

# PRINTABLE VERSION

## Quiz 3

You scored 70 out of 100

### Question 1

Your answer is CORRECT.

Suppose we are told that set A satisfies  $\{1, \pi, \clubsuit\} \cap A = \emptyset$ . Of the following options which can be used for the set A?

- a) ☐  $\{-1, \clubsuit, \heartsuit\}$
- b) ☐  $\{1, \pi, \clubsuit\}$
- c) ☐  $\{\pi, 2\}$
- d) ☐  $\mathbb{Z}$
- e) ☐ No set A will make this true.
- f) ☒  $\{\heartsuit\}$

### Question 2

Your answer is INCORRECT.

The statement  $A \cup B = A$  implies which of the following?

- a) ☐  $A = \emptyset \wedge B = \emptyset$
- b) ☐  $\forall x \in B, x \in A$ .
- c) ☒  $\forall x \in A, x \in B$ .
- d) ☐  $\exists x, x \in A \wedge x \in B$ .

### Question 3

Your answer is CORRECT.

Suppose  $|S| = 5$  and  $|S \times T| = 30$ . What is the cardinality of T?

- a) ☒  $|T| = 6$
- b) ☐  $|T| = 30$
- c) ☐  $|T| = 150$
- d) ☐  $|T| = 1$
- e) ☐  $|T| = 11$

#### Question 4

Your answer is CORRECT.

Suppose  $|T| = 4$  and  $|P(S) \times T| = 64$ . What is the cardinality of  $S$ ?

- a) ☐  $|S| = 16$
- b) ☒  $|S| = 4$
- c) ☐  $|S| = 64$
- d) ☐  $|S| = 2^4$
- e) ☐  $|T| = 4$

#### Question 5

Your answer is CORRECT.

Is it possible for  $\{5\} \subseteq \mathbb{R}$ ?

- a) ☒ This is true. It always happens!
- b) ☐ This can happen, but it doesn't always happen.
- c) ☐ This is impossible! It never happens!

#### Question 6

Your answer is CORRECT.

Consider the set  $S$  defined below:

$$S = \{n \in \mathbb{N} : 2n = 1 \vee 3n = 1\}$$

Which of the following is true?

- a) ☐  $S = \{2^b : b \in \mathbb{N}\}$
- b) ☐  $S = \mathbb{N}$
- c) ☐  $S = \{2i + 1 : i \in \mathbb{N}\}$
- d) ☐  $S = \{2m : m \in \mathbb{N}\}$
- e) ☒  $S = \emptyset$

#### Question 7

Your answer is CORRECT.

Suppose we have two sets  $S$  and  $T$ , each described in terms of a condition:  $S = \{x \in U : P(x)\}$  and  $T = \{x \in U : Q(x)\}$ . (Here  $U$  is a Universal set.) If it is also true that

$$T \subseteq S$$

then which of the following statements must be true?

- a) ☐  $\forall x \in U, Q(x) \not\Rightarrow P(x)$
- b) ☐  $\forall x \in U, P(x) \not\Rightarrow Q(x)$
- c) ☐  $\exists t \in U, P(t) \wedge Q(t)$
- d) ☐  $\forall x \in U, P(x) \Rightarrow Q(x)$
- e) ☒  $\forall x \in U, Q(x) \Rightarrow P(x)$

#### Question 8

Your answer is INCORRECT.

A Venn Diagram or De Morgan's Laws should help you complete this sentence:

$$\overline{(A \cap B)} =$$

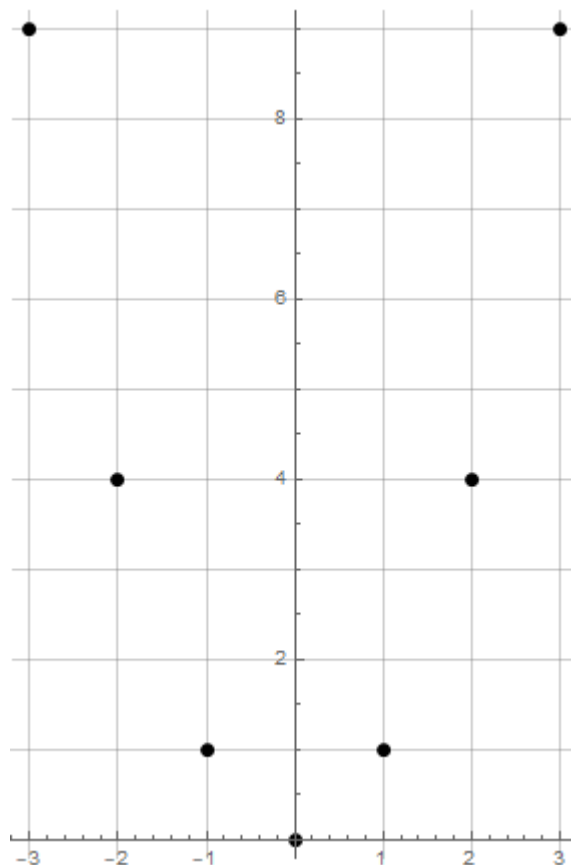
- a) ☐  $B \cup \overline{A}$
- b) ☐  $\overline{A} \cup B$
- c) ☐  $\overline{A} \cap \overline{B}$
- d) ☐  $\overline{A} \cup \overline{B}$

e) ☒  $A \cup \overline{B}$

### Question 9

Your answer is CORRECT.

Consider the image shown:



Which set of points is depicted in the image above?

a) ☐  $\{(x, \sqrt{9 - x^2}) : x \in \mathbb{Z} \wedge -3 \leq x \leq 3\}$

b) ☐  $\{(x, \sin(\pi x)) : x \in \mathbb{Z} \wedge -3 \leq x \leq 3\}$

c) ☐  $\{(2, x) : x \in \mathbb{Z} \wedge -3 \leq x \leq 3\}$

d) ☐  $\{(x, 2) : x \in \mathbb{Z} \wedge -3 \leq x \leq 3\}$

e) ☒  $\{(x, x^2) : x \in \mathbb{Z} \wedge -3 \leq x \leq 3\}$

f) ☐  $\{(x, 2x) : x \in \mathbb{Z} \wedge -3 \leq x \leq 3\}$

### Question 10

Your answer is INCORRECT.

$$P(\{2, 6\}) \cap P(\{2, -2, 6\}) =$$

a) ☒  $\{2, 6\}$

b) ☐  $\{ \{6\}, \{2, 6\} \}$

c) ☐  $\{ \emptyset, \{2\}, \{6\}, \{2, 6\} \}$

d) ☐  $\{ \{-2\} \}$

e) ☐  $\{2, 6, -2\}$

f) ☐  $\{ \{6\} \}$