NAT-1 RANDOM VARIABLES

Randon Variables:

a real valued function defined on the authorne of a probability experiment is called a random variable. Fx:
15 Tossing a Gin

Ex: U) TOSSING fair Coin

S= { H, T}

(ii) Throwing a fair die. 2) Tossing 2 coins Simultaneously

S= { HH, HT, TH, TT}

A Random variable is the rule that assigns a numerical value to each possible outcome of an experiment.

- 1) Discorete Random Variable
- ii) Continuous Random variable.

1) Discrete Random Variables: (countable)

A random variable whose set of possible values is either finite countably infinite is called discrete random variable.

Ex.: i) The number of Student in a class

- ii) The number of traffic accidents.
- ii) The number of Telephone Calls.

Probability mass function: (Pmp) P(x)

If x is a discrete random variable

P(x) = P[x=x] is called the probability mass

function, provided P(x); satisfy the following conditions.

- i) P(x) >0 (10) 0< P(x)<1
- in Z(PCX) =1

* Cumulataive distribution function (cdf) (distrete R.v)

The cumulative distribution function F(x) of a discrete random variable x with probability distribution por is given by

F(x)= P(X < x) = 2 P 26 KX

* Mean (or) Expected value of a Pandom Variable x.

mean E(n)= Zx.P(x)

* Variance:

Variance Var(x) = E(x2) - [E(x)] $E(\chi^2) = \mathcal{D}_{\chi^2} P(\chi)$

Proporties of distribution for: -

n F (-0) =0

ii) = (00) = 1

lin D(x) >0

 $P(x_1 \leq x \leq x_2) = F(x_2) - F(x_1).$ 140

Results:

PC X < 300) = 1 112

(\$P) P(X < -8) =0

liis $P(x>x) = 1 - P(x \leq x)$

147 P(x < x) = 1 - P(x > x)

Formula:

mean ECM) = Exp(xe) Vi) P(A/B) = P(ANB) 1) E(x2)= Zx(2p(x)) Cli P(B)

cni Variance Var(x) = E(x²) -[E(x)] **ÌV**>

E(ax+b) = a E(x)+bV>

Var [axtb] = a2 var[x] ٧) Standard deviation(S.D)= V var (x) = 6. 1. A random Variable x has the following Probability distribution

DC: -2 -1 0 1 2 3
PCOO: 011 K 0.2 2K 0.3 3K

a) Find K b) Evaluate P(x<2) and P(-2<2<2)

soln:

a) To find K

W.K.T ZPCRD =1

0.1 + K +0.2 +2k+0.3 +3K =1

6K+0.6 =1 => 6K= 1-0.6 = 0.4

 $K = \frac{0.4}{6} = \frac{4}{60} = \frac{1}{15}$ $K = X_5$

The probability distribution is

2: -2 -1 0 1 2 3

P(X=x): (6.1/2) 1/5 1/5 2/15 3/10 1/5

b) To find P(x<2) & P(-2< x<2)

P(x < 2) = P(x = 1) + P(x = 0) + P(x = -1) + P(x = -2)

 $P(x < 2) = \frac{2}{15} + \frac{1}{5} + \frac{1}{15} + \frac{1}{10} = \frac{4+6+2+3}{30} = \frac{15}{30} = \frac{1}{2}$

P(-2<x)<2) = P(x=4)+P(x=0)+P(x=1)

 $=\frac{1}{15} + \frac{1}{5} + \frac{2}{15} = \frac{1+3+2}{15} = \frac{6}{15} = \frac{2}{5/1}$

c) To find Cdf of x: = EFCX)

4) To find mean:

mean
$$E(x) = \sum_{10}^{10} P(30)$$

$$= (-2 \times \frac{1}{10}) + (-1 \times \frac{1}{15}) + (0 \times \frac{1}{5}) + (1 \times \frac{1}{15}) + (2 \times \frac{3}{10}) + (3 \times \frac{1}{5})$$

$$= \frac{1}{15} + \frac{1}{15} + 0 + \frac{2}{15} + \frac{2}{15} + \frac{3}{15} + \frac{3}{15}$$

$$= \frac{-3 - 1 + 2 + 9 + 9}{15} = \frac{16}{15}$$

Hw

1. The discrete random variable x has the probability distribution given by

Find (i) k (ii) mean (iii) variounce (iv) var(3x-4)

v) P(0<2<3/2/1).

```
(3)
                Variable x has the following Poolshilty
2) A random
  distribution
                              3 4 5 6 7
                          2
    of 1
                    K 2K 2K 3K K2 2K2 7K7K
  Find a) The Value of K (b) P(1.5< x < 4.5)/x>2)
  soln! Evaluate P(x<6), P(x>6)
     a) Find K:
        W.K.T ZP(28)=1
          0 + K + 2K + 2K + 3K + K^{2} + 7K^{2} + K = 1
10K^{2} + 9K - 1 = 0
10K^{2} + 9K - 1 = 0
2a
               -9 ± \81-4(10)(-1)
              K = -\frac{9 \pm \sqrt{121}}{20} = \frac{-9 \pm 11}{20} = \frac{21}{20} - \frac{1}{20}
             K=1/10 (01)-1
            PCX)70 the value k=-1 is not permissible.
                      2 3 4 5 6 7
      X
            0 10 20 20 10 100 100 100
       P(A/B) = \frac{P(ANB)}{P(B)}
        P(1.5 < x < 4.5)/xx) = P(x=2) + P(x=3) + P(x=4)/n(P(x=3) + P(x=4)) + P(x=5) + P(x=6) + P(x=7)
                                           P(x>2)
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P(x=4) + P(x=5) + P(x=6) + P(x=7) P(x>2) = P(x=3) + P(x=4) P(x=3) + P(x=4) + P(x=6) + P(x=6) + P(x=7) $= \frac{2}{10} + \frac{3}{10}$ $\frac{2}{10} + \frac{3}{10} + \frac{1}{100} + \frac{2}{100} + \frac{17}{100}$ $\frac{2}{100} + \frac{3}{100} + \frac{1}{100} + \frac{2}{100} + \frac{17}{100}$

$$P(1.52x<4.5|x>2) = \frac{5}{10}$$

$$\frac{7\phi}{10\phi} = \frac{5}{7}$$
c) To find the smallest value of λ which $P(x \le \lambda) > \frac{1}{2}$.

by trails
$$P(x \le 0) = 0$$

 $P(x \le 1) = 0 + \frac{1}{0} = \frac{3}{0}$
 $P(x \le 2) = \frac{1}{0} + \frac{2}{10} = \frac{3}{10}$
 $P(x \le 3) = \frac{3}{10} + \frac{2}{10} = \frac{5}{10} = \frac{2}{10}$
 $P(x \le 4) = \frac{1}{2} + \frac{3}{10} = \frac{8}{10} = \frac{3}{10}$

The Smallest value of a satisfying the Condition $P(x \le \lambda) > \frac{1}{2}$ is $\frac{4}{\lambda}$

d) To Find P(X<6) & P(X>6)

$$P(x \ge 6) = P(x=6) + P(x=7) = \frac{2}{100} + \frac{17}{100} = \frac{19}{100}$$

$$P(x < 6) = 1 - P(x > 6)$$

$$P(x < 6) = 1 - \frac{19}{100} = \frac{81}{100}$$

$$P(x < 6) = 1 - \frac{19}{100} = \frac{81}{100}$$

1. A discrete R.V x has the following probability distribution

9t: 0 1 2 3 4 5 6 7 8 P(20: a 3a 5a 7a 9a 11a 13a 15a 17a.

Find the value of a, P(xc3), variance and distribution function of x.

$$F(0) = \frac{1}{81}$$
 $F(1) = \frac{4}{81}$, $F(2) = \frac{9}{81}$, $F(3) = \frac{16}{81}$, $F(4) = \frac{25}{81}$
 $F(5) = \frac{36}{81}$ $F(6) = \frac{44}{81}$ $F(7) = \frac{44}{91}$ | $F(8) = 1$

3) If the Probability mass function of a R.V
$$\times$$
 is given by $P(x=0) = k v^3$; $v=1,2,3,4$ find (1) the value of k is $P(k < x < 5/2)(x > 1)$ with the mean and variance of k with the distribution function of x .

Given
$$p(x=v)=kv^3$$

The probability distribution is given by $X : 1 2 3 4$
 $p(v): k 8k 27k 64k$

(i) To Find
$$K!$$
 -

We know that $\sum P(xp) = 1$
 $k+8k+27k+64k=1$
 $100k=1$

$$\frac{\text{Cli) To Find P}\left(\frac{1}{2} < x < \frac{5}{2} / x > 1\right)}{P\left(\frac{1}{2} < x < \frac{5}{2} / x > 1\right) = \frac{P(5 < x < \frac{5}{2} \cap x > 1)}{P(x > 1)} = \frac{P(A | B)}{P(x = 2)}$$

$$= P(x = 2)$$

$$P(x=2)+P(x=3)+P(x=4)$$
=\frac{8k,}{8k+27k+64k} = \frac{8k}{99k}

P(\frac{1}{2}\leq \times \left(\frac{1}{2}\left(\times)\right) = \frac{8}{99}

$$X$$
: 1 2 3 4 $P(X)$: $\frac{1}{100}$ $\frac{8}{100}$ $\frac{27}{100}$ $\frac{64}{100}$

$$E(x) = \sum_{i} x_{i}^{2} P(x_{i}^{2}) = \frac{1 + 16 + 81 + 256}{100} + \frac{3(\frac{27}{100}) + 4(\frac{64}{100})}{100} = \frac{3.54}{100} = \frac{3.54}{100} = \frac{3.54}{100} = \frac{3.54}{100} = \frac{1 + 32 + 243 + 1024}{100} = \frac{13.00}{100}$$

$$E(x^{2}) = 13$$

$$Var(x) = E(x^2) - [E(x)]^2$$
= 13 - (3.54)^2 = 13 - 12.5316 = 0.4684

: mean(n)= 3.54 & variance= 0.4684

iv) to find the distribution for of x:

$$F(x) = P(x \le x)$$

$$F(x) = P(x)$$

$$F(x) = P(x$$

If the random variables x takes the values 1/2/3 and 4 such that 2P(x=1)=3p(x=2)=p(x=3)= Find the probability distribution and curroutative distribution function of x.

* is a discrete random Variable

given
$$2p(x=1)=3p(x=2)=p(x=3)=p(x=4)$$

lef $2P(x=1) = 3P(x=2) = P(x=3) = 5P(x=4) = k - x_0$

980m (2P(x=1)= $k \Rightarrow P(x=1)=\frac{1}{2}$; 3P(x=2)=k P(x=3)=k; $5P(x=4)=k \Rightarrow P(x=2)=\frac{1}{2}$; 2e: ! 1 2 3 4

 $P(80: \frac{K}{2} \frac{K}{3} \times \frac{K}{5}$

Neknow that $\Sigma P(3i)=1$ $\frac{K}{2} + \frac{K}{3} + K + \frac{K}{5} = 1$

 $\frac{15K+10K+30K+6K}{30}=1$

 $\frac{61k}{36} = 1 \Rightarrow \left[k = \frac{30}{61} \right]$

The Probability distribution is

ot: 1 2 3 4

P(x): 15 10 30 6 61 61

To Find commention distribution function of x:

25	P(25)	F(x)
1	15	F(1)=15 61
2	61	$F(0) = \frac{15}{61} + \frac{10}{61} = \frac{25}{61}$
3	30 G1	$F(3) = \frac{25}{61} + \frac{30}{61} = \frac{55}{61}$
4	61	$F(A) = \frac{55}{61} + \frac{6}{61} = \frac{61}{61} = 1$

The probability function of an infinite discrete distribution is given by $P(x=j) = \frac{1}{2}$; j=1/2,3....Find the mean and variance of the distribution. Also find P(x takeren), P[x > 5] and P[x is divisible by 3]. 9iven $P(x=\hat{j}) = \frac{1}{0^{3}} \hat{j} \hat{j} = 1, 2 \cdots \infty$

(i) To find Mean & Variance: -

Mean =
$$\frac{3}{5}$$
 $37 + 2(\frac{1}{2})^2 + 3(\frac{1}{2})^3 + \cdots$
= $\frac{1}{5} \left[1 + 2(\frac{1}{2})^4 + 3(\frac{1}{2})^2 + \cdots \right]$

Vav [x] = E [x2] - [E [x]]2

$$E(x^2) = \sum_{j=1}^{\infty} 2r_j^2 P(2r_j) = \sum_{j=1}^{\infty} (2r_j^2) (2r_j + 1) P(2r_j^2) = \sum_{j=1}^{\infty} 2r_j^2 P(2r_j^2)$$

$$E(x^{2}) = \left[(1)(2)(\frac{1}{2}) + (2)(3)(\frac{1}{2})^{2} + (3)(4)(\frac{1}{2})^{3} + \cdots \right] - 2$$

$$= \left(\frac{1}{2} \right) \left[(1)(2) + 2 \cdot 3(\frac{1}{2}) + 3 \cdot 4 \cdot (\frac{1}{2})^{2} + \cdots \right] - 2$$

$$= \left(\frac{1}{2} \right) \left[(1)(2)(\frac{1}{2}) + 2 \cdot 3(\frac{1}{2}) + 3 \cdot 4 \cdot (\frac{1}{2})^{2} + \cdots \right] - 2$$

$$=\frac{-3}{(1-\frac{1}{2})-2}$$

$$=(\frac{1}{2})^{-3}-2=2^{-2}=8-2=6$$

$$(1-3) = \frac{1}{2} (1.2 + 2.3 + 3.4 +$$

(Formula.

 $(1-3)^{\frac{1}{2}}=1+2x+3x^{2}+$

(1-x)=1/2(1.2+2.3 x+3.4. (1-25)=1+2+27+23+

$$Var(x) = E(x^2) - [E(x)]^2$$

= 6-(2)^2 = 6-4=2

li) To Find
$$P(x+x)=$$

$$P(x \text{ is even}) = P[x=2] + P[x=4] + P[x=6] + \cdots$$

$$P(x \mid s \text{ even}) = (\frac{1}{2})^{2} + (\frac{1}{2})^{4} + (\frac{1}{2})^{6} + \dots$$

$$= (\frac{1}{4}) + (\frac{1}{4})^{2} + (\frac{1}{4})^{3} + \dots$$

$$= (1 - \frac{1}{4})^{-1}$$

$$= (\frac{3}{4})^{-1} - 1 = \frac{4}{3} - 1 = \frac{1}{3}$$

$$P(x = i) = \frac{1}{2^{3}}$$

$$= (\frac{3}{4})^{-1} - 1 = \frac{4}{3} - 1 = \frac{1}{3}$$

B

(:M+x2+x3+-- = (1-8)-1)

iii) To find P[x>5]:

$$P[x>5] = P[x=5] + P[x=6] + P[x=7] + \cdots$$

$$= (\frac{1}{2})^{5} + (\frac{1}{2})^{6} + (\frac{1}{2})^{7} + \cdots$$

$$= (\frac{1}{2})^{5} [1+(\frac{1}{2})+(\frac{1}{2})^{7} + \cdots]$$

$$= (\frac{1}{2})^{5} [1-\frac{1}{2}]^{-1}$$

$$= (\frac{1}{2})^{5} [(1-\frac{1}{2})^{-1}]$$

$$= \left(\frac{1}{2}\right)^5 \left[\frac{1}{2}\right]^1 = \left(\frac{1}{2}\right)^5 \times 2 = \frac{1}{24} = \frac{1}{16}$$

iv) To Find P[x is divisible by 3 (or) P(x) is multiple of 2]

$$= \left(\frac{1}{2}\right)^{3} + \left(\frac{1}{2}\right)^{6} + \left(\frac{1}{2}\right)^{9} + \dots$$

$$= \left(\frac{1}{8}\right) + \left(\frac{1}{8}\right)^2 + \left(\frac{1}{2}\right)^3 + \cdots + \left(\frac{1}{(1-x^2)}\right) = 1 + x + x^2 + \cdots$$

$$= (1 - \frac{1}{8})^{-1} = \frac{8}{7} - 1 = \frac{1}{7}$$

Continuous Random Variables

Defn: A random variable x is said to be Continuous if it takes all possible values between Certain limits say from a to real number b'. Ex: height, weight, time.

Probability density function: (P.d.4)

For a continuous random variable x, a probability density function is such that

in \$ (20) >0
ii) \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ = 1

Concelative distribution functions (cd.f):-

The cumulative distribution function of a continuous random variable x is

 $F(x) = P(x \le x) = \int_{x}^{x} f(x) dx f(x) - x < x < x.$

Mean (or) Expected value of a C.R.V x: -

Let x be a Continuous bandom Variable with P.d. 4 '4' is defined in (-0,0) then expected value of x is defined as

 $E(x) = \int_{-\infty}^{\infty} x f(x) dx$.

(ECX)=X=M)

Variance of C.R.V (x'):- [Note:

Note: $Var(x) = E(x) - [E(x)]^{Q}$ $Var(x) = [E(x)]^{$ Note: If x is continuous R.y then

A continuous R.V x that can assume any value between x=2 and x=5 his a density for given by f(x) = k(1+2t). Find P[x<4].

Soln: given for = K(1+30 or & x=2 & 21 = 5.

Welknow that \$\int \partial \partial \tau = 1 \\
-\infty

$$\int K(1+2r)dx = 1$$

$$2$$

$$K \left[2x + \frac{2^{2}}{2}\right]_{2}^{5} = 1$$

$$K \left(5 + \frac{25}{2} - 2 - \frac{2}{2}\right) = 1$$

$$K \left(1 + \frac{25}{2}\right) = 1$$

$$K \left(\frac{27}{2}\right) = 1$$

$$K \left(\frac{27}{2}\right) = 1$$

$$K \left(\frac{27}{2}\right) = 1$$

(i) To Find P[x=4]; ... \$(20)=2 (1+20) & 20=22'
27 (1+20) & 20=22'

$$P[x < 43] = \int_{2}^{4} \frac{1}{27} (1+24) dx$$

$$= \frac{9}{27} \left[x + \frac{x^{2}}{2} \right]^{4}$$

$$= \frac{2}{27} \left[4 + \frac{16}{2} + 2 - \frac{27}{2} \right]$$

$$P[XZH] = \frac{16}{27}$$

2) The Pidit of a riv x is $\varphi(x) = kx$, $o \in x < 1$, find k and P(x > 0.5).

Soln:= given from = kee; 0 < x < 1

i) To find K :-

Ne know that
$$\int_{-\infty}^{\infty} f(x) dx = 1$$

$$\int_{-\infty}^{1} kx dx = 1$$

$$k \left[\frac{2}{2} \right]_{0}^{1} = 1 \implies k = 1 \implies [k=2]$$

: f(x)=2x; oxx<1

(iii) To find
$$P[x>0.5]$$
:

$$P[x>0.5] = \int_{0.5}^{291} 4\pi$$

$$= 2 \left[\frac{x^2}{2} \right]_{0.5}^{0.5} = 1 - 0.25 = 0.75$$

A Continuous RV x has a pd. $p(x) = kx^2 e^{2x}$; and variance.

Schot-

Given $p(x) = kx^2 e^{2x}$; and

into find k :

$$= k x^2 e^{-2x} dx = 1$$

$$= k x^2 e^{-2x} dx = 1$$

(i) $p(x) = kx^2 e^{-2x}$; and p

: Mean
$$E(x)=3$$

 $= \frac{1}{2} \times 3! = \frac{1}{2} \times 188 \times 3 = 3$

 $\int_{0}^{3} x^{5d} e^{3d} dx = 15$

ii) to find Variance:

$$=\int_{0}^{\infty} g e^{2} \left(\frac{1}{2} x^{2} e^{2x}\right) dx$$

$$=\frac{1}{2}\times4!=\frac{1}{2}\times1\times2\times3\times4$$

$$= 12 - 3^2 = 12 - 9 = \frac{3}{2}$$

4) A Continuous R.V x has a p.d. & from=32

, OCX<1 . Find as b such that

(i) P[X < a] = P[X > a] (ii) P[X > b] = 0.05

$$=\int 3\pi dn = 1$$

$$\Rightarrow 3\left[\frac{3}{3}\right]^{\alpha} = \frac{1}{2}$$

$$a^2 = k_2$$
 $a = (k_2)^2$

$$\frac{p_3}{2} = 1 - 0.02 = 0.00$$

P[x=J=/2)

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In a Continuous R.V the p.d. is given by $f(80) = k \propto (2-8c)$, 0 < 2 < 2. Find k, mean , variance and the distribution for.

F(x)= 1 [3x2-x3] When O ≤ x ≤ 2 & F(X)=1;

The diameter of an electric cable x is a continuous r.v with p.d.7 fcon= Kor (1-80); 0 < 24 < 1.

1) Find the Value of K.

ii) C.al. 7 04 x.

in the value of a such that P[x<a]=2p[x>a]
iv, P[xx\[x<\frac{2}{3}]:

Soln:- given fin= kx(1-x); osas!

we know that I for doc=1

 $\int K \Re(1-\pi) d\pi = 1$

 $K\left[\frac{3^2}{2} - \frac{3^2}{3}\right] = 1$

K[1/2-1/3]=1

 $\left\{ \begin{bmatrix} \frac{3-2}{6} \end{bmatrix} = 1 \right\} \left[\begin{array}{c} K = 6 \end{array} \right]$ $\left\{ \begin{bmatrix} \frac{1}{6} \end{bmatrix} = 1 \right\} \left[\begin{array}{c} f(x) = 6 \end{array} \right]$

: f(x)=6 x (1-x); 05x51

11) To find cumulative distribution for 69 x =-

(+) of xxx, F(x) =0 ; when x <0

FOND = I from doc.

F(20) = 5°6 (Dr (1-20)) doc = 6 5 0c-203dx $= 6 \left[\frac{3^2}{2} - \frac{3^3}{3} \right]^2 = 6 \left[\frac{3^2 - 2^3}{6} \right]^2$ $F(30) = 3x^2 - 230^3$ when $0 \le x \le 1$

FCX) =1 ishen or>1

P[x<a] = 2[P[x>a)] riin

P[x<a]= 2 P[x>a]

 $\int_{-\infty}^{\infty} \varphi(x) dx = \frac{1}{2} \int_{-\infty}^{\infty} \varphi(x) dx$

6 S & (1-8) dx = : 2x6 & (1-2) dze | f(x)=62-92+2

 $\left[\frac{\chi^2}{2} - \frac{\chi^3}{2}\right]^{\alpha} = \left[\frac{2}{2} - \frac{\chi^2}{2} - \frac{\chi^2}{2}\right]^{\alpha}$

 $3a^2 - 2a^3 = 2[(3-2) - (3a^2 - 2a^3)]$

 $3a^{2}-2a^{3}=[2\cdot(1)-8a^{2}+4a^{3}]$ $1x^{2}-2a^{3}+2a^{2}-6a^{2}+2a^{3}-6a^{2}+2=0.$

62-92-12=0

L Ma Botason a 01

ni) To find P[xeh/6<xc%]:

$$P(A/B) = \frac{P(A/B)}{P(B)}$$

$$= \frac{P(X \le \frac{1}{2}) \cdot 0 \cdot (\frac{1}{2} \times \frac{1}{2})}{P(\frac{1}{2} \times \frac{1}{2})} = \frac{P(\frac{1}{2} \times \frac{1}{2})}{P(\frac$$

If the density function of a confinceous random Variable x is given by

$$f(x) = \begin{cases} ax & 0 \leq x \leq 1 \\ a & 1 \leq x \leq 2 \\ 3a - x x & 2 \leq x \leq 3 \end{cases}$$
o otherwise

a) find the value of a and b) find the c.d.f ofx.

€ P[x>1.5].

Soln: a) To find a: - as

Sinct Cass is p.d. & Syconolar = 1

$$\int_{0}^{3} 4(x) dx = 1$$

$$\int_{0}^{2} ax dx + \int_{0}^{2} adx + \int_{0}^{3} (3a - ax) dx = 1$$

 $a \left[\frac{x^2}{2}\right]_0^1 + a \left[se\right]_1^2 + \left[sax - a\frac{x^2}{2}\right]_0^3 = 1$

 $\frac{9}{2} + a(2-1) + 3a(3) - a(9/2) - 6a + a(9/2) = 1$

9 +a +9a - 9a +6a +2a =1

a+99-69+20+(-90+0)=1

a+99-60+29-40=1

b) To find the c.d. φ of x:-

 $2a = 1 \Rightarrow \boxed{a = 16}$ $2a = 1 \Rightarrow \boxed{a = 16}$ $2a = 1 \Rightarrow \boxed{2}; 0 \le x \le 1$ $2 : 1 \le x \le 2$ $3 = \frac{x}{2}; 2 \le x \le 3$

 $F(x) = P[x \le x] = \int_{-\infty}^{\infty} f(x) dx$

(i) If x(0 then F(x)=0

(ii) If $0 \le x \le 1$ then F(x) = 0 $\frac{x}{2} dx = 1 \left[\frac{x^2}{2} \right]^3 = \frac{x^2}{4}$

ii) If
$$1 \le n \le 2$$
 then $F(n) = \int_{-\infty}^{\infty} f(x) dx$

$$= \int_{-\infty}^{\infty} \frac{1}{2} dx + \int_{-\frac{1}{2}}^{\frac{1}{2}} dx$$

$$= \left[\frac{n^2}{4}\right]_0^1 + \frac{1}{2} \left[x^{-1}\right] = \frac{1}{4} + \frac{1}{2} x - \frac{1}{2}$$

$$= \frac{1}{4} + \frac{1}{2} \left[x^{-1}\right] = \frac{1}{4} + \frac{1}{2} x - \frac{1}{2}$$

$$= \int_{-\frac{1}{2}}^{\infty} \frac{1}{2} dx + \int_{-\frac{1}{2}}^{\infty} \frac{1}{2}$$

C)
$$P[x > 1.5] = \int_{1.5}^{3} \varphi(x) dx$$

$$= \int_{1.5}^{2} \frac{1}{2} dx + \int_{2}^{3} \frac{3}{2} - \frac{x}{2} dx$$

$$= \frac{1}{2} \left[2r \right]_{1.5}^{2} + \left[\frac{3}{2} x - \frac{x}{4} \right]_{2}^{3}$$

$$= \frac{1}{2} \left[2 - 1.5 \right] + \frac{3}{2} \cdot 3 - 9 \cdot 4 - \frac{3}{2} \cdot (2) + \frac{4}{4}$$

$$= \frac{1}{2} \left(\frac{1}{2} \right) + \frac{9}{2} - 9 \cdot 4 - 3 + 1$$

$$= \frac{1}{4} + \frac{18 - 9}{4} - 2$$

$$= \frac{10 - 8}{4} = \frac{2}{4} = \frac{12}{4}$$

1) × is a continuous random variable with pidit given by from= kor in osorso = 2k in 25 or 4 and = 6R-Kx in 45086. Find the Value of Rand Floo.

F(x)=0 when aco

$$F(x) = \frac{x^2}{16} \text{ when } 0 \leq 87 \leq 2$$

$$F(x) = \frac{1}{4} (at-1)$$
 when $2 \le at \le 4$

$$P(x) = \frac{-1}{16}(20-122+3+^2)$$
 when $4 \le x \le 6$