SLLD - Module 1

Classification

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14/2/2024

Libraries

```
library(dplyr)
library(caret)
library(MASS)
library(klaR)
library(mvtnorm)
```

Data

We simulate data as follows

```
set.seed(123)
n <- 500
p <- 5
X <- matrix(rnorm(n*p), nrow = n, ncol = p)
X <- data.frame(X)
colnames(X) <- paste("X", 1:p, sep="")
eta<-0.5-1*X[,1]-2*X[,2]+X[,3]+3*X[,4]+0.5*X[,5]
piy<-(exp(eta))/(1+exp(eta))
mean(piy)</pre>
```

[1] 0.5653752

```
Y<-rbinom(n, 1, piy)</pre>
 summary(Y)
     Min. 1st Qu. Median
##
                             Mean 3rd Ou.
                                               Max.
              0.00 1.00 0.56
                                      1.00
                                               1.00
##
     0.00
df<-cbind(Y,X)</pre>
set.seed(123)
training_samples <- df$Y %>%
   caret::createDataPartition(p = 0.8, list = FALSE)
# p indicates the percentage of training data
train <- df[training_samples, ]</pre>
test <- df[-training samples, ]</pre>
```

Simple Logistic Regression

The **glm()** function can be used to fit many types of generalized linear models, including logistic regression.

It is similar to **lm()**, except that we must linear model pass in the argument **family** = **binomial** in order to tell R to run a logistic regression rather than some other type of generalized linear model.

Using the training set, we build a simple logistic regression model using X_1 as the only explanatory variable of the response Y

```
simple glm <- glm(Y \sim X1,
                 data = train, family = 'binomial')
summary(simple glm)
##
## Call:
## glm(formula = Y ~ X1, family = "binomial", data = train)
##
## Coefficients:
##
             Estimate Std. Error z value Pr(>|z|)
## (Intercept) 0.2409 0.1028 2.343 0.0191 *
     ## X1
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
      Null deviance: 549.22 on 399 degrees of freedom
##
## Residual deviance: 533.02 on 398 degrees of freedom
## AIC: 537.02
##
## Number of Fisher Scoring iterations: 4
```

Let's see predictive power of our model in terms of **accuracy** -- i.e. the proportion of correct predictions, both true positives and true negatives, among the total number of cases examined

```
# Test for accuracy: predict test data
predict_1 <- predict(simple_glm, newdata = test,type = 'response')

# round up the predictions
predict_1 <- ifelse(predict_1>0.5, 1, 0)

# calculate accuracy
accuracySim <- mean(predict_1==test$Y)
accuracySim</pre>
```

[1] 0.71

```
## Reference
## Prediction 0 1
## 0 22 8
## 1 21 49
```

Note: the "event" is 0!

Multiple Logistic Regression

```
glm complete <- glm(Y ~ ., data=train, family = 'binomial')</pre>
summary(glm complete)
##
## Call:
## glm(formula = Y ~ ., family = "binomial", data = train)
##
## Coefficients:
             Estimate Std. Error z value Pr(>|z|)
##
## (Intercept) 0.5152 0.1759 2.929 0.00340 **
     -1.2380 0.2220 -5.577 2.44e-08 ***
## X1
            -2.4090 0.2807 -8.582 < 2e-16 ***
## X2
## X3 1.0528 0.1935 5.441 5.29e-08 ***
              3.0775 0.3355 9.173 < 2e-16 ***
## X4
              ## X5
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##
      Null deviance: 549.22 on 399 degrees of freedom
## Residual deviance: 231.04 on 394 degrees of freedom
## AIC: 243.04
##
```

Let's see its predictive accuracy

```
# Test for accuracy: predict test data
predict_1 <- predict(glm_complete, newdata =</pre>
                        test,type = 'response')
# round up the predictions
predict 1 <- ifelse(predict 1>0.5, 1, 0)
# calculate accuracy
 accuracySat <- mean(predict_1==test$Y)</pre>
accuracySat
## [1] 0.92
ConfMat_LR = confusionMatrix(as.factor(predict_1),
                               as.factor(test$Y))
ConfMat LR$table
##
             Reference
## Prediction 0 1
           0 38 3
##
            1 5 54
##
```

LDA and QDA

We use the function **lda** to perform linear discriminant analysis

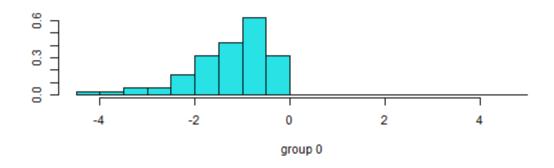
```
lda.Y <- lda(Y~ ., data=train)</pre>
lda.Y
## Call:
## lda(Y ~ ., data = train)
##
## Prior probabilities of groups:
## 0 1
## 0.4425 0.5575
##
## Group means:
##
            X1
                       X2
                                 Х3
                                            Χ4
                                                        X5
## 0 0.2168210 0.4320500 -0.1111468 -0.4935911 -0.20301669
## 1 -0.1689612 -0.3024828 0.1179516 0.5367388 0.04018593
##
## Coefficients of linear discriminants:
##
            LD1
## X1 -0.4173204
## X2 -0.8728278
## X3 0.4242211
## X4 1.1153619
## X5 0.2349530
```

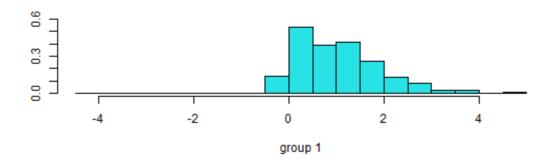
Here is the model accuracy on training data.

```
predmodel.train.lda = predict(lda.Y, data=train_transformed)
ConfMat_LDAtrain = confusionMatrix(as.factor(
  predmodel.train.lda$class),
                              as.factor(train$Y))
ConfMat_LDAtrain$table
            Reference
##
## Prediction 0 1
           0 150 32
##
##
           1 27 191
ConfMat_LDAtrain$byClass[1:2]
## Sensitivity Specificity
    0.8474576 0.8565022
##
```

The plot below shows how the response class has been classified by the LDA classifier. The x-axis shows the value of the line defined by the coefficient of linear discriminant for LDA. Groups are the ones in the response classes.

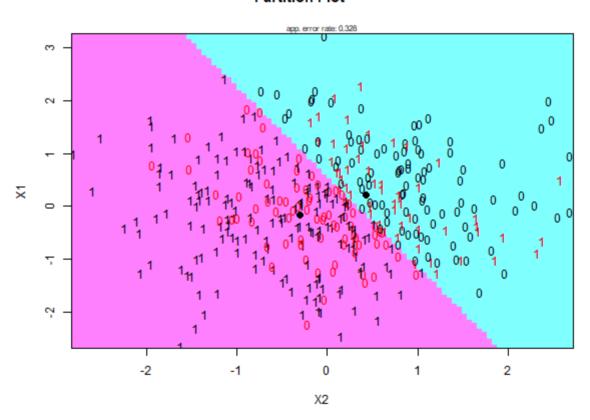
ldahist(predmodel.train.lda\$x[,1], g= predmodel.train.lda\$class)





We use the function **partimat** to see geometric division

Partition Plot



Now we check the model accuracy on test data.

```
predmodel.test.lda = predict(lda.Y, newdata=test)
ConfMat_LDAtest = confusionMatrix(as.factor(
  predmodel.test.lda$class),
                as.factor(test$Y))
ConfMat LDAtest$table
            Reference
##
## Prediction 0 1
          0 38 4
##
##
           1 5 53
mean(predmodel.test.lda$class==test$Y)
## [1] 0.91
ConfMat_LDAtest$byClass[1:2]
## Sensitivity Specificity
    0.8837209 0.9298246
##
```

Next we will fit the model trough QDA. The command is similar to LDA and it outputs the prior probabilities and Group means. Note that "Prior Probabilities" and "Group Means" values are same as of LDA.

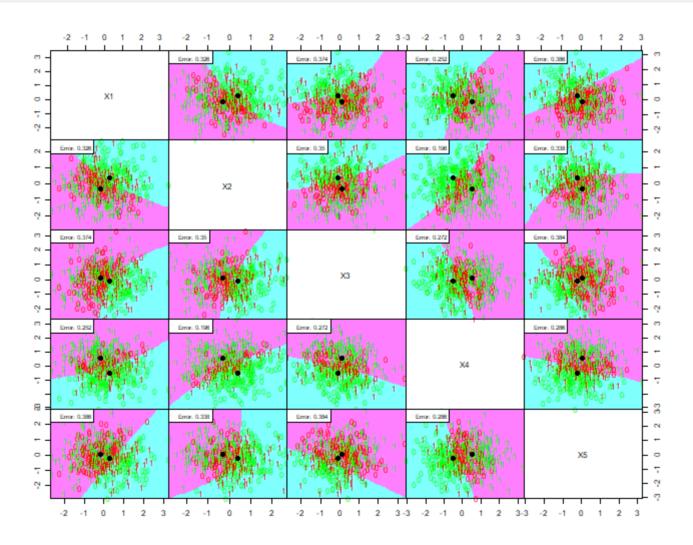
We try QDA on all original variables

```
qda.Y <- qda(Y~ ., data=df)
qda.Y
## Call:
## qda(Y \sim ., data = df)
##
## Prior probabilities of groups:
##
     0
## 0.44 0.56
##
## Group means:
             X1
                       X2
                                   X3
                                              X4
##
                                                           X5
## 0 0.2841825 0.3958666 -0.08118516 -0.5294269 -0.20558826
## 1 -0.1615176 -0.3152072 0.11057540 0.5208529 0.04717386
```

Now we check the model accuracy on test data.

```
predmodel.test.qda = predict(qda.Y, newdata=test)
ConfMat_QDAtest = confusionMatrix(as.factor(
  predmodel.test.qda$class),
                as.factor(test$Y))
ConfMat ODAtest$table
            Reference
##
## Prediction 0 1
## 0 37 4
##
          1 6 53
mean(predmodel.test.qda$class==test$Y)
## [1] 0.9
ConfMat_QDAtest$byClass[1:2]
## Sensitivity Specificity
    0.8604651 0.9298246
##
```

```
partimat(factor(Y) ~ .,
data=df, method = "qda", plot.matrix=TRUE,
col.correct='green', col.wrong='red')
```



kNN

We are going to use the **knn3** function within caret package. Let's train the knn with k = 1, 10

```
knn Y1 \leftarrow knn3(factor(Y) \sim ...data=train, k = 1)
 knn Y10 <- knn3(factor(Y) \sim .,data=train, k = 10)
predict_knn1 <- predict(knn_Y1, test, type='class')</pre>
ConfMat_knn1 = confusionMatrix(predict_knn1, as.factor(test$Y))
 ConfMat knn1$overall[1] # the accuracy
## Accuracy
       0.83
##
predict knn10 <- predict(knn Y10, test, type='class')</pre>
ConfMat knn10 = confusionMatrix(predict knn10, as.factor(test$Y))
 ConfMat knn10$overall[1] # the accuracy
## Accuracy
##
       0.86
```

Now it's your turn!!!