

**Lab Semantic Data Web**



**Outlier Detection on Financial RDF Data**

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**Lab Project Report**

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## **1 Introduction:**

### **1.1 Motivation:**

The World Wide Web has enabled the creation of a global information space comprising linked documents. Linked Data provides a publishing paradigm in which not only documents, but also data, can be a first class citizen of the Web, thereby enabling the extension of the Web with a global data space based on open standards.

Growing of Semantic data Web and Linked Data technologies additional to development data mining methods in data sciences field, contribute in growing the role semantic data web in developing enterprise systems for many goals. The idea is to use the Linked Open Data Cloud for retrieving additional information on e.g. demographics or economics to enrich the data sets at hand before analyzing them. The project concentrates on financial data and detects outlier then compares the results. Certain data mining methods can be applied to these separate datasets (Financial data) to efficiently detect anomalies/outliers, and by the use of Semantic Web concepts, we can have even more accurate findings.

### **1.2 Project Purpose:**

Applying different methods to detect outliers and anomalies in financial RDF data and compare the results.

### **1.3 Definitions:**

#### **1.3.1 What is an outlier/anomaly?**

An anomaly is something that deviates from what is standard, normal, or expected

#### **1.3.2 Anomaly detection in data-mining**

In data mining, anomaly detection (outlier detection) is the identification of items, events or observations, which do not conform to an expected pattern or other items in a dataset.

#### **1.3.3 Outliers in financial data:**

An outlier may indicate bad data. For example, the data may have been coded incorrectly or an experiment may not have been run correctly. If it can be determined that an outlying point is in fact erroneous, then the outlying value should be deleted from the analysis (or corrected if possible).

## 2 Project Time plan:

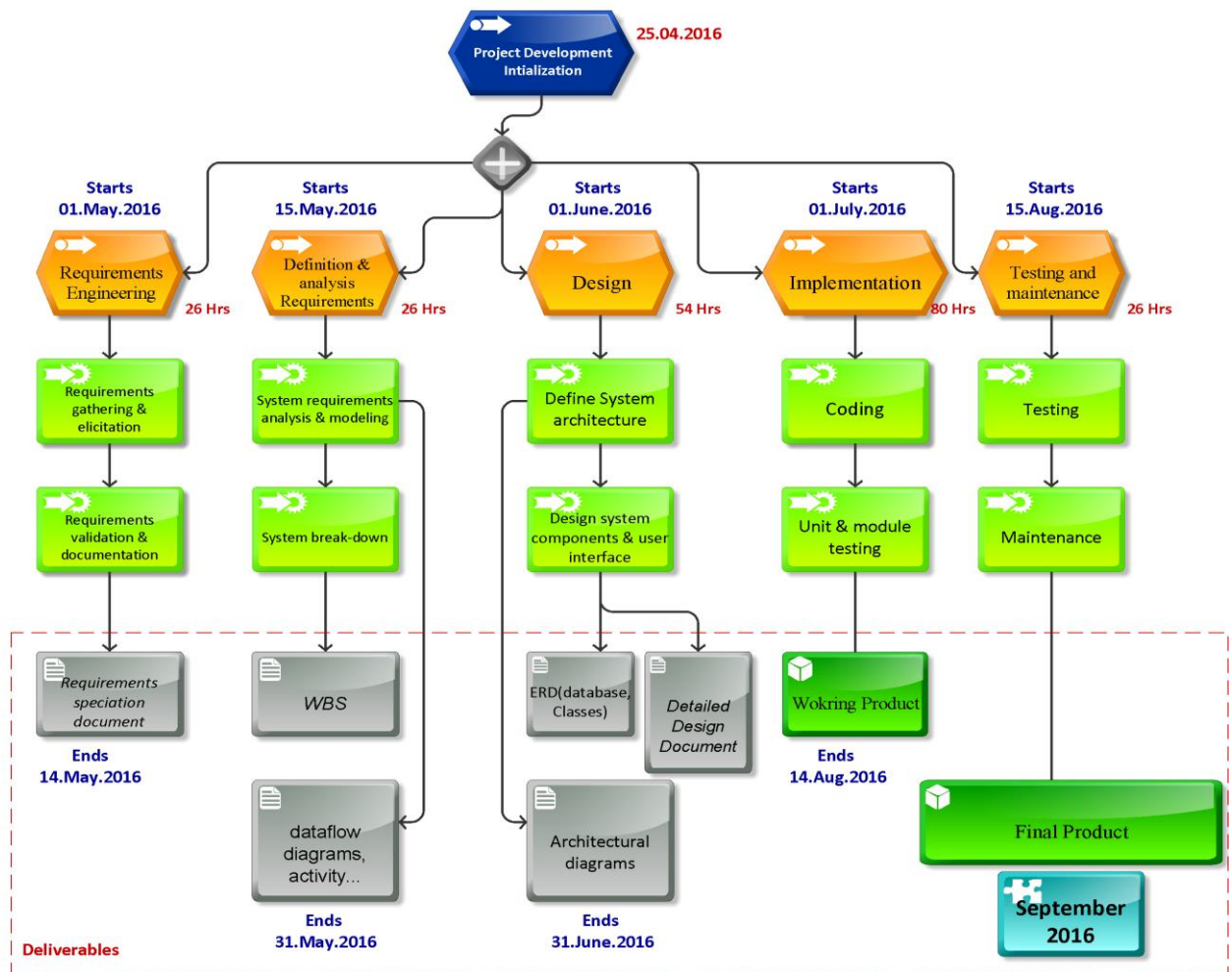


Figure 1 Time plan

### 3 System Requirements:

#### 3.1 Functional requirements:

ID	Name	Comments
FRQ - 1	The user shall import his/her RDF datasets	Datasets may be in XML/RDF format
FRQ - 2	The system shall Link local datasets to external dataset cloud	External dataset will be chose manually in financial field
FRQ - 3	The system shall apply and compare different data mining methods to detect outliers	Comparing aspects like accuracy and performance of the applied DM methods
FRQ - 4	The system shall provide reports on analyzed data	Reports may include: Comparison for DM methods Results visualization Explanations

#### 3.2 Technical Requirements:

The system shall be implemented using Java SE environment

- User interface: cross browser interface that runs on most web browsers (e.g. IE, Chrome, Firefox, Safari)
- Front end languages and technologies: HTML5/CSS3, JavaScript, JQuery library, AngularJS, Google Maps API
- Restful API for web services
- Tools to be used: Fuseki, Rapid miner and Apache Jena

##### 3.2.1 Fuseki:

Expose your triples as a SPARQL end-point accessible over HTTP. Fuseki provides REST-style interaction with your RDF data (Jena.apache.org, 2016).

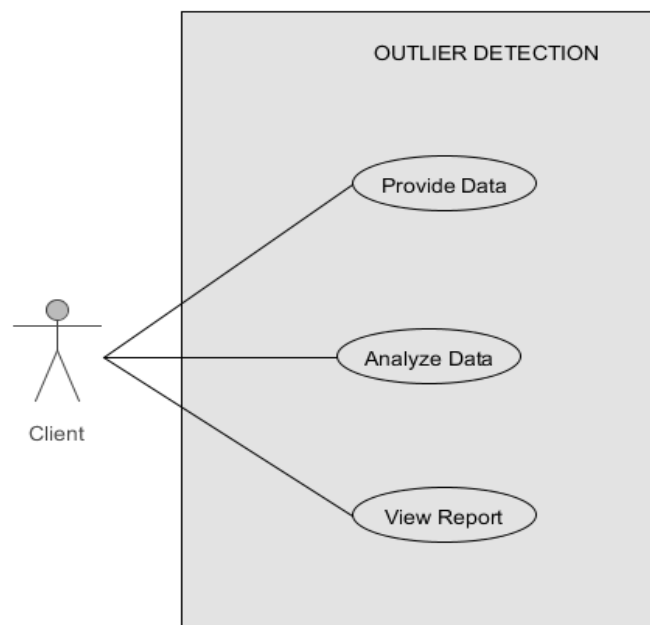
### 3.2.2 Apache Jena:

A free and open source Java framework for building Semantic Web and Linked Data applications (Jena.apache.org, 2016).

### 3.2.3 Rapid miner:

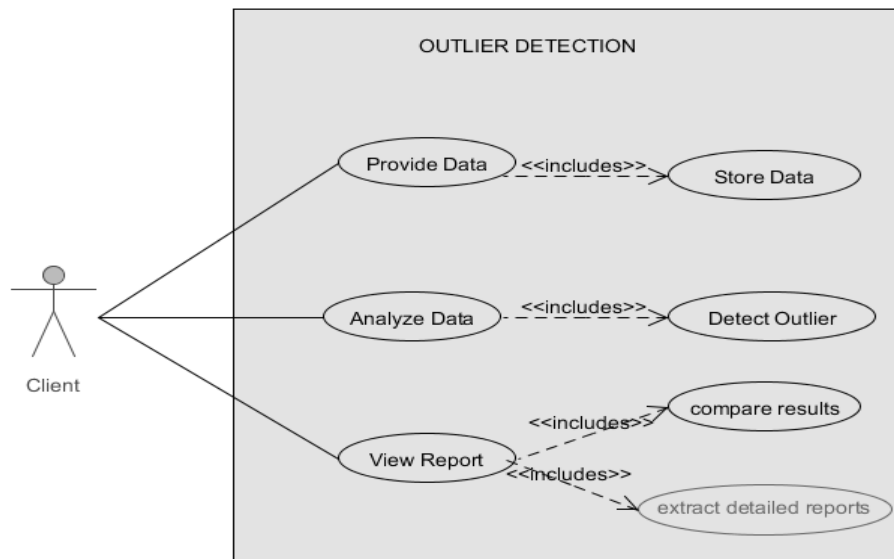
Open Source Predictive Analytics Prep data, create models, and embed in business processes  
Faster than ever before (Platform, 2016).

## 3.3 Use case:



**Figure 2 Use case Diagram Level 0**





**Figure 3** Use case Level 1

### 3.4 Non- functional requirements:

ID	Name	Comments
NRQ - 1	Reliability	The system should be able to perform the required functions under stated conditions for specific period.
NRQ - 2	Usability	The system has to give ease with which a user can learn to operate, Prepare inputs for, and interpret outputs of system. Additionally easy-to-use interfaces.
NRQ - 3	Capacity	The ability of the system to handle transactional volumes is a very important characteristic for a system

NRQ – 4	Performance	The system should consider the Processed transactions per second and Response time to user input and performance of the implemented DM methods
NRQ – 5	Open source	Source code made available with a license in which the copyright holder provides the rights to study, change, and distribute the software to anyone and for any purpose.
NRQ – 6	Quality	Quality of the outlier and detection methods for giving precise result.

#### 4 System architecture:

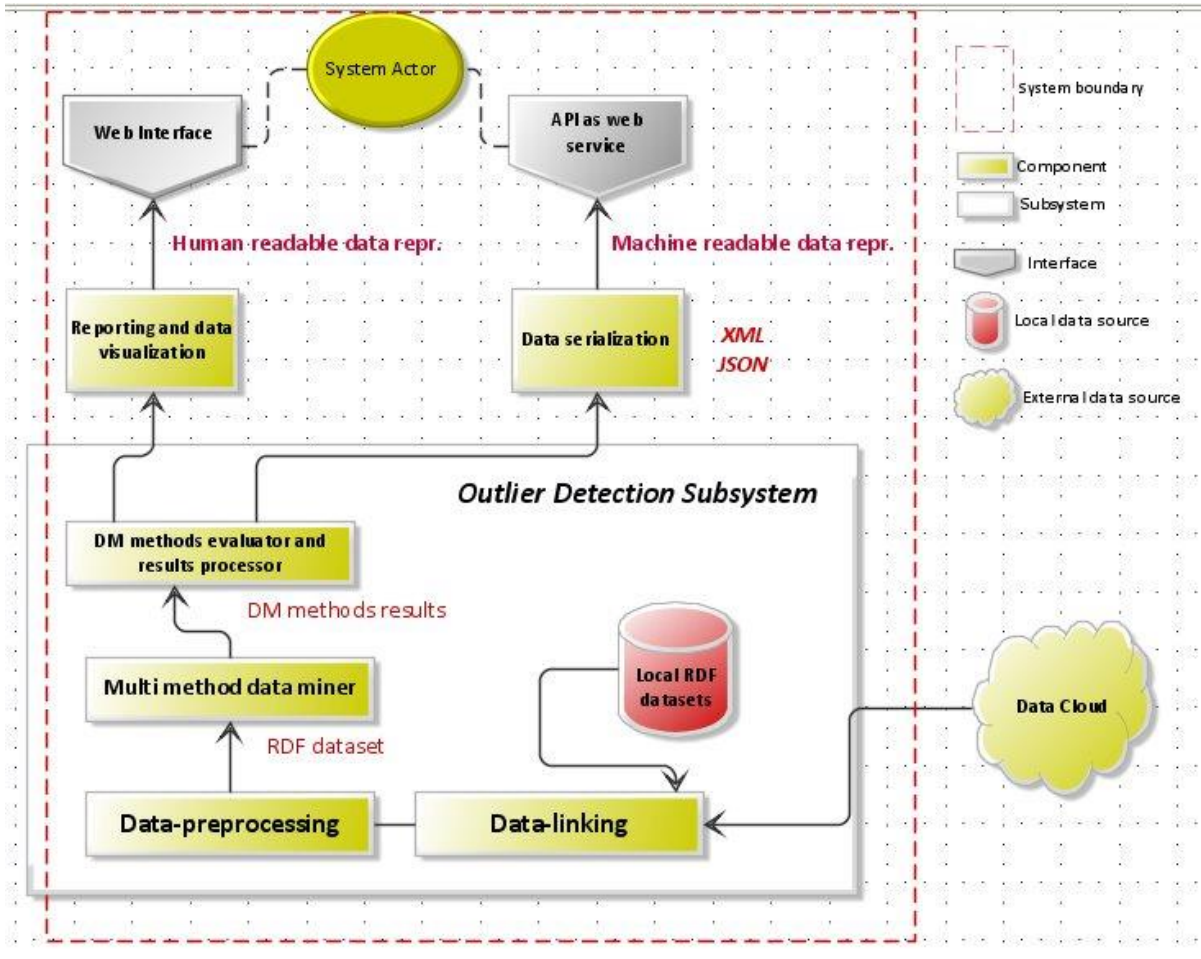
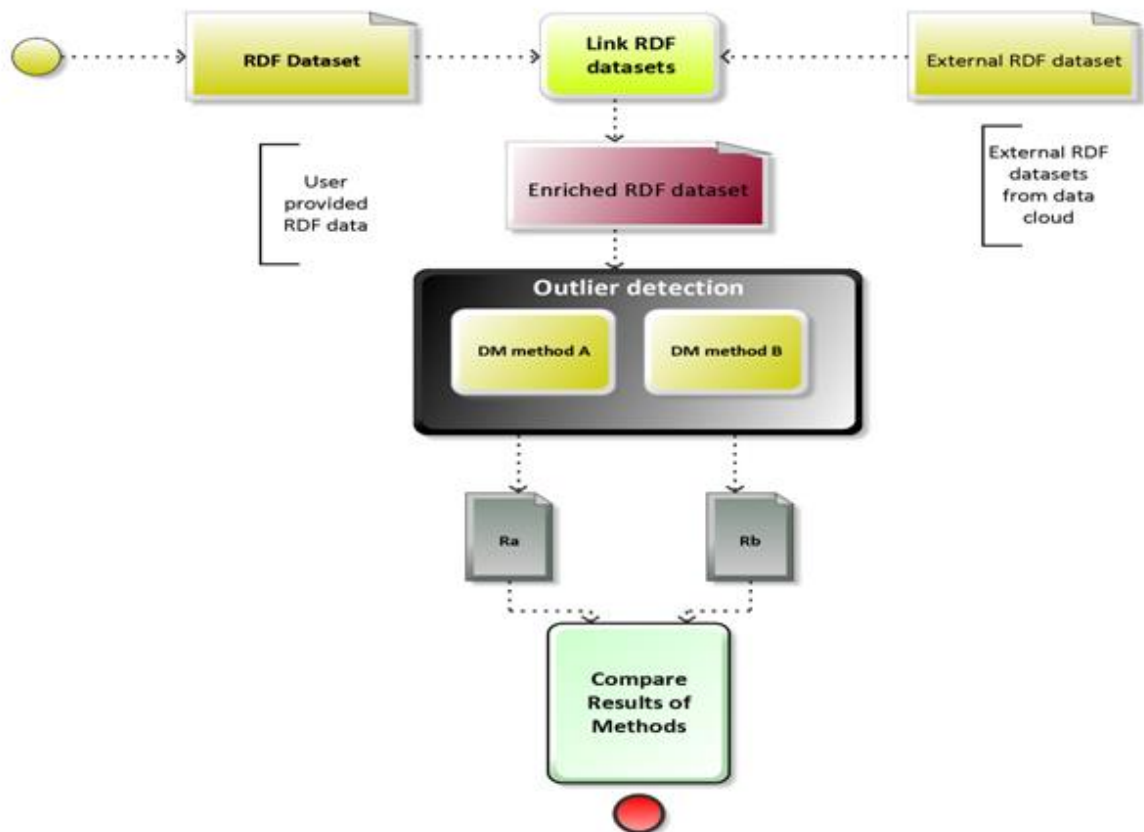


Figure 4 System Architecture



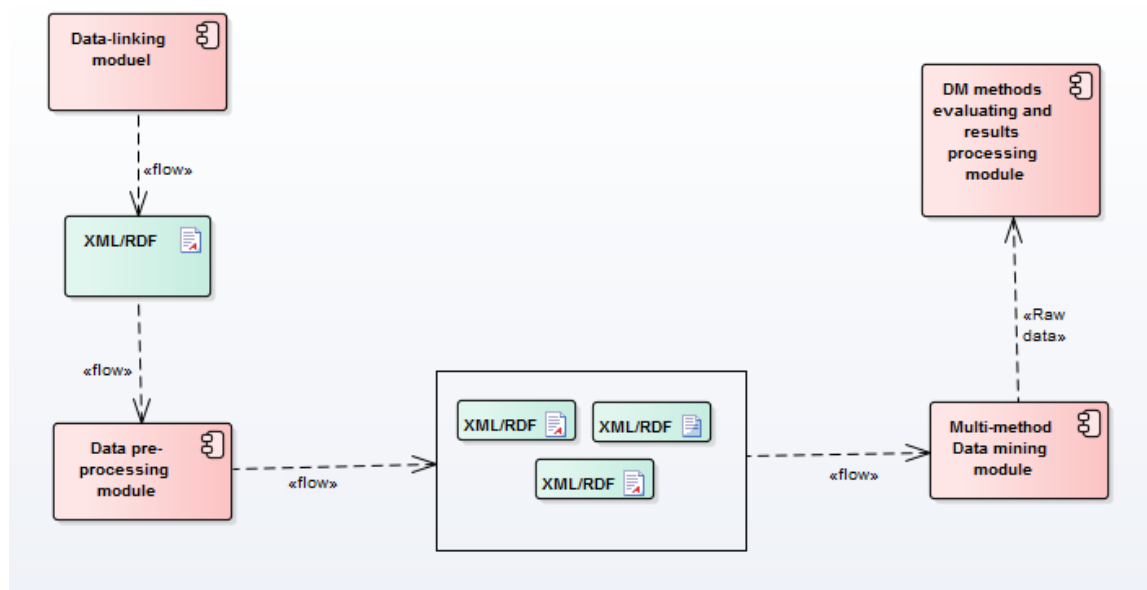
**Figure 5 : System Architecture**

Component ID	CP-DL
Component Name	Data-linking module
Component core functionality	Links a local RDF dataset to a DBpedia and enrich it with additional predicate-value pairs
Dependencies	Apache Jena Framework, DBpedia HTTP Endpoint
Input	Local RDF Dataset
Output	Enriched local RDF Dataset

Component ID	CP-DP
Component Name	Data-preprocessing module
Component core functionality	Optimizing an RDF Dataset by applying sub-population data methods
Dependencies	---
Input	RDF Dataset
Output	Sub datasets from the input dataset

Component ID	CP-MMD
Component Name	Multi-method Data Mining Module
Component core functionality	Applies multiple data mining methods on RDF dataset
Dependencies	-----
Input	RDF Dataset
Output	List of outliers

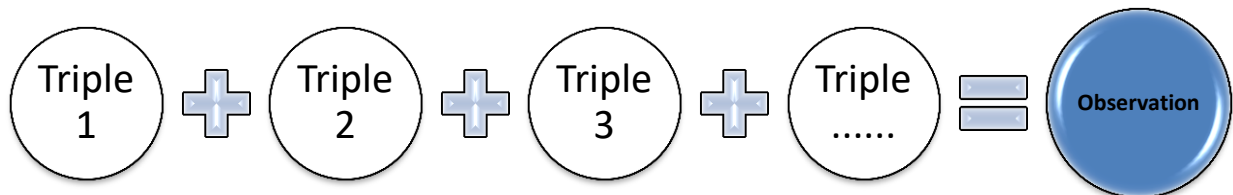
Component ID	CP-ENP
Component Name	DM methods evaluating and results processing module
Component core functionality	Compares applied DM methods and processes the resulted output from component CP-MMD
Dependencies	Component CP-MMD
Input	Output of component CP-MMD
Output	-



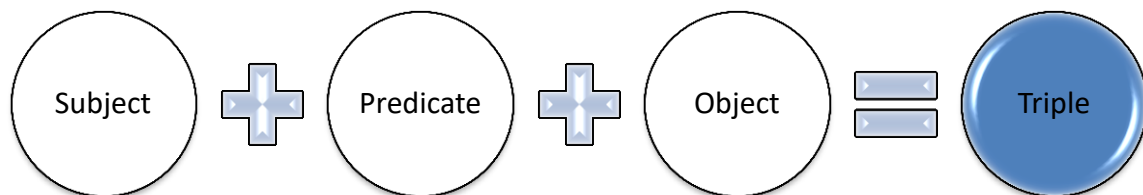
**Figure 6 : DFD diagram of system components**

## 4.1 Subpopulation:

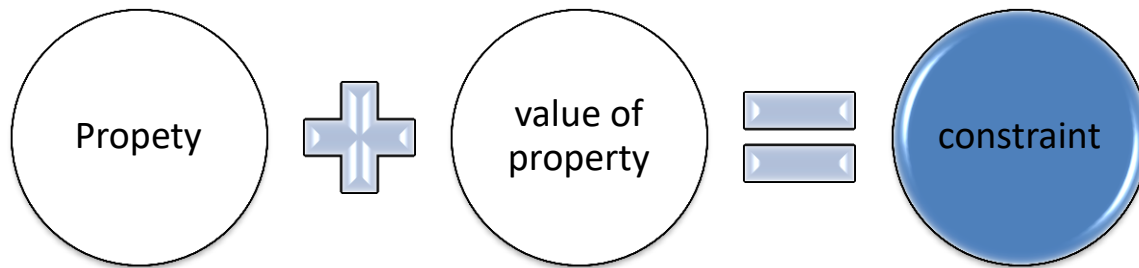
We use experimental data set and the numerical value in this data set are randomly generated values. A subset of a population that shares one or more additional properties is called a subpopulation. For example, if the population is all German people, a subpopulation is all German males; if the population is all Ph.D. students in the world, a subpopulation is all Ph.D. in Germany. By contrast, a sample is a subset of a population that is not chosen to share any additional property. Before start subpopulation, there are some concepts that have to be clear because this concept will play a vital role to have a correct subpopulation. In RDF file, we have many triples that are categorized in different observations .Each triple is formed by subject, predicate, and object. For instance, (Germany - located in - Europ = S:P:O).Located in is a property and Europe is a value of this property then located in is a constraint .



**Figure 7 Observation structure**



**Figure 8 Triple structure**



**Figure 9 Structure constraint**

We propose three different types of constraints:

- **Class constraints:** A class constraint on class *C* applied to an instance set limits it to instances which belong to this class.
- **Property constraints:** A property constraint *p* limits the instances to those connected to an arbitrary object (instance or data value) by means of *p*.
- **Property value constraints:** A property value constraint is defined by a property *p* and a value *v* which can be either an instance or a data value. It limits the instances to those which are connected to a value *v* by means of *p*.

#### 4.1.1 Pre-subpopulation:

1. Use parser to extract the triples from data set file (for instance file.ttl).
2. Format these triples in this formula: "S: P: O".

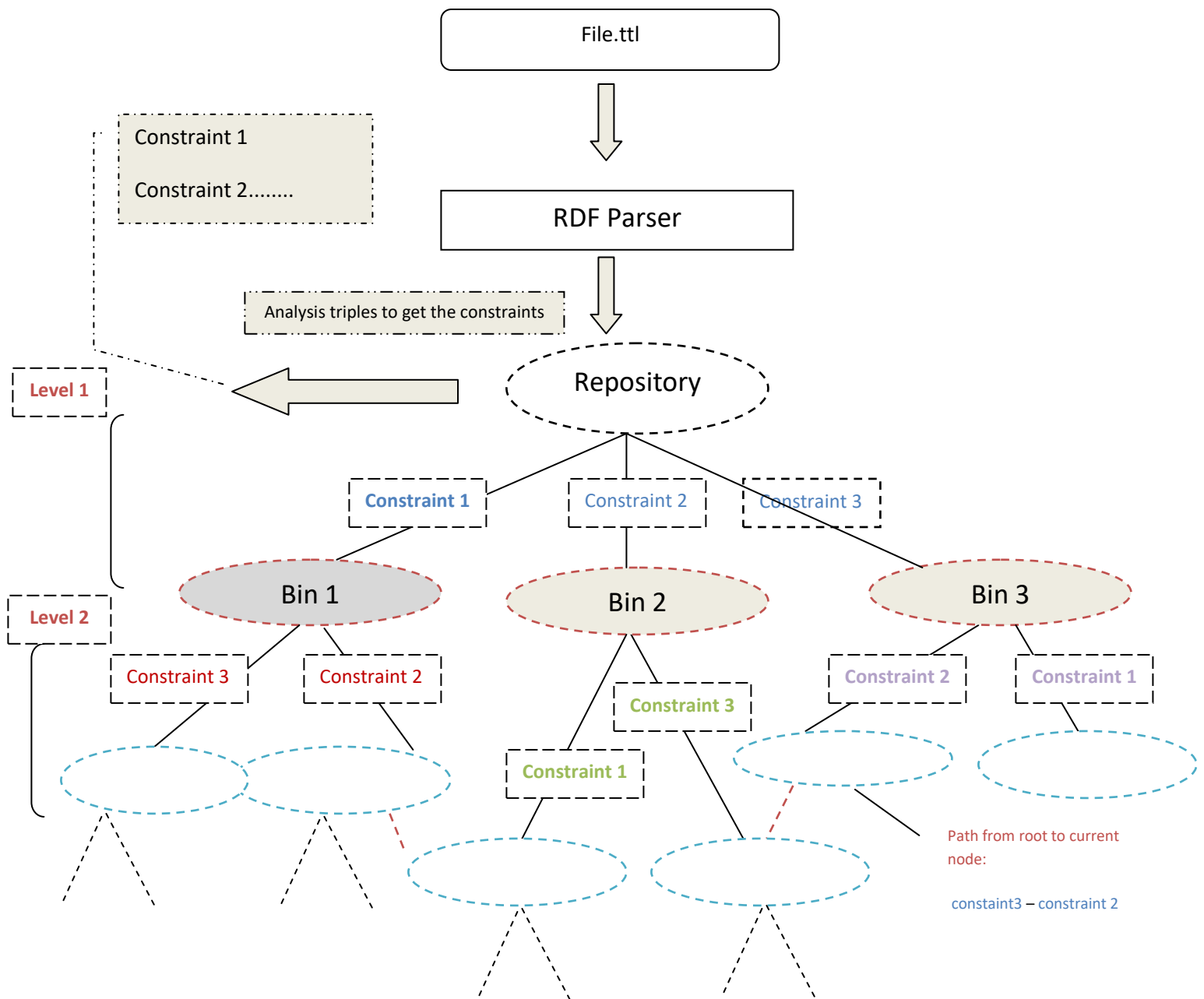
#### 4.1.2 Subpopulation :

1. The root node has the empty constraint set assigned and thus represents all instances and corresponding values of the currently considered property.
2. For this set of instances, we compute a histogram which represents the distribution of values in the subpopulation.
3. Starting with the root node, our approach manages a queue of all not yet extended nodes and thus extends the lattice in a breadth-first-manner.
4. When processing a node from this queue, we create its child nodes, each having an additional constraint compared to the parent node.



5. The additional constraints are those from the set of possible constraints which are not yet used in the parent node.
6. If a node for the resulting set of constraints already exists in the lattice, we do not consider the new node further.
7. We determine the instances which adhere to this new set of constraints and compute the histogram of the value distribution [articles] .
8. in each step of subpopulation ( each level ) , we have to make correlation lattice and finding the sharing bins between the paths in the lattice .this step will prevent repeated triples and collect the triples that have the same path from current node to root node with attention about sequence of constant in the path.
9. We prune subpopulations which only contain a low number of instances or maybe no instances at all, we consider the instance reduction ratio. For instance, the change ratio in the number of instances of the new node compared to its parent node. If the additional constraint leads to a reduction of less than 1%, our approach prunes the node.
10. Too low KL divergence and for not reducing the instance set further, we prune the node.

$$\text{divergence}(\text{parent}, \text{child}) = \left| \frac{|\text{child}|}{|\text{parent}|} \cdot \sum_{i=1}^B \ln \left( \frac{h_{\text{parent}}(i)}{h_{\text{child}}(i)} \right) h_{\text{parent}}(i) \right|$$



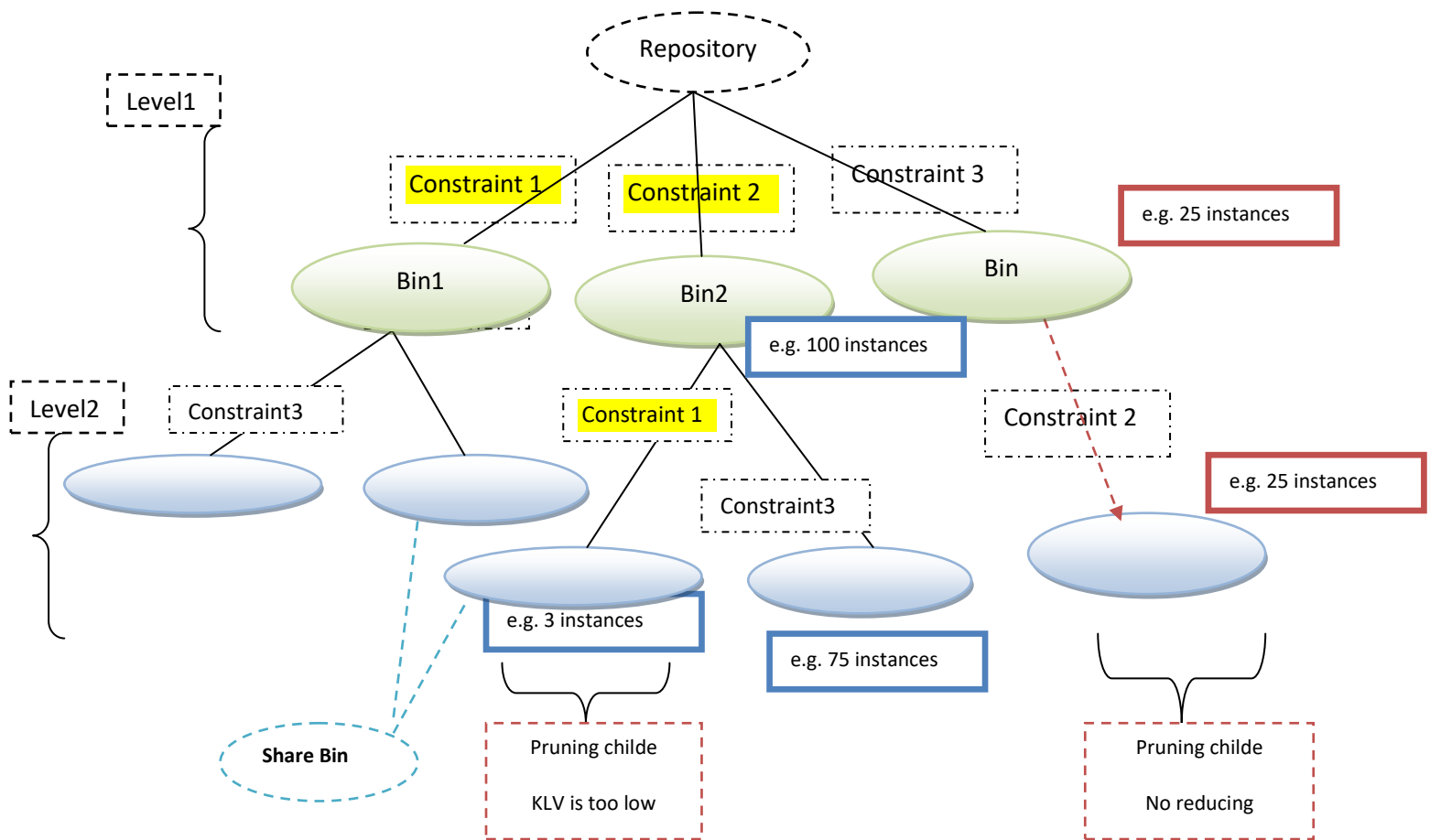
**Figure 10 : Sub population - process**

It is so important to analysis the triples and concludes the values of each property especially the properties that have many different values in a data set .For instance (budget Phase= approved, budget Phase = draft ...Etc).each property with its values gives constraint and value of recursive levels related to a number of properties with considering the repeating in a list of properties and constraints. With increasing the number of levels the bins that are created by subpopulation will increase but the rule of pruning sometimes decrease the number of the bin in each level especially we apply pruning for each level.

#### **4.1.3 Affect pruning on subpopulation – histogram:**

Number of the bins in each level will increase when we move from level to other. With applying pruning process, there is probability to decrease the number of bins in the level where we apply pruning.

**Before pruning:**



**Figure 11: Pruning - subpopulation**

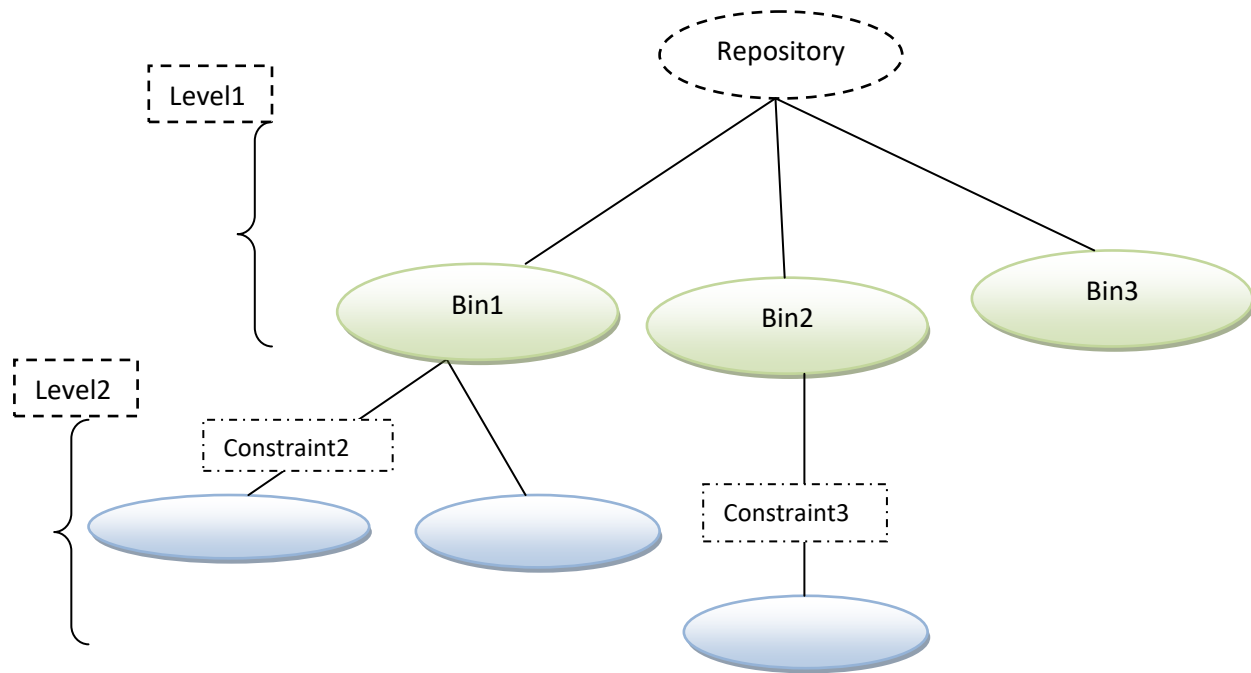
Before pruning we can note from graph above many important points:

· Some branches in the lattice has the same constraint (property=value) but these constraints has a different sequence . In this status, we have to pay attention at this point and collect the triples that are found in the last level in same Bin.

(Path = constraint 1 → constraint 2) ⇔ (Path = constraint 2 → constraint 2)

- For each pair parent-child, we calculate the KLV value and not reducing rule between the parent and child.

### After pruning:



**Figure 12: Lattice after pruning**

We can note that the number of bins in the second level was decreased as result to apply pruning rules between the parent bins in the level1 and children bins in the level 2 .

## 4.2 Outlier detection

After finishing subpopulation stage, we perform outlier detection on all non-pruned nodes of the lattice and store the resulting outlier scores together with the set of constraints which led to the corresponding instance set. Values may not only be detected as outliers when they are wrong but also if they are natural outliers in the considered dataset. To prevent this false detection, we apply an additional cross-checking step to the results of the first outlier detection.

One of the unique selling points of Linked Data is the interlinking of datasets. These equivalence assertions allow us to retrieve additional property values for the same instance. Even if the vocabulary is not reused, ontology matching techniques [7] can enable the retrieval of additional property values by determining equivalent properties.

#### **4.2.1 K-means algorithm for outlier detection:**

An outlier is an object that differs from most other objects significantly. Therefore it can be considered as an anomaly. For outlier detection, only the distance to the appropriate centroid of the normal cluster is calculated. If the distance between an object and the centroid is larger than a predefined threshold  $d_{max}$ , the object is treated as an outlier.

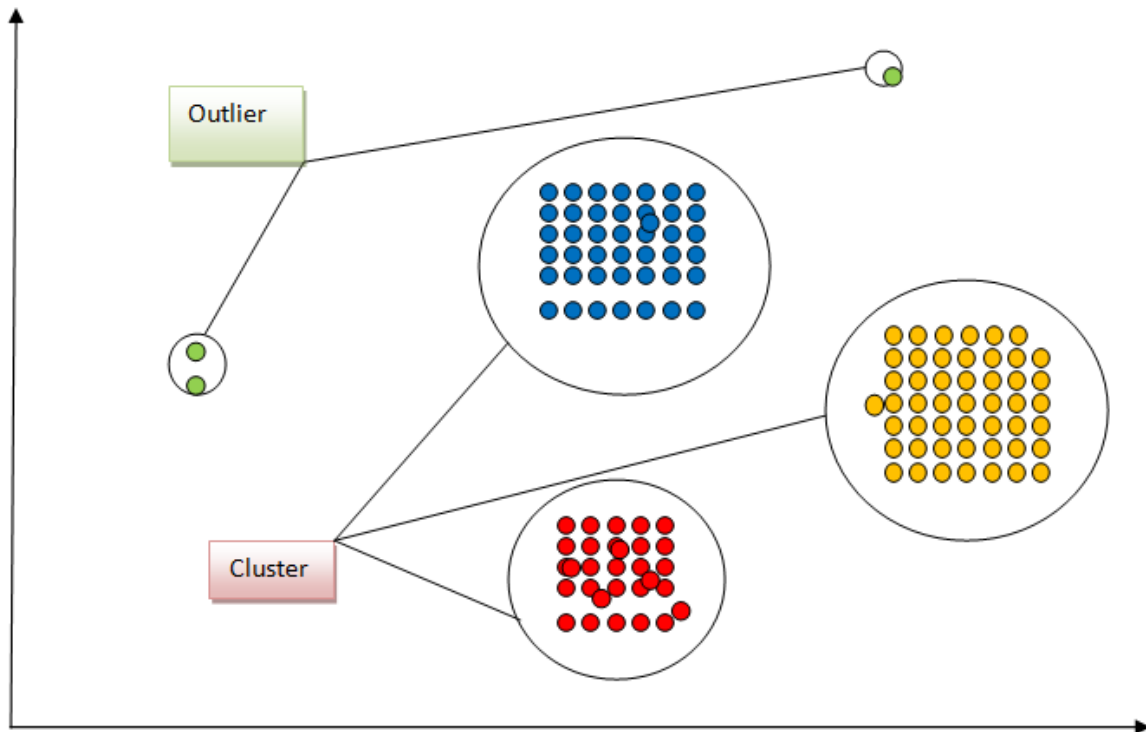
In cluster analysis, a fundamental problem is to determine the best estimate of the number of clusters, which has a deterministic effect on the clustering results. However, a limitation in current applications is that no convincingly acceptable solution to the best-number-of clusters problem is available due to high complexity of real datasets [12].

K-Means clustering intends to partition  $n$  objects into  $k$  clusters in which each object belongs to the cluster with the nearest mean. This method produces exactly  $k$  different clusters of greatest possible distinction. The best number of clusters  $k$  leading to the greatest separation (distance) is not known a priori and must be computed from the data. The Algorithm includes these steps :

1. Clusters the data into  $k$  groups where  $k$  is predefined.
2. Select  $k$  points at random as cluster centers.
3. Assign objects to their closest cluster center according to the Euclidean distance function.
4. Calculate the centric or mean of all objects in each cluster.
5. Repeat steps 2, 3 and 4 until the same points are assigned to each cluster in consecutive rounds.

K-Means is relatively an efficient method. However, we need to specify the number of clusters, in advance and the final results are sensitive to initialization and often terminates at

a local optimum. Unfortunately there is no global theoretical method to find the optimal number of clusters. A practical approach is to compare the outcomes of multiple runs with different  $k$  and choose the best one based on a predefined criterion. In general, a large  $k$  probably decreases the error but increases the risk of over fitting.



**Figure 13: K-means clusters**

#### **4.2.1.1 Cons of K-means algorithm:**

- 1) Uniform effect: often produce clusters with relatively uniform size even if the input data have different cluster size.
- 2) Spherical assumption hard to satisfy: correlation between features breaks it, would put extra weights on correlated features (should take actions depending on the problems); cannot find non-convex clusters or clusters with unusual shapes;

- 3) Different densities: may work poorly with clusters with different densities but spherical shape.
- 4) K value not known
- 5) Sensitive to outliers
- 6) Sensitive to initial points and local optimal, and there is no unique solution for a certain K value.

#### **4.2.1.2 Pros of K-means algorithm:**

- 1) Practical, works well even some assumptions are broken;
- 2) Simple, easy to implement;
- 3) Easy to interpret the clustering results;
- 4) Fast and efficient in terms of computational cost, typically  $O(K \cdot n \cdot d)$ ;

#### **4.2.2 Chauvenet's Criterion**

The idea behind Chauvenet's criterion is to find a probability band, centered on the mean of a normal distribution that should reasonably contain all  $n$  samples of a data set. By doing this, any data points from the  $n$  samples that lie outside this probability band can be considered to be outliers, removed from the data set, and a new mean and standard deviation based on the remaining values and new sample size can be calculated.

This identification of the outliers will be achieved by finding the number of standard deviations that correspond to the bounds of the probability band around the mean ( $D_{\max}$ ) and comparing that value to the absolute value of the difference between the suspected outliers and the mean divided by the sample standard deviation.

##### **Steps Chauvenet's Criterion:**

- Step 1: Calculate the sample mean
- Step 2: Find the sample standard deviation.
- Step 3: Use the following formula to find the standardized deviation from the mean for all suspected outliers, data values "i."

$$\tau = |\mathbf{X}_i - \bar{\mathbf{x}}| / s$$



- Step 4: Compare the values you got in Step 4 with a table of Chauvenet's criterion values to see if you can reject each data point.

#### **4.2.2.1 Properties Chauvenet's Criterion:**

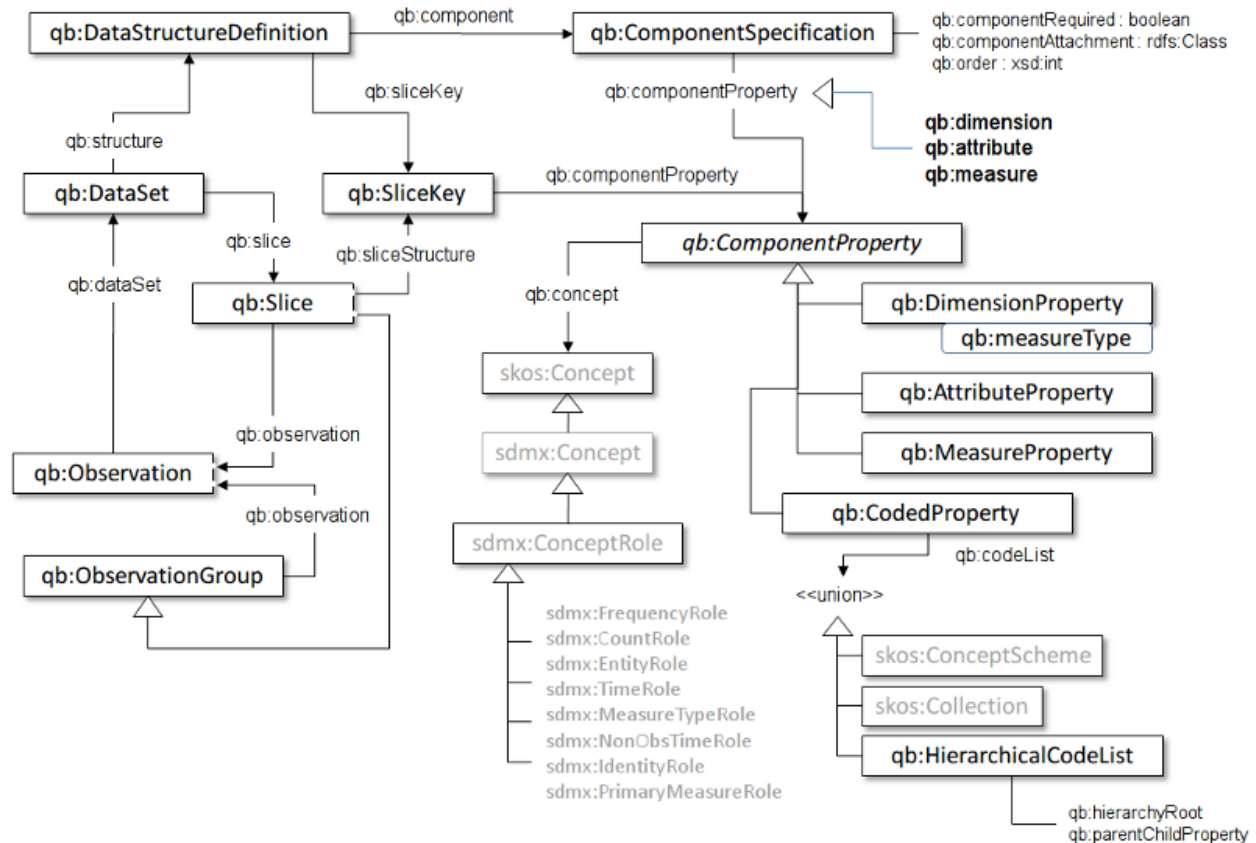
A long established method based on probability theory that is widely used in government, universities and industry for outlier detection - and deletion. It has the disadvantage (unlike methods previously considered) that it assumes that data are from a normal distribution - always a very questionable assumption! If this is assumed, then outliers are identified based on the mean and standard deviation of the data.

### **4.3 Semantic Web role:**

#### **4.3.1 RDF data model:**

##### **4.3.1.1 The Data Cube Vocabulary overview:**

Data Cube Vocabulary represents datasets as data cubes, i.e. collections of data that comprises of observed values (observations), associated dimensions, and metadata. The DCV provides a set of classes and properties for representing the data cubes in RDF and publishing them according to the linked data principles (see Berners-Lee, 2006).



**Figure 14 : Key terms and relationships in The RDF Data Cube Vocabulary**

source: (Cyganiak & Reynolds, 2014)

For every dataset (qb:DataSet) a definition of its structure (qb:DataSetDefinition) needs to be developed. This structure is made of specifications of its components properties (qb:ComponentProperty). There are 3 types of components properties:

- **Measures** (qb:MeasureProperty) – measure properties specify the types of the observed values in the dataset.
- **Dimensions** (qb:DimensionProperty) – dimension properties specify dimensions used in the dataset to organize the observed values in a multidimensional space.
- **Attributes** (qb:AttributeProperty) – attribute properties specify additional attributes of the observed values, such as currency or accuracy.

Datasets using the DCV are made of observations (qb:Observation). An observation might be seen as a record of measures (one or more observed values) and the respective values of the specified dimensions and attributes. By selecting specific values of one or more dimensions, a view on the data called slice (qb:Slice) can be defined.

#### 4.3.1.2 Observations, DataSet, and Data Structure Definition :

The RDF Data Cube Vocabulary builds upon an abstract cube model, i.e. a multidimensional space where measured values are indexed by multiple dimensions.

Using an excerpt of the total general government expenditure expressed as percentage of GDP published by Eurostat (2015) as an example.

Reference area\year	2003	2004	2005	2006	2007	2008	2009	2010	2011	2012	2013	2014
EU (28 countries)	:	:	:	45,6	44,9	46,5	50,3	50	48,6	49	48,6	48,2
EU (27 countries)	:	:	:	45,6	44,9	46,5	50,3	50	48,6	49	48,6	48,2
Euro area (19 countries)	:	:	:	46	45,3	46,6	50,7	50,5	49,1	49,7	49,6	49,4
Euro area (18 countries)	:	:	:	46,1	45,3	46,6	50,7	50,5	49,1	49,8	49,6	49,4
Euro area (17 countries)	:	:	:	46,1	45,4	46,6	50,7	50,5	49,1	49,8	49,7	49,4

**Table 1: Total general government expenditure (% of GDP, excerpt)**

source: excerpt from (Eurostat, 2015b)

The total general government expenditure expressed as percentage of GDP is the measured phenomenon, as illustrated in Table 1, which is indexed by two dimensions: **reference area** and **year**. The total government expenditure in EU28 in 2010 represents a single observation. The collection of observations forms a dataset, i.e. a data cube.

The following example shows a data structure definition for the dataset described in Table 1.

```
@prefix rdfs:      <http://www.w3.org/2000/01/rdf-schema#> .
@prefix qb:       <http://purl.org/linked-data/cube#> .
@prefix sdmx-attribute: <http://purl.org/linked-data/sdmx/2009/attribute#> .
@prefix xsd:      <http://www.w3.org/2001/XMLSchema#> .

@prefix ex-dimension: <http://data.example.org/ontology/dsd/dimension/> .
@prefix ex-dsd:       <http://data.example.org/resource/dsd/> .
@prefix ex-measure:   <http://data.example.org/ontology/dsd/measure/> .

ex-dsd:total-general-government-expenditure a qb:DataStructureDefinition ;
  rdfs:label "Total general government expenditure"@en ;
  # Dimensions
  qb:component [
    qb:dimension ex-dimension:refPeriod ;
    qb:order 1 ;
    rdfs:label "Dimension representing a year for which the total general
government expenditure is reported"@en
  ] ;
  qb:component [
    qb:dimension ex-dimension:refArea ;
    qb:order 2 ;
    rdfs:label "Dimension representing a state or group of states for which the
total general government expenditure is reported"@en
  ] ;
  # Measure
  qb:component [
    qb:measure ex-measure:total-general-government-expenditure ;
```

### 4.3.1.3 Dimensions, Measures and Attributes:

Data structure definition of a dataset represented using DCV is made of specifications of its components (qb:ComponentSpecification). There are 3 types of components: measures, dimensions, and attributes. The DCV provides specific classes to represent these components: qb:MeasureProperty, qb:DimensionProperty, qb:AttributeProperty. Component specification thus links data structure definition with instances of these classes that can be shared among multiple data structure definitions.

Measures (qb:MeasureProperty) represent types of the measured phenomenon, such as population of a given area or the total general government expenditure expressed as percentage of GDP, as illustrated in Table 1.

In the following example, we provide RDF representation of these components.

```
@prefix interval:      <http://reference.data.gov.uk/def/intervals/> .
@prefix qb:           <http://purl.org/linked-data/cube#> .
@prefix rdf:          <http://www.w3.org/1999/02/22-rdf-syntax-ns#> .
@prefix rdfs:         <http://www.w3.org/2000/01/rdf-schema#> .
@prefix sdmx-concept: <http://purl.org/linked-data/sdmx/2009/concept#> .
@prefix sdmx-dimension: <http://purl.org/linked-data/sdmx/2009/dimension#> .
@prefix sdmx-measure: <http://purl.org/linked-data/sdmx/2009/measure#> .
@prefix xsd:          <http://www.w3.org/2001/XMLSchema#> .

@prefix ex:           <http://data.example.org/ontology/> .
@prefix ex-codelist:  <http://data.example.org/resource/codelist/> .
@prefix ex-dimension: <http://data.example.org/ontology/dsd/dimension/> .
@prefix ex-measure:   <http://data.example.org/ontology/dsd/measure/> .

# Dimension properties

ex-dimension:refPeriod a rdf:Property, qb:DimensionProperty ;
  rdfs:label "reference period"@en ;
  rdfs:subPropertyOf sdmx-dimension:refPeriod ;
  rdfs:range interval:Interval ;
  qb:concept sdmx-concept:refPeriod .

ex-dimension:refArea a rdf:Property, qb:DimensionProperty ;
  rdfs:label "reference area"@en ;
  rdfs:subPropertyOf sdmx-dimension:refArea ;
  rdfs:range ex:GeopoliticalEntity ;
  qb:codelist ex-codelist:geo ;
  qb:concept sdmx-concept:refArea .

# Measure properties

ex-measure:total-general-government-expenditure a rdf:Property, qb:MeasureProperty ;
  rdfs:label "total general government expenditure"@en ;
  rdfs:subPropertyOf sdmx-measure:obsValue ;
  rdfs:range xsd:decimal .
```

**Example 3: Vocabulary for the data structure definition of the dataset described in Table 1**

#### 4.3.1.4 Code lists:

Possible values of dimensions are limited to items of the used code lists.

Code list can be defined as “a predefined list from which some statistical coded concepts take their values. The DCV implements an approach to the definition of code lists via qb:HierarchicalCodeList – see <sup>1</sup>

<sup>1</sup> (Cyganiak & Reynolds, 2014). For a detailed description of the Data Cube Vocabulary please refer to the User documentation for DCV at:

<http://openbudgets.eu/assets/deliverables/D1.4.pdf>

Footer: <https://stats.oecd.org/glossary/detail.asp?ID=3371> <sup>1</sup>

#### **4.3.1.5 Data Linking Module:**

We use DBPedia as an external data repository to enrich our local dataset uploaded by the user.

By using special SPARQL queries we fetch following information:

- Area and population values for both location (usually a city) and the country where this city is located.
- Latitude and longitude values for the location
- GDP per capita value for the country

Each and every observation in the provided RDF dataset must be linked to a location (usually a city) so that that location can be used to retrieve the formerly mentioned information from DBPedia endpoint.

<HTTP://DATA.OPENBUDGETS.EU/RESOURCE/DATASET/EXAMPLE-BUDGET-CITIES/OBSERVATION/1A> A QB:OBSERVATION ;  
HTTP://DATA.OPENBUDGETS.EU/ONTOLOGY/DSD/DIMENSION/ORGANIZATION  
HTTP://DBPEDIA.ORG/RESOURCE/PARIS;  
<HTTP://DATA.OPENBUDGETS.EU/ONTOLOGY/DSD/MEASURE/AMOUNT> 14881;

#### **4.3.1.6 Enrichment stage steps:**

1. we go through all locations we have to fetch the relevant country, geo-spatial, area and population information

```
+ "CONSTRUCT \n"
+ "{\n"
+ " ?location dbo:populationTotal ?pop.\n"
+ " ?location geo:lat ?lat.\n"
+ " ?location geo:long ?long.\n"
+ " ?location dbo:areaTotal ?area. \n"
+ " ?location dbo:country ?country ."
+ " ?country dbp:gdpPppPerCapita ?countryGDP ."
+ " ?country dbo:populationTotal ?countryPopulation ."
+ " ?country dbo:areaTotal ?countryArea ."
+ "\n"
+ " } \n"
+ " where {\n"
+ " ?subject datacube:isLocation ?location .\n"
+ " \n"
+ " SERVICE <http://dbpedia.org/sparql> { \n"
+ " ?location dbo:populationTotal ?pop.\n"
+ " ?location geo:lat ?lat.\n"
+ " ?location geo:long ?long.\n"
+ " OPTIONAL {"
+ " ?location dbo:areaTotal ?area ."
+ " ?location dbo:country ?country ."
+ " ?country dbp:gdpPppPerCapita ?countryGDP ."
+ " ?country dbo:populationTotal ?countryPopulation ."
+ " ?country dbo:areaTotal ?countryArea ."
+ " }\n"
```

2. we go through all observations we have and according to its location we attach the country and geo-spatial information again to the observation

```
+ "CONSTRUCT \n"
+ "{\n"
+ " ?observation datacube:info_lat ?lat.\n"
+ " ?observation datacube:info_long ?long.\n"
+ " ?observation datacube:info_country ?country.\n"
+ "\n"
+ " } \n"
+ " where {\n"
+ " ?observation a qb:Observation .\n"
+ " ?observation " + locationPredName + " ?location.\n"
+ " ?location geo:lat ?lat.\n"
+ " ?location geo:long ?long.\n"
+ " OPTIONAL {"
+ " ?location dbo:country ?country."
+ " } \n"
+ " . . ."
```

In our example the "locationPredName" is

[HTTP://DATA.OPENBUDGETS.EU/ONTOLOGY/DSD/DIMENSION/ORGANIZATION](http://data.openbudgets.eu/ontology/dsd/dimension/organization)

3. Finally we again go through all observations and attach the GDP, area and population information for both country and location.

```
+ "CONSTRUCT \n"
+ "{\n"
+ "  ?observation datacube:info_countrypopulation \"low\".\n"
+ "} \n"
+ "where {\n"
+ "  ?observation a qb:Observation .\n"
+ "  ?observation datacube:info_country ?country .\n"
+ "  ?country dbo:populationTotal ?pop .\n"
+ "  filter(?pop > " + Ranges.countryPopLow + " && ?pop < " + Ranges.countryPopMid + ").\n"
```

Example SPARQL query on how to generate county population information

```
+ "CONSTRUCT \n"
+ "{\n"
+ "  ?observation datacube:info_area \"mid\".\n"
+ "} \n"
+ "where {\n"
+ "  ?observation a qb:Observation .\n"
+ "  ?observation " + locationPredName + " ?location .\n"
+ "  ?location dbo:areaTotal ?area .\n"
+ "  filter(?area > " + Ranges.locationAreadMid + " && ?area < " + Ranges.locationAreadHigh + ").\n"
```

Example SPARQL query on how to generate location area information

By the end of these steps the dataset is ready to go through the subpopulation stage.

## 4.4 User Input and Interface:

The user is required to input different information to start a new session. During creating the session the system goes through enrichment and preprocessing (subpopulation) and then the user can select which sample groups to find outliers for.



## Create and new session

Outlier predicate name:

predicate\_name of the URI containing the outlier object

Location predicate name:

predicate\_name of the URI containing the location object

How many outlier properties?: 1

Property name:

predicates names of the URIs containing the objects to run the subpopulation method on

How many datasets?: 1

Upload your file(s):

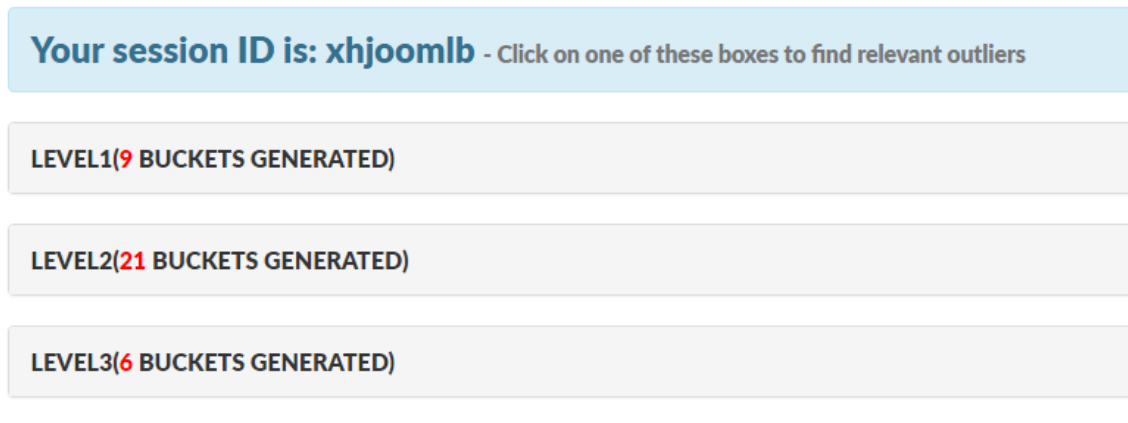
Choose File No file chosen base dataset file

Submit

Figure 15: User Interface

After the session is created the user should keep the shown session ID to view the session again without going through the above-mentioned stages.

#### 4.5 Results in each level:



**Figure 16: Subpopulation Results**

By pressing certain level the user can view the different buckets that we generated for each level and choose one bucket to apply one of the two used outlier detection methods.

#### 4.6 Property Name and constraint:

For the property that are used in subpopulation , we used three property and the user can choose any property and apply subpopulation for any number of property .

- info\_population.
- info\_countryarea
- budgetPhase

Depending on this property, the system analysis the data set automatically to find the constraint depending on these properties and its values.

#### For example:

- info\_population=high , info\_population=mid if it is available in data set ,  
info\_population=low if it is available in data set
- info\_countryarea=mid.... Etc.
- budgetPhase=approved.... Etc.

## 4.7 Choose a bin(bucket) to apply outlier detection:

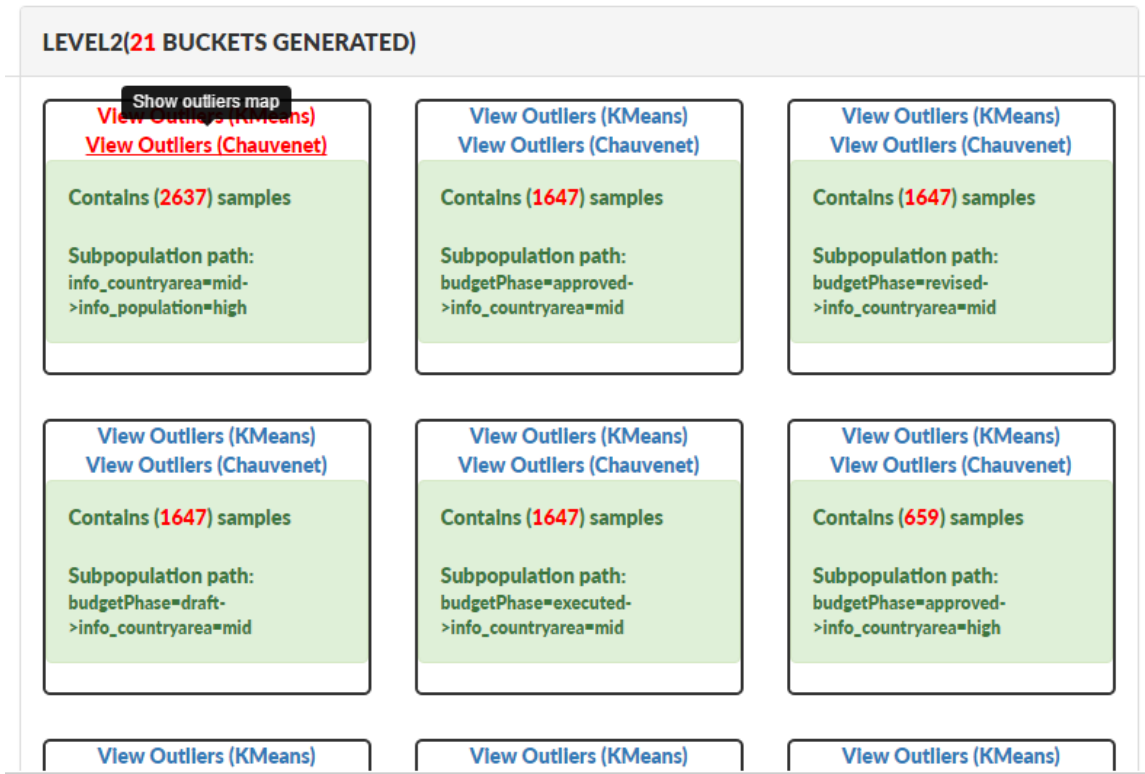
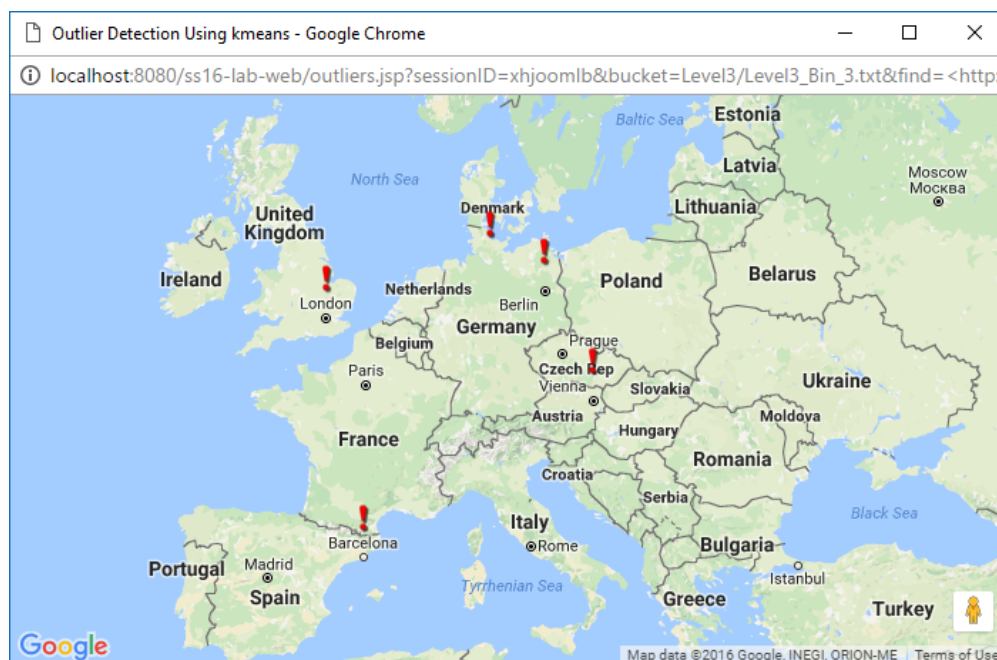


Figure 17 : Details of results sub population

## Visualization of the results:



**Figure 18: A Google Map shows outliers found in a number of cities.**

After the outlier results are found, a cache entry is created for that specific outlier results based on the applied method, session ID and bucket name so that these results can be later retrieved directly from the cache in both web interface and restful interface.

#### 4.7.1.1 Restful Service Interface:

The system also provides a web service that can be used to retrieve the results of a previously cached outlier method in a certain session for a certain bucket, therefore the user is required to provide three pieces of information using the PUT method, and then can use the GET method to retrieve the results in a JSON format.

```
HttpClient client = new DefaultHttpClient();
HttpPut put = new HttpPut("http://localhost:8080/ss16-lab-web/resources/outliers/session");
put.setEntity(new StringEntity("upenkwbq")); // session ID
client.execute(put);
put.releaseConnection();

put = new HttpPut("http://localhost:8080/ss16-lab-web/resources/outliers/bucket");
put.setEntity(new StringEntity("Level1/Level1_Bin_1.txt")); // bucket name
client.execute(put);
put.releaseConnection();

put = new HttpPut("http://localhost:8080/ss16-lab-web/resources/outliers/method");
put.setEntity(new StringEntity("chauvenet")); // method name
client.execute(put);
put.releaseConnection();

HttpGet get = new HttpGet("http://localhost:8080/ss16-lab-web/resources/outliers");
HttpResponse response = client.execute(get);
HttpEntity en = response.getEntity();
InputStreamReader i = new InputStreamReader(en.getContent());
BufferedReader rd = new BufferedReader(i);
```

**Figure 19: Example illustrates how to build restful client**

## 5 Comparison of Outlier Detection Methods:

Since different outlier detection algorithms are based on disjoint sets of assumption, a direct comparison between them is not always possible. In many cases, the data structure and the outlier generating mechanism on which the study is based dictate which method will outperform the others. There are few works that compare different classes of outlier detection methods. In particular, the methods depend on: whether or not the data set is multivariate normal, the dimension of the data set, the type of the outliers, the proportion of outliers in the dataset.

### 5.1 Comparing Example by our system:

The project can process any data set dynamically and this point is one of the strongest points that support the project. Our data set that is used in testing the project and comparing the result is “Budget-EU.ttl”. The statistics in the tables below are generated automatically inside the project folder in the statistics folder and include all information that we used to analysis and compare the results.

There are three criteria for comparing the result:

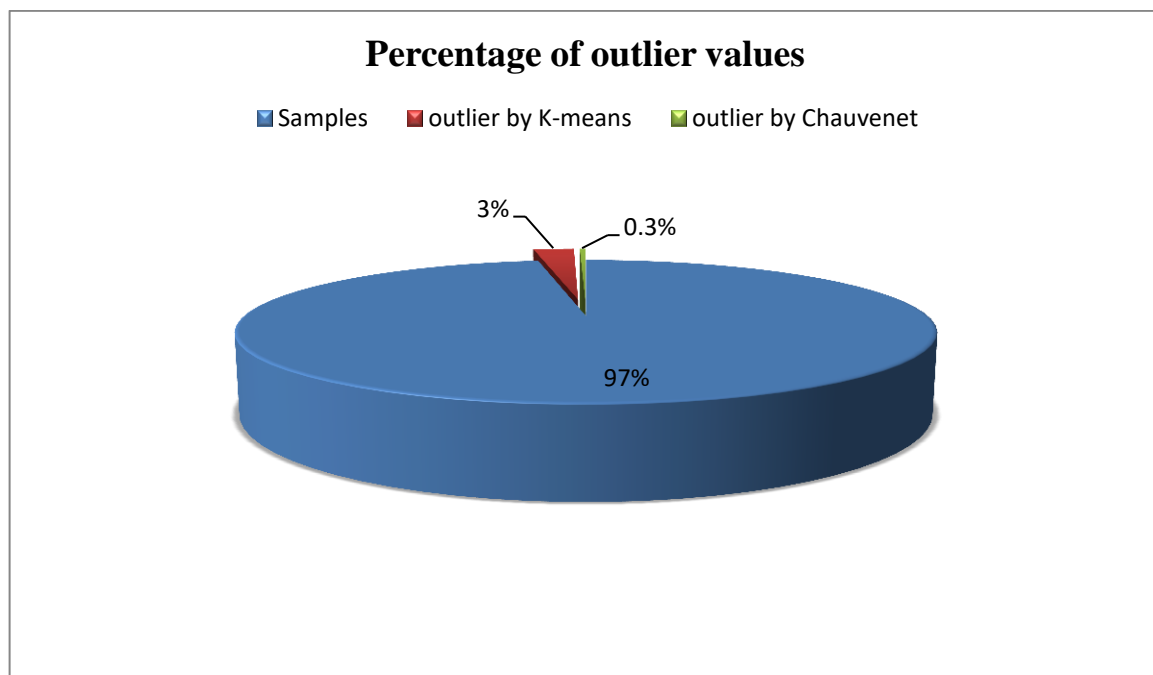
- Comparing number of outliers in each bin in each level for each method.

In these criteria, we will calculate the number of all observations that are specified by K-means method as an outlier and compare it with a number of all observations that are specified by Chauvenet method.

	Number of instances (samples) in each bin	Outliers found by K- means	Outliers found by Chauvenet
Level 1			
Bin 1.1	5273	15	26
Bin 1.2	5265	9	9
Bin1.3	6585	14	29
Bin1.4	2633	5	5

Bin1.5	1317	1	1
Bin1.6	2964	2	6
Bin1.7	2964	11	12
Bin1.8	2964	8	9
Bin1.9	2964	7	10
<b>Level 2</b>			
Bin2.1	2637	13	20
Bin2.2	1317	2	1
Bin2.3	1319	2	5
Bin2.4	1319	8	9
Bin2.5	1319	3	5
Bin2.6	3949	6	6
Bin2.7	1317	1	1
Bin2.8	1317	423	0
Bin2.9	1317	5	5
Bin2.10	1647	2	6
Bin2.11	1647	6	7
Bin2.12	1647	8	9
Bin2.13	1647	12	8
Bin2.14	659	190	0
Bin2.15	659	4	4
Bin2.16	659	199	0
Bin2.17	659	1	1
Bin2.18	330	88	0
Bin2.19	330	1	1
Bin2.20	330	105	0
Bin2.21	330	84	0
<b>Level 3</b>			
B3.1	660	2	4
B3.2	660	8	8

B3.3	660	3	4
B3.4	330	102	0
B3.5	330	106	0
B3.6	330	71	0
Sum	62254	1527	211
<b>Results</b>		1527	211
<b>Chauvenet maximum number of found outliers in a bin(bucket)</b>		29	
<b>Chauvenet minimum number of found outliers in a bin(bucket)</b>		0	
<b>Kmeans maximum number of found outliers in a bin(bucket)</b>		423	
<b>Kmeans minimum number of found outliers in a bin(bucket)</b>		1	



**Figure 20: Percentage of outlier values**

Using “Budget-Eu” data set in as input to a project will give about 3% outliers for k-means method comparing with Chauvenet method that gave only 0.3 % outliers. Depending on this comparison we can conclude that k-means algorithm is more sensitive to outlier compared to Chauvenet method but that does not mean k-means is better than Chauvenet because each algorithm follows specific process and special rules .As a result, we can conclude following points related to K-means:

- Strong sensitivity to outliers and noise
- Doesn't work well with non-circular cluster shape - number of cluster and initial seed value need to be specified beforehand
- Low capability to pass the local optimum.
- K-means is the simplest to implement and to run
- Scale the degree of agreement by calculates Min, Max.

We followed a special scale in the measure of the degree of agreement between the results of outlier in each method. This scale range is between [0,1] display the different degree of agreement .



The degree of agreement is the number of the shared outliers between both methods divided by the maximum number of found outliers by each method.

**For instance:**

Method A gave 4 outliers values: Value \_A= 4.

Method B gave 4 outliers values: Value\_B =4.

The number of shared outliers: Value\_C

Maximum value when comparing value\_A and value\_B : Value\_D



**e.g. status 1:**

If number of shared outliers between both methods is 4, that means there is a full matching (agreement) in the results

**e.g. status 2:**

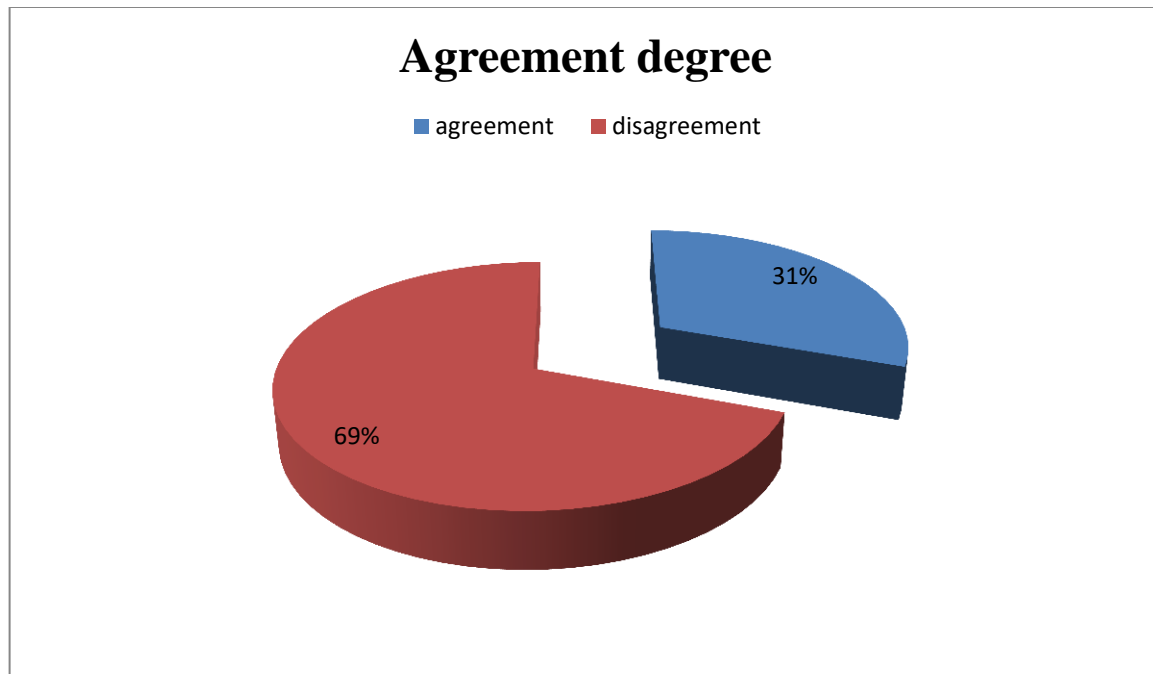
If number of shared outliers between both methods is 0, that means there is no matching in the results

$$\frac{Value\_C}{Value\_D} = \frac{4}{4} = 1 \text{ full agreement}$$

$$\frac{Value\_C}{Value\_D} = \frac{0}{4} = 0 \text{ full disagreement}$$

	Number of instances (samples) in each bin	Degree of agreement	Notes
<b>Level 1</b>			
Bin 1.1	5273	0	
Bin 1.2	5265	1	
Bin1.3	6585	0	
Bin1.4	2633	1	
Bin1.5	1317	1	
Bin1.6	2964	0	
Bin1.7	2964	0	
Bin1.8	2964	0	
Bin1.9	2964	0	
<b>Level 2</b>			
Bin2.1	2637	0	
Bin2.2	1317	1	
Bin2.3	1319	0	
Bin2.4	1319	0	

Bin2.5	1319	0	
Bin2.6	3949	1	
Bin2.7	1317	1	
Bin2.8	1317	0	
Bin2.9	1317	1	
Bin2.10	1647	0	
Bin2.11	1647	0	
Bin2.12	1647	0	
Bin2.13	1647	0	
Bin2.14	659	0	
Bin2.15	659	1	
Bin2.16	659	0	
Bin2.17	659	1	
Bin2.18	330	0	
Bin2.19	330	1	
Bin2.20	330	0	
Bin2.21	330	0	
<b>Level 3</b>			
B3.1	660	0	
B3.2	660	1	
B3.3	660	0	
B3.4	330	0	
B3.5	330	0	
B3.6	330	0	
Results			
Agreement value = 1	11		
Disagreement value = 0	25		



**Figure 21:Agreement degree**

We can conclude from the graph that the agreement between these two methods ( k-means and Chauvenet ) is bad and that reflect the differences in strategy of the work between these methods .

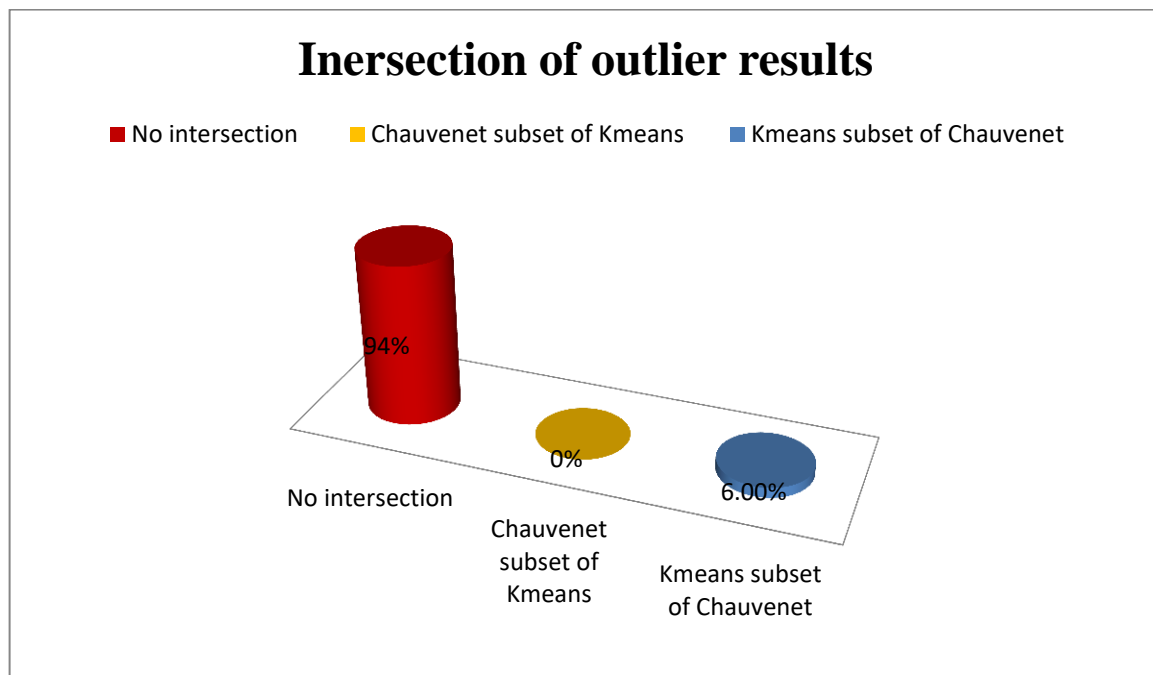
Compare the states where outlier results from K-means are a subset of outlier's results from Chauvenet .additionally, states where outlier results from K- Chauvenet are a subset of outlier's results from K-means.

	Number of instances in each bin (samples )	Chauvenet subset of Kmeans	Kmeans subset of Chauvenet
<b>Level 1</b>			
Bin 1.1	5273	false	false
Bin 1.2	5265	false	false
Bin1.3	6585	false	false
Bin1.4	2633	false	false
Bin1.5	1317	false	false

Bin1.6	2964	false	false
Bin1.7	2964	false	false
Bin1.8	2964	false	false
Bin1.9	2964	false	false
<b>Level 2</b>			
Bin2.1	2637	false	false
Bin2.2	1317	false	false
Bin2.3	1319	false	false
Bin2.4	1319	false	false
Bin2.5	1319	false	true
Bin2.6	3949	false	false
Bin2.7	1317	false	false
Bin2.8	1317	false	false
Bin2.9	1317	false	false
Bin2.10	1647	false	false
Bin2.11	1647	false	false
Bin2.12	1647	false	false
Bin2.13	1647	false	false
Bin2.14	659	false	false
Bin2.15	659	false	false
Bin2.16	659	false	false
Bin2.17	659	false	false
Bin2.18	330	false	false
Bin2.19	330	false	false
Bin2.20	330	false	false
Bin2.21	330	False	false
<b>Level 3</b>			
B3.1	660	false	false
B3.2	660	false	false
B3.3	660	false	true

B3.4	330	false	false
B3.5	330	false	false
B3.6	330	false	false
<b>No intersection</b>		34 cases	
<b>Chauvenet subset of Kmeans</b>		0 cases	
<b>Kmeans subset of Chauvenet</b>		2 cases	

- No intersection status means that there is no shared outliers between the k-means method and Chauvenet method. According to our results, there are 34 cases.
- Chauvenet subset of Kmeans means the outliers that we got from Chauvenet is subset of outliers that we got from k-means. According to our results, there no case of that.
- Kmeans subset of Chauvenet means the outliers that we got from Kmeans is part of an outlier that we got from Chauvenet. According to our results, there are 2 cases.
- The average of agreement depending on all result from our data set is approximately 0.30%.



**Figure 22: Inersection of outlier results**

## 5.2 Clarification example depending on Rapid Minder:

We use in rapid miner the same samples of example that are used in the project.

### 5.2.1 Nearest Neighbor Based: Local Outlier Factor (LOF)

The LOF anomaly detection calculates the anomaly score according to the local outlier factor algorithm proposed by Breunig[10]. There are several steps in the calculation of the LOF. The initial step involves getting the nearest neighbors set. The definition states that the  $k$ -distance( $p$ ) has at least  $k$  neighbors with distinct spatial coordinates that have a distance less than or equal it and at most  $k-1$  of such neighbors with distance strictly less than it. The reachability distance ( $\text{reach-dist}(p,o)$ ) is the maximum of the distance between point  $p$  and  $o$  and the  $k$ -distance( $o$ ). The local reachability is the inverse of the average reachability distance over the nearest neighborhood set. Finally the LOF is calculated as the average of the ratio of the local reachability density over the neighborhood set. The values of the LOF oscillates with the change in the size of the neighborhood. Thus a range is defined for the size of the neighborhood. The maximum LOF over that range is taken as the final LOF score. A normal instance has an outlier value of approximately 1, while **outliers have values greater than 1**. The operator is also able to read and write a model containing the  $k$  nearest neighbors set.

### 5.2.2 Statistical Based: Histogram Based Outlier Score (HBOS):

Calculates an outlier score by creating an histogram with a fixed or a dynamic binwidth.

This method calculates a separate univariate histogram for every column in the Example Set. There are two modes, one with a static and one with a dynamic bandwidth[11]. In the static mode every bin has the same binwidth equally distributed over the value range. In the dynamic mode the binwidth can vary, but you can specify a minimum number of examples contained in a bin. The parameter number of bins sets the total number of bins used for either mode. The binwidth / minimum number values per bin is then calculated automatically. In the dynamic mode it is possible that there are less bins then specified if some bins contain more than the minimum number of values. To compute the outlier score, the histograms are normalized to one in height first. Then, the score is inverted, so that **anomalies have a high score** and normal examples a low score.

We choose some bins from all level of the results and applied different outlier methods in Rapidminer as follow :

**Example 1:**

834	2452d	11504.0	
835	2585d	12808.0	
836	2452c	11400.0	
837	3212d	12954.0	
838	3345c	14415.0	
839	3212b	13418.0	
840	3345d	13464.0	
841	3212c	12966.0	
842	3345a	14412.0	
843	3345b	13651.0	
844	3212a	14058.0	
845	2147a	13233.0	
846	2013d	15473.0	
847	2146d	10255.0	
848	2013c	15375.0	
849	1915d	18044.0	
850	2013b	13202.0	
851	2146c	10585.0	Level1_Bin2
852	2146b	10903.0	
853	2013a	14606.0	
854	2146a	10974.0	
855	1915a	16949.0	
856	2279b	12095.0	
857	2279c	13573.0	
858	1915c	18414.0	
859	2279d	11908.0	
860	1915b	15690.0	

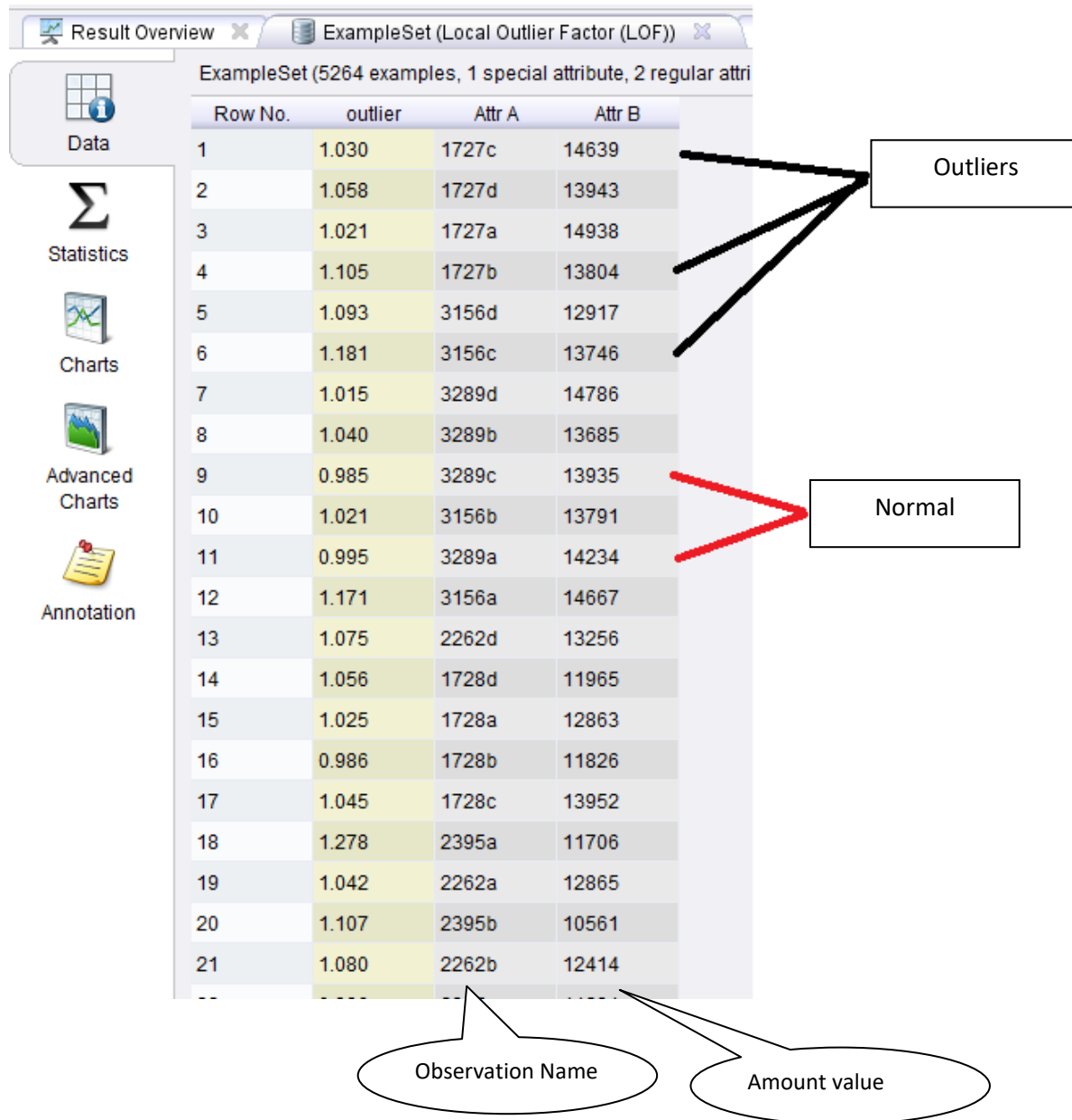
Observation Name

Amount value

**Figure 23:Data sample**

### Outliers by Nearest Neighbor Based: Local Outlier Factor (LOF):

Criteria : Outliers have values greater than 1

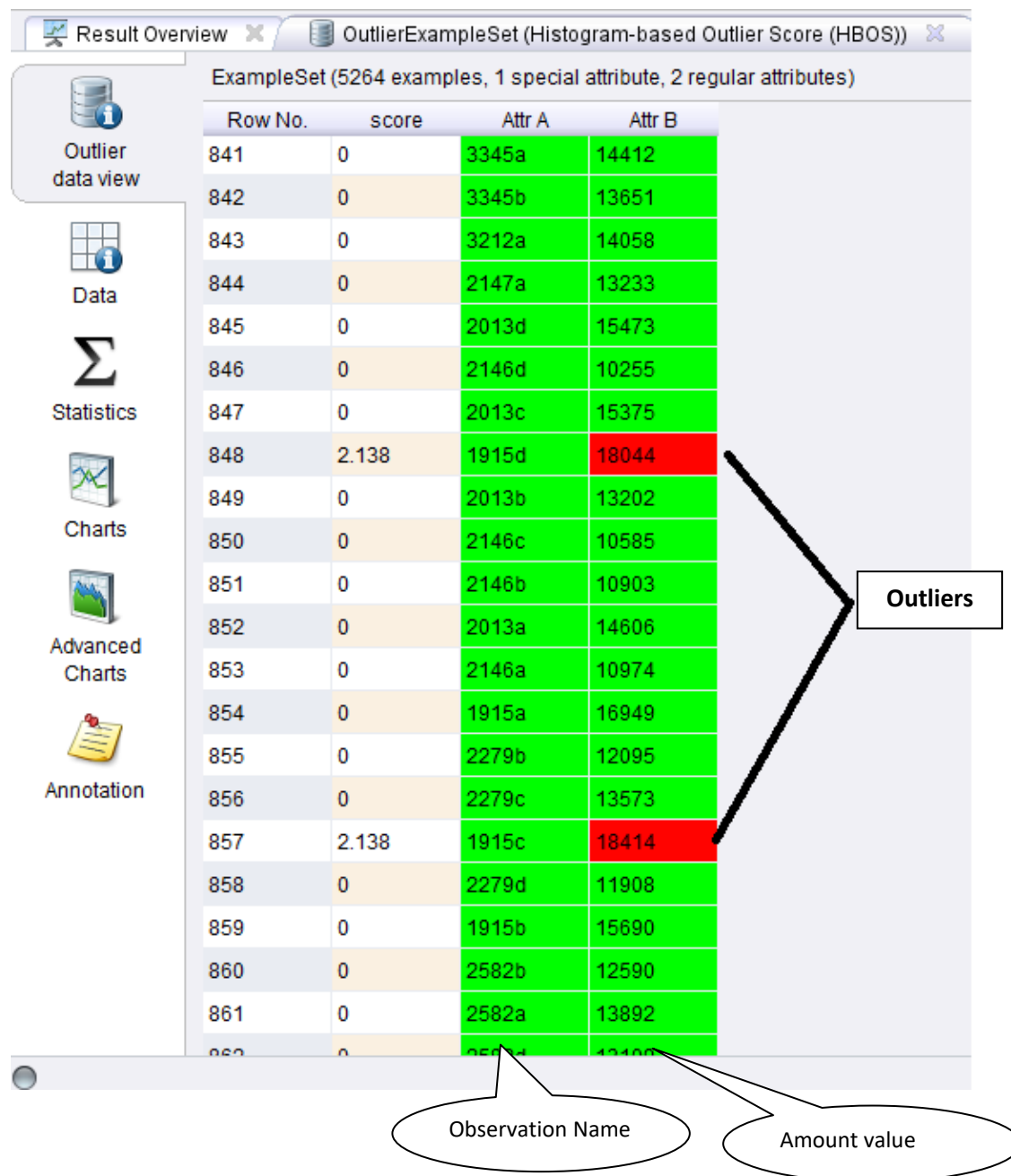


**Figure 24 : Result outlier in Rapidminer**



### Outliers by Statistical Based: Histogram Based Outlier Score (HBOS):

**Criteria:** anomalies have a high score and normal examples a low score



**Figure 25: outlier in Rapidminer**

**Example 2 :**

1	Observation	Amount value		
2	2925d	12750.0		
3	2925c	14187.0		
4	2707d	10151.0		
5	2925b	12982.0		
6	495a	15576.0		
7	495b	14908.0		
8	495c	15184.0		
9	2925a	13352.0		
10	2707b	10160.0		
11	495d	13846.0		
12	580a	11753.0		
13	2707c	10846.0		
14	580b	11427.0		
15	580c	12881.0		
16	2707a	11203.0		
17	580d	12523.0		Level2_Bin1
18	3023c	11777.0		
19	3023b	12260.0		
20	3023d	13208.0		
21	3023a	13059.0		
22	496a	14557.0		
23	496b	13463.0		

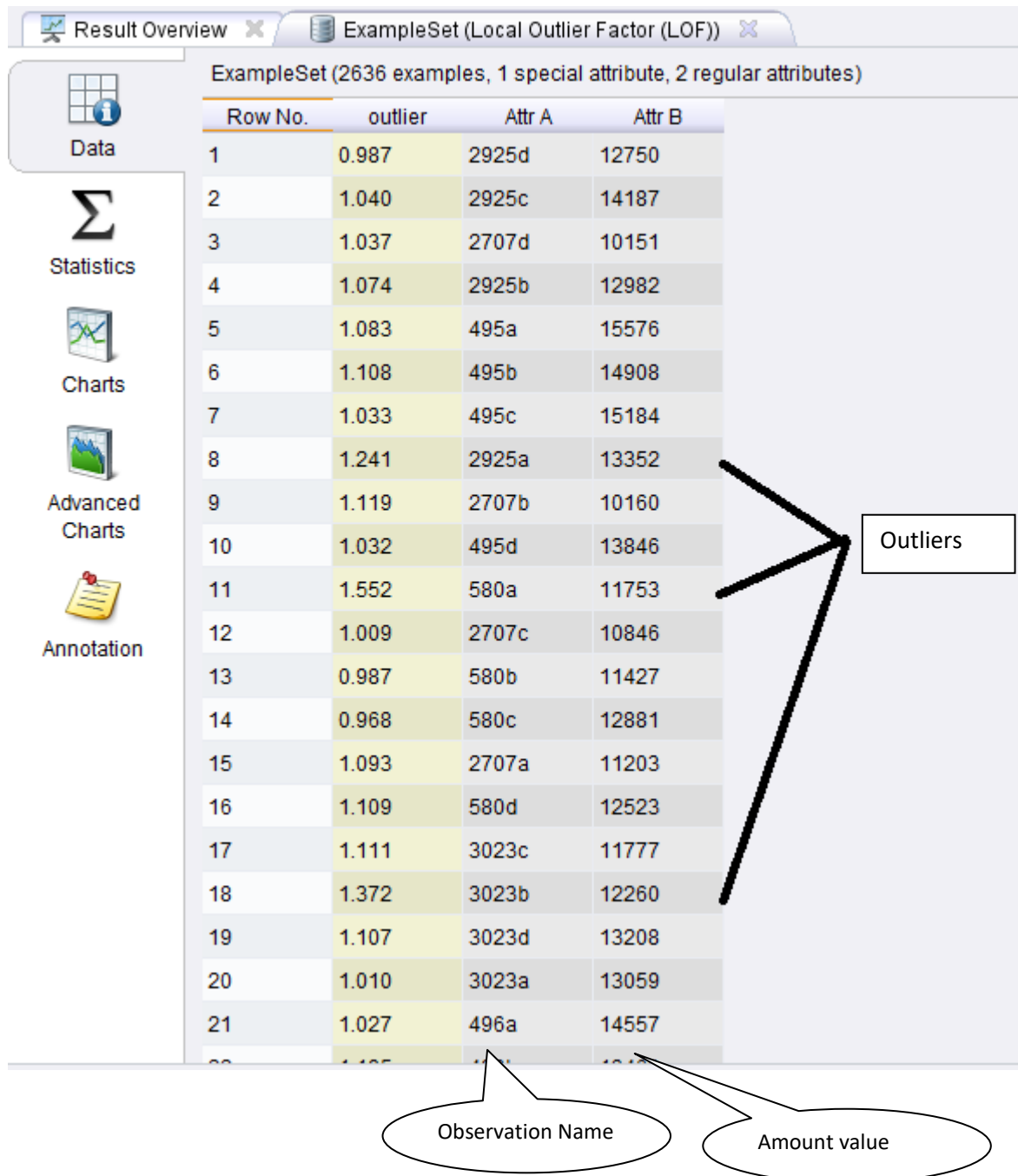
Observation Name

Amount value

**Figure 26: Data Sample**

### Outliers by Nearest Neighbor Based: Local Outlier Factor (LOF):

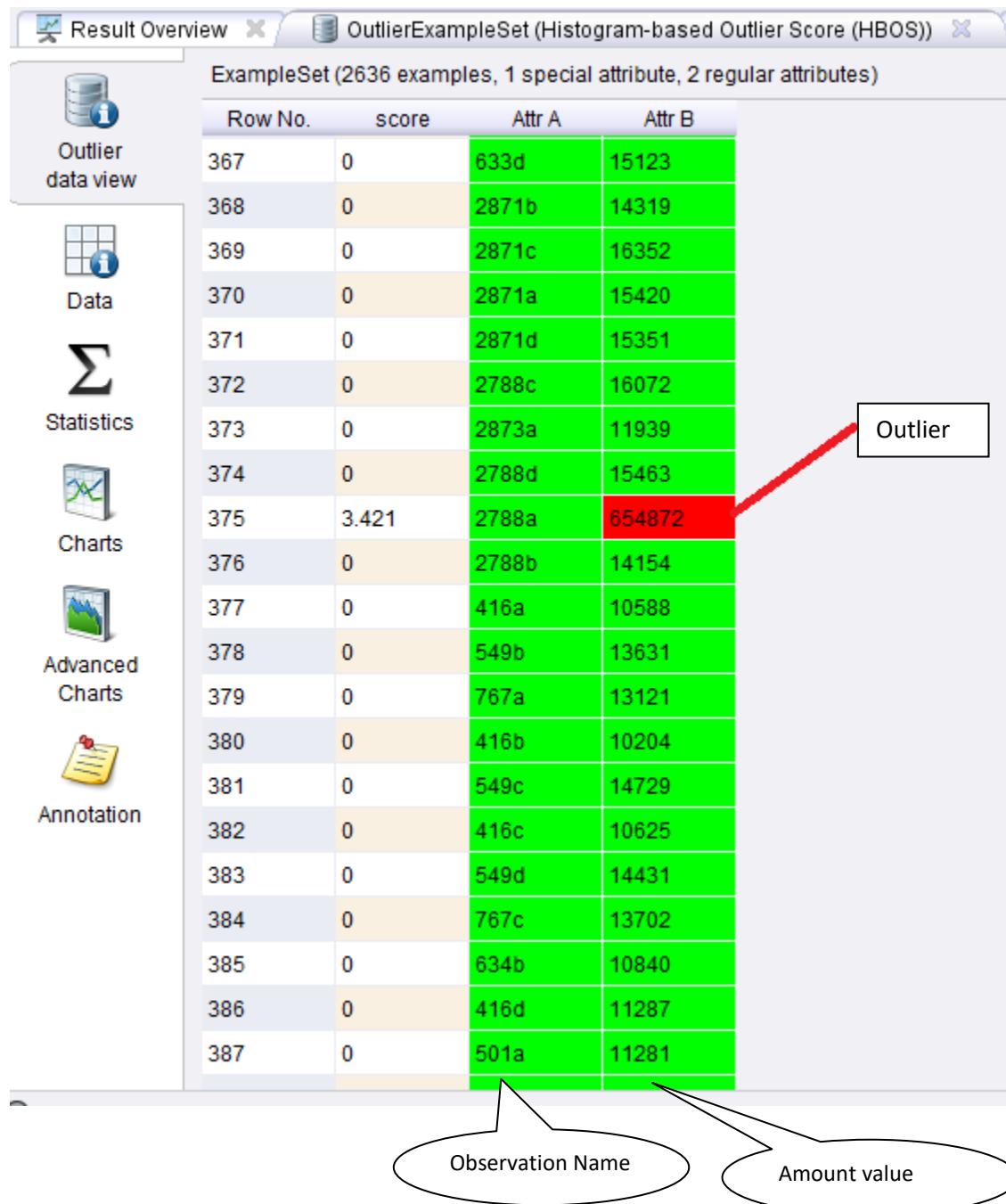
Criteria : Outliers have values greater than 1



**Figure 27: result outlier in Rapidminer**

## Outliers by Statistical Based: Histogram Based Outlier Score (HBOS):

**Criteria:** anomalies have a high score and normal examples a low score



**Figure 28:results outlier in Rapidminer**

Comparing outlier methods in Rapidminer	
Local Outlier Factor (LOF)	Histogram Based Outlier Score (HBOS)
❖ Outliers have values greater than 1.	❖ anomalies have a high score and normal examples a low score
❖ LOF is able to identify outliers in a data set that would not be outliers in another area of the data set.	❖ The histogram based outlier detection approach is typically applied when the data has a single feature.
❖ It has experimentally been shown to work very well in numerous setups, often outperforming the competitors	❖ Histogram based detection methods are simple to implement and hence are quite popular in domain such as intrusion detection
❖ LOF family of methods can be easily generalized and then applied to various other problems, such as detecting outliers in geographic data	❖ Frequency (relative amount) of samples in a bin is used as density estimation
❖ Local outlier detection reconsidered: a generalized view on locality with applications to spatial, video, and network outlier detection	❖ Assumes independence of features similar to Naive Bayes

We can not that each method follows special process and depends on different assumption to specify the outliers in data set and that make us sure about idea that clear different outlier methods are not necessary the same outlier values, sometimes we can have matched in outlier value or outer result by methods are subset of outlier results other method .

Comparing outlier methods in Rapidminer					
Local Outlier Factor (LOF)			Histogram Based Outlier Score (HBOS)		
outlier	Attr A	Attr B	score	Attr A	Attr B
0.987	2925d	12750	0	633d	15123
1.040	2925c	14187	0	2871b	14319
1.037	2707d	10151	0	2871c	16352
1.074	2925b	12982	0	2871a	15420
1.083	495a	15576	0	2871d	15351
1.108	495b	14908	0	2788c	16072
1.033	495c	15184	0	2873a	11939
1.241	2925a	13352	0	2788d	15463
1.119	2707b	10160	3.421	2788a	654872
1.032	495d	13846	0	2788b	14154
1.552	580a	11753	0	416a	10588
1.009	2707c	10846	0	549b	13631
0.987	580b	11427	0	767a	13121
0.968	580c	12881	0	416b	10204
1.093	2707a	11203	0	549c	14729
1.109	580d	12523	0	416c	10625
1.111	3023c	11777	0	549d	14431
1.372	3023b	12260			

❖ LoF gave use outlier score for each value then we make negotiation choose the outlier depending on the criteria “Outliers have values greater than 1”.

❖ HBOS use the score and clearly, we get the outlier depending on the criteria anomalies have a high score and normal examples a low score.

## **6 Conclusion:**

Most real-world data sets contain outliers that have unusually large or small values when compared to others in the data set. Outliers may cause a negative effect on data analyses, or may provide useful information about data when we look into an unusual response to a given study. There are some important points that have to be considered :

- Different methods are based on different assumptions to model outliers.
- Different models consider outliers at different resolutions.

Basically, a key question arises as to how the effectiveness of an outlier detection algorithm should be evaluated. Unfortunately, this is often a difficult task, because outliers, by definition, are rare. This means that the ground-truth about which data points are outliers, is often not available. This is especially true for unsupervised algorithms, because if the ground-truth were indeed available, it could have been used to create a more effective supervised algorithm. For instance, In the unsupervised scenario (without ground-truth), it is often the case, that no realistic quantitative methods can be used in order to judge the effectiveness of the underlying algorithms in a rigorous way. Therefore, much of the research literature uses case studies in order to provide an intuitive and qualitative evaluation of the underlying outliers in unsupervised scenarios. In some cases, the data sets may be adapted from imbalanced classification problems, and the rare labels may be used as surrogates for the ground truth outliers. On the other hand, if the algorithm declares too many data points as outliers, then it will lead to too many false positives. This tradeoff can be measured in terms of precision. In most practical real-life settings, samples of the outlier generating mechanism are non-existent. Depending on our comparison between many different outlier methods in the project, we can be sure basically that different methods are based on different assumptions to model outliers and different models consider outliers at different resolutions.

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