

Geography 4203 / 5203

# **GIS & Spatial Modeling**

**Class 4: Raster Analysis I**

# Some Updates

- **Readings discussions**

Reminder: Summaries!!! Submitted BEFORE discussion starts...

- **Labs next week:**

Start (delayed) of lab season as scheduled (M / W 9-11am)

# Last Lecture

- We talked about **raster data** as one form of **tessellation**, their properties and important things you will find when working with them
- These facts are important to understand **storage** limitations, **data types**, **bit depths** and **resolution-related** problems
- In this context the **assignment** of pixel values in classifications or vector-raster conversions can become complex and is crucial

# Last Class Meeting

- Right, and remember the last session which was a readings discussion about the **field-object** debate
- Take some impressions with you from this nice session - we did not come to an end (nobody ever did)
- Keep in mind the different **conceptual model** approaches and their counterparts in different disciplines
- Try to remember what the advantages of field representations are in **modeling**, **error analysis** and **mapping**

# Today's Outline

- We will talk about some important basics of **raster analysis** and **Map Algebra**
- You will hear about the **principles** of Map Algebra as the foundation of **GIS modeling framework**
- We will talk about the single **building blocks** of this **modeling language**: operators, functions, parameters and objects
- This will give you an impression of the **concepts** behind it

# Learning Objectives

- You will learn what **Map Algebra** stands for and what the single components are
- You will have insights into the **functioning** of Map Algebra
- You will understand what **functions** you are going to use, what an **operator** is and how to combine all elements for **iterative** models under **control**

# Some Repitition

## Binary Columns

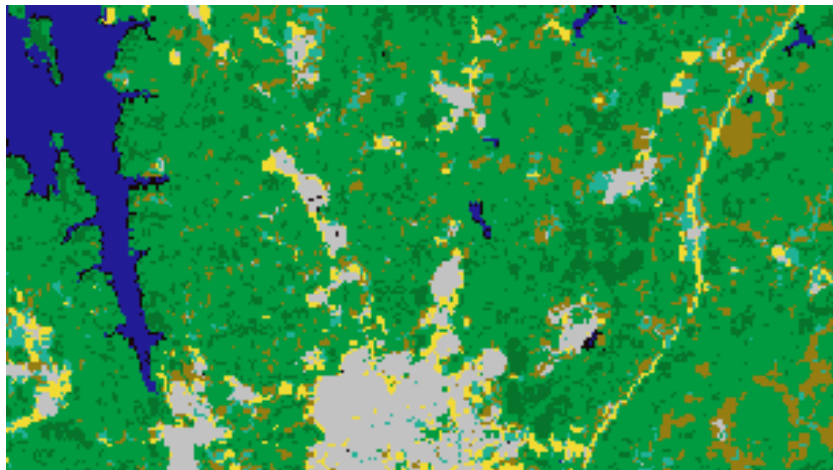
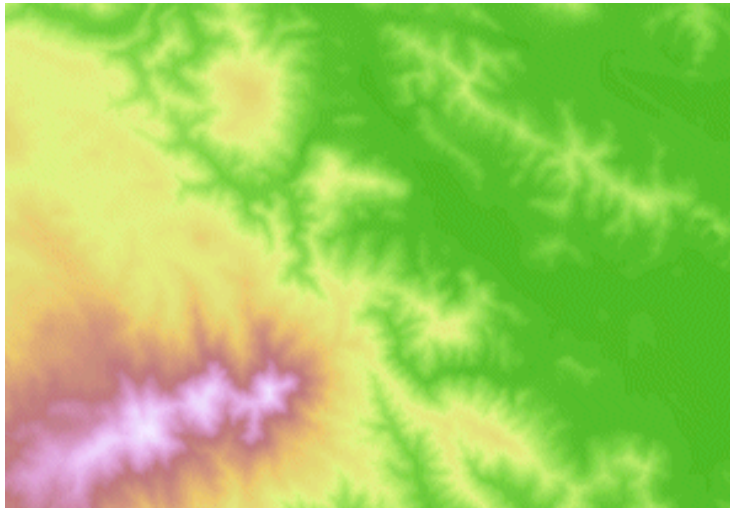
eights column  
fours column  
twos column  
ones column

1 1 0 1

$$8 + 4 + 0 + 1 = 13$$

binary	decimal
00000001	1
00000010	2
00000011	3
00000100	4
00000101	5
00000110	6
00000111	7

00001000	Bit depth	Range of values that each cell can contain
00001001	1 bit	0 to 1
00001010	2 bit	0 to 3
00001011	4 bit	0 to 15
....	Unsigned 8 bit	0 to 255
	Signed 8 bit	-128 to 127
	Unsigned 16 bit	0 to 65535
	Signed 16 bit	-32768 to 32767
	Unsigned 32 bit	0 to 4294967295
	Signed 32 bit	-2147483648 to 2147483647
	Floating-point 32 bit	-3.402823466e+38 to 3.402823466e+38





# World Files for Georeferencing Information

- Some image formats store GI in a header of the image file (grids, img, GeoTIFF)
- Others use world (ASCII) files (.tfw)
- Origin of an image is ul (row values increase downward), of a coord system ll

```
20.17541308822119 - A
0.0000000000000000 - D
0.0000000000000000 - B
-20.17541308822119 - E
424178.11472601280548 - C
4313415.90726399607956 - F
```

A = x-scale; dimension of a pixel in map units in x direction

B, D = rotation terms

C, F = translation terms; x,y map coordinates of the center of the upper left pixel

E = negative of y-scale; dimension of a pixel in map units in y direction

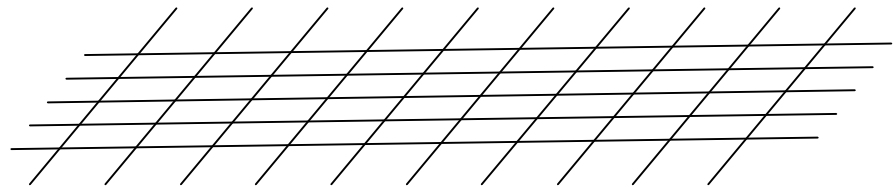
# **Critical Points in Working with Raster Data**

- Noise, false colors, mixed colors
- Object separation / identification
- Neighborhoods for Morphology operators
- Assignment and coding
- Edges, contours and transitions between objects and background (blurring)

# Raster and Raster Analysis

- **Two-dimensional arrays** organized in columns and rows as basis for efficient computation (translation into code)
- Making use of the **simple** and **flexible** data structure
- Fields, objects, regions, connected components, networks
- **Developing** and **extending** functionalities and operators

`MyRaster[row][col]`



# Understanding Raster Analysis

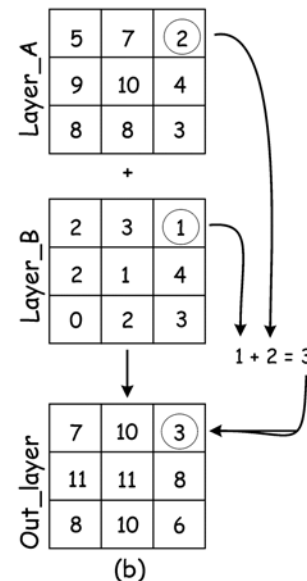
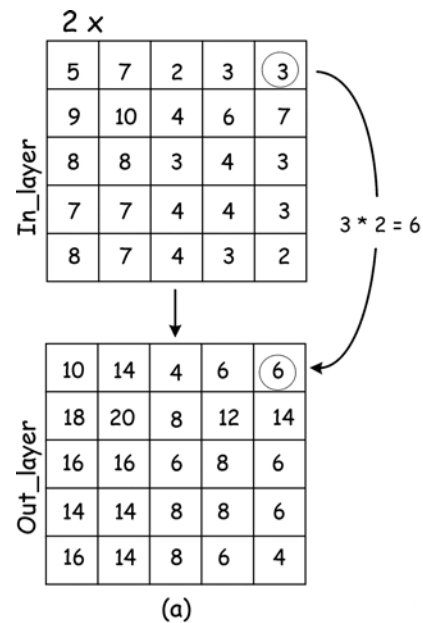
- To apply **analysis tools** is easy and straightforward
- Behind existing tools are complex **algorithms** implying mathematics, geometry and matrix operations between datasets and within regions of the same layer
- Thus a basic **understanding** of the concepts behind these tools is fundamental

# Map Algebra

- Introduced by Dana **Tomlin** and Joseph **Berry**
- **Cell-by-cell** combination of raster data layers (addition, subtraction, multipl.,...)
- Simple **operations** on numbers stored as values at **raster** cell locations
- Output grids with results at the cell locations **corresponding to input cells**

# Map Algebra Operations

- **Unary Operations**
- **Binary Operations**
- **Higher-order Operations**



# Map Algebra and Matrix Algebra

- **One-to-one** locational correspondence throughout all functions applied
- \*, /, \*\*, root are defined by the same rules of maintaining the one-to-one translation
- **Matrix Algebra** would apply rules for mathematical matrices (do you remember them?)
- If A is a 2x3 and B is a 3x2 matrix:

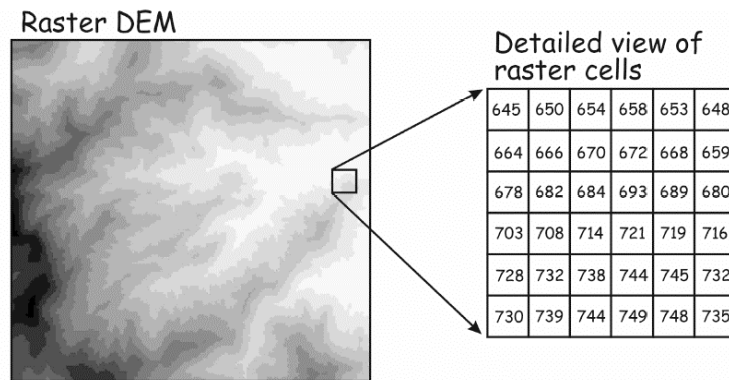
$$AB = \begin{bmatrix} a_{11}b_{11} + a_{12}b_{21} + a_{13}b_{31} & a_{11}b_{12} + a_{12}b_{22} + a_{13}b_{32} \\ a_{21}b_{11} + a_{22}b_{21} + a_{23}b_{31} & a_{21}b_{12} + a_{22}b_{22} + a_{23}b_{32} \end{bmatrix}$$

$$BA = \begin{bmatrix} b_{11}a_{11} + b_{12}a_{21} & b_{11}a_{12} + b_{12}a_{22} & b_{11}a_{13} + b_{12}a_{23} \\ b_{21}a_{11} + b_{22}a_{21} & b_{21}a_{12} + b_{22}a_{22} & b_{21}a_{13} + b_{22}a_{23} \\ b_{31}a_{11} + b_{32}a_{21} & b_{31}a_{12} + b_{32}a_{22} & b_{31}a_{13} + b_{32}a_{23} \end{bmatrix}$$

$$A + B = \begin{bmatrix} a_{11} + b_{11} & a_{12} + b_{12} & \cdots & a_{1n} + b_{1n} \\ a_{21} + b_{21} & a_{22} + b_{22} & \cdots & a_{2n} + b_{2n} \\ \vdots & \vdots & & \vdots \\ a_{p1} + b_{p1} & a_{p2} + b_{p2} & \cdots & a_{pn} + b_{pn} \end{bmatrix}$$

# Why we are not doing Matrix Algebra

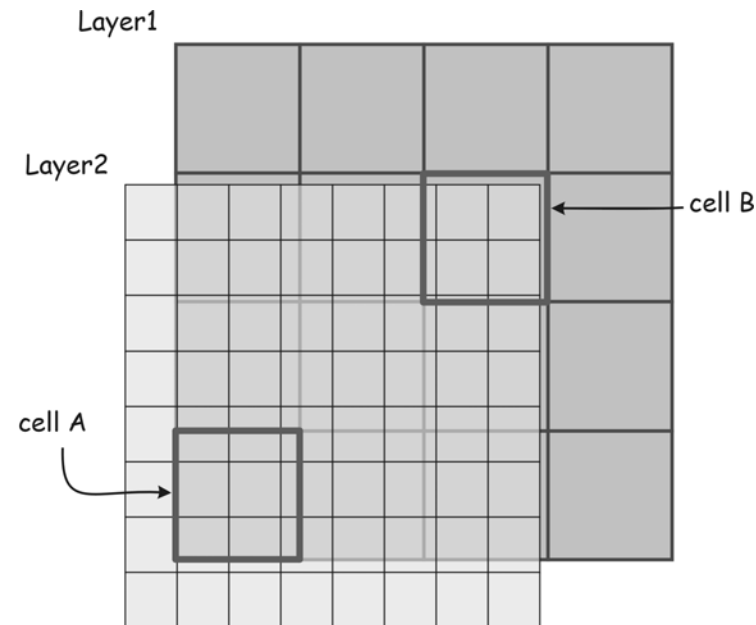
- So that is the special sense of Map Algebra:
- **Position** of individual grid cells corresponds to their position in **geographic space** (not in math matrices)
- Cell values are changed but **not** their position...
- Intuitively easy to get but it is important to know these differences... and **why** they exist





# Raster-Related Problems

- Different **extents** and **NoData** values (the common or “shared” area?)
- Different raster **cell sizes** (how to define comb.)
- **Misalignment** of raster cells
- **Resampling & Transformations**



# Map Algebra as Modeling Language

- Something like a modified version of Matrix Algebra, yes!
- But it can be seen as a **complete modeling language** (taken as standard for industry)
- Allows for program **control, development** and **iteration** + mathematical manipulation and logical **operators** of comparison
- ...and thus for the **whole complexity** of modeling
- Fuzzy logic as one example

# Rules to be Followed

- E.g. in ESRI's Spatial Analyst
- **Building blocks** for Map Algebra language are:

**Objects** - datasets, layers, values (as inputs or storage location)

**Actions** - performed on objects; *operators* and *functions* (loc,foc,zon,glob) + *application functions*

**Qualifiers on the actions** - parameters determining the conduction of a function

# Actions I: Basic Operators

- Computations **within & between** objects
- Remember **NoData** values...
- **Arithmetic** (+, -, \*, /, \*\*, root, mod)
- **Relational** / Compare / Conditional (<, >, ==, >=, ...)
- **Boolean** / Logical (&&, ||, !, XOR)
- **Combinatorial** (and, or; unique identifiers not Boolean)
- **Assignment** (=)
- **Accumulative** (+=, -=, ...)
- **Logical** (IN, DIFF, OVER)

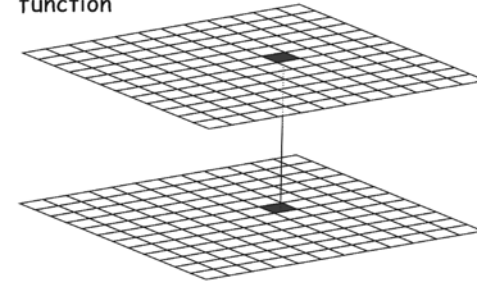
# **Actions II: Functions**

- Spatial **modeling** tools for cell-based data
- **Higher-order** GIS operations
- Important building blocks for model **implementation** based on Map Algebra
- **Parameter-dependent**

# Function Types in Map Algebra

- **Local:** cell-by-cell
  - **Neighborhood (Focal):** neighborhood analysis
  - **Block:** whole blocks of cells
  - **Zonal:** within homogeneous areas, zonal analysis/statistics
  - **Global:** incorporation of the full dataset
  - Special types
- 
- **Uniform** definition of **entities** in raster data

Local function



e.g.,

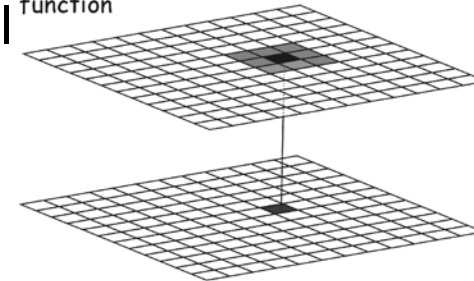
10	12	42
30	9	4
-12	8	15

plus 4

↓

14	16	46
34	13	8
-8	12	19

Neighborhood function



e.g.,

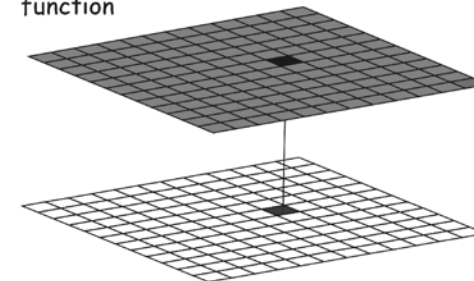
10	12	42
30	9	4
-12	8	15

neighborhood maximum

↓

33	42	42
30	42	42
30	30	17

Global function



e.g.,

10	12	42
30	9	4
-12	8	15

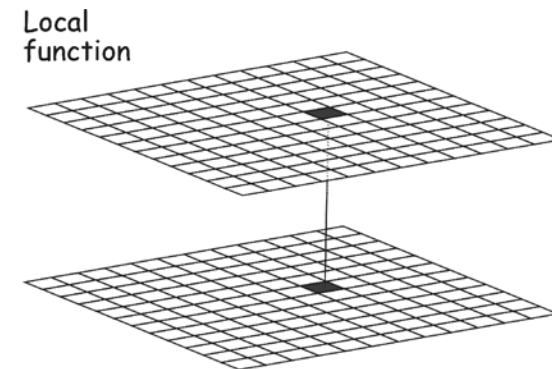
global maximum

↓

42	42	42
42	42	42
42	42	42

# Local Functions

- **Uniform** cell size presumed for cell-by-cell analysis (**ul** start)
- **Mathematical/arithmetic** functions
- **Logical** operations
- **Reclassification**
- **Nested** functions
- **Overlay** in raster data
- `sin(c\ :temp\myRaster)`



e.g.,

10	12	42
30	9	4
-12	8	15

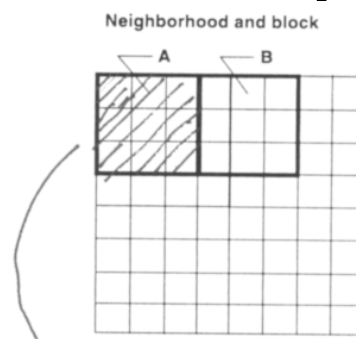
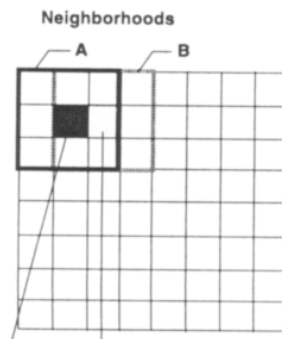
plus 4

↓

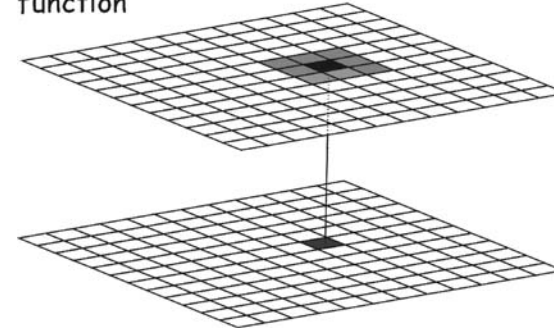
14	16	46
34	13	8
-8	12	19

# Neighborhood (Focal) Functions

- Everyday needs in raster GIS (slope, aspect)
- Also neighborhoods **uniform**
- Cell is characterized/modified based on a predefined **neighborhood** of grid cells
- `Focalsum([inlayer], rectangle, 3, 3)`
- **Neighborhoods and moving windows**
- **Blocks non-overlapping**



Neighborhood function



e.g.,

10	12	42
30	9	4
-12	8	15

neighborhood maximum

33	42	42
30	42	42
30	30	17



# Zonal Functions

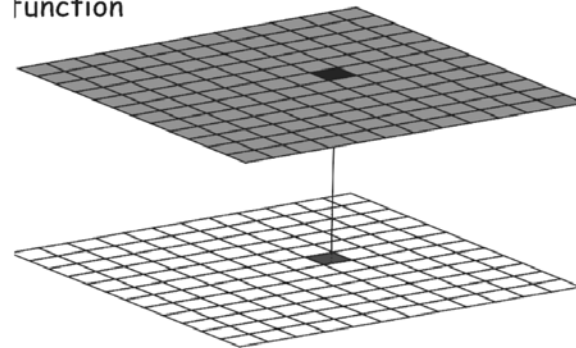
- Zones identified from **another** layer for evaluation of the target cell
- Zones are **geographic areas** with certain characteristics (not necessarily connected such as regionGroups)
- Internal **attribute homogeneity**
  - `meangrid = zonalmean(zonalgrid,valuegrid)`
- Statistics are written **into each cell of a zone**
- **Blocks** similar but predefined “roving window corresponds to the zone

1							
1						4	4
1							4
1							
		2					
	2	2		3	3		
	2	2			3	3	
2	2				3		

# Global Functions

- Operate on the **entire grid** at once
- Each cell is a **function** of all input cells
- EucDistance, WeightDistance, Hydrological, Surface, Visibility, Viewshed, Max,...
- **eucdist(...)**

Global  
function



e.g.,

10	12	42
30	9	4
-12	8	15

global  
maximum

42	42	42
42	42	42
42	42	42

# Further Functions

- We will see many specialized functions implemented in GIS tools
- Complex functions which **integrate** many of **basic** functions
- **Hydrological** functions
- **Surface** analysis

# Flow Control

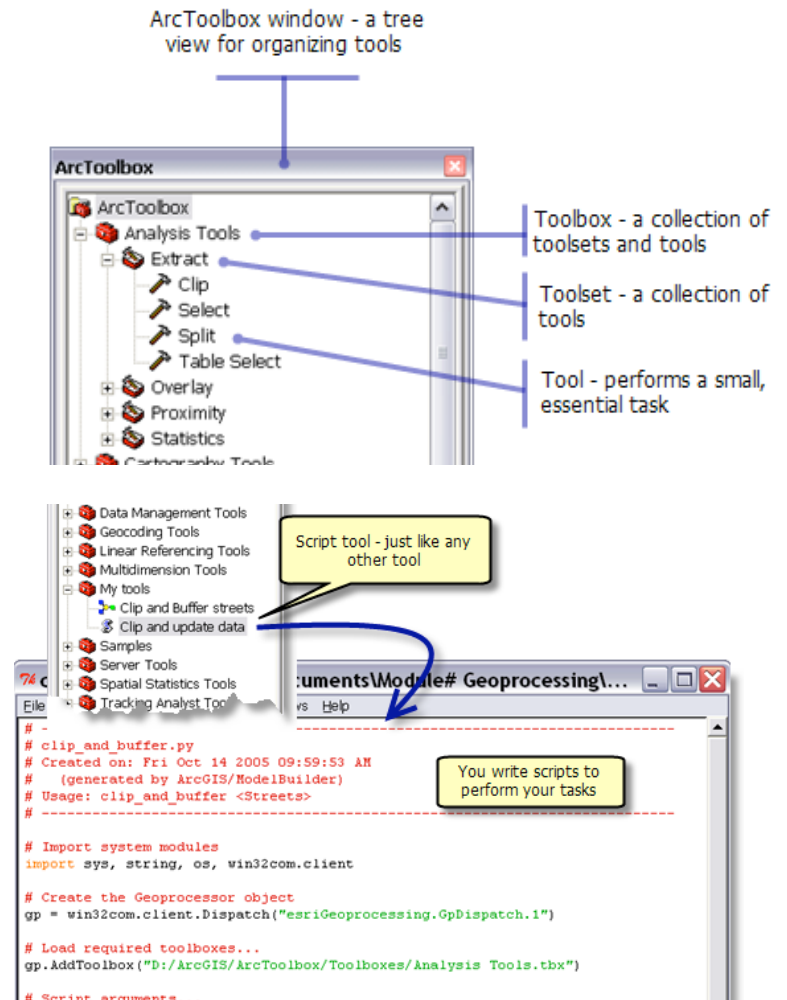
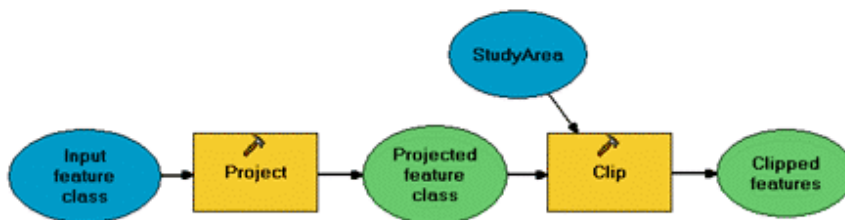
- Integral component of Map Algebra
- **Command line** framework / **GUI** as **interface** with the GIS user
- Composed of two elements (that work with **operations** and **functions**):
- **Statements**: verbal representation of operations to link operators, functions and programming commands
- **Programs**: notational representation of a procedure in Map Algebra; ordered sequence of statements

# Iteration

- **Repeated** execution of the same sequence of statements under **varying conditions** or with other **datasets** or subsets or based on **testing for conditions** (“for looping”, “while looping”)
- Combined with **if then** logic
- Makes a modeling framework more **powerful**

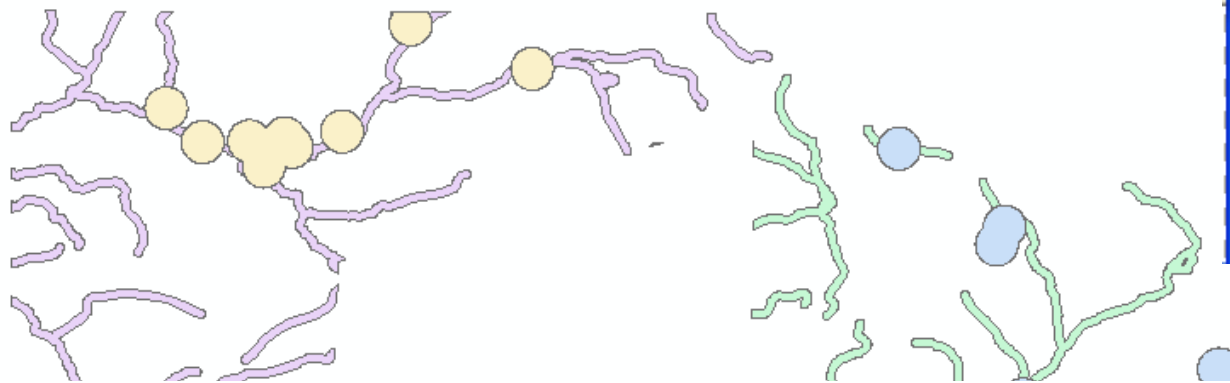
# ... Geoprocessing Framework in ArcGIS

- **Tool dialog:** Single tasks
- **Command line**
- **Model-building:** This is GIS2!
- **Scripting/Programming:** This is where we'll go in GIS3!

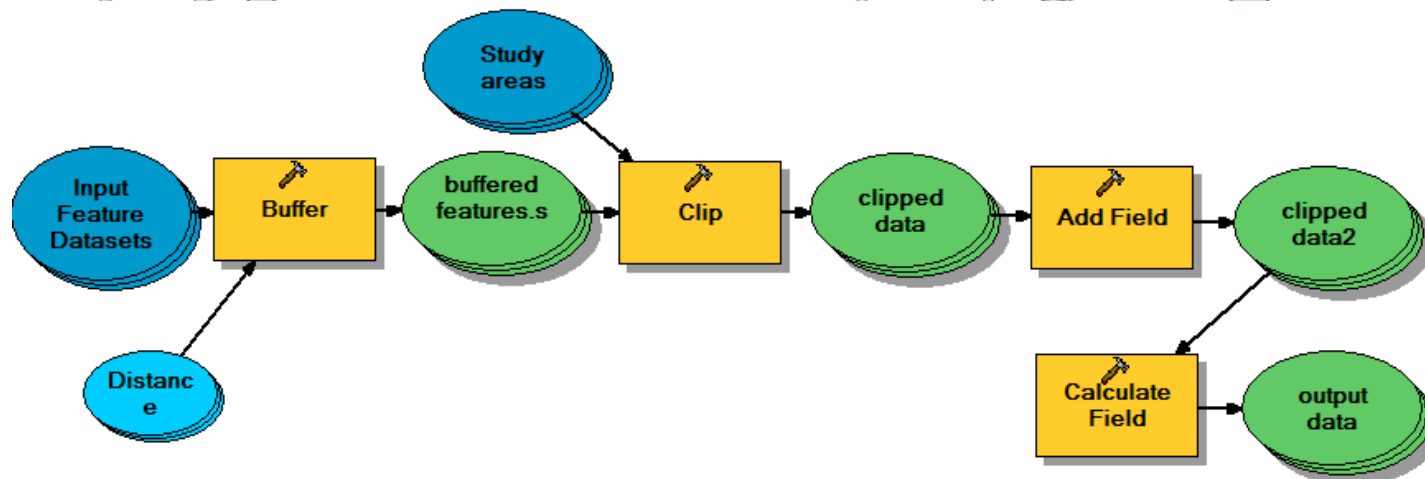


# “Graphical” Modeling Framework

Different Buffer distances for different features in different areas

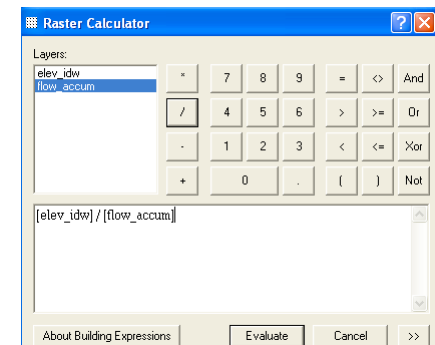


Distance [value or field]	
Distance [value or field]	
1	1000 Meters
2	5000 Meters

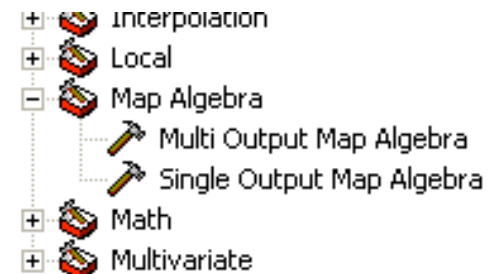


# How to Access Map Algebra

- Spatial Analyst: **Raster Calculator**
- Command line prompt in **ArcGrid** (going to be gone...)
- ArcToolbox: **Single Output Map Algebra** (for use in ModelBuilder)
- ArcToolbox: **Multiple Output Map Algebra** (for use in scripting)



```
Arc: grid
Copyright (C) 1982-2006 Environmental Systems Research Institute, Inc.
All rights reserved.
GRID 9.2 (Sun Sep 17 16:05:34 PDT 2006)
Grid: streamsBuff = EXPAND(streams,5,LIST,1)
```





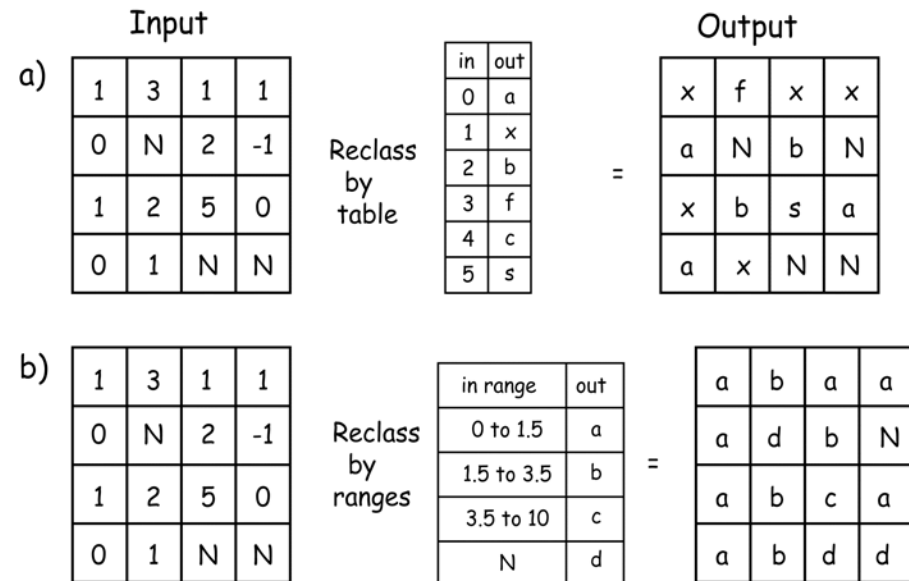
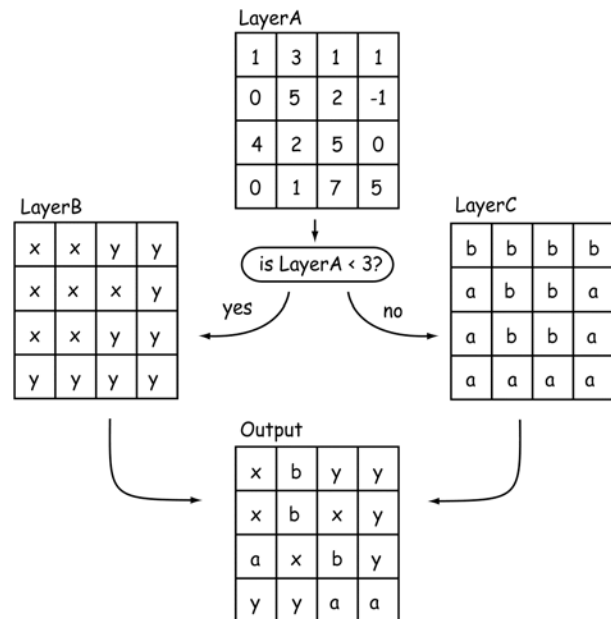
# More on Local Functions

- Basically the **operators** we have seen before are executed **cell-by-cell**
- Remember the handling with **NoData** values, **0-values** and values **unequal** to **zero**
- Higher level operations based on local processing are **reclassifications**, **nested functions** and **overlays**...
- ...trigonometric, exp., log., select, statistical,...

# Local Functions: Reclassifications

- Assigning output values that depend on the specific set of input values
- Based on a **table**, **ranges of values** (for automated reclassification) or **conditional tests**

Output = CON (LayerA < 3, LayerB, LayerC)



# Local Functions: Nested Functions

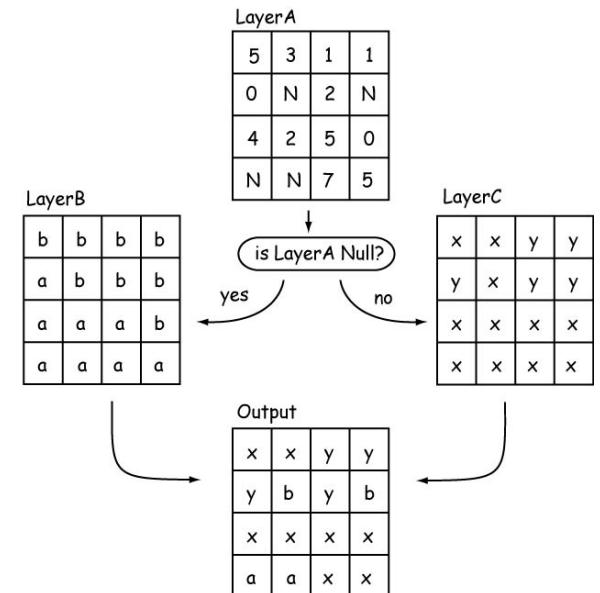
- Functions as arguments in other functions

`absValues = ABS ( Input )`

`LogValues = LN ( absValues )`

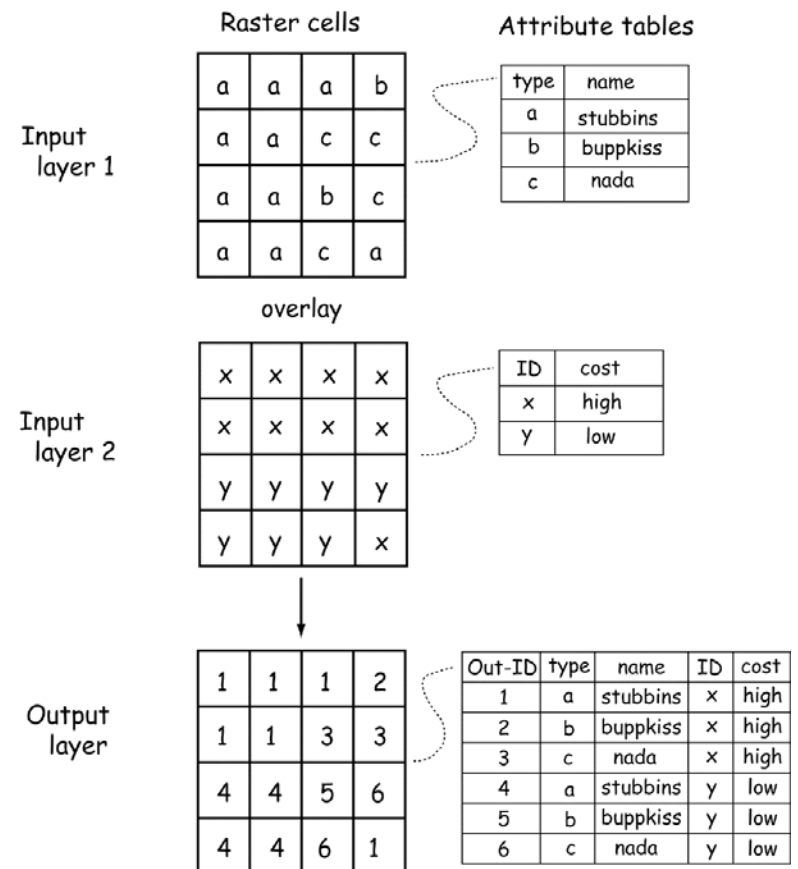
`LogValues = LN ( ABS ( Input ) )`

`Output = CON ( ISNULL ( LayerA ), LayerB, LayerC )`



# Local Functions: Overlay I

- **Cell-by-cell comparison** to register unique combinations of variables
- “**vectors**” of attributes given in a **table** (many to one relationships and extended rasters)

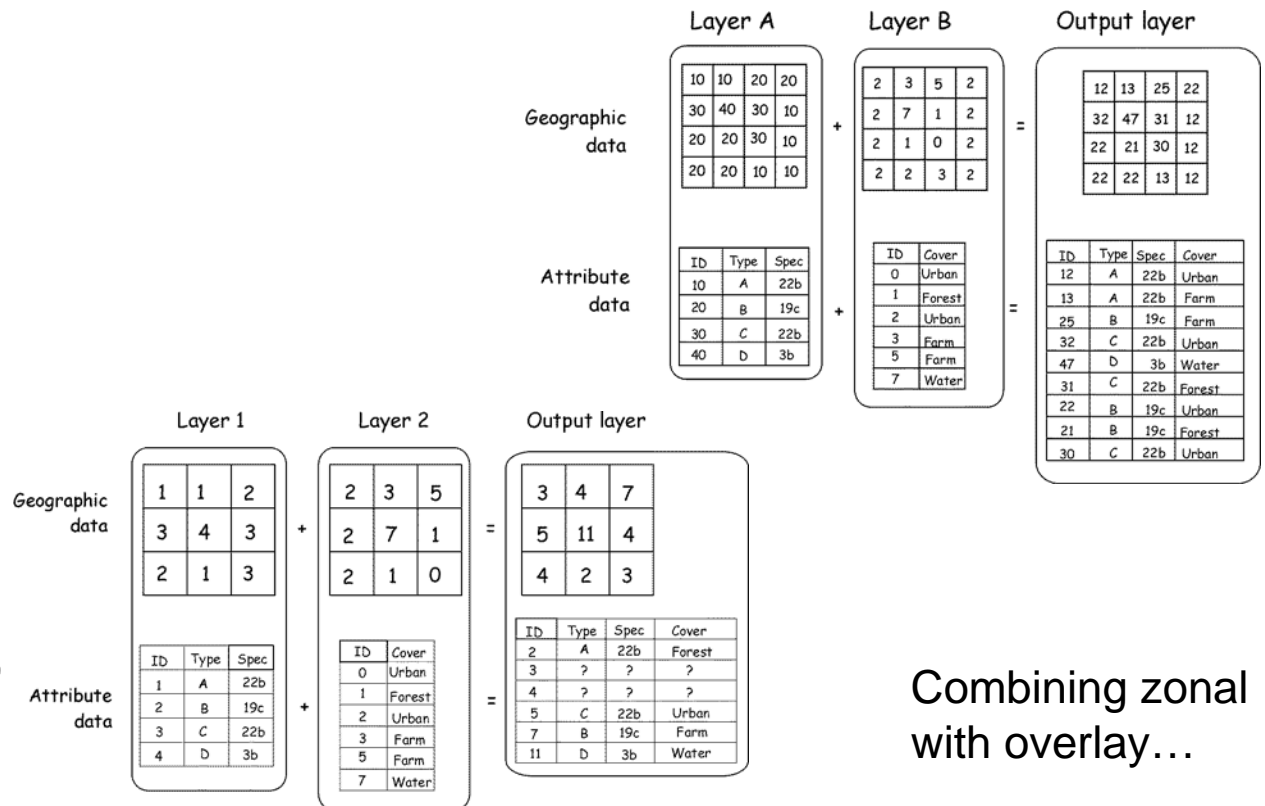


# Local Functions: Overlay II

- Multiplication to mimic **clip (extraction)** using source and template layers (binary masks)

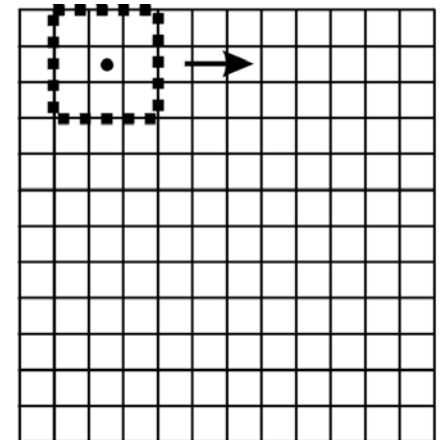
Source		Template		Output																																																
<table><tr><td>1</td><td>3</td><td>4</td><td>7</td></tr><tr><td>6</td><td>3</td><td>2</td><td>-1</td></tr><tr><td>1</td><td>2</td><td>5</td><td>0</td></tr><tr><td>0</td><td>1</td><td>3</td><td>2</td></tr></table>	1	3	4	7	6	3	2	-1	1	2	5	0	0	1	3	2	Clip	<table><tr><td>0</td><td>0</td><td>0</td><td>1</td></tr><tr><td>0</td><td>0</td><td>1</td><td>1</td></tr><tr><td>0</td><td>1</td><td>1</td><td>1</td></tr><tr><td>0</td><td>1</td><td>1</td><td>0</td></tr></table>	0	0	0	1	0	0	1	1	0	1	1	1	0	1	1	0	=	<table><tr><td>N</td><td>N</td><td>N</td><td>7</td></tr><tr><td>N</td><td>N</td><td>2</td><td>-1</td></tr><tr><td>N</td><td>2</td><td>5</td><td>0</td></tr><tr><td>N</td><td>1</td><td>3</td><td>N</td></tr></table>	N	N	N	7	N	N	2	-1	N	2	5	0	N	1	3	N
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6	3	2	-1																																																	
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- **Addition** to mimic **union** (same id's for disjunct pixels with same characteristics through many-to-one rs. + ambiguous if same values out of different combinations)



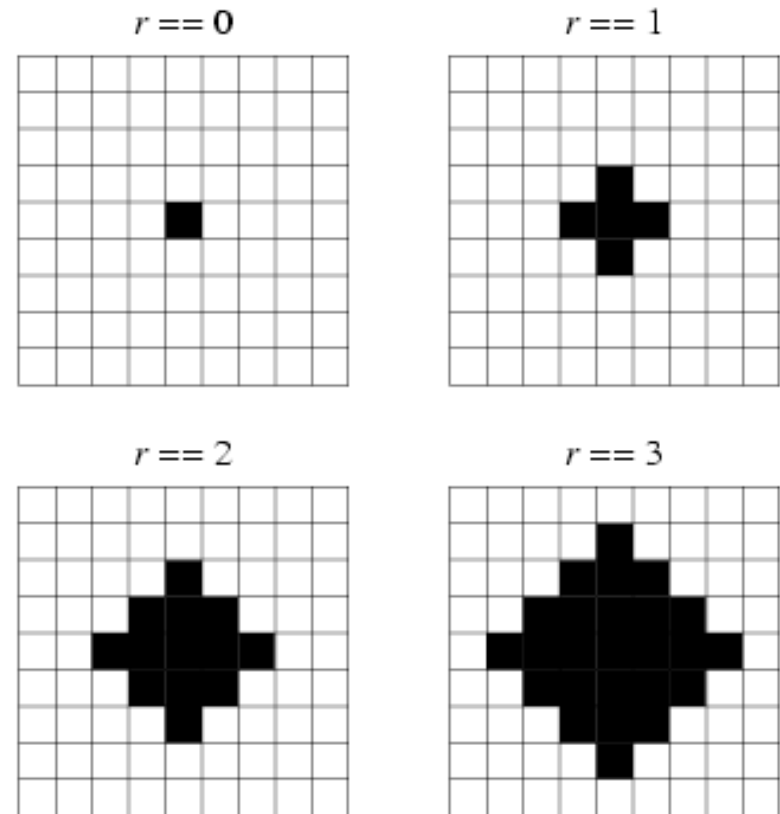
# More on Neighborhood Functions

- Often based on the concept of **moving windows**:
- Configuration of raster cells that is positioned over the input raster and defines the input for an **operation** to be applied. Result associated with **center** and written to the **output**. Window “**moves**” to the next location...
- Much depends on the **neighborhood**...
- Any ideas of functions that use NF?



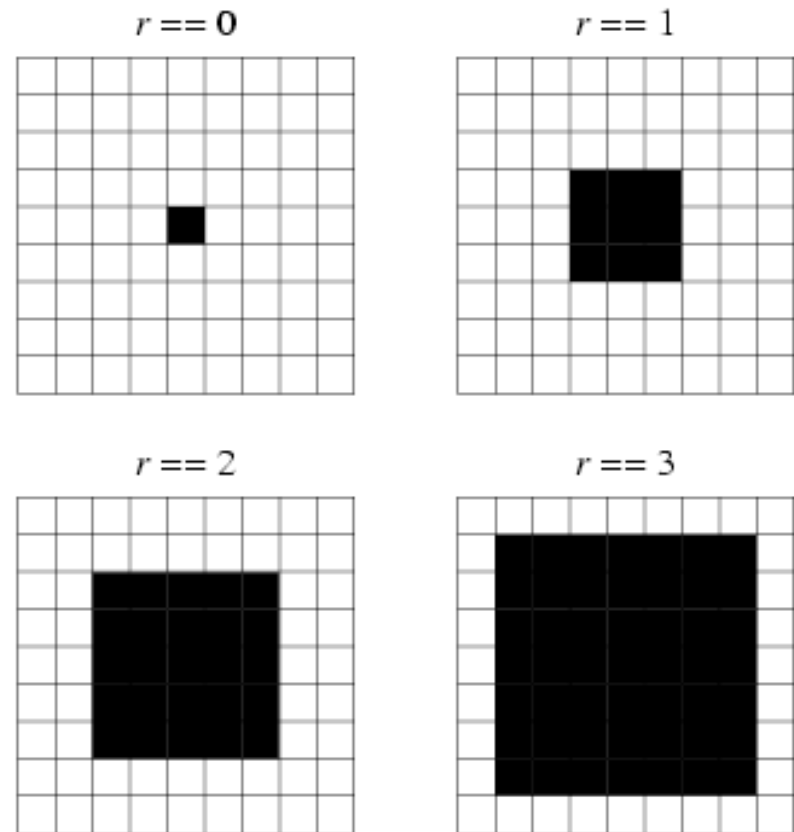
# Von Neumann Neighborhood

- **Diamond-shaped**
- To define a set of cells surrounding a given cell
- Ranges  $r = 0, 1, 2, 3$
- $N = 2 * r(r+1) + 1$
- “centered square number”



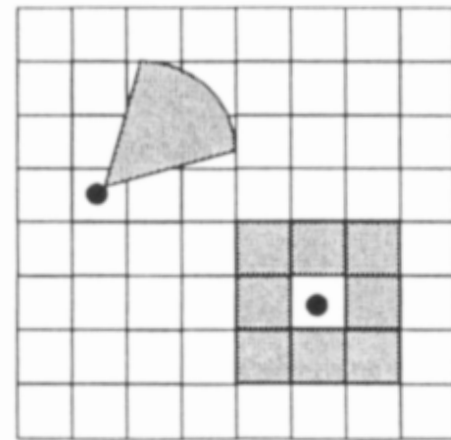
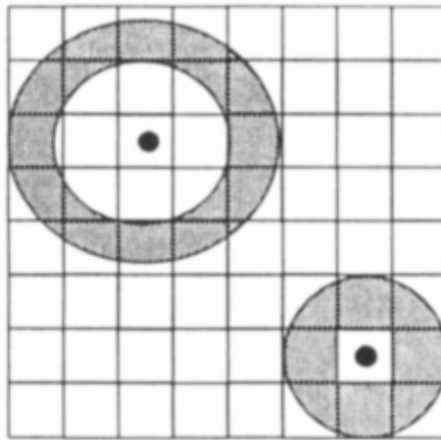
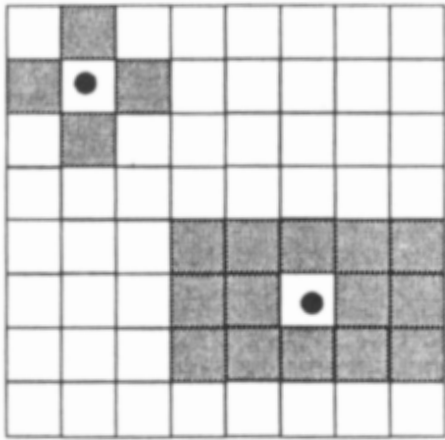
# Moore Neighborhood

- **Square-shaped**
- To define a set of cells surrounding a given cell
- Ranges  $r = 0, 1, 2, 3$
- $N = (2r+1)^2$
- “**odd squares**”



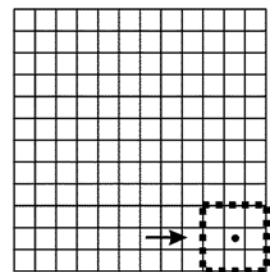
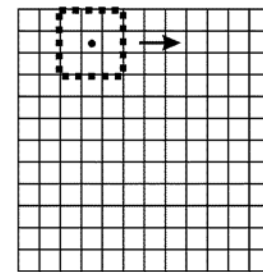
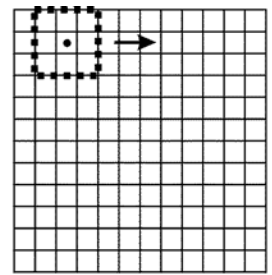
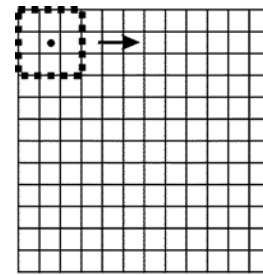


# Other Types of Neighborhood

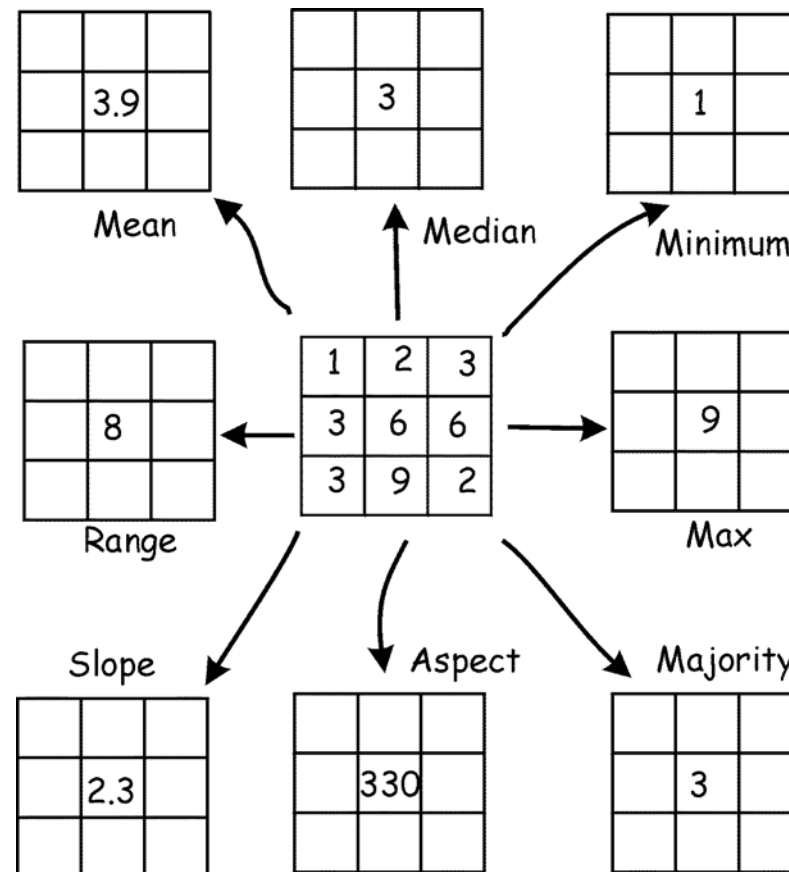


# The Principles of Moving Windows

- Left-to-right and top-to-bottom
- **Dimensions:** size of the neighborhood
- **Odd-numbered** in x and y to provide a **natural center** cell and square- or rectangular-shaped (or L or wedge or circular)

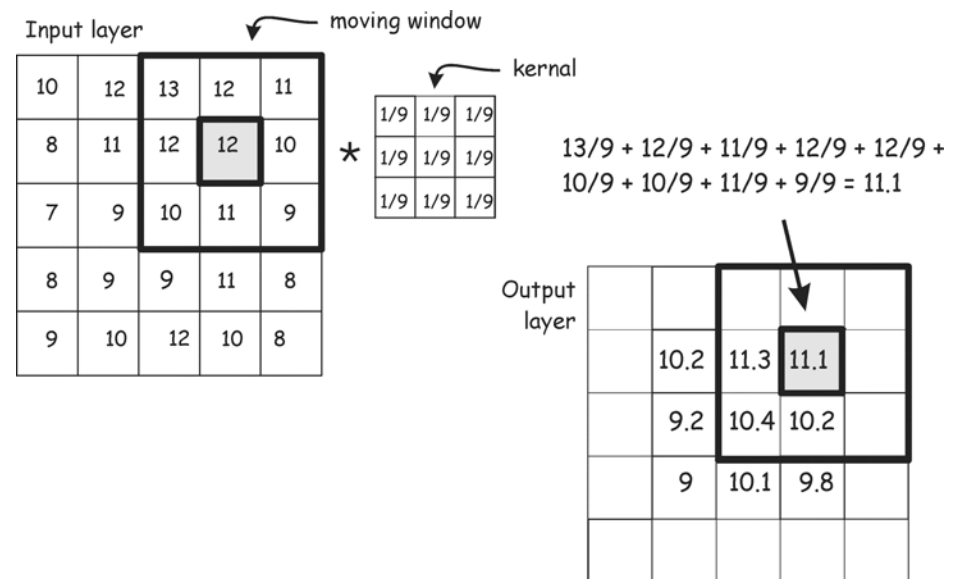


# Examples for Moving Window NFs



# Moving Windows and Kernels

- Set of **constants** for a given window size and shape
- Are applied with a **function** to every moving window **location**
- What can you see at the **margins** of the output grid?



# Moving Windows and Margin Erosion

- Loss of margins in the original raster dataset: width of cells from the center cell away
- Solutions: (a) **Enlargement** of study areas  
(b) **MW-** and **Kernel modification** at corners (2x2; 1/4) and edges (2x3; 1/6)

Mean function kernels

corner

$\frac{1}{4}$	$\frac{1}{4}$
$\frac{1}{4}$	$\frac{1}{4}$

margin

$\frac{1}{6}$	$\frac{1}{6}$	$\frac{1}{6}$
$\frac{1}{6}$	$\frac{1}{6}$	$\frac{1}{6}$

corner

$\frac{1}{4}$	$\frac{1}{4}$
$\frac{1}{4}$	$\frac{1}{4}$

margin

$\frac{1}{6}$	$\frac{1}{6}$
$\frac{1}{6}$	$\frac{1}{6}$
$\frac{1}{6}$	$\frac{1}{6}$

main

$\frac{1}{9}$	$\frac{1}{9}$	$\frac{1}{9}$
$\frac{1}{9}$	$\frac{1}{9}$	$\frac{1}{9}$
$\frac{1}{9}$	$\frac{1}{9}$	$\frac{1}{9}$

margin

$\frac{1}{6}$	$\frac{1}{6}$
$\frac{1}{6}$	$\frac{1}{6}$
$\frac{1}{6}$	$\frac{1}{6}$

corner

$\frac{1}{4}$	$\frac{1}{4}$
$\frac{1}{4}$	$\frac{1}{4}$

margin

$\frac{1}{6}$	$\frac{1}{6}$	$\frac{1}{6}$
$\frac{1}{6}$	$\frac{1}{6}$	$\frac{1}{6}$

corner

$\frac{1}{4}$	$\frac{1}{4}$
$\frac{1}{4}$	$\frac{1}{4}$

example application, lower right corner

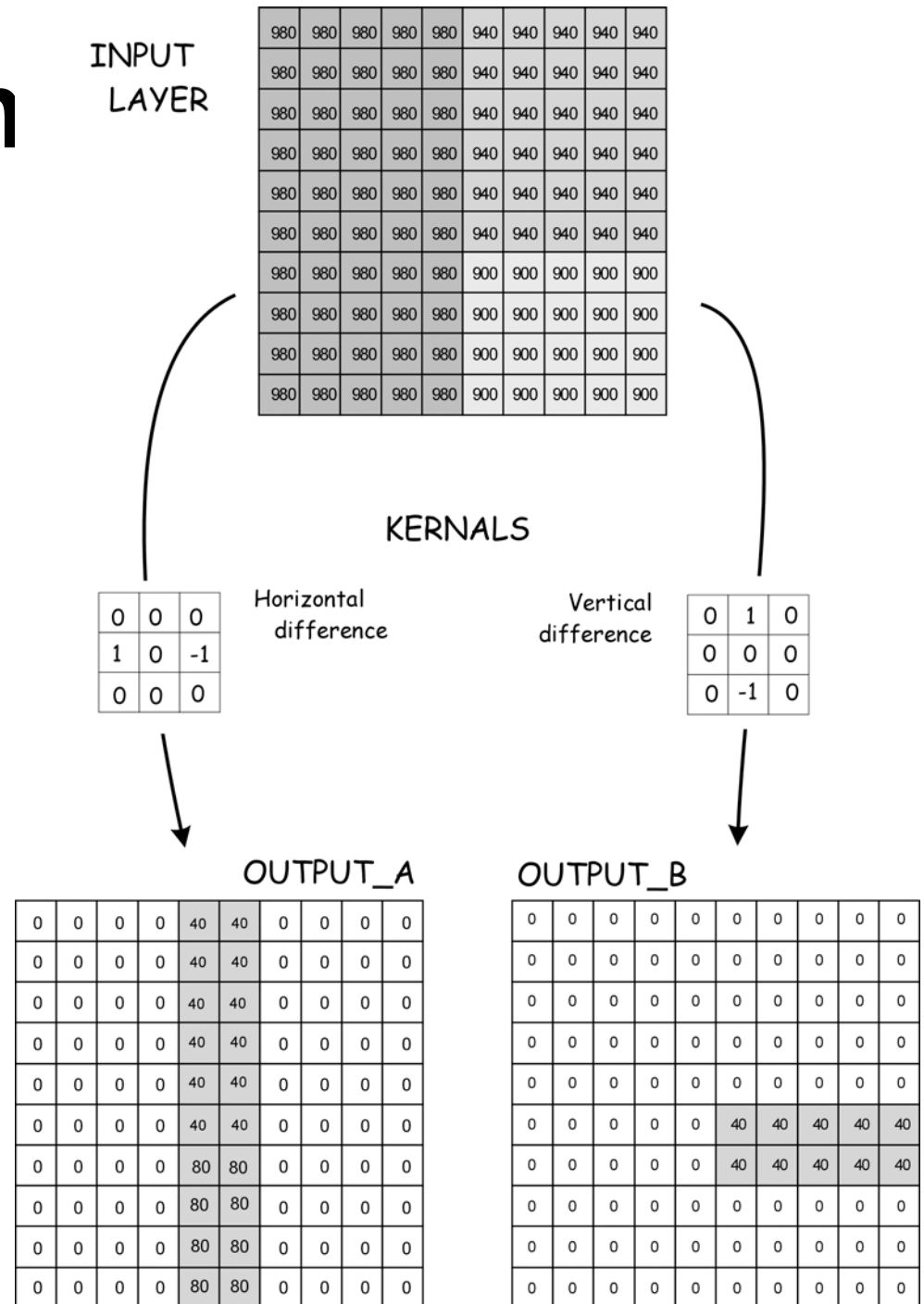
10	12	13	12	11
8	11	12	12	10
7	9	10	11	9
8	9	9	11	8
9	10	12	10	8

		$9\frac{1}{4}$

$$\frac{1}{4} \cdot 11 + \frac{1}{4} \cdot 8 + \frac{1}{4} \cdot 10 + \frac{1}{4} \cdot 8 = 9\frac{1}{4}$$

# Edge Detection Using Kernels

- Concentration changes; elevation changes,...
- Discovering **contrasts** / **differences** within the local neighborhood



# Noise Filtering Using Kernels

- **Smoothing:** Reducing differences between neighboring cells (mean Kernels / operators; **low-pass filters**)
- **Noise:** Errors in measurement, recording or transforming the data or due to data loss

# High-Pass Filter

- Accentuates differences between adjacent cells in a moving window
- Identifying “spikes” (+ >>) and “pits” (- >>)

kernel for high-pass filter

$$\frac{1}{9} \times \begin{bmatrix} -1 & -1 & -1 \\ -1 & 9 & -1 \\ -1 & -1 & -1 \end{bmatrix}$$

$$\left( \begin{array}{l} (-1) \times 1065 + \\ (-1) \times 1068 + \\ (-1) \times 924 + \\ (9) \times 963 + \\ (-1) \times 947 + \\ (-1) \times 1142 + \\ (-1) \times 1005 + \\ (-1) \times 1151 \end{array} \right) / 9$$

= 35.7

Input Layer with “noise”

1065	1068	929	864	960	1113	974	896	890	841	759	719	705	696	720	708
1038	963	947	950	999	1021	1011	1015	995	1044	870	773	734	703	676	684
1142	1005	1151	310	1117	1056	1007	1002	902	954	935	913	789	756	724	700
1116	1114	1270	1165	1097	1025	922	917	821	829	860	838	807	810	758	760
1275	1170	1295	1114	1009	942	953	847	835	729	738	797	723	718	694	670
1441	1263	1196	1055	913	869	829	771	736	765	766	688	694	1676	684	698
1348	2900	1056	969	948	951	940	867	818	863	784	732	704	733	776	804
1377	1238	1122	1019	1089	950	956	896	2000	800	760	698	779	867	896	744
1489	1320	1188	1152	1050	942	922	952	815	841	721	780	852	28	845	738
1432	1415	1196	1100	1001	974	924	911	914	756	809	861	898	830	746	710
1412	1474	1240	1100	1001	982	873	835	829	853	931	937	845	706	685	680
1493	1368	1201	1090	1064	970	902	902	958	952	1015	841	782	803	786	711
1437	1407	118	1145	1070	1107	982	1047	1077	1052	954	884	44	940	828	771
1349	1369	1267	1247	1194	1196	1077	1214	1145	999	906	894	1024	1046	923	862
1319	1292	1378	1400	1367	1276	1162	1088	961	930	872	985	1010	1178	1148	1000

spikes



pits



Output Layer

35	142	141	177	105	112	162	156	250	99	59	61	58	43		
33	292	-657	270	145	121	158	60	147	148	179	85	89	74		
66	345	235	237	124	61	107	41	76	111	108	102	146	110		
62	256	114	100	95	161	93	122	23	41	117	-58	-43	-59		
-35	-7	110	40	37	35	12	14	68	88	28	-59	1039	-69		
1784	-140	35	79	118	152	-16	-38	37	109	79	-59	-54	-14		
-74	-83	66	202	83	131	-23	1238	-45	69	18	179	243	281		
158	125	178	135	68	88	25	-82	-1	20	71	214	-718	227		
220	86	108	78	119	102	126	159	10	66	108	249	207	165		
278	135	111	80	125	50	33	42	57	150	161	105	-3	21		
281	207	207	123	83	46	68	119	99	192	130	115	179	105		
340	-1004	228	68	167	47	129	158	162	115	166	-758	247	67		
306	227	253	104	169	69	265	215	121	64	151	248	257	59		



# Mean Filtering

- Remove the spikes and pits identified by high-pass filtering

$\frac{1}{9}$

kernel for  
mean filter

1	1	1
1	1	1
1	1	1

$$\left( \begin{array}{l} (1)*1065 + \\ (1)*1068 + \\ (1)*929 + \\ (1)*1038 + \\ (1)*963 + \\ (1)*947 + \\ (1)*1142 + \\ (1)*1005 + \\ (1)*1151 \\ \hline 9 \end{array} \right)$$

= 1034

Input layer with "noise"

1065	1068	929	864	960	1113	974	896	890	841	759	719	705	696	720	708
1038	963	947	950	999	1021	1011	1015	995	1044	870	773	734	703	676	684
1142	1005	1151	310	1117	1056	1007	1002	902	954	935	913	789	756	724	700
1116	1114	1270	1165	1097	1025	922	917	821	829	860	838	807	810	758	760
1275	1170	1295	1114	1009	942	953	847	835	729	738	797	723	718	694	670
1441	1263	1196	1055	913	869	829	771	736	765	766	688	694	1676	684	698
1348	2900	1056	969	948	951	940	867	818	863	784	732	704	733	776	804
1377	1238	1122	1019	1089	950	956	896	2000	800	760	698	779	867	896	744
1489	1320	1188	1152	1050	942	922	952	815	841	721	780	852	28	845	738
1432	1415	1196	1100	1001	974	924	911	914	756	809	861	898	830	746	710
1412	1474	1240	1100	1001	982	873	835	829	853	931	937	845	706	685	680
1493	1368	1201	1090	1064	970	902	902	958	952	1015	841	782	803	786	711
1437	1407	118	1145	1070	1107	982	1047	1077	1052	954	884	44	940	828	771
1349	1369	1267	1247	1194	1196	1077	1214	1145	999	906	894	1024	1046	923	862
1319	1292	1378	1400	1367	1276	1162	1088	961	930	872	985	1010	1178	1148	1000

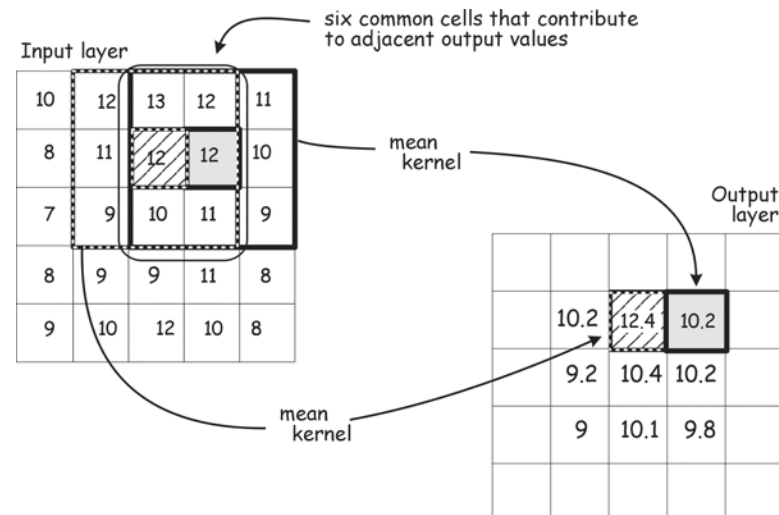
☐ smoothed  
spike or pit

Output layer

1034	909	914	932	1028	1010	965	948	910	867	799	754	722	707		
1082	986	1000	971	1028	997	954	942	912	890	835	791	750	730		
1170	1066	1058	981	1014	963	911	870	844	843	822	794	753	732		
1237	1182	1123	1021	951	897	847	805	786	778	767	861	840	829		
1438	1335	1061	974	928	885	844	803	781	762	736	829	822	828		
1437	1313	1040	973	938	892	979	946	921	761	733	841	867	875		
1448	1329	1065	1007	972	930	1018	983	933	775	756	685	720	714		
1308	1194	1101	1030	978	936	1032	987	935	780	795	732	749	711		
1351	1242	1114	1033	963	923	886	856	829	832	848	748	715	663		
1359	1242	1110	1031	965	919	894	878	890	883	879	833	786	739		
1238	1127	1003	1058	994	955	933	945	957	935	803	753	713	767		
1223	1134	1044	1120	1062	1044	1033	1038	1006	944	816	806	797	852		
1215	1180	1131	1222	1159	1127	1083	1057	988	941	841	889	904	966		

# Moving Windows and Spatial Covariance

- The more moving window operations / functions carried out the more related (autocorrelated) the cell values are
- Adjacent cells share six of nine cells in the local neighborhood for the computation...



# References

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