

# Exam 1 C - MATH 4322

Spring 2024

Name:

PSID:

## Instructions

- Allow one sheet of notes front and back to be turned in for extra credit.
- Allow calculator.
- Total possible points 100.
- For multiple choice circle your answer on this test paper.
- For short answer questions answer fully on this test paper, partial credit will be given.
- Once completed turn in to TA or instructor.
- Data sets are coming from

[UCI Machine Learning Repository](#) and R.

## Problem 1

(36 possible points, 4 points each part) We want to know which features helps us predict the average amount of **Balance** individuals maintain on their credit cards.

The features are as follows:

- *Income*: Income in \$1,000's
- *Rating*: Credit rating
- *Age*: Age in years
- *Education*: Education in years
- *Student*: A factor with levels **No** and **Yes** indicating whether the individual is a student or not
- The response variable - *Balance*: Average credit card balance in \$.

The name of the data set is called **Credit**.

- a. Is this a inference or prediction statistical learning problem?
- b. Is this a regression or classification problem?
- c. Give the model formula for our problem. Use the variable names in the formula.
- d. Give the R code to get the model for predicting the average **Balance**, given the features.

e. The following is the output from the data. Write out the equation with the estimates.

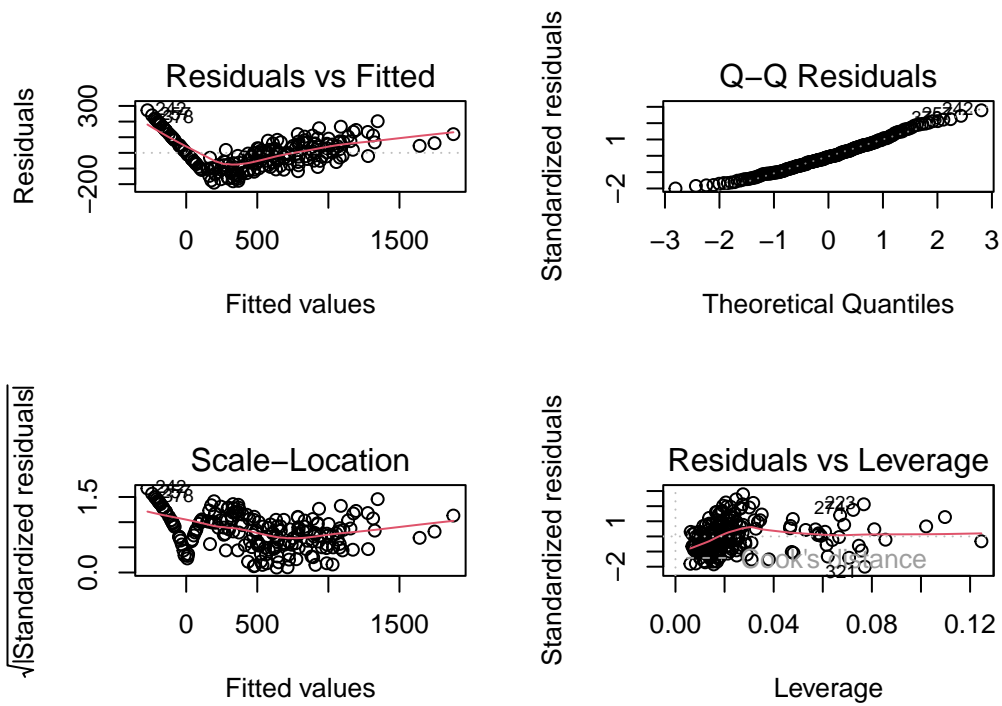
	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	-541.6613	29.1596	-18.5758	0.0000
Income	-7.4094	0.3318	-22.3303	0.0000
Rating	3.8874	0.0756	51.4424	0.0000
Age	-0.4332	0.4192	-1.0333	0.3028
StudentYes	402.0016	24.7729	16.2275	0.0000

f. Give the interpretation of the coefficient for the variable Age.

g. Are there any variables that are not needed in this model? Justify your answer.

h. What are the assumptions of this model?

i. The plot below are the diagnostics plots. Are any of the assumptions violated with this model?



## Problem 2

(28 points, 4 points each part) The aim is to predict which customers will default on their credit card debt.

*Response* - default: A factor with levels **No** and **Yes** indicating whether the customer defaulted on their debt.

### Predictors

- *student*: A factor with levels **No** and **Yes** indicating whether the customer is a student.
- *balance*: The average balance that the customer has remaining on their credit card after making their monthly payment.
- *income*: Income of customer.
- Data is called **Default**.

a. Is this a inference or prediction statistical learning problem?

b. Is this a regression or classification problem?

c. Give the model formula for our problem. Use the variable names in the formula.

d. Give the R code to get the model to predict the probability that a customer defaults given the other 3 features as the input variables.

- e. The following is the output from the data. Write out the equation with the estimates.

	Estimate	Std. Error	z value	Pr(> z )
(Intercept)	-17.0791	3.6264	-4.71	0.0000
studentYes	2.2897	1.5677	1.46	0.1441
balance	0.0064	0.0014	4.44	0.0000
income	0.0001	0.0001	2.17	0.0303

- f. Give the predicted probability of the customer default, given not a student, balance = 835.50 and income = 34,000. Would you predict the customer to default given these inputs?

- g. The following is the output from R. Determine  $R^2$  and give an interpretation.

Null deviance: 107.79 on 399 degrees of freedom  
 Residual deviance: 50.71 on 396 degrees of freedom

### Problem 3

(8 possible points) The following is using the `regsubset` function in R to determine the best subsets of variables to predict **Balance**.

```

      Income Rating Age StudentYes
1  ( 1 ) " "      "*"      " " " "
2  ( 1 ) "*"      "*"      " " " "
3  ( 1 ) "*"      "*"      " " "*"
4  ( 1 ) "*"      "*"      "*" "*"

```

	Adj.R2	Cp	BIC
1 Predictor	0.78	681.79	-295.92
2 Predictors	0.89	265.56	-420.05
3 Predictors	0.95	4.07	-585.11
4 Predictors	0.95	5.00	-580.90

- How many predictors would be best to predict **Balance**, (1, 2, 3, or 4)?
- Write the formula of the model with the best subset of predictors based on the output above.

#### Problem 4

(12 points) The following is the confusion matrix based on the model from problem 2 to predict if a customer will default. The columns are the actual customers (given observations), the rows are the predicted customers (predicted values).

	No	Yes
No	387	8
Yes	1	4

- Write the full code used to get this confusion matrix.
- Based on the confusion matrix, what is the error rate?
- Based on the confusion matrix, what is the sensitivity rate?



### Problem 5

(4 points) The following is a 95% confidence interval for **balance** from problem 1, with only **income** and **student** as the predictors. We want to predict **balance** for a student that has an income of \$45,000. Which statement is correct?

	fit	lwr	upr
1	747.56	571.52	923.59

- a. For one student that has an income of \$45,000, we predict the **balance** to be between 571.52 and 923.59 with 95% confidence.
- b. On average for all students that have an income of \$45,000, we we predict the **balance** to be between 571.52 and 923.59 with 95% confidence.
- c. For one student that regardless of the income, we predict the **balance** to be between 571.52 and 923.59 with 95% confidence.
- d. On average for all students regardless of income, we we predict the **balance** to be between 571.52 and 923.59 with 95% confidence.
- e. For a student that has an income of \$45,000, the **balance** will be 747.56.

### Problem 6

(4 points) The following is the ANOVA table from problem 1, where  $n = 200$  using **Income** and **Student** to predict **Balance**. What is the *AIC* statistic?

	Df	Sum Sq	Mean Sq	F value	Pr(>F)
Income	1	10823004.60	10823004.60	76.20	0.0000
Student	1	1154073.36	1154073.36	8.13	0.0048
Residuals	197	27981562.66	142038.39		

- a. 2185.7734
- b. 1738.0982
- c. 10823005
- d. 1154073
- e. 2375.7478

### Problem 7

(4 points) What value refers to the amount by which  $\hat{f}$  would change if we estimated it using a different training data set. This is the measurement of the precision of the data.

- a. Variance
- b. Bias
- c.  $\hat{\beta}_j$
- d.  $VIF$
- e.  $AIC$

### Problem 8

(4 points) Why do we split the data into training and testing data?

- a. To reduce the number of predictors.
- b. To increase the error.
- c. To avoid overfitting.
- d. To make sure we are correct all of the time with the model.
- e. None of these.