

$$\begin{bmatrix} 1 & 1 & 0 & 0 & 0 \\ -1 & -1 & 1 & 0 & 0 \\ 0 & -1 & 1 & 1 & 0 \\ 0 & 0 & -1 & 1 & 1 \\ 0 & 0 & 0 & -1 & 1 \end{bmatrix} \xrightarrow{R_1 + R_2 \rightarrow R_2}$$

$$\begin{bmatrix} 1 & 1 & 0 & 0 & 0 \\ 0 & p & 1 & 0 & 0 \\ 0 & -1 & 1 & 1 & 0 \\ 0 & 0 & -1 & 1 & 1 \\ 0 & 0 & 0 & -1 & 1 \end{bmatrix} \xrightarrow{R_2 + \frac{1}{p}R_2 \rightarrow R_2} \begin{bmatrix} 1 & 1 & 0 & 0 & 0 \\ 0 & p & 1 & 0 & 0 \\ 0 & 0 & \frac{p+1}{p} & 1 & 0 \\ 0 & 0 & -1 & 1 & 1 \\ 0 & 0 & 0 & -1 & 1 \end{bmatrix}$$

$$1 \times \begin{vmatrix} -1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 1 \\ 0 & 0 & 1 & 1 \\ 0 & 0 & 0 & 1 \end{vmatrix} - 1 \times \begin{vmatrix} 0 & 1 & 0 & 0 \\ 0 & \frac{p+1}{p} & 1 & 0 \\ 0 & -1 & 1 & 1 \\ 0 & 0 & -1 & 1 \end{vmatrix} + 0 - 0 + 0 =$$

$$= p \times \begin{vmatrix} \frac{p+1}{p} & 1 & 0 \\ 1 & 1 & 1 \\ 0 & -1 & 1 \end{vmatrix} - 1 \times \begin{vmatrix} 0 & 1 & 0 \\ 0 & 1 & 1 \\ 0 & -1 & 1 \end{vmatrix} =$$

$$p \times \begin{vmatrix} \frac{p+1}{p} & 1 & 0 \\ 1 & 1 & 1 \\ 0 & -1 & 1 \end{vmatrix} = p \times \left(\underbrace{\frac{p+1}{p} \times p - (1 \times 1)}_{p+1} \right) = p \times \Sigma = \Lambda$$