Reg. No.							

B.Tech. DEGREE EXAMINATION, NOVEMBER 2019

Third Semester

18ECC104T - SIGNALS AND SYSTEMS

(For the candidates admitted during the academic year 2018-2019 onwards)

Note:

- Part A should be answered in OMR sheet within first 45 minutes and OMR sheet should be handed (i) over to hall invigilator at the end of 45th minute.
- Part B and Part C should be answered in answer booklet. (ii)

Time: Three Hours

Max. Marks: 100

$PART - A (20 \times 1 = 20 Marks)$

Answer ALL Questions

- 1. Which of the following is a periodic signal?
 - (A) x(t) = Au(t)

(B) $x(t) = Ae^{-jbt}$

(C) $x(t) = Ae^{bt}$

- (D) x(t) = At
- 2. The differentiation of a unit step signal is
 - (A) Ramp signal

(B) Impulse signal

(C) Exponential signal

- (D) Parabolic signal
- 3. Identify the energy signal from the following signals
 - (A) $x(t) = Ae^{j\Omega_0 t}$

(B) $x(t) = A \sin \Omega_0 t$

(C) $x(t) = B\cos\Omega_0 t$

- (D) $x(t) = e^{-at}u(t)$
- 4. Which of the following is a non-causal system?
 - $y(t) = \frac{dx(t)}{dt}$

 $y(t) = \int_{0}^{t} x(\tau) d\tau$ (D) $y(t) = x(t^{2})$

(C) $y(t) = e^{x(t)}$

- 5. For waveforms with odd symmetry, the Fourier coefficients a_0 and a_n are always
 - (A) Zero

(B) One

(C) Two

- (D) Infinity
- 6. If a signal x(t) has odd and half wave symmetry, then the Fourier series will have
 - (A) Odd harmonics of sine terms
- (B) Even harmonics of sine terms
- (C) Constant term and odd harmonics of (D) Odd harmonics of cosine terms cosine terms
- 7. The Fourier transform for x(t) exists only if

(C) $\int_{0}^{\infty} x(t)dt < \infty$ $\int_{0}^{\infty} x(t)e^{j\Omega t}dt < \infty$

8.	The Fourier transform	of the	signal	x(t)	$=e^{7t}u$	(-t)	is
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(A)
$$\frac{1}{7+j\Omega}$$

(B)
$$\frac{7}{1+j\Omega}$$

(C)
$$\frac{7}{1-j\Omega}$$

(D)
$$\frac{1}{7-i\Omega}$$

9. The convolution of u(t) with u(t) is equal to

(A)
$$s(t)$$

(B)
$$u(t)$$

(C)
$$tu(t)$$

(D)
$$t^2u(t)$$

10. If x(t), y(t) and h(t) are input, output and impulse response of LTI continuous time system respectively then

(A)
$$h(t) = x(t) * y(t)$$

(B)
$$x(t) = y(t) * h(t)$$

(C)
$$y(t) = x(t) * h(t)$$

(D)
$$y(t) = h(t) * h(t)$$

11. The Laplace transform of the causal signal $t^n u(t)$ is

(A)
$$\frac{n!}{s^n+1}$$

(B)
$$n!$$

(C)
$$\frac{n}{s^n + 1}$$

(B)
$$\frac{n!}{s^n}$$
(D) $\frac{n}{s^n}$

The inverse Laplace transform of $X(s) = \frac{2}{s^2 + 2s + 5}$ is

(A)
$$x(t) = e^{-t} \cos 2t$$

(B)
$$x(t) = e^{-t} \sin 2t$$

(C)
$$x(t) = e^{-t} \cos 5t$$

(D)
$$x(t) = e^{-2t} \sin 5t$$

13. If $x(n) = a^n u(n)$ is the input signal, then the particular solution $y_p(n)$ will be

(A)
$$K^n a^n u(n)$$

(B)
$$Ka^nu(n)$$

(C)
$$K_1 a^n u(n) + K_2 a^n u(n)$$

(D)
$$Ka^{-n}u(n)$$

14. The zero input or natural response is mainly due to

- (A) Initial stored energy in the system
- (B) Present conditions in the system

(C) Specific input signal

(D) Specific output signal

15. In N-point DFT of L-point sequence, the value of N to avoid aliasing in frequency spectrum

$$(A) \quad N \neq L$$

(B)
$$N \leq L$$

(C)
$$N \ge L$$

(D)
$$N = L$$

16. The inverse DFT of x(n) can be expressed as

(A)
$$x(n) = \frac{1}{N} \sum_{K=0}^{N} X(k) e^{\frac{-j2\pi kn}{N}}$$

(B)
$$\frac{1}{N} \sum_{k=0}^{N-1} X(k) e^{\frac{j2\pi kn}{N}}$$

(C)
$$\frac{1}{N} \sum_{n=0}^{N-1} X(n) e^{\frac{-j2\pi kn}{N}}$$

(B)
$$\frac{1}{N} \sum_{K=0}^{N-1} X(k) e^{\frac{j2\pi kn}{N}}$$
(D)
$$N \sum_{n=0}^{N-1} X(k) e^{\frac{-j2\pi kn}{N}}$$

- 17. The ROC of the sequence x(n) = u(-n) is
 - (A) |Z| > 1

(B) |Z| < 1

(C) No ROC

- (D) -1 < |Z| < 1
- 18. Inverse Z-transform of $\frac{3}{Z-4}$ |Z| > 4 is
 - (A) $3(4)^n u(n-1)$

(B) $3(4)^{n-1}u(n)$

(C) $3(4)^{n-1}u(n+1)$

- (D) $3(4)^{n-1}u(n-1)$
- 19. The structure that uses separate delays for the input and output samples is
 - (A) Direct form II

(B) Direct form I

(C) Cascade form

- (D) Parallel form
- 20. Number of multipliers and adders required for direct form realization of Nth order FIR system are
 - (A) N, N+1

(B) N, N-1

(C) N+1, N

(D) N-1, N+1

PART - B (5 × 4 = 20 Marks) Answer ANY FIVE Questions

- 21. Sketch the given signal and calculate its energy $x(t) = e^{-10t}u(t)$
- 22. Find the inverse Fourier transform of the following signals
 - (i) $\delta(\Omega)$
 - (ii) $\delta(\Omega-\Omega_0)$
- 23. Find the Laplace transform of the signal and find ROC $x(t) = e^{-3t}u(t) + e^{-2t}u(t)$
- 24. Find the convolution of the following signals.

$$x(n) = \cos \pi n u(n); h(n) = \left(\frac{1}{2}\right)^n u(n)$$

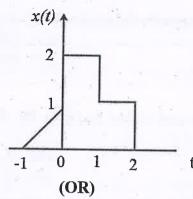
- 25. Determine the Z transform of the signal $x(n) = -b^n u(-n-1)$. Find the region of convergence.
- 26. Find the odd and even components of the signal $x(n) = \{-2, 1, 2, -1, 3\}$
- 27. What are the properties of region of convergence?

$PART - C (5 \times 12 = 60 Marks)$

Answer ALL Questions

28. a. For the signal x(t) shown below, find the following

- x(t-2)(i)
- x(2t+3)(ii)
- (iii)
- (iv)



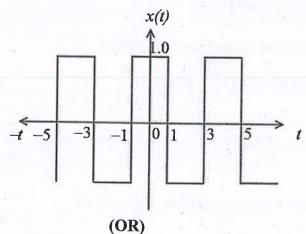
b. Check whether the following systems are

- Static/Dynamic (i)
- (ii) Linear/Non Linear
- Causal/Non Causal (iii)
- (iv) Time Invariant/ Time Variant

(1)
$$y(t)\frac{d^2y(t)}{dt^2} + \frac{3tdy(t)}{dt} + y(t) = x(t)$$

- (2) y(n) = x(n)x(n-1)(3) $y(n) = \cos[x(n)]$

29. a. Find the trigonometric Fourier series for the periodic signal shown below



b. State and derive the following properties of Fourier transform

- (i) Convolution theorem
- (ii) Differentiation in time
- (iii) Parseval's energy theorem

30. a. Determine the complete response of the system described by the equation $\frac{d^2y(t)}{dt^2} + 4\frac{dy(t)}{dt} + 4y(t) = \frac{dx(t)}{dt} + x(t) \text{ when the initial conditions are } y(0^+) = \frac{9}{4};$ $\frac{dy(0^+)}{dt} = 5 \text{ and when the input is } e^{-3t}u(t).$

(OR)

- b.i. List the steps for convolution of 2 signals using graphical method.
- ii. Find the convolution of the following signals using graphical method $x(t) = e^{-2t}u(t)$; h(t) = u(t+2)
- 31. a. For the given system y(n)-1.5y(n-1)+0.5y(n-2)=x(n) with initial conditions y(-1)=1, y(-2)=0. Find the response due to input signal $x(n)=2^nu(n)$.

(OR)

b.i. State and prove the circular time shifting property of DFT.

(4 Marks)

- ii. Using concentric circle method find the circular convolution of the sequences $x_1(n) = \left\{1, -1, 2, 3\right\}, x_2(n) = \left\{0, 1, 2, 3\right\}.$ Verify the answer using matrix method. (8 Marks)
- 32. a. Using partial fraction method, find the inverse z-transform of the following

(i)
$$X(z) = \frac{\frac{1}{4}z^{-1}}{\left(1 - \frac{1}{2}z^{-1}\right)\left(1 - \frac{1}{4}z^{-1}\right)};$$
 ROC $|z| > \frac{1}{2}$

(ii)
$$X(z) = \frac{1}{1-z^{-1}+z^{-2}};$$
 ROC $|z| > 1$

(OR)

b. Obtain Direct form I and Direct form II realization for the system described by the difference equation $y(n) - \frac{5}{6}y(n-1) + \frac{1}{6}y(n-2) = x(n) + 2x(n-1)$

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