

AC Characteristics of op-amp :

→ The ac characteristic of op-amp are frequency response and slew rate.

Frequency response :

- The manner in which gain of the op-amp respond to different frequencies is called frequency response.
- A graph of the magnitude of gain (in dB) versus frequency is called frequency response.
- Ideally, an op-amp should have infinite bandwidth i.e., gain of op-amp remains same for frequencies.
- The practical op-amp gain decreases at higher frequencies (roll-off).
- The reason for gain roll-off is due to capacitive component (capacitance) present in the equivalent circuit of op-amp.
- The capacitance is due to the physical characteristics of the device (BJT or FET) used, and internal construction of op-amp.
- For an op-amp with only one break frequency, all the capacitor effect can be represented by single capacitor C .

→ There is one pole R_0C and one 20 dB/decade roll-off comes into effect.

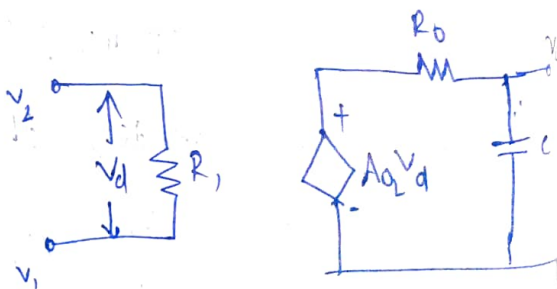


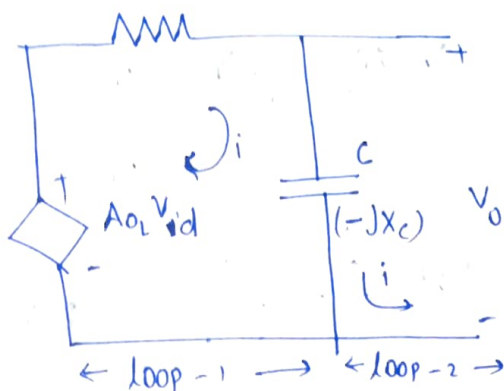
Fig. High frequency model of op-amp with single corner frequency.

Open loop voltage gain as a function of frequency

→ The reactance value of capacitance = $\frac{1}{2\pi f C} = X_c$

→ The impedance value of capacitance is $-jX_c$.

Applying KVL in loop-1



~~or~~ A_{OL}

$$-A_{OL} V_d + i R_O - jX_c i = 0$$

$$\Rightarrow i(R_O - jX_c) = A_{OL} V_d$$

$$\Rightarrow i = \frac{A_{OL} V_d}{R_O - jX_c}$$

Applying KVL in loop-2

$$V_O = -jX_c i \quad \text{--- (1)}$$

putting value of i in above equation

$$\Rightarrow V_O = -jX_c \cdot \frac{A_{OL} V_d}{R_O - jX_c} \quad \text{--- (2)}$$

As we know, $X_c = \frac{1}{2\pi f C} \Rightarrow -jX_c = \frac{1}{j2\pi f C}$

putting value of $-jX_c$ in eqn-2

$$V_O = \frac{1}{j2\pi f C} \cdot \frac{A_{OL} V_d}{R_O + \frac{1}{j2\pi f C}} = \frac{A_{OL} V_d}{R_O \cdot j2\pi f C + 1}$$

$$\therefore V_o = \frac{A_{OL} V_d}{R_o \cdot j2\pi f C + 1}$$

$$\text{voltage gain} = \frac{V_o}{V_d} = A = \frac{A_{OL}}{1 + R_o j2\pi f C} \quad \text{--- (3)}$$

Let $f_1 = \frac{1}{2\pi R_o C}$ putting this value in above equation

$$A(f) = \frac{A_{OL}}{1 + j\left(\frac{f}{f_1}\right)}$$

Here $A(f)$ = open loop voltage gain as function of frequency

A_{OL} = gain of op-amp at 0Hz

f = operating frequency

f_1 = break frequency or corner frequency,

$$\text{Magnitude of open loop gain} = |A(f)| = \frac{A_{OL}}{\sqrt{1 + \left(\frac{f}{f_1}\right)^2}}$$

$$\text{phase angle of open loop gain} = \phi(f) = -\tan^{-1}\left(\frac{f}{f_1}\right)$$

$$|A(f)| \text{ dB} = 20 \log |A(f)|$$

$$= 20 \log \left| \frac{A_{OL}}{\sqrt{1 + \left(\frac{f}{f_1}\right)^2}} \right|$$

$$\therefore |A(f)|_{dB} = 20 \log(A_{OL}) - 20 \log \left(\sqrt{1 + \left(\frac{f}{f_1}\right)^2} \right)$$

(i) When $f < f_1$, then $\left(\frac{f}{f_1}\right)^2 \ll 1$

so, $|A(f)|_{dB} = 20 \log(A_{OL})$

(ii) When $f = f_1$ then: $\left(\frac{f}{f_1}\right)^2 = 1$,

So, $|A(f)|_{dB} = 20 \log(A_{OL}) - 20 \log(\sqrt{2})$

So, -3 dB decrease.

(iii) 20 dB decrease/decade after corner frequency. ($f > f_1$)

$$\phi(f) = -\tan^{-1}\left(\frac{f}{f_1}\right)$$

If $f = 0 \Rightarrow \phi(f) = 0$

(ii) If $f = \infty \Rightarrow \phi(f) = -90^\circ$

(iii) If $f = f_1 \Rightarrow \phi(f) = -45^\circ$

→ The phase angle is zero at frequency $f = 0$.

→ At corner frequency, the phase angle is -45° & infinite frequency the phase angle is -90°

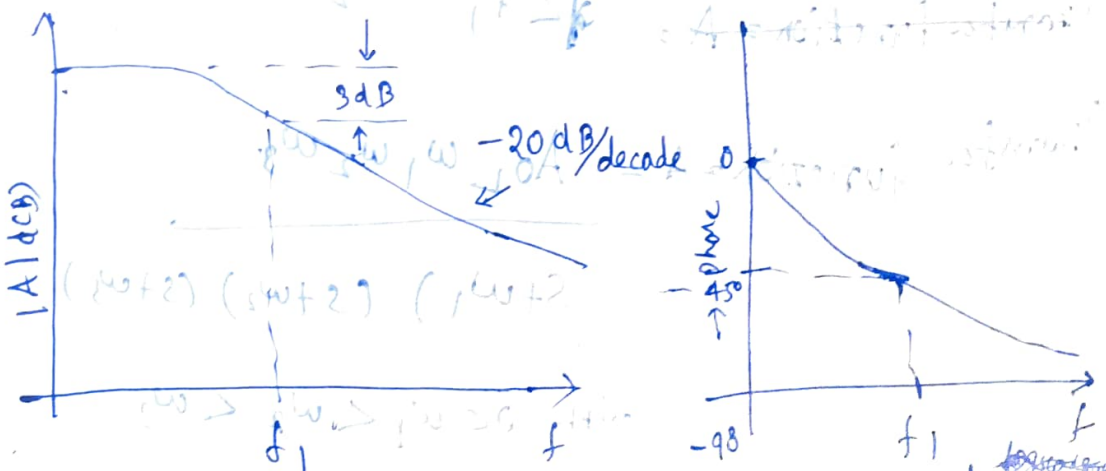


Fig. Open loop magnitude & phase characteristics for an op-amp with single-pole frequency response.

$$A(f) = \frac{A_{OL}}{1 + j\left(\frac{f}{f_1}\right)} = \frac{A_{OL}}{1 + j\left(\frac{\omega}{\omega_1}\right)}$$

→ The voltage transfer function in s-domain can be written as:

$$A(f) = \frac{A_{OL} \omega_1}{\omega_1 + j\omega} \quad \text{as } j\omega \approx s$$

$$A(f) = \frac{A_{OL} \omega_1}{\omega_1 + s}$$

→ A practical op-amp has number of stages and each stage produces a capacitive component. Thus there will be different frequencies due to number of RC pole pairs.

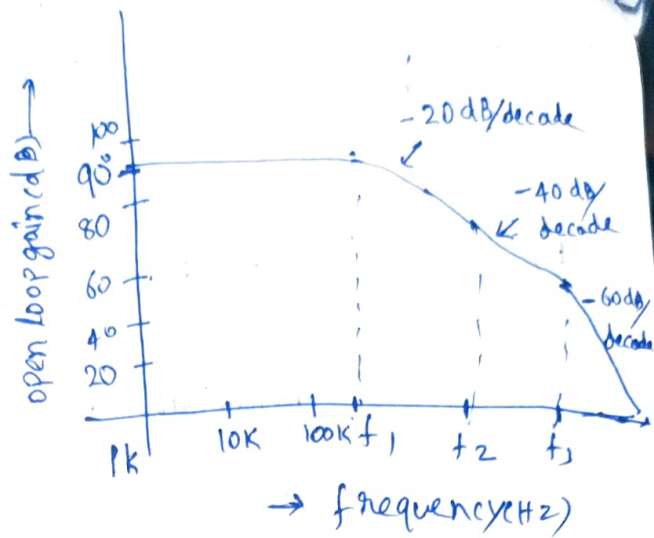
The transfer function of an op-amp with 3 break frequencies

$$A = \frac{A_{OL}}{\left(1 + j\frac{f}{f_1}\right) \left(1 + j\frac{f}{f_2}\right) \left(1 + j\frac{f}{f_3}\right)}$$

Transfer function = $A = \frac{A_{OL}}{\left(1 + j\frac{f}{f_1}\right) \left(1 + j\frac{f}{f_2}\right) \left(1 + j\frac{f}{f_3}\right)}$ with $0 < f_1 < f_2 < f_3$

Transfer function = $A = \frac{A_{OL} \omega_1 \omega_2 \omega_3}{(s + \omega_1)(s + \omega_2)(s + \omega_3)}$

with $0 < \omega_1 < \omega_2 < \omega_3$



Unity gain bandwidth

The frequency where op-amp gain equal to unity is called unity gain bandwidth.

$$\text{unity gain bandwidth} = B = \frac{0.35}{\text{rise time}}$$

$$\text{open loop at gain of } f = \frac{\text{bandwidth at unity gain}}{\text{input signal frequency}}$$

bandwidth of inverting or non-inverting

$$\text{amplifier} = f_H = \frac{B}{(R_f + R_i)/R_i}$$

Where B = unit gain bandwidth

R_f = feedback resistance

R_i = input resistance

140+ A 741 op-amp has a rise time of 0.35 μsec .

Find the small-signal or unity gain bandwidth.

(b) what is the open loop voltage gain of op-amp at 1 MHz?

(c) what is open-loop voltage gain at 100 kHz?

Ans: (a) Given rise time = 0.35 μ sec

$$B = \frac{0.35}{\text{rise time}} = \frac{0.35}{0.35 \mu\text{sec}} = 1 \text{ MHz}$$

(b) Open loop gain at 1 MHz = $\frac{1 \text{ MHz}}{1 \text{ MHz}} = 1$

bandwidth at unity gain
(maximum input signal frequency)

(c) open loop gain at 100 kHz = $\frac{1 \text{ MHz}}{100 \text{ kHz}} = 10$