

$$\begin{vmatrix} 0 & 0 & a_1 & b_1 \\ 0 & 0 & a_r & b_r \\ a_r & b_r & 0 & 0 \\ a_r & b_r & 0 & 0 \end{vmatrix} \rightarrow \text{سطر اول} = a_1 (b_r (a_r b_r - b_r a_r) + b_1 (a_r (a_r b_r - b_r a_r))$$

$$= (a_r b_r - b_r a_r) (a_1 b_r + a_r b_1)$$

$$\begin{vmatrix} a_1 & 0 & 0 & b_1 \\ 0 & a_r & b_r & 0 \\ 0 & b_r & a_r & 0 \\ b_r & 0 & 0 & a_r \end{vmatrix} = \rightarrow \text{سطر اول، سطر اول}$$

$$= a_1 \begin{vmatrix} a_r & b_r & 0 \\ b_r & a_r & 0 \\ 0 & 0 & a_r \end{vmatrix} - b_1 \begin{vmatrix} 0 & a_r & b_r \\ 0 & b_r & a_r \\ b_r & 0 & 0 \end{vmatrix}$$

$$= a_1 a_r (a_r a_r - b_r b_r) - b_1 b_r (a_r a_r - b_r b_r)$$

$$= (a_r a_r - b_r b_r) (a_1 a_r - b_1 b_r)$$