

8. The Fourier transform of the signal $x(t) = e^{7t}u(-t)$ is
- (A) $\frac{1}{7 + j\Omega}$ (B) $\frac{7}{1 + j\Omega}$
 (C) $\frac{7}{1 - j\Omega}$ (D) $\frac{1}{7 - j\Omega}$
9. The convolution of $u(t)$ with $u(t)$ is equal to
- (A) $s(t)$ (B) $u(t)$
 (C) $tu(t)$ (D) $t^2u(t)$
10. If $x(t)$, $y(t)$ and $h(t)$ are input, output and impulse response of LTI continuous time system respectively then
- (A) $h(t) = x(t) * y(t)$ (B) $x(t) = y(t) * h(t)$
 (C) $y(t) = x(t) * h(t)$ (D) $y(t) = h(t) * h(t)$
11. The Laplace transform of the causal signal $t^n u(t)$ is
- (A) $\frac{n!}{s^n + 1}$ (B) $\frac{n!}{s^n}$
 (C) $\frac{n}{s^n + 1}$ (D) $\frac{n}{s^n}$
12. The inverse Laplace transform of $X(s) = \frac{2}{s^2 + 2s + 5}$ is
- (A) $x(t) = e^{-t} \cos 2t$ (B) $x(t) = e^{-t} \sin 2t$
 (C) $x(t) = e^{-t} \cos 5t$ (D) $x(t) = e^{-2t} \sin 5t$
13. If $x(n) = a^n u(n)$ is the input signal, then the particular solution $y_p(n)$ will be
- (A) $K^n a^n u(n)$ (B) $K a^n u(n)$
 (C) $K_1 a^n u(n) + K_2 a^n u(n)$ (D) $K a^{-n} u(n)$
14. The zero input or natural response is mainly due to
- (A) Initial stored energy in the system (B) Present conditions in the system
 (C) Specific input signal (D) Specific output signal
15. In N-point DFT of L-point sequence, the value of N to avoid aliasing in frequency spectrum is
- (A) $N \neq L$ (B) $N \leq L$
 (C) $N \geq L$ (D) $N = L$
16. The inverse DFT of $x(n)$ can be expressed as
- (A) $x(n) = \frac{1}{N} \sum_{K=0}^{N-1} X(k) e^{\frac{-j2\pi kn}{N}}$ (B) $\frac{1}{N} \sum_{K=0}^{N-1} X(k) e^{\frac{j2\pi kn}{N}}$
 (C) $\frac{1}{N} \sum_{n=0}^{N-1} X(n) e^{\frac{-j2\pi kn}{N}}$ (D) $\frac{1}{N} \sum_{n=0}^{N-1} X(k) e^{\frac{-j2\pi kn}{N}}$

17. The ROC of the sequence $x(n) = u(-n)$ is
 (A) $|Z| > 1$ (B) $|Z| < 1$
 (C) No ROC (D) $-1 < |Z| < 1$
18. Inverse Z-transform of $\frac{3}{Z-4}$ $|Z| > 4$ is
 (A) $3(4)^n u(n-1)$ (B) $3(4)^{n-1} u(n)$
 (C) $3(4)^{n-1} u(n+1)$ (D) $3(4)^{n-1} u(n-1)$
19. The structure that uses separate delays for the input and output samples is
 (A) Direct form II (B) Direct form I
 (C) Cascade form (D) Parallel form
20. Number of multipliers and adders required for direct form realization of N^{th} order FIR system are
 (A) $N, N+1$ (B) $N, N-1$
 (C) $N+1, N$ (D) $N-1, N+1$

PART – B ($5 \times 4 = 20$ Marks)
 Answer ANY FIVE Questions

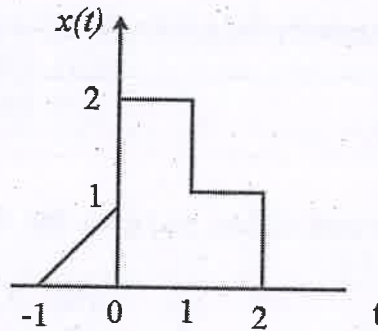
21. Sketch the given signal and calculate its energy
 $x(t) = e^{-10t} u(t)$
22. Find the inverse Fourier transform of the following signals
 (i) $\delta(\Omega)$
 (ii) $\delta(\Omega - \Omega_0)$
23. Find the Laplace transform of the signal and find ROC
 $x(t) = e^{-3t} u(t) + e^{-2t} u(t)$
24. Find the convolution of the following signals.
 $x(n) = \cos \pi n u(n); h(n) = \left(\frac{1}{2}\right)^n u(n)$
25. Determine the Z transform of the signal $x(n) = -b^n u(-n-1)$. Find the region of convergence.
26. Find the odd and even components of the signal
 $x(n) = \{-2, 1, 2, -1, 3\}$
27. What are the properties of region of convergence?

PART – C (5 × 12 = 60 Marks)

Answer **ALL** Questions

28. a. For the signal $x(t)$ shown below, find the following

- (i) $x(t-2)$
- (ii) $x(2t+3)$
- (iii) $x\left(\frac{3}{2}t\right)$
- (iv) $x(-t+1)$



(OR)

b. Check whether the following systems are

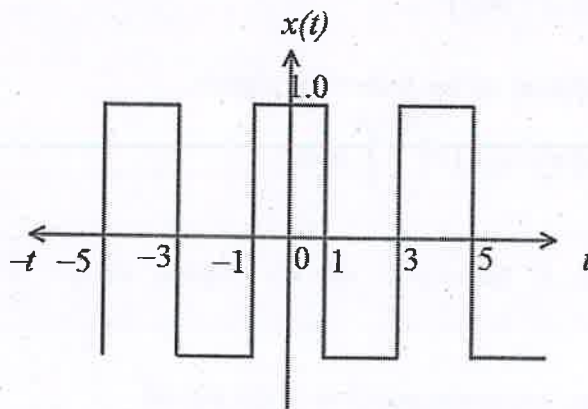
- (i) Static/Dynamic
- (ii) Linear/Non Linear
- (iii) Causal/Non Causal
- (iv) Time Invariant/ Time Variant

(1) $y(t) \frac{d^2 y(t)}{dt^2} + \frac{3t dy(t)}{dt} + y(t) = x(t)$

(2) $y(n) = x(n)x(n-1)$

(3) $y(n) = \cos[x(n)]$

29. a. Find the trigonometric Fourier series for the periodic signal shown below



(OR)

b. State and derive the following properties of Fourier transform

- (i) Convolution theorem
- (ii) Differentiation in time
- (iii) Parseval's energy theorem

30. a. Determine the complete response of the system described by the equation

$$\frac{d^2 y(t)}{dt^2} + 4 \frac{dy(t)}{dt} + 4y(t) = \frac{dx(t)}{dt} + x(t) \quad \text{when the initial conditions are } y(0^+) = \frac{9}{4};$$

$$\frac{dy(0^+)}{dt} = 5 \quad \text{and when the input is } e^{-3t}u(t).$$

(OR)

b.i. List the steps for convolution of 2 signals using graphical method.

ii. Find the convolution of the following signals using graphical method

$$x(t) = e^{-2t}u(t); h(t) = u(t+2)$$

31. a. For the given system $y(n) - 1.5y(n-1) + 0.5y(n-2) = x(n)$ with initial conditions $y(-1) = 1, y(-2) = 0$. Find the response due to input signal $x(n) = 2^n u(n)$.

(OR)

b.i. State and prove the circular time shifting property of DFT.

(4 Marks)

ii. Using concentric circle method find the circular convolution of the sequences

$$x_1(n) = \left\{ \underset{\uparrow}{1}, -1, 2, 3 \right\}, x_2(n) = \left\{ \underset{\uparrow}{0}, 1, 2, 3 \right\}. \quad \text{Verify the answer using matrix method.} \quad (8 \text{ Marks})$$

32. a. Using partial fraction method, find the inverse z-transform of the following

$$(i) \quad X(z) = \frac{\frac{1}{4}z^{-1}}{\left(1 - \frac{1}{2}z^{-1}\right)\left(1 - \frac{1}{4}z^{-1}\right)}; \quad \text{ROC } |z| > \frac{1}{2}$$

$$(ii) \quad X(z) = \frac{1}{1 - z^{-1} + z^{-2}}; \quad \text{ROC } |z| > 1$$

(OR)

b. Obtain Direct form I and Direct form II realization for the system described by the difference

$$\text{equation } y(n) - \frac{5}{6}y(n-1) + \frac{1}{6}y(n-2) = x(n) + 2x(n-1)$$

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