

$$①) f_1: [a \rightarrow b]$$

$$f_1 \text{ is } a = \text{map } (\lambda f \Rightarrow f a) \text{ is}$$

$$2) f_2 \text{ is Leaf} = []$$

$$f_2 \text{ is } (\text{Node } l \text{ } r) = f_2 \text{ l } ++ (f_2 \text{ r} : f_2 \text{ l } r)$$

$$3) q_5 [] = []$$

$$q_5 (x:xs) = (q_5 [a | a \leftarrow xs, a \leq x]) ++ [x] ++$$

$$(q_5 [a | a \leftarrow xs, a > x])$$

$$4) f_4 \text{ is } f g x = f x (g x)$$

$$5) f_5 \text{ is } f g x = f (\lambda a \Rightarrow g a x) x$$

✍

② 1) $(2x.xx)(2x.xx) = \Omega$

Can not be normalized, because each reduction step doesn't change term.

$$\Omega \xrightarrow{\beta} \Omega$$

2) $(2x.xxx)(2x.xxx)$

Can not be normalized, because grows after each ~~each~~ each β -reduction step.

$$(2x.xxx)(2x.xxx) \xrightarrow{\beta^n} \underbrace{(2x.xxx) \dots (2x.xxx)}_{n+2}$$

3)

③ 1) Int isomorphic to Nat, and
 Nat isomorphic to $L()$
 ($n \Leftrightarrow$ list of length n)

2) 4) Either a (Either b (c, d))
 isomorphic to
 Either (c, d) (Either a b)

Because

Left $x \Rightarrow$ Right (Left x)

Right (Left x) \Rightarrow Right (Right x)

Right (Right x) \Rightarrow Left x

5) $(a \Rightarrow b, a \Rightarrow c)$ isomorphic to
 $(a, a) \Rightarrow (b, c)$

Because

$(f, g) \Leftrightarrow \lambda (x, y) \rightarrow (f x, g y)$

3) iso \nmid We can think about List as abt
 a mapping $\# \text{Nat} \rightarrow a$. Also $\text{Nat} \Leftrightarrow \text{Int}$
 \Rightarrow List a isomorphic to Map Int a

2) \nmid figured out only primitive example
 of Either $()$ (Tree $a, a, \text{Tree } a$)