

$$\det \begin{bmatrix} 1 & r & r \\ \lambda & q & \Sigma \\ v & \gamma & \omega \end{bmatrix} \stackrel{\text{Sarrus}}{=} (-1)^{1+1} \times 1 \times \begin{vmatrix} q & \Sigma \\ \gamma & \omega \end{vmatrix} + (-1)^{1+2} \times \lambda \times \begin{vmatrix} r & r \\ \gamma & \omega \end{vmatrix} + (-1)^{1+3} \times v \times \begin{vmatrix} r & r \\ q & \Sigma \end{vmatrix}$$

$$\det = \overset{r1}{(\Sigma\omega - r\Sigma)} + \overset{-\lambda}{- \lambda (10 - 11)} + \overset{-19}{v(1 - rv)} = \boxed{-\Sigma\lambda}$$

$$\det \begin{bmatrix} 1+x & r+x & r+x \\ \lambda+x & q+x & \Sigma+x \\ v+x & \gamma+x & \omega+x \end{bmatrix} \stackrel{\text{Sarrus}}{=} (-1)^{1+1} \times (1+x) \begin{vmatrix} q+x & \Sigma+x \\ \gamma+x & \omega+x \end{vmatrix} + (-1)^{1+2} \times (\lambda+x) \begin{vmatrix} r+x & r+x \\ \gamma+x & \omega+x \end{vmatrix}$$

$$+ (-1)^{1+3} \times (v+x) \begin{vmatrix} r+x & r+x \\ q+x & \Sigma+x \end{vmatrix} = (1+x) \left[\overset{\Sigma x + r1}{(q+x)(\omega+x) - (\gamma+x)(\Sigma+x)} \right]$$

$$- (\lambda+x) \left[\underset{-rx-1}{(r+x)(\omega+x) - (r+x)(\gamma+x)} \right] + (v+x) \left[\underset{-7x-19}{(r+x)(r+x) - (q+x)(r+x)} \right]$$

$$= \underline{\Sigma x} + \underline{r1} + \underline{\Sigma x r} + \underline{r1 x} + \underline{14x} + \underline{4\Sigma} + \underline{rx r} + \underline{\lambda x} - \underline{\Sigma x x} - \underline{11r^2} - \underline{7x r} - \underline{19x}$$

$$\det = \boxed{-12x - \Sigma\lambda}$$

$$\begin{aligned}
 \det \begin{bmatrix} x^1 & x^2 & x^3 \\ x^4 & x^5 & x^6 \\ x^7 & x^8 & x^9 \end{bmatrix} &= (-1)^{1+1} x^1 \begin{vmatrix} x^5 & x^6 \\ x^8 & x^9 \end{vmatrix} + (-1)^{1+2} x^2 \begin{vmatrix} x^4 & x^6 \\ x^7 & x^9 \end{vmatrix} + (-1)^{1+3} x^3 \begin{vmatrix} x^4 & x^5 \\ x^7 & x^8 \end{vmatrix} \\
 &+ (-1)^{2+1} x^4 \begin{vmatrix} x^1 & x^3 \\ x^5 & x^6 \end{vmatrix} = x(x^5 - x^8) - x^2(x^4 - x^7) + x^3(x^4 - x^7) \\
 &= x^{11}(x^3 - 1) - x^{10}(1 - x^2) + x^{11}(1 - x^2)
 \end{aligned}$$