

Linear Algebra
Assignment 5 **MATH 2318 (Fall 2022)**

Deadline: Saturday October 8th, 11:59pm.

Policy to turn in assignment:

- Assignment should be submitted via BlackBoard.
- Student needs to turn in their assignment as a single PDF file.
- No email or late submission will be accepted.

4 points

1. Let $T : \mathbb{R}^2 \rightarrow \mathbb{R}^2$ be a linear transformation that first reflects points through the x_1 -axis, and then reflects points through the line $x_2 = x_1$. Find the standard matrix of T . Draw a picture to support your claims.

3 points

2. Let $T : \mathbb{R}^3 \rightarrow \mathbb{R}^2$ be a linear transformation defined by

$$T \left(\begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} \right) = \begin{bmatrix} x_1 - 5x_2 + 4x_3 \\ x_2 - 6x_3 \end{bmatrix}$$

Determine if T is onto and/or one-to-one. *Hint:* Find A , the standard matrix of T , and study the number of solutions of $A\vec{x} = \vec{b}$ for any $\vec{b} \in \mathbb{R}^2$.

6 points

3. Let $A = \begin{bmatrix} 2 & 0 & -1 \\ 4 & -5 & 2 \end{bmatrix}$, $B = \begin{bmatrix} 7 & -5 & 1 \\ 1 & -4 & -3 \end{bmatrix}$, $C = \begin{bmatrix} 1 & 2 \\ -1 & 3 \end{bmatrix}$. Compute the following

- a) $CA - 3B$.
- b) $A^T C + B^T$.

3 points

4. For each of the following, determine if the statement is true or false. Provide a short reasoning (one or two sentences).
- a) Let $T : \mathbb{R}^n \rightarrow \mathbb{R}^m$ be a linear transformation. If $m > n$, then T cannot be onto.
 - b) Let $T : \mathbb{R}^n \rightarrow \mathbb{R}^m$ be a linear transformation. If $n > m$, then T cannot be one-to-one.
 - c) Let T be a linear transformation. If $T(\vec{x}) = \vec{0}$, then $\vec{x} = \vec{0}$.