

SECTION A (50 Marks)

Answer all the questions

1. Using logarithms evaluate

$$\left[\frac{0.9329}{4.329^2 - 3.921^2} \right]^{\frac{1}{5}}$$

2. If $x = -\frac{1}{2}$ and $x = \frac{2}{3}$ are the solutions of a quadratic equation. Write the equation in the form

$$ax^2 + bx + c = 0 \text{ where } a, b \text{ and } c \text{ are integers}$$

3. A student corrected $2.\dot{3}\dot{2}$ to 2 s.f as 2.3. Determine the percentage error in the estimation.

4. The figure below represents a scale drawing of a rectangular piece of land, RSTU. RS=18cm and ST=14cm.



An electric post P, is to be erected inside the piece of land. On the scale drawing, shade the possible region in which P would lie such that $PU > PT$ and $PS = 14\text{cm}$.

5. Two points A and B have coordinates (-2, 3) and (1, 3) respectively. A translation maps point A to A'(10,10). a) Find the coordinates of B', the image of B under the translation.
6. Solve the inequality

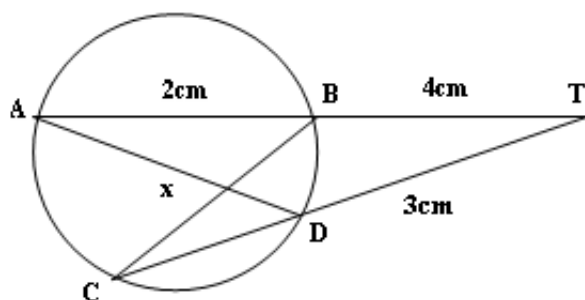
$$3 - 2x < x \leq \frac{2x+5}{3} \text{ and show the solution on a number line.}$$

7. Without using tables evaluate

$$\frac{\cos 30^\circ}{\tan 60^\circ - \sin 45^\circ}$$

9. Konango invested Ksh 8000 compounded quarterly at a rate of r% p.a. The value of the money after $2\frac{1}{4}$ years is Kshs 18000. Determine the value of r.

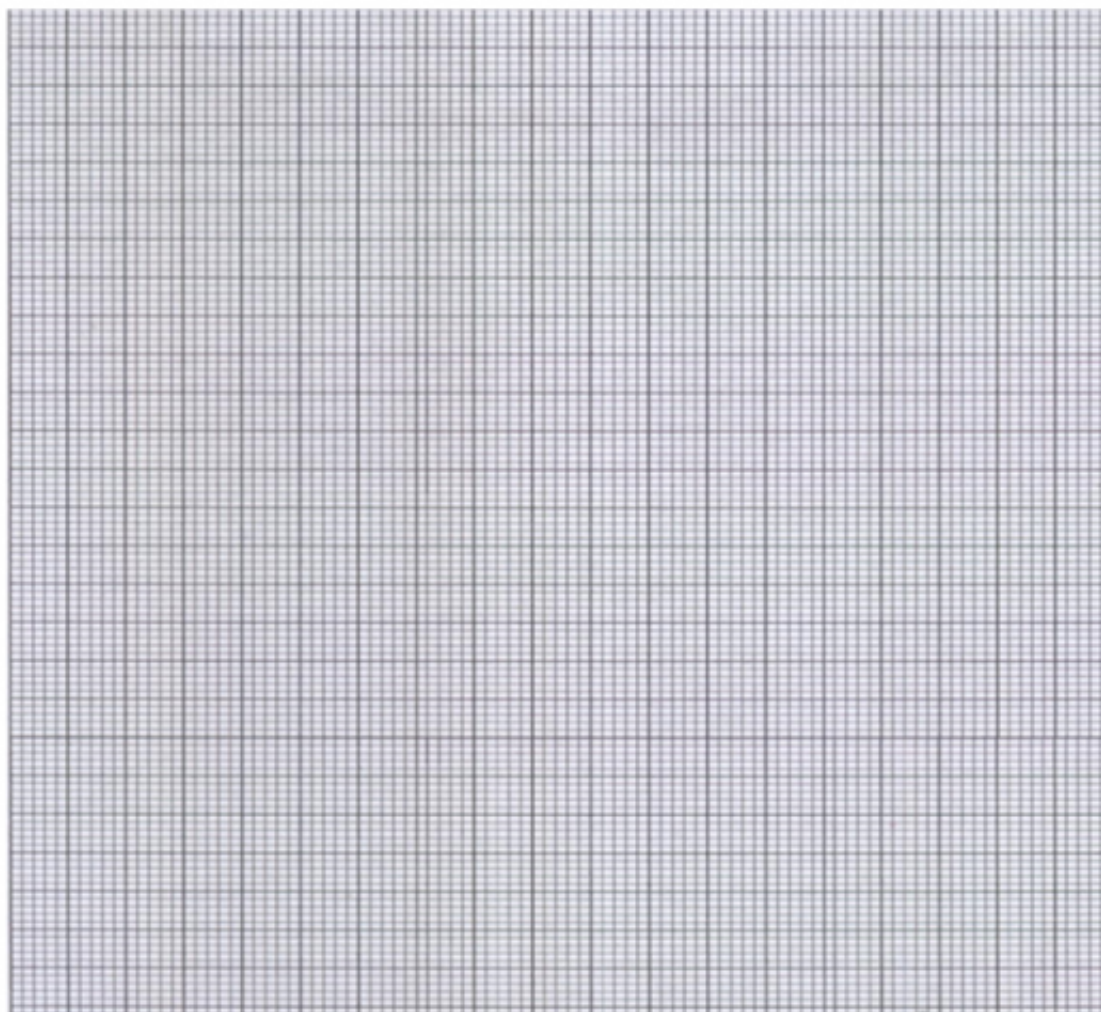
10. The figure below shows a circle with chords AB and CD produced and meeting externally at T. Chords AD and BC intersect internally at x. If BT= 4cm, AB=2cm and DT=3cm



- a) Find CT
- b) Show that triangles ADT and CBT are similar.
11. If $A = \begin{pmatrix} 3 & 5 \\ 4 & 7 \end{pmatrix}$ and $B = \begin{pmatrix} 2 & 3 \\ -1 & 5 \end{pmatrix}$. Find C if $C = A^{-1} B + B^2$
12. Make P the subject of the formula $\frac{y}{r} = \frac{a}{pn} + \frac{b}{ap}$
13. A varies as a constant and partly inversely as the cube root of P. When A=8, P=8, when A=7, P=27. Find the law connecting A and P Hence find A when P=125.
14. a) Expand $\left(2x - \frac{1}{x^2}\right)^3$ upto the fourth term.
- b) Use your expansion to give the coefficient of x^{-4}
15. The table below shows values of x and y for the function $y = 2 \sin 3x^\circ$ in the range $0^\circ \leq x \leq 150^\circ$.

x°	0	15	30	45	60	75	90	105	120	135	150
y	0	1.4	2	1.4	0	-1.4	-2	-1.4	0	1.4	2

- a) On the grid provided, Draw the graph of $y = 2 \sin 3x^\circ$.



b) From the graph determine the period.

SECTION B (50 Marks)

ANSWER ONLY FIVE QUESTIONS

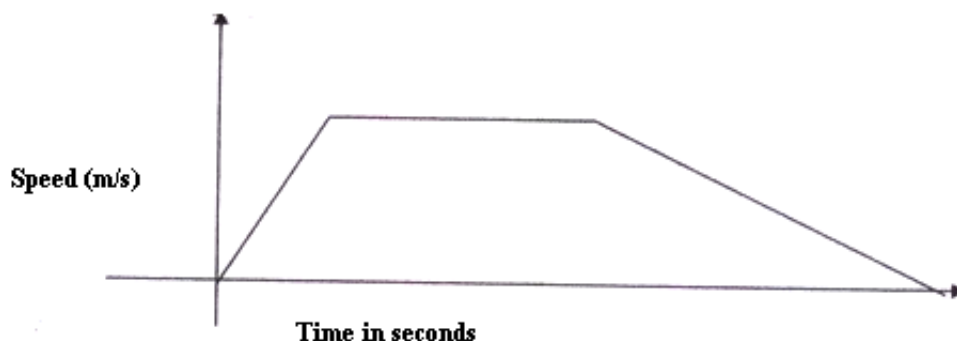
17. The table below shows income tax rates for all income earned.

Monthly income in Kenya shillings (Kshs)	Tax rate percentage % in each shilling
Upto 9680	10
From 9681 to 18800	15
From 18801 to 27920	20
From 27921 to 37040	25
From 37041 and above	30

Owenga pays a monthly tax of Kshs 4600. His monthly relief is Ksh 1200. He gets medical allowance of Ksh 3500 monthly. He is housed by the employer and pays a nominal rent of Ksh.960 per month.

Determine

- a) His gross tax per annum.
- b) His taxable income in Kshs. per month.
- c) His basic salary per month in Kshs.
18. The diagram below shows the speed- time for a train travelling between two stations. The train starts from rest and accelerates uniformly for 150 seconds. It then travels at a constant speed for 300 seconds and finally decelerates uniformly for 200 seconds.



Given that the distance between the two stations is 10450m, calculate the;

- a) Maximum speed , Km/h, the train attained;
- b) Acceleration;
- c) Distance the train travelled during the last 100 seconds;
- d) Time the train takes to travel the first half of the journey.
19. The probability that it rains on a given day is $\frac{3}{5}$. If it rains the probability of a student going to school by bus is $\frac{7}{10}$ otherwise he walks. If it does not rain, the probability of walking to school is $\frac{9}{10}$. When he walks to school the probability of getting late is $\frac{9}{10}$. When he goes by bus the probability of getting late is $\frac{1}{5}$.
- a) Draw a tree diagram to represent the information.
- b) Find the probability that i) A student goes to school by bus.
- ii) A student is late for school.
- iii) A student walks to school and arrives in time.
20. a) Two towns A and B lie on the same latitude in the southern hemisphere. When it is 8.00a.m at A, it is 10.00a.m at B same day. If the longitude of A is 40°E find the longitude of B.
- b) A plane leaves A going to B and takes 5 hours to arrive at B travelling along a parallel of latitude at 400km/hr. Find
- i) the maximum time the plane could have taken to travel from A to B.

ii) the radius of the circle of latitude on which towns A and B are situated.

iii) The latitude of the two towns

(Take $R=6370\text{km}$ and $\pi = \frac{22}{7}$)

21. A water vendor has a tank of capacity 18,900 litres. The tank is being filled with water from two pipes A and B which are closed immediately when the tank is full. Water flows at the rate of $150000\text{cm}^3/\text{minute}$ through pipe B.
- a) If the tank is empty and the two pipes are opened at the same time, calculate the time it takes to fill the tank.
- b) On a certain day the vendor opened the two pipes A and B to fill the empty tank. After 25 minutes he opened the outlet tap to supply water to his customers at an average rate of 20 litres per minute.
- i) Calculate the time it took to fill the tank on that day.
- ii) The vendor supplied a total of 542 jerricans, each containing 25 litres of water, on that day. If the water that remained in the tank was 6 300 litres, calculate, in litres, the amount of water that was wasted.
22. The table below shows the marks scored by students in a chemistry exam.

Marks	30 - 34	35 -39	40 - 44	45 - 49	50 -54	55 -59	60 - 64
No. of students	3	6	5	12	8	9	7

- a) Calculate the interquartile range
- b) Using an assumed mean of 47;
- i) Determine the variance of the distribution.
- ii) Hence determine the standard deviation.
23. The product of the first three terms of a geometric progression is 64. If the first term is a, and the common ratio is r.
- a) Express r in terms of a.
- b) Given that the sum of the three terms is 14
- i) Find the values of a and r and hence write down two possible sequences each up to the 4th term
24. a) Draw a graph of $y = x^2 + 1$ for $0 \leq x \leq 4$
- b) Estimate the area bounded by the y-axis and the line $x=4$ using trapezium rule with 8 trapezia.
- c) Determine the actual area by integration.
- d) Calculate the error in the area obtained by applying the trapezoidal rule.