t. the squared error between the empirical mean of a cluster and the points in the cluster is minimized. More precisely, let $\mu_k := the$ mean of cluster C_k and define

$$J(C_{R}) := \sum_{\substack{\text{X}j \in C_{R} \\ \text{and}}} \| X_{j} - \mu_{R} \|^{2}$$
and
$$J(C) := \sum_{\substack{\text{X}j \in C_{R} \\ \text{A}}} J(C_{R})$$

K-means tries to find a partition (clustering) C s.t. J(C) -> min.

· This minimization problem is known to be NP-hand (non-deterministic polynomial-time hand, i.e., at least as hand as any NP problem, e.g. might require the exhaustive search or trials)

· Hence, the result of the K-means may be just a local minimum, not necessarily the global minimum of J(C)

• J(C) always decreases if K increases. In fact, if K=n, then J(C)=0! So, we should fix K as $I < K \ll n$.

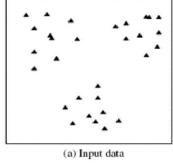
Here one the main steps of the K-means algorithm.

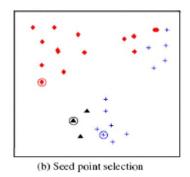
<u>Step1</u>: Select an initial partition with K clusters; repeat Steps 2 & 3 until cluster membership stabilizes

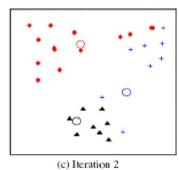
Step 2: Generate a new partition by assigning each point (vector) to its closest cluster center.

Step 3: Compute new cluster centers.

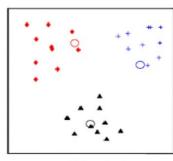
K-means in action!

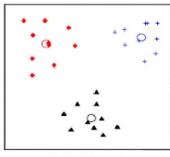






Both from A.K.Jain: paper

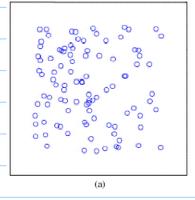


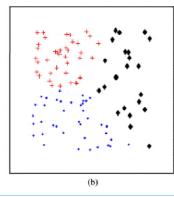


(d) Iteration 3

(e) Final clustering

Problems of the K-means Alg.
 How to preset K?





K=3 سے

- The computed clusters are just local minimum of J(C).

3) one option would be to run the K-means algorithm (with fixed K) several times, and pick the best one.

Two MATLAB Demonstrations

(1) Breast Concer Data set from

UC Irvine Machine Learning Repository

d = 9, n = 683 (after removing

patients of some

measurements based missing measurements)

on cytological images of breast cells

including: clump thickness; uniformity of

cell size; uniformity of cell shape; etc.

Out of 683 subjects, 444: benign

239: malignant

Suppose we do not know these diagnostic results, and use the K-means alg.

with K = 2 on this data matrix

X \in IR 9×683. Can we classify

benign & malignant cells correctly?

binarize a face image.

Here d=1 (pixel value), $n=128^2$ (# of pixels)

also K=2.

We can also use K=3,4,5,...to see how the image looks like after

replacing the true pixel values by the

cluster center values.