

$$1 \times 1: A = [1 \ 0]_{1 \times 2}, B = A^T \Rightarrow AB = 1 \rightarrow \text{invertible} \checkmark$$

$$2 \times 2: A = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \end{bmatrix}_{2 \times 3}, B = A^T \Rightarrow AB = I_2 \rightarrow \text{invertible} \checkmark$$

$$3 \times 3: A = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{3 \times 4}, B = A^T \Rightarrow AB = I_3 \rightarrow \text{invertible} \checkmark$$

$$\vdots$$

$$n \times n: A = \begin{bmatrix} 1 & 0 & \dots & 0 & 0 \\ 0 & 1 & & & \\ \vdots & & \ddots & & \\ 0 & 0 & \dots & 1 & 0 \end{bmatrix}_{n \times (n+1)}, B = A^T \Rightarrow AB = I_n \rightarrow \text{invertible} \checkmark$$

B

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