

$$T(n) = T\left(\frac{n}{2}\right) + 5$$

$$a = 1 \quad b = 2 \quad \log_2 1 = 0 = k = 0$$

$$k = 0 \quad p = 0$$

$$\text{Case 2: } p > -1$$

$$\Theta(n^0 \log^{0+1} n) = \Theta(\log n)$$

$$T(n) = 7T\left(\frac{n}{2}\right) + 10n^2$$

$$a = 7 \quad b = 2 \quad \log_2 7 < \log_2 8 = 3$$

$$k = 2 \quad p = 0 \quad \text{Case 1: } \log_2 7 > k$$

$$\Theta(n^{\log_2 7})$$

$$T(n) = 2T(n-1) + 1$$

$$a = 2 \quad b = 1$$

$$k = 0$$

$$\text{Case 3: } a > 1$$

$$O(n^k a^{\frac{n}{b}})$$

$$= \Theta(n^0 2^{\frac{n}{1}})$$

$$= \Theta(2^n)$$

$$T(n) = 2T\left(\frac{n}{8}\right) + \sqrt{n}$$

$$a = 2 \quad b = 8$$

$$k = \frac{1}{2} \quad p = 0$$

$$\log_8 2 < \log_8 64 = 2$$

$$\log_8 2 < \frac{1}{2}$$

$$\text{Use 3: } \log_b a < k$$

$$p \geq 0 \rightarrow \Theta(n^k \log^p n)$$

$$= \Theta(n^{\frac{1}{2}} \log^0 n) = \Theta(\sqrt{n})$$