

Circuit Theory

- ① Deals with Voltage (V) & Current (I).
- ② V & I are scalars
- ③ V & I are produced from E & H
- ④ V & I are functions of time
- ⑤ Cannot be applied in free space (Radiation effects are neglected)
- ⑥ Basic Laws are Ohms Law, Kirchhoff's Law
- ⑦ Basic Theorems are Thevenin's, Norton's, Reciprocity, Superposition, MPT Theorems.

Field Theory ①

Deals with Electric Field (E) & Magnetic Field (H).

\vec{E} & \vec{H} are Vectors.

E & H are produced from V & I .

E & H are functions of time & space

(x, y, z) (or) (ρ, ϕ, z) (or) (r, θ, ϕ) .

Applicable in free space. (Radiation effects are considered)

Coulomb's Law, Gauss Law, Amperes Circuital Law.

Reciprocity, Helmholtz, Stokes, Divergence & Poynting Theorems.

Electromagnetics \rightarrow Study of fields & waves. ⁽²⁾

\vec{E}

- ① $\vec{E} \rightarrow$ Electric field Intensity
Electric Field
E - Field
Electric field strength
Unit \rightarrow V/m (or) Newton/C.
(Belongs to Voltage)

\vec{D}

- ② $\vec{D} \rightarrow$ Electric Flux Density
Electric Displacement Vector
Electric charge Density
 \rightarrow D - Field.

Unit \rightarrow Coulomb/m²
C/m²

Gauss law :-

Surface Integral of Electric flux density = Charge enclosed by the surface

$$\oint_S \vec{D} \cdot d\vec{s} = Q.$$

\vec{H}

- $\vec{H} \rightarrow$ Magnetic field Intensity.
 \rightarrow Magnetic Field
 \rightarrow H - Field
 \rightarrow Magnetic Field strength
Unit \rightarrow A/m.
(Belongs to Current).

\vec{B}

- $\vec{B} \rightarrow$ Magnetic Flux Density.
 \rightarrow Magnetic Displacement Vector.
 \rightarrow Magnetic charge Density
 \rightarrow B - Field.

Unit \rightarrow Weber/m² (or)
A/m². Tesla.

$$\oint_S \vec{B} \cdot d\vec{s} = 0.$$

$$\vec{E}$$

$$\textcircled{3} \quad \vec{D} = \epsilon_e E.$$

$\epsilon_e \rightarrow$ Total permittivity of the medium.

$$\epsilon_e = \epsilon_0 \epsilon_r.$$

\downarrow Permittivity in free space. \downarrow Relative permittivity of the medium.

$$8.854 \times 10^{-12} \text{ Fd/m.}$$

$\textcircled{4}$ Capacitance
Capacitance/unit length.

5. $Q \rightarrow$ Charge.
Unit \rightarrow Coulomb.

$\psi \rightarrow$ Electric flux
(or)
Electric charge
Unit \rightarrow Coulomb.

6. $Q = C \cdot V.$

7 EMF unit \rightarrow Volts.

$$\vec{H}$$

$\textcircled{3}$

$$\vec{B} = \mu \vec{H}$$

$\mu \rightarrow$ Total permeability of the medium.

$$\mu = \mu_0 \mu_r$$

\downarrow $4\pi \times 10^{-7} \text{ H/m.}$
 \downarrow Henry.

Inductance

Inductance/unit length.

$\phi \rightarrow$ Magnetic Flux
Unit \rightarrow Weber.

$$\phi = L I.$$

{ If more than one turns
then use $\Lambda = N\phi$ }
 \downarrow
 No. of Turns.
 MMF unit \rightarrow Amp Turns

(4)

 \vec{E} Electric Field Intensity (V/m)

$$\frac{C}{m}$$

$$\frac{C}{m^2}$$

$$\frac{C}{m^3}$$

↓
Line Charge
Density↓
Surface Charge
Density.↓
Volume charge
density. \vec{H} Magnetic Field Intensity (A/m)

$$\frac{A}{m}$$

$$\frac{A}{m^2}$$

$$\frac{A}{m^3}$$

↓
Line Current
Density↓
Surface Current
Density↓
Volume
Current
Density.Power Density & Energy DensityPower Density \rightarrow Power / Unit surface area
(W/m^2)

$$\vec{P} = \vec{E} \times \vec{H}$$

$$= \frac{V}{m} \times \frac{A}{m} = \frac{VA}{m^2} = \frac{W}{m^2}$$

 \rightarrow power flow thro' plane (or) area. \rightarrow It is a Scalar Quantity.

[Related Vector Quantity is Poynting Vector]

Energy Density \rightarrow Energy / Unit volume $\Rightarrow (J/m^3)$ \rightarrow Energy flow through Volume.

[illegible]

1. $E \rightarrow V = \oint E \cdot dl \quad V/m$
Electric field Intensity.

2. $\underset{\text{Electric Flux Density}}{D} \longrightarrow \psi_e = \iint_S D \cdot d\mathbf{s} \quad \text{C/m}^2.$

3. $\int_V \rho_v \rightarrow Q = \iiint_V \rho_v \cdot dv$ Coulomb/m³.
Total charge Volume

4. $H \longrightarrow I = \oint H \cdot dl$ Amp/m.
Magnetic Field Intensity

5. $B \longrightarrow \Psi_m = \iint_S B \cdot ds \text{ Wb/m}^2$
Magnetic flux density

6. $\mathbf{J} \longrightarrow \mathbf{I} = \iint_S \mathbf{J} \cdot d\mathbf{s} \quad \text{Amp/m}^2$

$\mathbf{J}_d \rightarrow$ Displacement Current Density $\left(\frac{\partial \mathbf{D}}{\partial t}\right)$
&
 $\mathbf{J}_c \rightarrow$ Conduction Current Density
[Current Density]

(i) Line charge distribution

(b)

$$Q = \int \rho_l \cdot dl \rightarrow \text{Wire Antenna.}$$

(ii) Surface charge distribution.

$$Q = \iint \rho_s ds \rightarrow \text{plate (or) sheet.}$$

(iii) Volume charge distribution.

$$Q = \iiint \rho_v \cdot dv. \rightarrow \text{Parabolic Antenna.}$$

Three Constitutive relations in Field Theory
Analysis :-

$$\vec{D} = \epsilon_e \vec{E} \rightarrow (1)$$

Electric flux density

$$\vec{B} = \mu \vec{H} \rightarrow (2)$$

Magnetic flux Density

$$\vec{J} = \sigma \vec{E} \rightarrow (3)$$

Current density, \vec{J}

① Dot product of two Vectors is a 7
Scalar Quantity.

$$\vec{A} = A_x \hat{i} + A_y \hat{j} + A_z \hat{k}.$$

$$\vec{B} = B_x \hat{i} + B_y \hat{j} + B_z \hat{k}.$$

$$\gamma = \vec{A} \cdot \vec{B} = |\vec{A}| \cdot |\vec{B}| \cdot \cos \theta.$$

$$\boxed{\gamma = A_x B_x + A_y B_y + A_z B_z}.$$

② Cross product of two Vectors is a
Vector Quantity.

$$\vec{A} = A_x \hat{i} + A_y \hat{j} + A_z \hat{k}$$

$$\vec{B} = B_x \hat{i} + B_y \hat{j} + B_z \hat{k}.$$

$$\vec{\gamma} = \vec{A} \times \vec{B} = |\vec{A}| \cdot |\vec{B}| \cdot \sin(\theta) \cdot \hat{n}.$$

↓
Resultant Direction

$$\Rightarrow \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ A_x & A_y & A_z \\ B_x & B_y & B_z \end{vmatrix}$$

$$\Rightarrow \hat{i}(A_y B_z - B_y A_z) - \hat{j}(A_x B_z - A_z B_x) + \hat{k}(A_x B_y - A_y B_x).$$

Dot Product :-

⑧.

$$1. \vec{A} \cdot \vec{B} = \vec{B} \cdot \vec{A}.$$

$$2. \vec{i} \cdot \vec{i} = \vec{j} \cdot \vec{j} = \vec{k} \cdot \vec{k} = 1.$$

$$3. \vec{i} \cdot \vec{j} = \vec{j} \cdot \vec{k} = \vec{k} \cdot \vec{i} = 0.$$

Cross Product :-

$$1. \vec{A} \times \vec{B} \neq \vec{B} \times \vec{A}.$$

$$2. \vec{A} \times \vec{B} = -\vec{B} \times \vec{A}.$$

$$3. \vec{i} \times \vec{i} = \vec{j} \times \vec{j} = \vec{k} \times \vec{k} = 0.$$

$$4. \begin{array}{l} \vec{i} \times \vec{j} = \vec{k} \\ \vec{j} \times \vec{k} = \vec{i} \\ \vec{k} \times \vec{i} = \vec{j} \end{array} \quad \parallel \quad \begin{array}{l} \vec{j} \times \vec{i} = -\vec{k} \\ \vec{k} \times \vec{j} = -\vec{i} \\ \vec{i} \times \vec{k} = -\vec{j} \end{array}$$