Lightweight Multi-Objective Evolutionary Neural Architecture Search with Low-Cost Proxy Metrics (Supplementary Material)

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In this Supplementary, we report the results of the following multi-objective evolutionary neural architecture search (MOENAS) approaches on the NAS-Bench-101 and NAS-Bench-201 benchmarks. The details of all methods are listed in Table 1:

Table 1: List of MOENAS methods.

Algorithm	Performance metric	Search method
NSGA-II (val_error)	Validation error rate at the 12-th epoch	Training-based
$\operatorname{NSGA-II}\left(\mathtt{val_loss}\right)$	Validation loss at the 12-th epoch	Training-based
$\operatorname{NSGA-II} (\mathtt{train_loss})$	Training loss at the 12-th epoch [9]	Training-based
MOENAS-PSI	Validation error rate at the 12-th epoch	Training-based
MOENAS-TF-PSI	Validation error rate at the 12-th epoch	Training-based
ENAS-TFI	Validation error rate at the 12-th epoch	Training-based
$\operatorname{NSGA-II}$ (synflow)	Synaptic Flow (synflow) [10]	Training-free
NSGA-II (jacov)	Jacobian Covariance (jacov) [5]	Training-free
$\operatorname{NSGA-II}$ (snip)	SNIP [3]	Training-free
$\operatorname{NSGA-II}\left(\operatorname{\texttt{grad_norm}}\right)$	Gradient Norm [1]	Training-free
$\operatorname{NSGA-II}\left(\mathtt{grasp}\right)$	Gradient Signal Preservation [12]	Training-free
$\operatorname{NSGA-II}$ (fisher)	Fisher [11]	Training-free
$\operatorname{NSGA-II}$ (synflow+jacov)	Sum of synflow and jacov	Training-free
	Sum of:	
NGCA II (I G.I D. 1 :)	• Logarithm of synflow	Theiring free
NSGA-II (LS+LR+skip)	• Linear Regions (also known as naswot [4])	Training-free
	• #skipped layers #skip connections in a cell [2]	
E-TF-MOENAS (ours)	synflow and jacov	Training-free

1. Additional results on NAS-Bench-101

In this section, we present the performance of MOENAS approaches on the problem instances created on NAS-Bench-101. Regarding the evaluation of the obtained architectures in terms of test error rate and FLOPs, Figure 1 and Table 3 indicate that our method E-TF-MOENAS significantly outperforms other

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training-free methods at both Inverted Generational Distance (IGD) and Hypervolume (HV) indicators. Compared to training-based competitors, E-TF-MOENAS is also significantly better in terms of IGD but is slightly worse in terms of HV. However, we note that the search cost of E-TF-MOENAS is less than approximately 30 times the search cost of training-based methods.

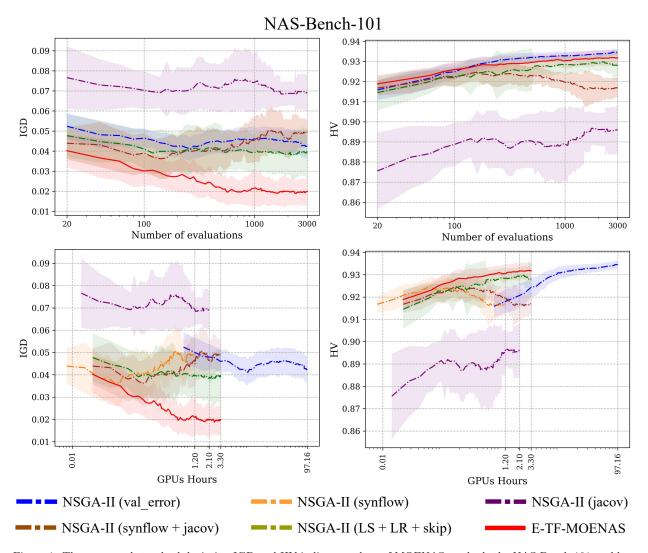


Figure 1: The mean and standard deviation IGD and HV indicator values of MOENAS methods the NAS-Bench-101 problem that minimizes the test error rate and FLOPs. The horizontal axis (log scale): the number of evaluations (Above); the GPUs hours (Below).

Table 2 contains the IGD and HV results for the obtained approximation fronts of architectures evaluated in terms of test error rate and the number of parameters. Table 3 contains the IGD and HV results for the obtained approximation fronts of architectures evaluated in terms of test error rate and FLOPs.

2. More results on NAS-Bench-201

On NAS-Bench-201, besides the MONAS problem formulation that optimizes the test error rate and FLOPs, we additionally create two problem instances by replacing the FLOPs with the number of parameters and latency:

- Figure 2 and Table 4 present the IGD and HV results of MOENAS methods optimizing test error rate and number of parameters.
- Table 5 presents the IGD and HV results of MOENAS methods optimizing test error rate and FLOPs.
- Figure 3 and Table 6 present the IGD and HV results of MOENAS methods optimizing test error rate and latency.

Similar to the results achieved on NAS-Bench-101, Figure 2, Figure 3, Table 4, and Table 6 indicate that E-TF-MOENAS also outperforms other training-free methods. For training-based methods, E-TF-MOENAS is only worse than NSGA-II (train_loss) at only the IGD value (for the problem optimizing the number of parameters, see Table 4) or the HV (for the problem optimizing the latency, see Table 6). On the other hand, our method is significantly better than the remaining training-based methods at both IGD and HV values.

Regarding the transferability of the obtained architectures, experimental results are reported in the following tables:

- Table 7 presents the transferred IGD and HV values with respect to test error rate and number of parameters.
- Table 8 presents the transferred IGD and HV values with respect to test error rate and FLOPs.
- Table 9 presents the transferred IGD and HV values with respect to test error rate and latency.

We verify the transferability of architectures obtained by MOENAS methods when searching on CIFAR-10 by re-evaluating them on CIFAR-100 and ImageNet16-120. Table 7 and Table 9 exhibit the superior transferability of E-TF-MOENAS since our method is significantly better than the other approaches at both IGD and HV metric values.

Table 2: The search time and the final IGD & HV values (mean \pm standard deviation) of MOENAS methods on the MONAS problem instance created on NAS-Bench-101 that minimizes the test error rate and the number of parameters. Bold results indicate statistical significance.

Algorithm	IGD*	HV**	Search Cost (sec.)			
Training-based						
NSGA-II (val_error)	0.0427 ± 0.0071	0.8984 ± 0.0024	349,760			
MOENAS-PSI [6, 8]	0.0410 ± 0.0075	0.8987 ± 0.0026	355,304			
MOENAS-TF-PSI [8]	0.0409 ± 0.0079	$\bf 0.8994 \pm 0.0027$	346,471			
ENAS-TFI [7]	0.0384 ± 0.0067	$\boldsymbol{0.9001 \pm 0.0021}^{\dagger}$	366,664			
	Training-free					
NSGA-II (synflow)	0.0479 ± 0.0075	0.8710 ± 0.0092	3347			
NSGA-II (jacov)	0.0722 ± 0.0064	0.8354 ± 0.0242	2001			
NSGA-II (snip)	0.0945 ± 0.0084	0.7632 ± 0.0124	1992			
NSGA-II (grad_norm)	0.0974 ± 0.0072	0.7695 ± 0.0109	2124			
NSGA-II (grasp)	0.0906 ± 0.0151	0.8064 ± 0.0261	11,322			
$\operatorname{NSGA-II}$ (fisher)	0.0868 ± 0.0049	0.8042 ± 0.0138	2476			
NSGA-II (synflow+jacov)	0.0480 ± 0.0079	0.8736 ± 0.0074	7268			
NSGA-II (LS+LR+skip)	0.0389 ± 0.0109	0.8898 ± 0.0088	7583			
E-TF-MOENAS (ours)	$0.0188 \pm 0.0052^{\dagger}$	0.8952 ± 0.0040	5709			

[†] indicates the best result of each problem instance.

 $^{^{\}ast}$ For IGD values, the lesser the better.

^{**} For HV values, the greater the better.

Table 3: The search time and the final IGD & HV values (mean \pm standard deviation) of MOENAS methods on the MONAS problem instance created on NAS-Bench-101 that minimizes the test error rate and FLOPs. Bold results indicate statistical significance.

Algorithm IGD*		HV**	Search Cost (sec.)			
Training-based						
NSGA-II (val_error)	349, 584					
MOENAS-PSI [6, 8]	0.0447 ± 0.0065	0.9336 ± 0.0016	356, 196			
MOENAS-TF-PSI [8]	0.0414 ± 0.0074	0.9348 ± 0.0019	354,834			
ENAS-TFI [7]	0.0375 ± 0.0047	$0.9361\pm0.0008^\dagger$	370, 156			
	Training-free					
NSGA-II (synflow)	0.0495 ± 0.0070	0.9169 ± 0.0046	4316			
NSGA-II (jacov)	0.0691 ± 0.0088	0.8959 ± 0.0117	7570			
NSGA-II (snip)	0.0927 ± 0.0072	0.8416 ± 0.0068	6095			
NSGA-II (grad_norm)	0.0961 ± 0.0078	0.8506 ± 0.0086	6117			
NSGA-II (grasp)	0.0957 ± 0.0143	0.8674 ± 0.0170	16,720			
NSGA-II (fisher)	0.0858 ± 0.0049	0.8721 ± 0.0096	7840			
NSGA-II (synflow+jacov)	0.0495 ± 0.0070	0.9169 ± 0.0046	11,879			
NSGA-II (LS+LR+skip)	0.0392 ± 0.0122	0.9281 ± 0.0072	11,878			
E-TF-MOENAS (ours)	$0.0199 \pm 0.0070^\dagger$	0.9318 ± 0.0034	11,882			

[†] indicates the best result of each problem instance. * For IGD values, the lesser the better. ** For HV values, the greater the better.

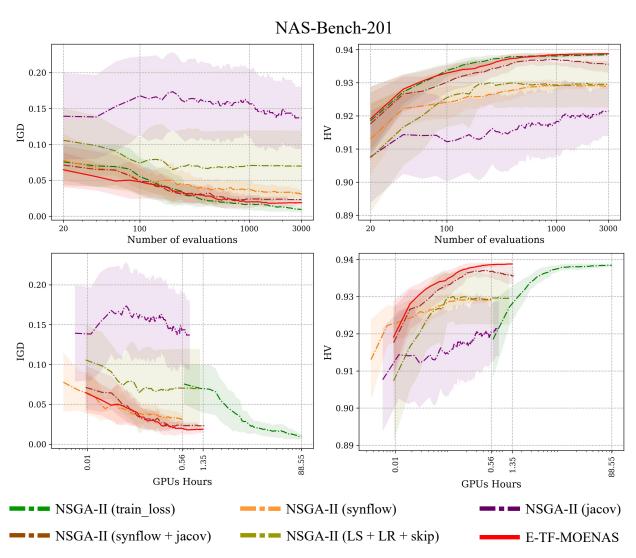


Figure 2: The mean and standard deviation IGD and HV indicator values of MOENAS methods on the NAS-Bench-201 problem instance that minimizes the test error rate and the number of parameters. The horizontal axis (log scale): the number of evaluations (Above); the GPUs hours (Below).

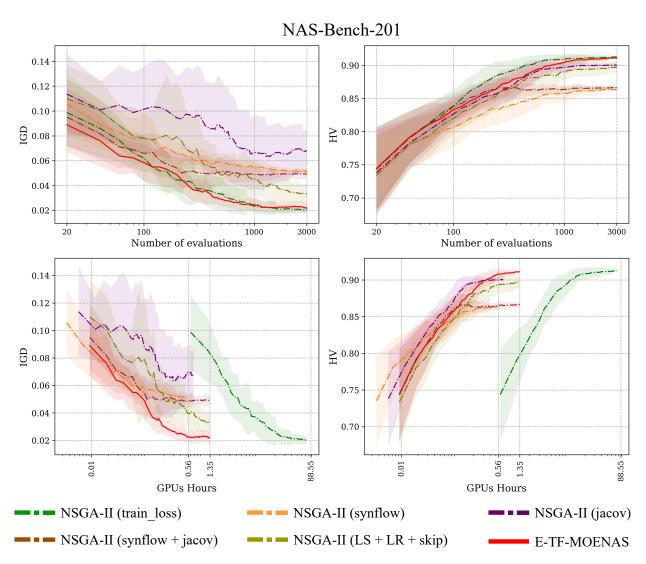


Figure 3: The mean and standard deviation IGD and HV indicator values of MOENAS methods on the NAS-Bench-201 problem instance that minimizes the test error rate and the latency. The horizontal axis (log scale): the number of evaluations (Above); the GPUs hours (Below).

Table 4: The search time and the final IGD & HV values (mean \pm standard deviation) of MOENAS methods on the MONAS problem instance created on NAS-Bench-201 that minimizes the test error rate and the number of parameters. Bold results indicate statistical significance.

Algorithm	IGD^*	HV**	Search Cost (sec.)		
Training-based					
NSGA-II (val_error)	0.0453 ± 0.0130	0.9352 ± 0.0012	275, 802		
NSGA-II (val_loss)	0.0495 ± 0.0098	0.9346 ± 0.0011	279,604		
NSGA-II (train_loss)	$\boldsymbol{0.0094 \pm 0.0037^{\dagger}}$	0.9384 ± 0.0004	318,782		
MOENAS-PSI [6, 8]	0.0495 ± 0.0182	0.9347 ± 0.0024	275,836		
MOENAS-TF-PSI [8]	0.0431 ± 0.0131	0.9353 ± 0.0011	284,170		
ENAS-TFI [7]	0.0439 ± 0.0139	0.9353 ± 0.0013	280,058		
Training-free					
NSGA-II (synflow)	0.0312 ± 0.0050	0.9290 ± 0.0008	2016		
NSGA-II (jacov)	0.1370 ± 0.0434	0.9213 ± 0.0074	2785		
NSGA-II (snip)	0.2402 ± 0.0009	0.8675 ± 0.0022	2906		
NSGA-II (grad_norm)	0.2389 ± 0.0005	0.8708 ± 0.0012	2893		
NSGA-II (grasp)	0.2387 ± 0.0006	0.8718 ± 0.0012	8317		
NSGA-II (fisher)	0.2409 ± 0.0031	0.8680 ± 0.0012	2971		
NSGA-II (synflow+jacov)	0.0232 ± 0.0010	0.9356 ± 0.0025	5199		
NSGA-II (LS+LR+skip)	0.0698 ± 0.0494	0.9295 ± 0.0070	4290		
E-TF-MOENAS (ours)	0.0187 ± 0.0046	$0.9388 \pm 0.0004^\dagger$	4876		

 $^{^\}dagger$ indicates the best result of each problem instance. * For IGD values, the lesser the better. ** For HV values, the greater the better.

Table 5: The search time and the final IGD & HV values (mean \pm standard deviation) of MOENAS methods on the MONAS problem instance created on NAS-Bench-201 that minimizes the test error rate and the FLOPs. Bold results indicate statistical significance.

Algorithm	IGD*	HV**	Search Cost (sec.)		
Training-based					
NSGA-II (val_error)	0.0474 ± 0.0112	0.8891 ± 0.0013	276, 168		
NSGA-II (val_loss)	0.0502 ± 0.0082	0.8885 ± 0.0012	278,753		
$NSGA$ -II (train_loss)	$\boldsymbol{0.0083 \pm 0.0028}^\dagger$	0.8930 ± 0.0004	318,207		
MOENAS-PSI [6, 8]	0.0490 ± 0.0180	0.8887 ± 0.0027	275,397		
MOENAS-TF-PSI [8]	0.0464 ± 0.0126	0.8893 ± 0.0015	283,849		
ENAS-TFI [7]	0.0454 ± 0.0117	0.8892 ± 0.0013	284,296		
Training-free					
NSGA-II (synflow)	0.0479 ± 0.0075	0.8710 ± 0.0092	3347		
NSGA-II (jacov)	0.0722 ± 0.0064	0.8354 ± 0.0242	2001		
NSGA-II (snip)	0.0945 ± 0.0084	0.7632 ± 0.0124	1992		
NSGA-II (grad_norm)	0.0974 ± 0.0072	0.7695 ± 0.0109	2124		
NSGA-II (grasp)	0.0906 ± 0.0151	0.8064 ± 0.0261	11,322		
NSGA-II (fisher)	0.0868 ± 0.0049	0.8042 ± 0.0138	2476		
NSGA-II (synflow+jacov)	0.0305 ± 0.0116	0.8828 ± 0.0021	9961		
NSGA-II (LS+LR+skip)	0.0795 ± 0.0553	0.8821 ± 0.0084	8622		
E-TF-MOENAS (ours)	0.0113 ± 0.0043	$0.8932 \pm 0.0006^\dagger$	9671		

 $^{^\}dagger$ indicates the best result of each problem instance. * For IGD values, the lesser the better. ** For HV values, the greater the better.

Table 6: The search time and the final IGD & HV values (mean \pm standard deviation) of MOENAS methods on the MONAS problem instance created on NAS-Bench-201 that minimizes the test error rate and the latency. Bold results indicate statistical significance.

Algorithm	IGD^*	HV**	Search Cost (sec.)		
Training-based					
NSGA-II (val_error)	0.0634 ± 0.0185	0.9088 ± 0.0008	238,946		
NSGA-II (val_loss)	0.0666 ± 0.0165	0.9027 ± 0.0029	239,030		
$\operatorname{NSGA-II}$ (train_loss)	$0.0204\pm0.0028^\dagger$	$\boldsymbol{0.9127 \pm 0.0004^\dagger}$	269, 185		
MOENAS-PSI [6, 8]	0.0586 ± 0.0207	0.9091 ± 0.0009	235, 250		
MOENAS-TF-PSI [8]	0.0627 ± 0.0159	0.9091 ± 0.0005	238,324		
ENAS-TFI [7]	0.0570 ± 0.0202	0.9092 ± 0.0007	240,965		
Training-free					
NSGA-II (synflow)	0.0514 ± 0.0011	0.8636 ± 0.0021	1935		
NSGA-II (jacov)	0.0679 ± 0.0170	0.9003 ± 0.0027	2465		
NSGA-II (snip)	0.0750 ± 0.0258	0.8855 ± 0.0128	2807		
NSGA-II (grad_norm)	0.0683 ± 0.0269	0.8720 ± 0.0176	2818		
NSGA-II (grasp)	0.0760 ± 0.0342	0.8870 ± 0.0106	7493		
NSGA-II (fisher)	0.0761 ± 0.0360	0.8869 ± 0.0132	2844		
NSGA-II (synflow+jacov)	0.0495 ± 0.0042	0.8665 ± 0.0035	4931		
NSGA-II (LS+LR+skip)	0.0332 ± 0.0080	0.8972 ± 0.0081	4771		
E-TF-MOENAS (ours)	0.0219 ± 0.0043	0.9112 ± 0.0007	4793		

[†] indicates the best result of each problem instance. * For IGD values, the lesser the better. ** For HV values, the greater the better.

Table 7: The transfer results on the NAS-Bench-201 problems with respect to the test error rate and the number of parameters. The NAS runs are conducted on the CIFAR-10 dataset and the found architectures are then transferred to the CIFAR-100 and ImageNet-16-120 datasets. Bold results indicate statistical significance.

Algorithm	CIFAR-100		ImageNet16-120	
	IGD*	HV**	IGD^*	HV**
NSGA-II (val_error)	0.0732 ± 0.0238	0.7202 ± 0.0043	0.0535 ± 0.0147	0.4711 ± 0.0050
$NSGA-II (val_loss)$	0.0846 ± 0.0168	0.7192 ± 0.0038	0.0603 ± 0.0101	0.4693 ± 0.0050
$\operatorname{NSGA-II} (\mathtt{train_loss})$	0.0288 ± 0.0092	0.7350 ± 0.0006	0.0319 ± 0.0041	0.4875 ± 0.0015
MOENAS-PSI	0.0781 ± 0.0254	0.7191 ± 0.0064	0.0555 ± 0.0190	0.4698 ± 0.0081
MOENAS-TF-PSI	0.0704 ± 0.0266	0.7207 ± 0.0041	0.0564 ± 0.0126	0.4704 ± 0.0050
ENAS-TFI	0.0732 ± 0.0241	0.7207 ± 0.0046	0.0541 ± 0.0164	0.4705 ± 0.0055
$\operatorname{NSGA-II}$ (synflow)	0.0320 ± 0.0028	0.7216 ± 0.0009	0.0249 ± 0.0045	0.4793 ± 0.0016
NSGA-II (jacov)	0.1587 ± 0.0382	0.7073 ± 0.0108	0.1115 ± 0.0331	0.4579 ± 0.0148
$\operatorname{NSGA-II}$ (snip)	0.2846 ± 0.0075	0.5993 ± 0.0111	0.3397 ± 0.0289	0.2335 ± 0.0279
NSGA-II (grad_norm)	0.2811 ± 0.0036	0.6047 ± 0.0055	0.2926 ± 0.0201	0.2824 ± 0.0231
NSGA-II (grasp)	0.2889 ± 0.0036	0.5956 ± 0.0059	0.3250 ± 0.0142	0.2478 ± 0.0182
NSGA-II (fisher)	0.2781 ± 0.0039	0.6093 ± 0.0059	0.3499 ± 0.0291	0.2263 ± 0.0313
NSGA-II (synflow+jacov)	0.0447 ± 0.0016	0.7299 ± 0.0033	0.0180 ± 0.0016	0.4842 ± 0.0010
NSGA-II (LS+LR+skip)	0.0908 ± 0.0600	0.7171 ± 0.0136	0.0679 ± 0.0476	0.4675 ± 0.0186
E-TF-MOENAS (ours)	$0.0089 \pm 0.0050^\dagger$	$0.7365 \pm 0.0008^\dagger$	$0.0141 \pm 0.0063^\dagger$	$0.4887 \pm 0.0009^\dagger$

 $^{^{\}dagger}$ indicates the best result of each problem in stance.

Table 8: The transfer results on the NAS-Bench-201 problems with respect to the test error rate and the FLOPs. The NAS runs are conducted on the CIFAR-10 dataset and the found architectures are then transferred to the CIFAR-100 and ImageNet-16-120 datasets. Bold results indicate statistical significance.

Algorithm	CIFAR-100		ImageN	et16-120
	IGD*	HV**	IGD^*	HV**
NSGA-II (val_error)	0.0768 ± 0.0221	0.6679 ± 0.0040	0.0545 ± 0.0131	0.3999 ± 0.0045
$NSGA-II (val_loss)$	0.0853 ± 0.0123	0.6668 ± 0.0034	0.0609 ± 0.0067	0.3976 ± 0.0045
NSGA-II (train_loss)	0.0298 ± 0.0096	0.6835 ± 0.0006	0.0313 ± 0.0048	0.4169 ± 0.0014
MOENAS-PSI	0.0761 ± 0.0264	0.6675 ± 0.0067	0.0548 ± 0.0200	0.3988 ± 0.0085
MOENAS-TF-PSI	0.0749 ± 0.0246	0.6681 ± 0.0048	0.0533 ± 0.0140	0.3998 ± 0.0050
ENAS-TFI	0.0754 ± 0.0226	0.6688 ± 0.0040	0.0545 ± 0.0142	0.3992 ± 0.0051
NSGA-II (synflow)	0.0328 ± 0.0146	0.6698 ± 0.0028	0.0281 ± 0.0105	0.4084 ± 0.0032
NSGA-II (jacov)	0.1975 ± 0.0469	0.6452 ± 0.0168	0.1548 ± 0.0470	0.3700 ± 0.0254
NSGA-II (snip)	0.1716 ± 0.0415	0.5767 ± 0.0123	0.2296 ± 0.0397	0.2323 ± 0.0274
NSGA-II (grad_norm)	0.1780 ± 0.0496	0.5707 ± 0.0196	0.2356 ± 0.0482	0.2279 ± 0.0359
NSGA-II (grasp)	0.2329 ± 0.0580	0.5606 ± 0.0224	0.2479 ± 0.0413	0.2314 ± 0.0257
NSGA-II (fisher)	0.2480 ± 0.0331	0.5469 ± 0.0039	0.2428 ± 0.0273	0.2299 ± 0.0153
NSGA-II (synflow+jacov)	0.0319 ± 0.0107	0.6692 ± 0.0032	0.0270 ± 0.0094	0.4079 ± 0.0035
NSGA-II (LS+LR+skip)	0.0998 ± 0.0652	0.6641 ± 0.0154	0.0733 ± 0.0536	0.3947 ± 0.0195
E-TF-MOENAS (ours)	$0.0101 \pm 0.0076^\dagger$	$\boldsymbol{0.6844 \pm 0.0012^{\dagger}}$	$0.0165 \pm 0.0081^\dagger$	$0.4189 \pm 0.0018^{\dagger}$

 $^{^{\}dagger}$ indicates the best result of each problem in stance.

^{*} For IGD values, the lesser the better.

 $^{^{\}ast\ast}$ For HV values, the greater the better.

^{*} For IGD values, the lesser the better.

^{**} For HV values, the greater the better.

Table 9: The transfer results on the NAS-Bench-201 problems with respect to the test error rate and the latency. The NAS runs are conducted on the CIFAR-10 dataset and the found architectures are then transferred to the CIFAR-100 and ImageNet- $16\mbox{-}120$ datasets. Bold results indicate statistical significance.

Algorithm	CIFAR-100		ImageN	et16-120
	IGD*	HV**	IGD^*	HV**
NSGA-II (val_error)	0.0903 ± 0.0316	0.6778 ± 0.0030	0.0244 ± 0.0029	0.6455 ± 0.0066
$\operatorname{NSGA-II} (\mathtt{val_loss})$	0.1051 ± 0.0321	0.6677 ± 0.0090	0.0302 ± 0.0056	0.6370 ± 0.0135
$\operatorname{NSGA-II}\left(\mathtt{train_loss}\right)$	0.0369 ± 0.0071	0.6941 ± 0.0020	0.0165 ± 0.0028	0.6737 ± 0.0029
MOENAS-PSI	0.0858 ± 0.0336	0.6791 ± 0.0027	0.0242 ± 0.0039	0.6472 ± 0.0077
MOENAS-TF-PSI	0.1024 ± 0.0295	0.6783 ± 0.0013	0.0240 ± 0.0027	0.6444 ± 0.0059
ENAS-TFI	0.0890 ± 0.0353	0.6794 ± 0.0025	0.0232 ± 0.0030	0.6462 ± 0.0064
$\operatorname{NSGA-II}$ (synflow)	0.0802 ± 0.0062	0.6331 ± 0.0071	0.0547 ± 0.0022	0.6558 ± 0.0010
NSGA-II (jacov)	0.0768 ± 0.0151	0.6605 ± 0.0048	0.0397 ± 0.0067	0.6159 ± 0.0171
NSGA-II (snip)	0.0755 ± 0.0143	0.6412 ± 0.0067	0.0578 ± 0.0053	0.5694 ± 0.0065
NSGA-II (grad_norm)	0.0885 ± 0.0180	0.6268 ± 0.0124	0.0807 ± 0.0256	0.5388 ± 0.0484
NSGA-II (grasp)	0.0857 ± 0.0224	0.6480 ± 0.0119	0.0709 ± 0.0194	0.5613 ± 0.0421
NSGA-II (fisher)	0.0901 ± 0.0263	0.6461 ± 0.0116	0.0636 ± 0.0205	0.5606 ± 0.0384
NSGA-II (synflow+jacov)	0.0608 ± 0.0064	0.6521 ± 0.0060	0.0376 ± 0.0061	0.6622 ± 0.0017
NSGA-II (LS+LR+skip)	0.0583 ± 0.0116	0.6671 ± 0.0121	0.0442 ± 0.0091	0.6651 ± 0.0052
E-TF-MOENAS (ours)	$0.0301 \pm 0.0036^\dagger$	$0.6903 \pm 0.0017^\dagger$	$0.0155 \pm 0.0026^\dagger$	$0.6741 \pm 0.0010^{\dagger}$

 $^{^\}dagger$ indicates the best result of each problem instance. * For IGD values, the lesser the better. ** For HV values, the greater the better.

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