

## 4 Integer Representation

4.1 write  $(10001010111)_2$  in base 10

$$\begin{aligned}\text{first we calculate } & (1 \cdot 2^{10} + 1 \cdot 2^6 + 1 \cdot 2^4 + 1 \cdot 2^2 + 1 \cdot 2^1 + 1 \cdot 2^0) \\ & = (1024 + 64 + 16 + 4 + 2 + 1) \\ & = \underline{\underline{1111}}\end{aligned}$$

$$\underline{\underline{(10001010111)_2 = (1111)_{10}}}$$

4.2

first we convert  $(1032113)_4$  to base 10

$$1 \cdot 4^6 + 3 \cdot 4^4 + 2 \cdot 4^3 + 1 \cdot 4^2 + 1 \cdot 4^1 + 3$$
$$4096 + 768 + 128 + 16 + 4 + 3 = 5015$$

Then we find the binary expansion of  $(5015)_{10}$

$$5015 = 2507 \cdot 2 + 1$$

$$2507 = 1253 \cdot 2 + 1$$

$$1253 = 626 \cdot 2 + 1$$

$$626 = 313 \cdot 2 + 0$$

$$313 = 156 \cdot 2 + 1$$

$$156 = 78 \cdot 2 + 0$$

$$78 = 39 \cdot 2 + 0$$

$$39 = 19 \cdot 2 + 1$$

$$19 = 9 \cdot 2 + 1$$

$$9 = 4 \cdot 2 + 1$$

$$4 = 2 \cdot 2 + 0$$

$$2 = 2 \cdot 1 + 0$$

$$1 = 2 \cdot 0 + 1$$

$$\underline{(1032113)_4 = (10011176010111)_2}$$