

Overview of the Yambo code: main features and performance

D. Sangalli

Istituto di Struttura della Materia (CNR),
Area della Ricerca di Roma 1, Monterotondo Scalo, Italy.

the **Yambo** team



CNR
Istituto di Struttura
della Materia

11 – 15 March 2024

I. The yambo code

II. abinitio MBPT & the QP concept

III. Excitons: the BSE



Part I

The yambo code

Theory

Many-Body perturbation Theory

Time-dependent density
functional theory

Interfaces

Planewave

Pseudopotential codes:



www.yambo-code.eu

MaX flagship code

the Yambo team

Theory

Many-Body perturbation Theory

Time-dependent density
functional theory

Interfaces

Planewave

Pseudopotential codes:



Libraries

ScaLAPACK



www.yambo-code.eu

MaX flagship code

the Yambo team

Theory

Many-Body perturbation Theory

Time-dependent density
functional theory

Interfaces

Planewave
Pseudopotential codes:



Libraries

ScaLAPACK



www.yambo-code.eu

MaX flagship code

Different projects



Developers



the Yambo team

Properties

GPL

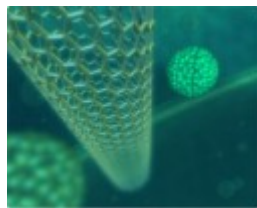
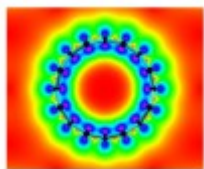
Quasi-particles
Optics and excitons
Magneto-optics & dichroism
Electron-phonon coupling
Real-time propagation
Non-linear optics
Pump and probe experiments



Development (pre-GPL) version

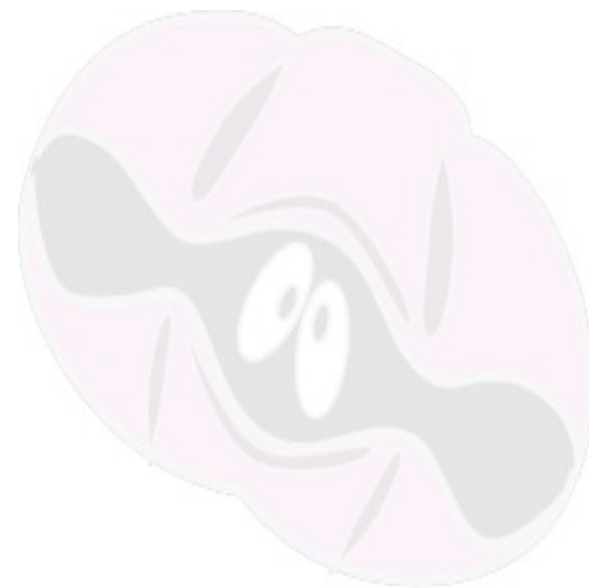
Exciton-phonon coupling
Carrier dynamics
Ehrenfest dynamics
Magnons

Applications



www.yambo-code.eu

MaX
flagship code



the Yambo team

Properties

GPL

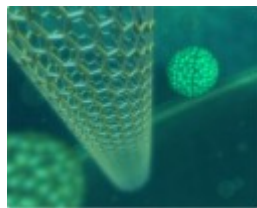
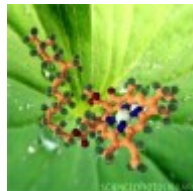
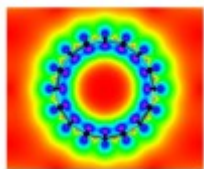
Quasi-particles
Optics and excitons
Magneto-optics & dichroism
Electron-phonon coupling
Real-time propagation
Non-linear optics
Pump and probe experiments



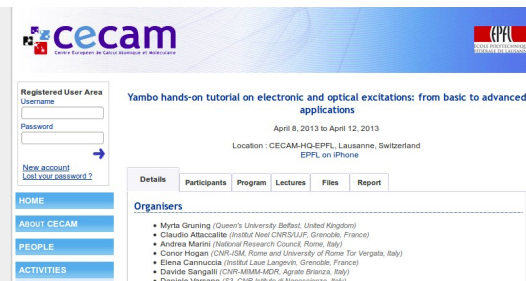
Development (pre-GPL) version

Exciton-phonon coupling
Carrier dynamics
Ehrenfest dynamics
Magnons

Applications



Schools



Community & Publications

Growing community
of users using
Yambo for fore-
front research.
More than 200
publications.



Support & reach out



Git
repository



Online documentation
and tutorials

www.yambo-code.eu

MaX
flagship code



Dedicated User Forum

the Yambo team

Properties

GPL

Quasi-particles

Optics and excitons

Magneto-optics & dichroism

Electron-phonon coupling

Real-time propagation

Non-linear optics

Pump and probe experiments

Development (pre-GPL) version

Exciton-phonon coupling

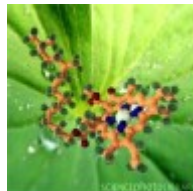
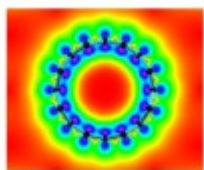
Carrier dynamics

Ehrenfest dynamics

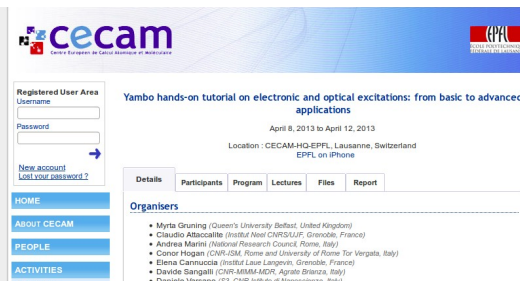
Magnons



Applications



Schools

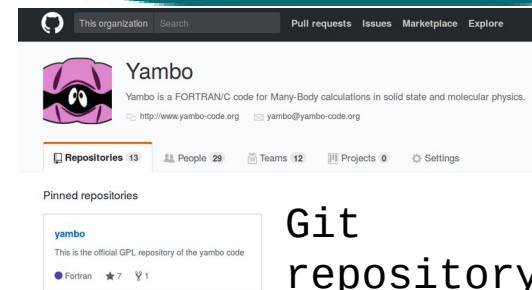


Community & Publications

Growing community of users using Yambo for fore-front research. More than 200 publications.



Support & reach out



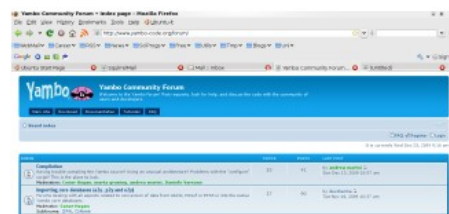
Git repository



Online documentation and tutorials

www.yambo-code.eu

**MaX
flagship code**

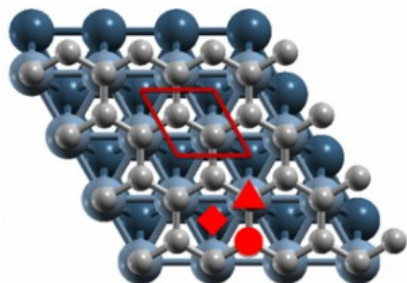


Dedicated User Forum

the Yambo team

Performances

GW study of
Graphene @ Co(0001) interface

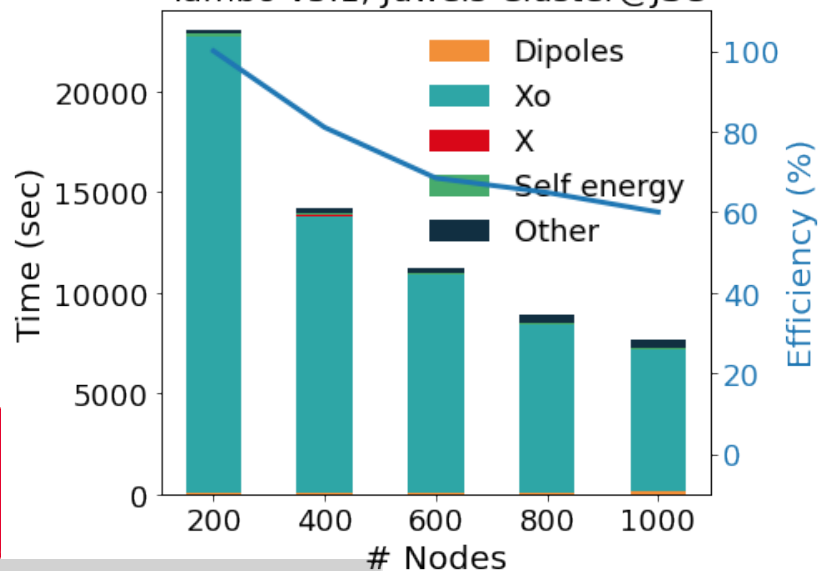


Yambo compiled with ifort (**intel**).
MPI + OpenMP

`mpirun -np #MPI`
`#MPI=4`
`#THREADS=24 (2*#cores / #MPI)`

Juwels-Cluster.
48 **intel** cores per node

Yambo v5.1, Juwels-Cluster@JSC

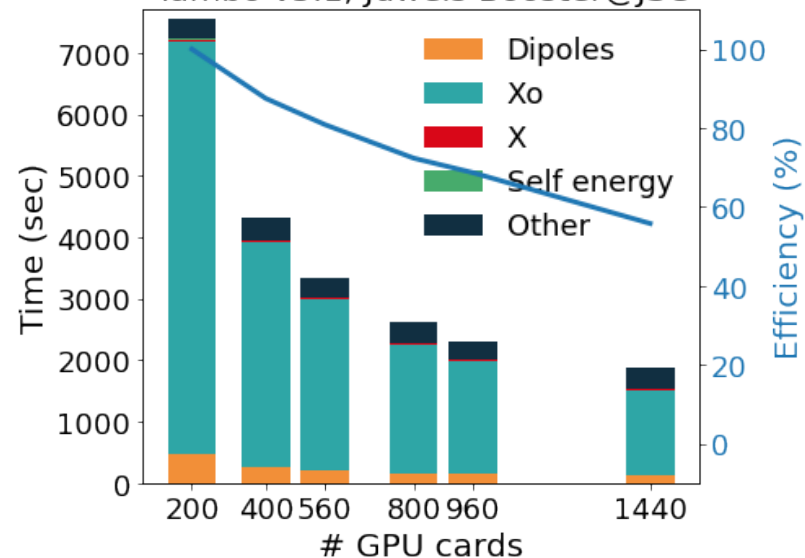


Yambo compiled with nvfortran (**nvidia**).
MPI + OpenMP + Cudafortran
(working on OpenACC)

`mpirun -np #MPI`
`#MPI=4 (= #cards per node)`
`#THREADS=8 (no effect here)`

Juwels-Booster.
48 AMD cores per node
4 **Nvidia** A100 cards per node

Yambo v5.1, Juwels-Booster@JSC



Data available at: <http://www.gitlab.com/max-centre/Benchmarks>

MAX

the Yambo team



Part II

Abinitio

Many-body

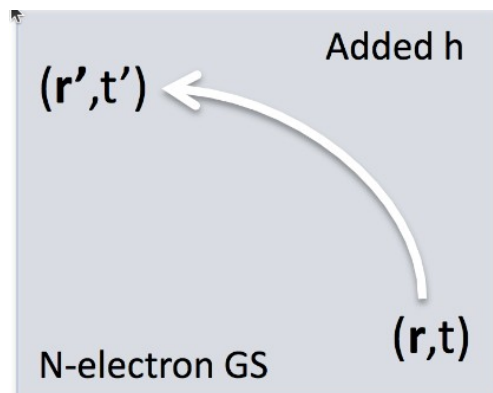
Perturbation-Theory

The Many Body Green Function

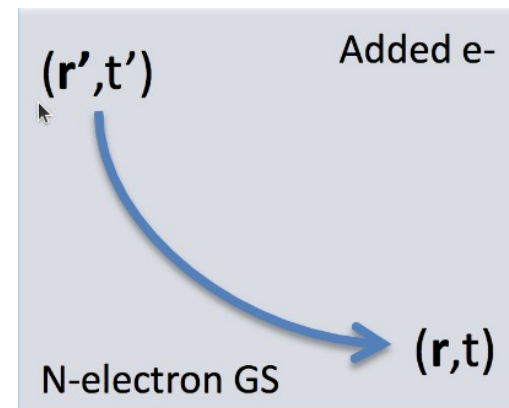
Time ordered Green function

$$iG(r, t; r', t') = \langle \phi_0^N | T [\hat{\psi}(r, t) \hat{\psi}^\dagger(r', t')] | \phi_0^N \rangle$$

$$-\theta(t' - t) \langle \phi_0^N | \hat{\psi}^\dagger(r', t') \hat{\psi}(r, t) | \phi_0^N \rangle + \theta(t - t') \langle \phi_0^N | \hat{\psi}(r, t) \hat{\psi}^\dagger(r', t') | \phi_0^N \rangle$$

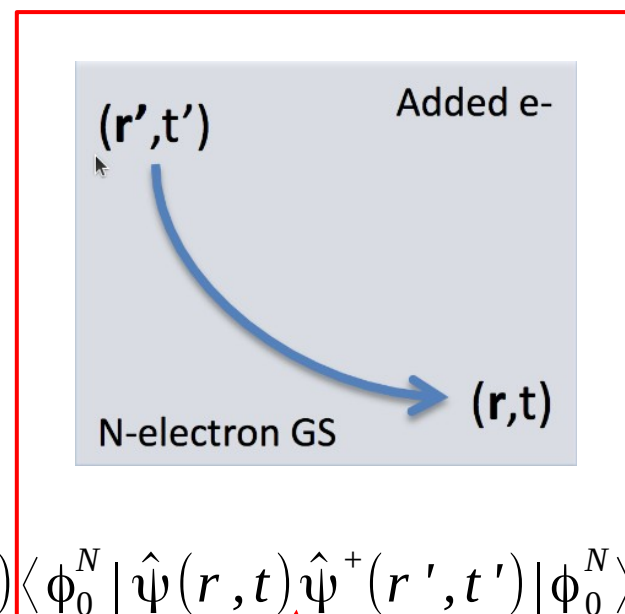
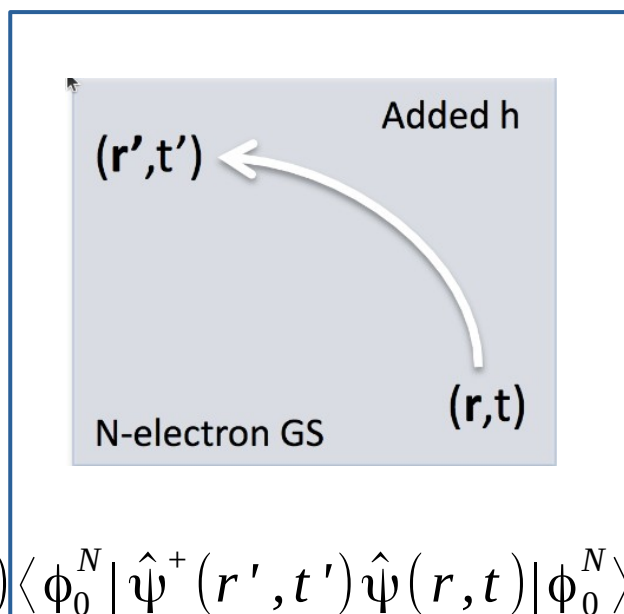


$$iG^<(r, t; r', t')$$



$$iG^>(r, t; r', t')$$

Lehmann Representation



$$-\theta(t'-t)\langle\phi_0^N|\hat{\psi}^+(r',t')\hat{\psi}(r,t)|\phi_0^N\rangle+\theta(t-t')\langle\phi_0^N|\hat{\psi}(r,t)\hat{\psi}^+(r',t')|\phi_0^N\rangle$$

$$iG(r,t;r',t')=\theta(t'-t)\sum_{\lambda}\langle\phi_0^N|\hat{\psi}^+(r',t')|\phi_{\lambda}^{N-1}\rangle\langle\phi_{\lambda}^{N-1}|\hat{\psi}(r,t)|\phi_0^N\rangle$$

$$-\theta(t-t')\sum_{\lambda}\langle\phi_0^N|\hat{\psi}(r,t)|\phi_{\lambda}^{N+1}\rangle\langle\phi_{\lambda}^{N+1}|\hat{\psi}^+(r',t')|\phi_0^N\rangle$$

Lehmann Representation

$$iG(r, t; r', t') = \theta(t' - t) \sum_{\lambda} \langle \phi_0^N | \hat{\psi}^+(r', t') | \phi_{\lambda}^{N-1} \rangle \langle \phi_{\lambda}^{N-1} | \hat{\psi}(r, t) | \phi_0^N \rangle$$

$$- \theta(t - t') \sum_{\lambda} \langle \phi_0^N | \hat{\psi}(r, t) | \phi_{\lambda}^{N+1} \rangle \langle \phi_{\lambda}^{N+1} | \hat{\psi}^+(r', t') | \phi_0^N \rangle$$

$$\hat{\psi}(r, t) = e^{i\hat{H}t} \hat{\psi}(r) e^{-i\hat{H}t}$$

$$f_{\lambda}^{N-1}(r) = \langle \phi_{\lambda}^{N-1} | \hat{\psi}(r) | \phi_0^N \rangle$$

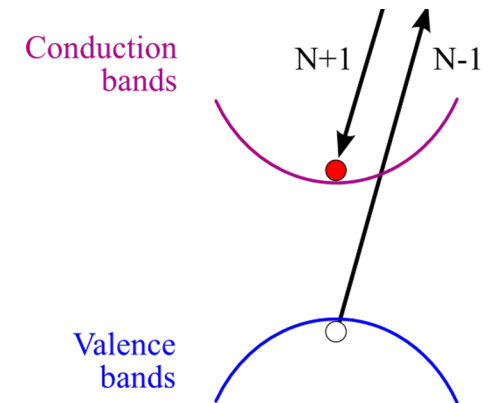
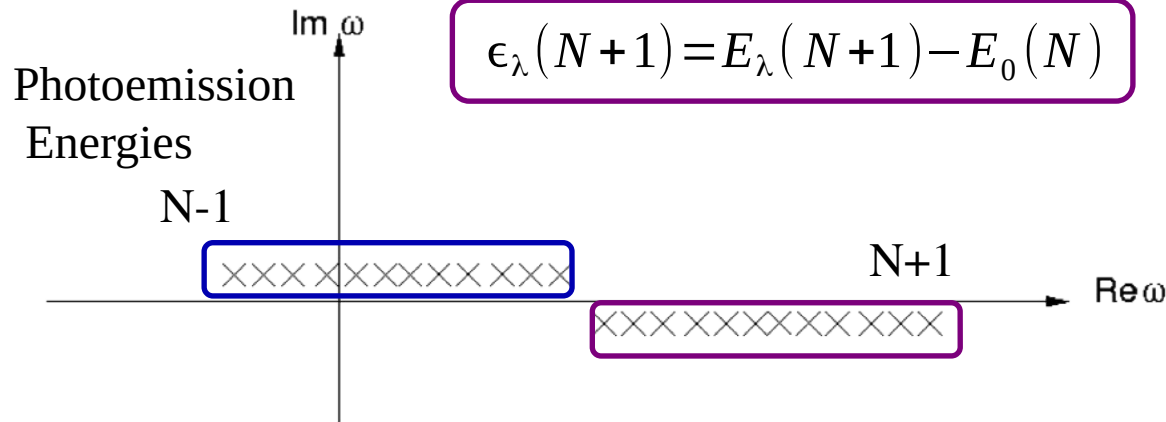
$$G(r, r', \omega) = \lim_{\eta \rightarrow 0} \sum_{\lambda} \frac{[f_{\lambda}^{N-1}(r)]^* f_{\lambda}^{N-1}(r')}{\omega + (E_{\lambda}^{N-1} - E_0^N) - i\eta} + \frac{f_{\lambda}^{N+1}(r) [f_{\lambda}^{N+1}(r')]^*}{\omega - (E_{\lambda}^{N+1} - E_0^N) + i\eta}$$

Poles of the GF

$$G(r, r', \omega) = \lim_{\eta \rightarrow 0} \sum_{\lambda} \frac{[f_{\lambda}^{N-1}(r)]^* f_{\lambda}^{N-1}(r')}{\omega + (E_{\lambda}^{N-1} - E_0^N) - i\eta} + \frac{f_{\lambda}^{N+1}(r) [f_{\lambda}^{N+1}(r')]^*}{\omega - (E_{\lambda}^{N+1} - E_0^N) + i\eta}$$

$$\epsilon_{\lambda}(N-1) = -(E_{\lambda}(N-1) - E_0(N)) \quad G^{<}$$

$$\epsilon_{\lambda}(N+1) = E_{\lambda}(N+1) - E_0(N) \quad G^{>}$$

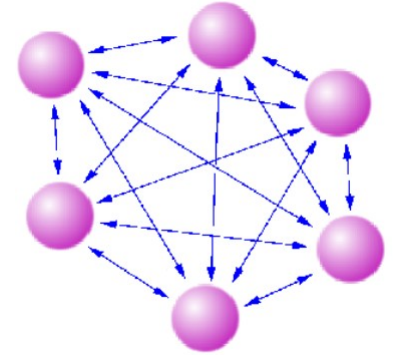


Many-Body Perturbation-Theory

$$H = \sum_{i=1}^N h(\mathbf{r}_i) + \sum_{\substack{i,j=1 \\ i \neq j}}^N V(\mathbf{r}_i, \mathbf{r}_j)$$

Interacting particles
Ground state

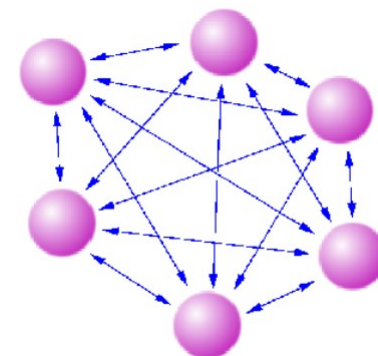
$$iG(r, t; r', t') = \langle \phi_0^N | T[\hat{\psi}(r, t) \hat{\psi}^+(r', t')] | \phi_0^N \rangle$$



Many-Body Perturbation-Theory

$$H = \sum_{i=1}^N h(\mathbf{r}_i) + \sum_{\substack{i,j=1 \\ i \neq j}}^N V(\mathbf{r}_i, \mathbf{r}_j)$$

Interacting particles
Ground state



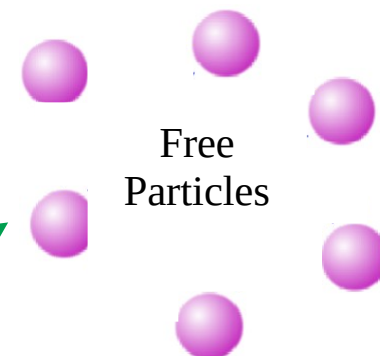
$$iG(r, t; r', t') = \langle \phi_0^N | T[\hat{\psi}(r, t) \hat{\psi}^\dagger(r', t')] | \phi_0^N \rangle$$

Gell-Mann & Low theorem

$$G(\mathbf{r}, t, \mathbf{r}', t') = -\frac{i}{\langle \psi_0 | \hat{U} | \psi_0 \rangle} \sum_{n=0}^{+\infty} \frac{(-i)^n}{n!} \int_{-\infty}^{+\infty} dt_1 \cdots dt_n e^{-\eta(|t_1| + \cdots + |t_n|)} \times$$

$$\langle \psi_0 | T[\hat{V}(t_1) \cdots \hat{V}(t_n) \hat{\psi}(t) \hat{\psi}^\dagger(t')] | \psi_0 \rangle$$

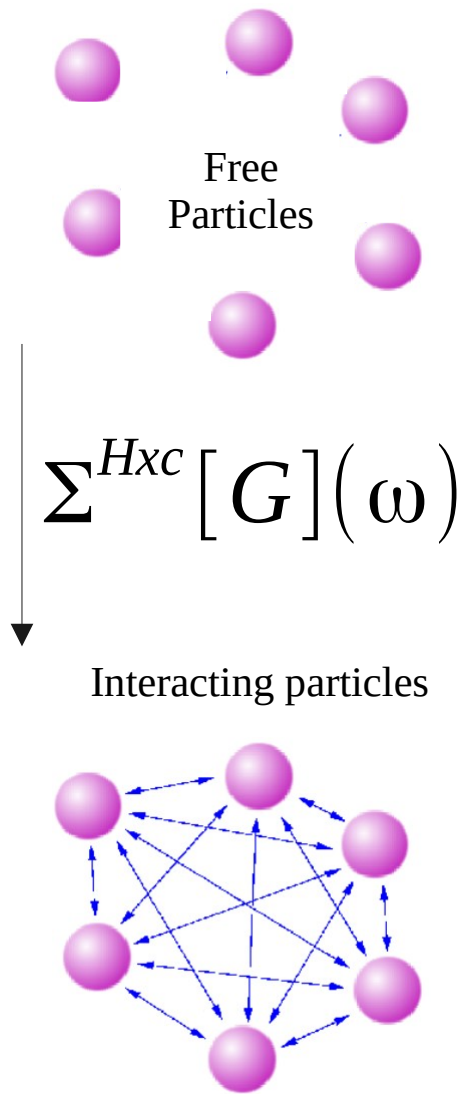
Free
Particles



$$\Sigma^{H_{xc}}[G](r, r', \omega)$$

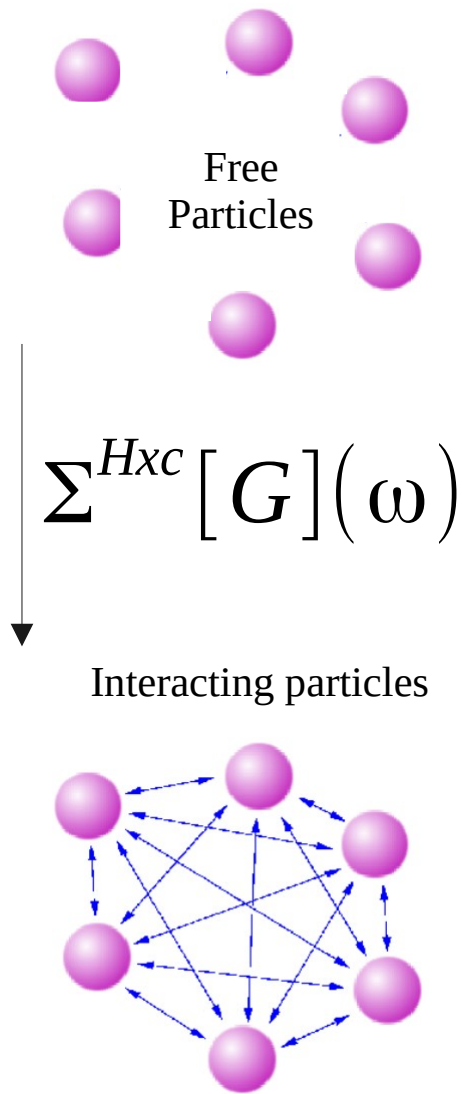
$$G^0(r, r', \omega) = \sum_{nk} \frac{\psi_{nk}^*(r) \psi_{nk}(r')}{\omega - \epsilon_{nk}^0 + i\eta \theta(k - k_F)}$$

The QP concept



$$G(\omega) = G^0(\omega) + G^0(\omega) \Sigma^{Hxc}[G](\omega) G(\omega)$$

The QP concept



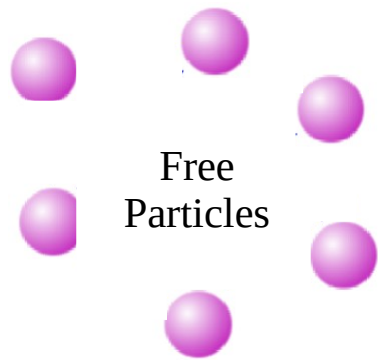
$$G^0(r, r', \omega) = \sum_{nk} \frac{\psi_{nk}^*(r) \psi_{nk}(r')}{\omega - \epsilon_{nk}^0 + i\eta \theta(k - k_F)}$$

$$G(\omega) = G^0(\omega) + G^0(\omega) \Sigma^{Hxc} [G](\omega) G(\omega)$$

#poles of $G \gg$ #poles of G^0

$$G(r, r', \omega) = \sum_{\lambda} \frac{[f_{\lambda}^{N-1}(r)]^* f_{\lambda}^{N-1}(r')}{\omega - \epsilon_{\lambda}^{N-1} - i\eta} + \frac{f_{\lambda}^{N+1}(r) [f_{\lambda}^{N+1}(r')]^*}{\omega - \epsilon_{\lambda}^{N+1} + i\eta}$$

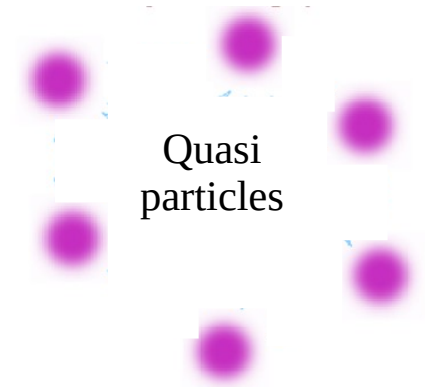
The QP concept



$$\Sigma^{Hxc} [G](\epsilon^{qp})$$

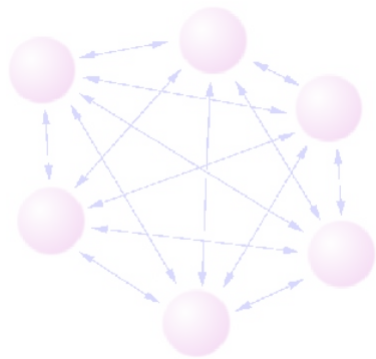
$$G^{QP} = G^0 + G^0 \Sigma^{Hxc}(\epsilon_{QP}) G^{QP}$$

$$\# \text{poles of } G^{QP} = \# \text{poles of } G^0$$



$$\Sigma^{Hxc} [G](\omega)$$

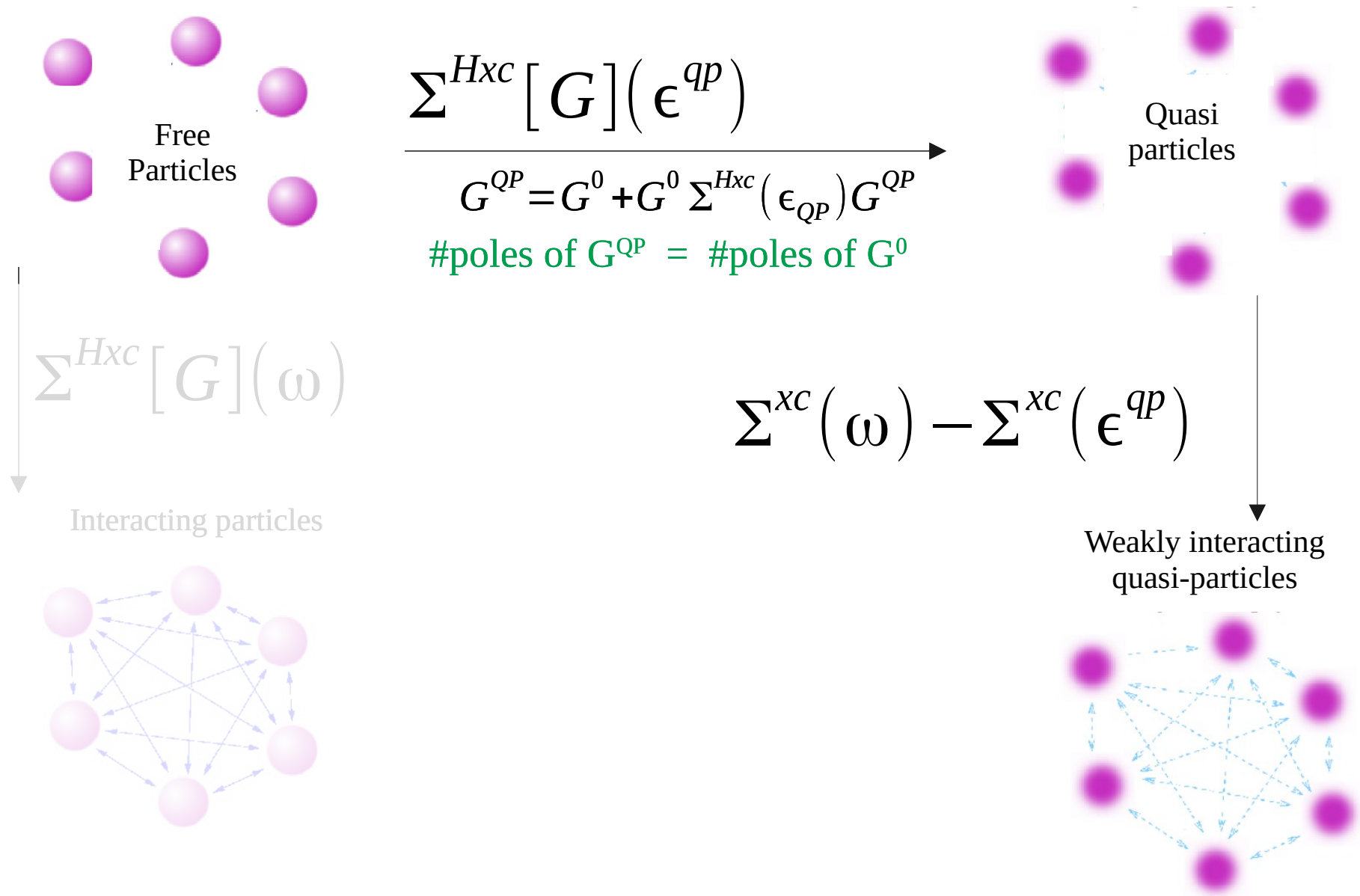
Interacting particles



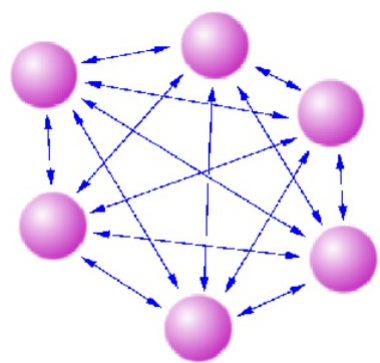
NB: this is trivial only for static self-energies
For dynamical self-energies evaluated at the QP energy
we assume that well defined quasi-particle poles exist
[no strongly correlated materials]

$$G^{QP}(r, r', \omega) = \sum_{nk} \frac{[f_{nk}^{QP}(r)]^* f_{nk}^{QP}(r')}{\omega - \epsilon_{nk}^{QP} + i\eta\theta(k - k_F)}$$

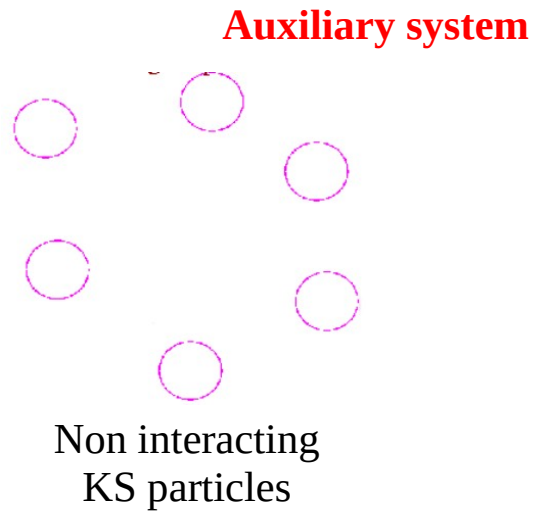
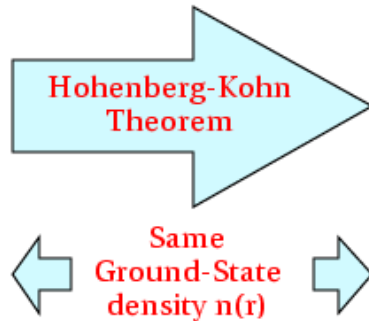
The QP concept



DFT vs MBPT

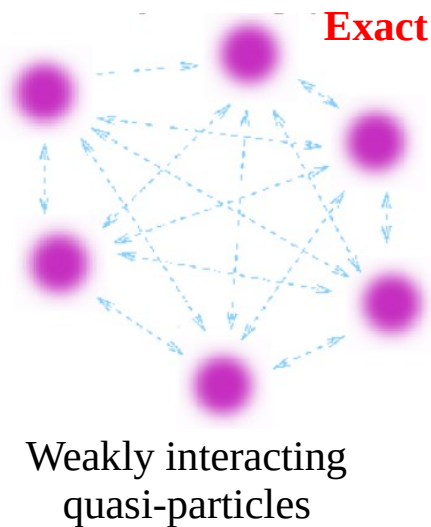
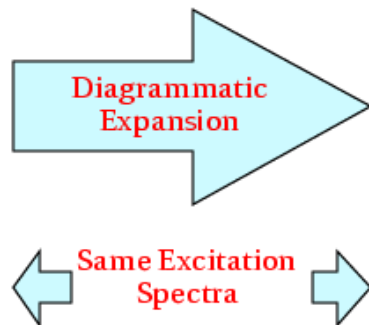
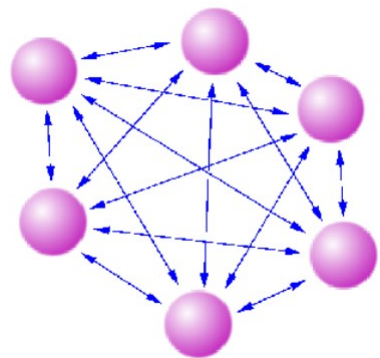


Strongly interacting particles



DFT

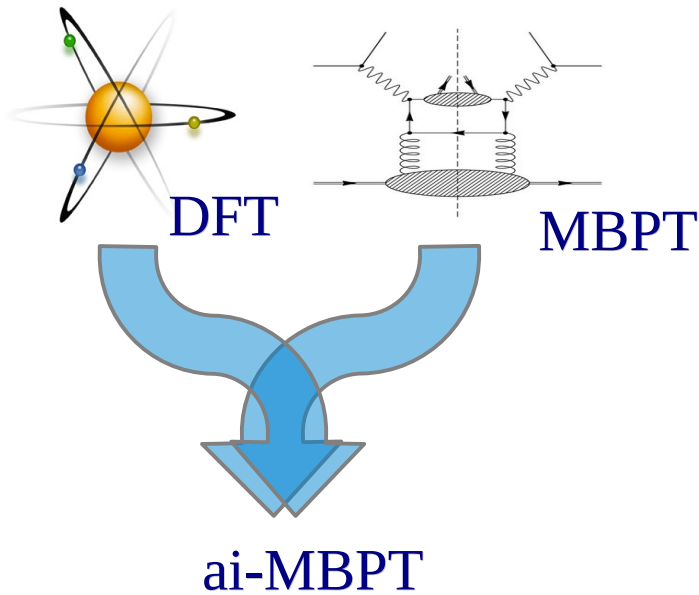
$$v^{xc}[\rho](r)$$



MBPT

$$\Sigma^{xc}[G](r, r', \omega)$$

DFT + MBPT



G. Onida, L. Reining, and A. Rubio,
Rev. Mod. Phys. 74, 601 (2002)

DFT

$$\left[\frac{-\nabla^2}{2} + v^{ext} + v^{Hxc} \right] \psi_{nk}(r) = \epsilon_{nk} \psi_{nk}(r)$$

MBPT

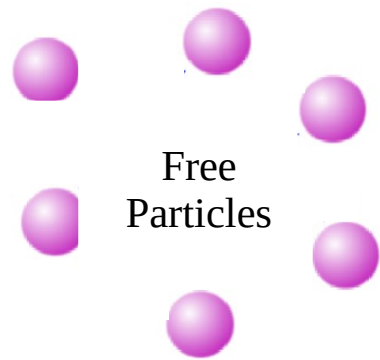
$$G^{KS}(r, r', \omega) = \sum_{nk} \frac{\psi_{nk}^*(r) \psi_{nk}(r')}{\omega - \epsilon_{nk}^{KS} + i\eta}$$

$$G = G^{KS} + G^{KS} (\Sigma^{xc} - v^{xc}) G$$

$$\textcircled{\Sigma} = \text{diagram 1} + \text{diagram 2}$$

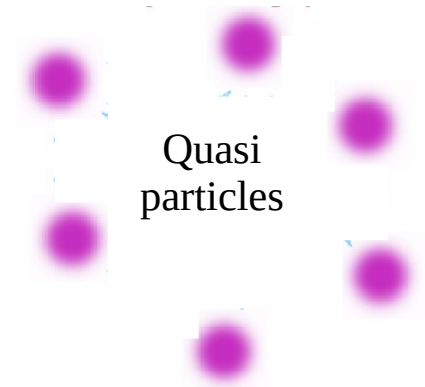
The diagram shows the self-energy Σ as a sum of two terms. The first term is a diagram with a wavy line (representing an exchange interaction) and a solid line (representing a correlation interaction). The second term is a diagram with two wavy lines (representing exchange interactions) and a solid line (representing a correlation interaction).

MBPT



Free
Particles

$$\Sigma^{xc}[G](\epsilon^{qp})$$

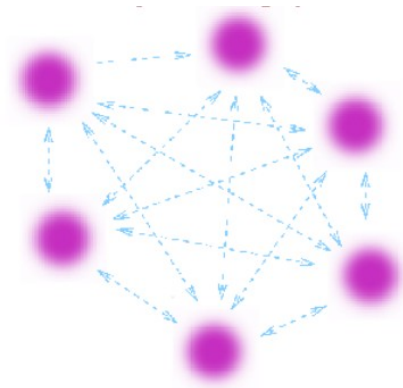


Quasi
particles

$$\Sigma^{xc}(\omega) - \Sigma^{xc}(\epsilon^{qp})$$

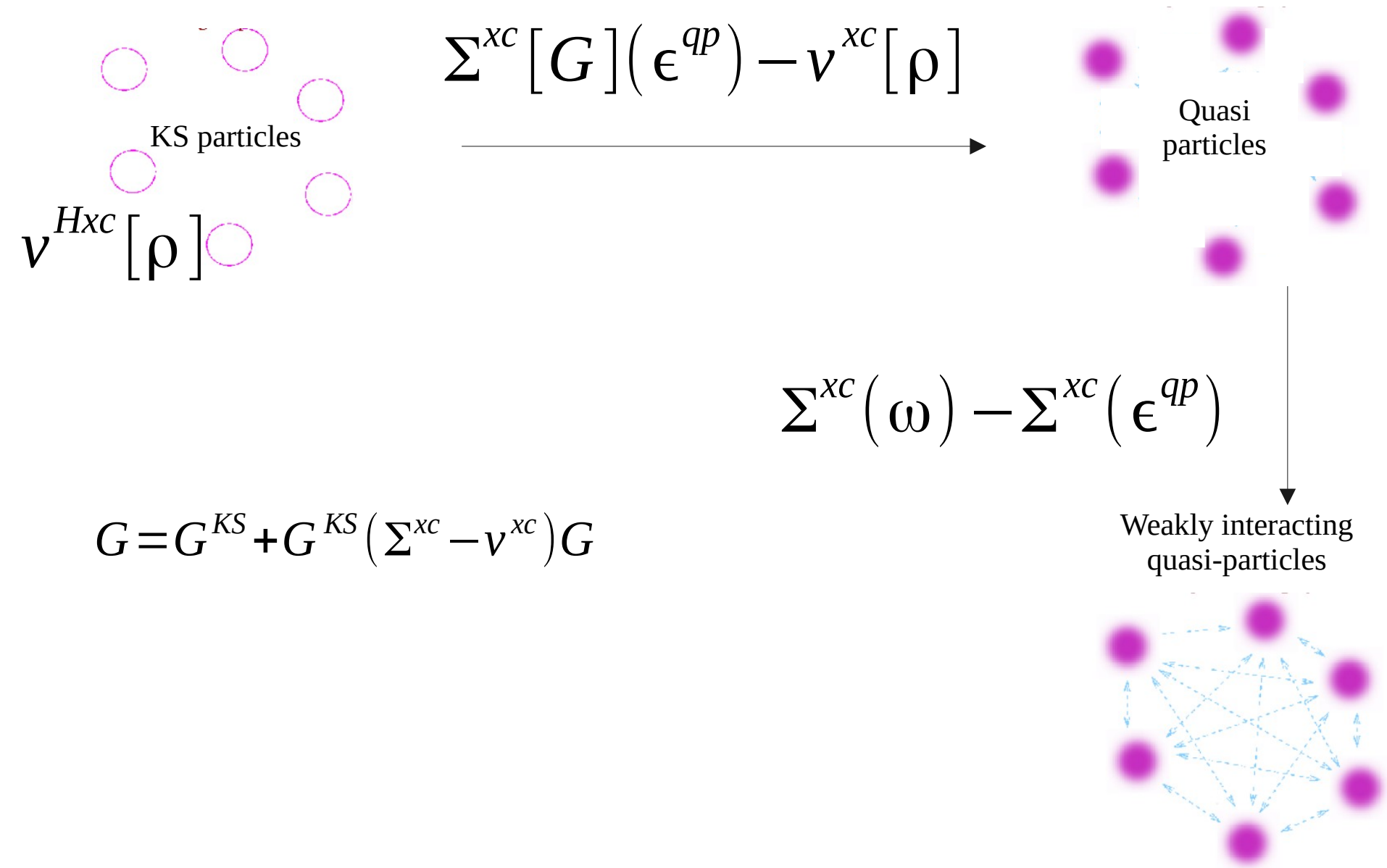


Weakly interacting
quasi-particles



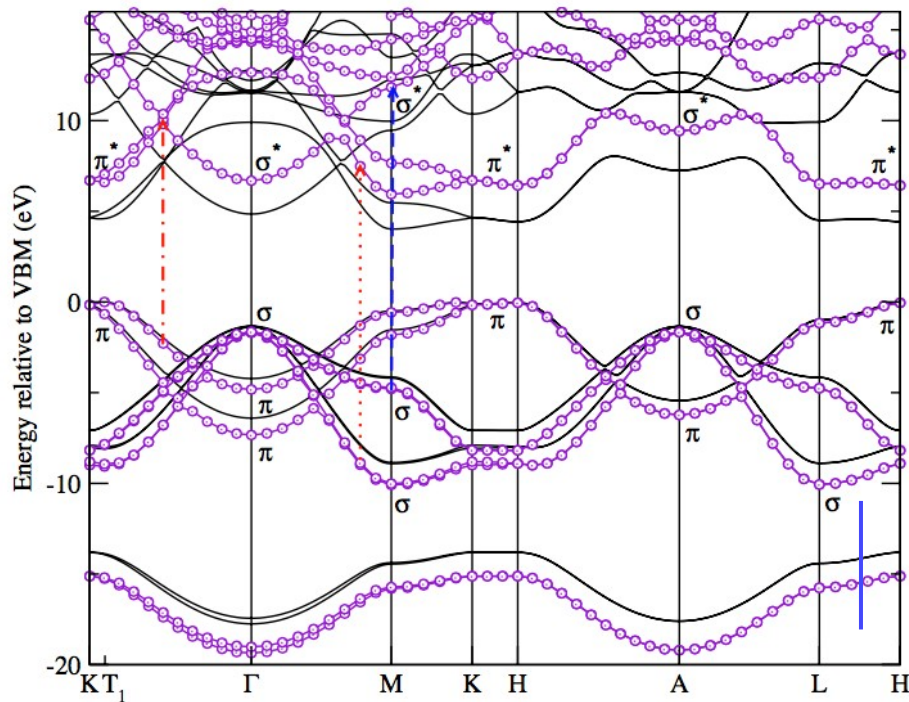
$$G = G^0 + G^0 \Sigma^{Hxc} G$$

abinitio MBPT



DFT and MBPT bands

DFT vs **MBPT** band structure in hBN



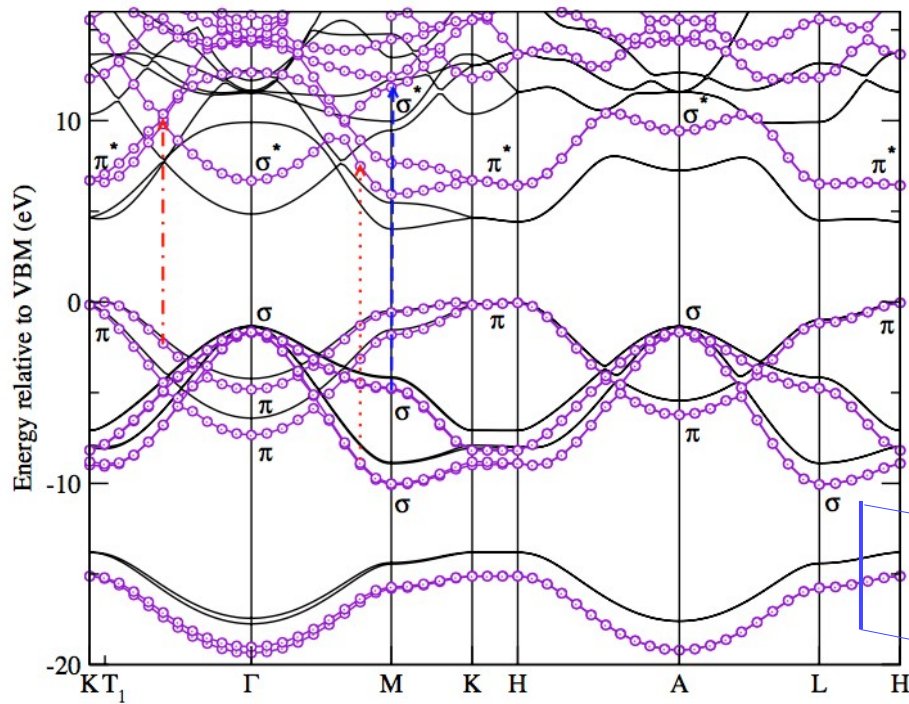
B. Arnaud, S. Lebègue, P. Rabiller, and M. Alouani,
Phys. Rev. Lett. **96**, 026402 (2006)

$$\Sigma^{xc}[G](\epsilon^{qp}) - v^{xc}[\rho]$$

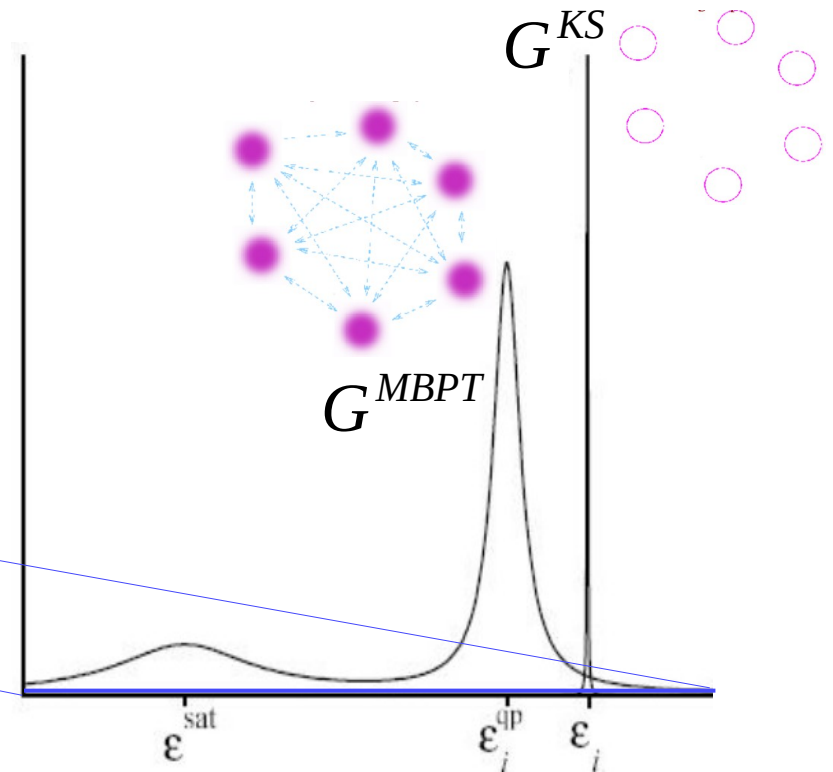
DFT and MBPT bands

$$\Im[G(k, \omega)]$$

DFT vs **MBPT** band structure in hBN



Angle resolved photoemission spectral function



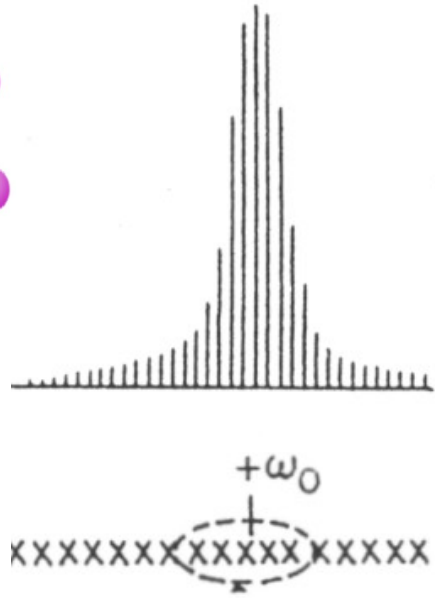
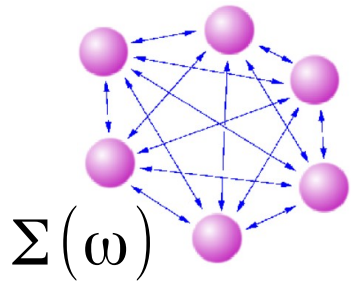
B. Arnaud, S. Lebègue, P. Rabiller, and M. Alouani,
Phys. Rev. Lett. **96**, 026402 (2006)

$$\Sigma^{xc}[G](\epsilon^{qp}) - v^{xc}[\rho]$$

$$\Sigma^{xc}(\omega) - \Sigma^{xc}(\epsilon^{qp})$$

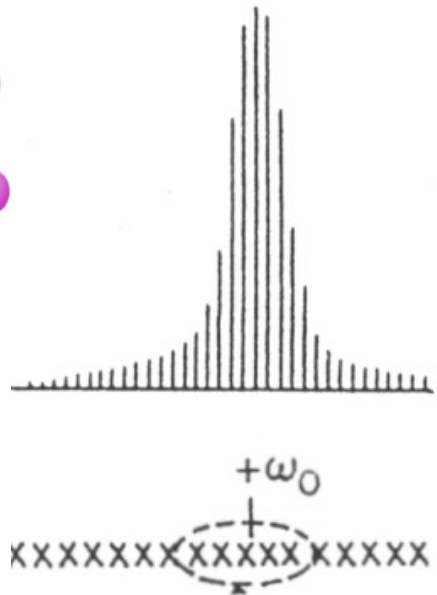
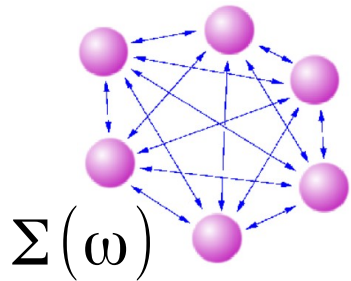
QP complex energies

$$\Im[G(k, \omega)]$$



QP complex energies

$$\Im[G(k, \omega)]$$

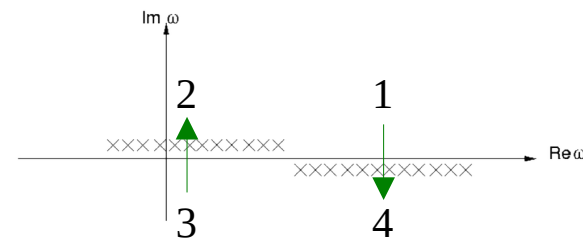


Analitic continuation $\Sigma(z)$

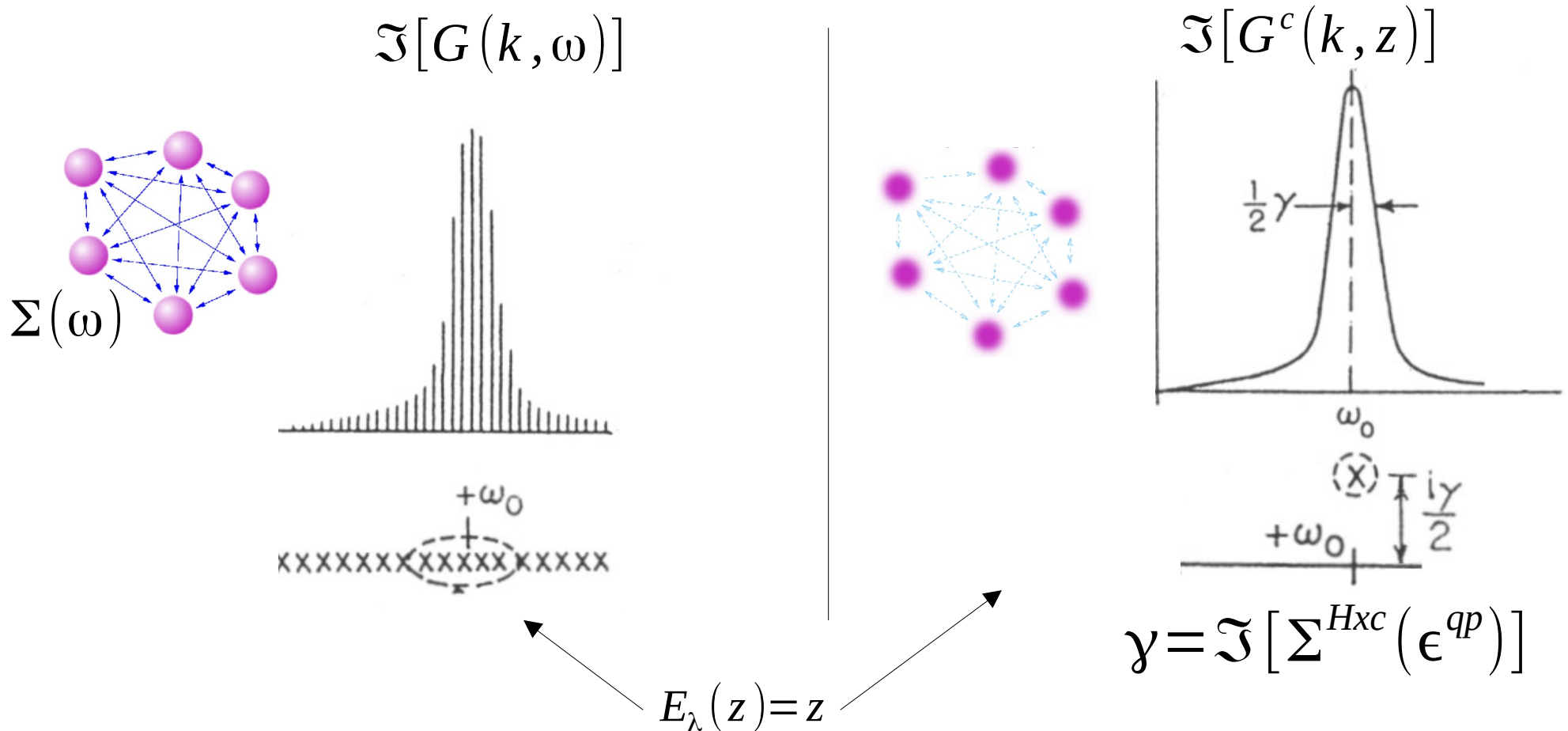
$$[h_0 + \Sigma(z)] \psi_\lambda^r(z) = E_\lambda(z) \psi_\lambda^r(z)$$

$$\begin{cases} G^<(r, r', z) = \sum_\lambda \frac{\psi_\lambda^l(r, z) \psi_\lambda^r(r', z)}{z - E_\lambda(z)} \\ E_\lambda(z) = z \end{cases}$$

Multivalued functions



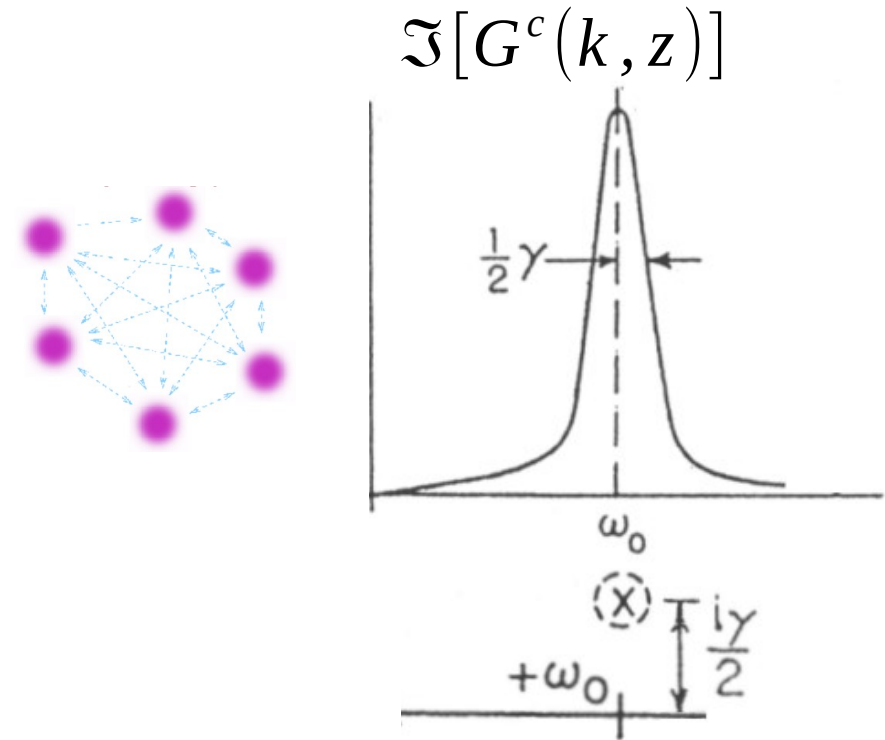
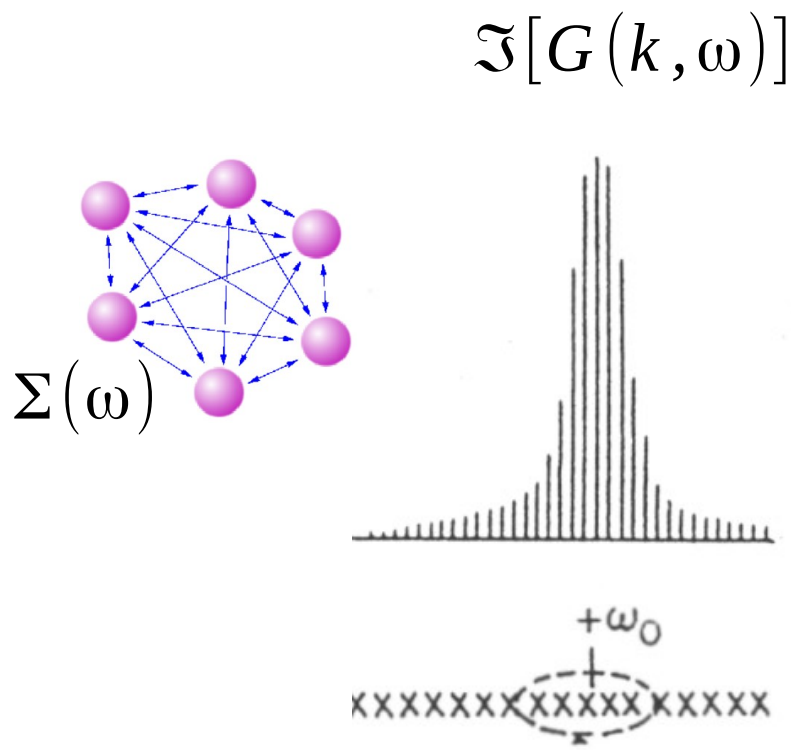
QP complex energies



G. Onida, L. Reining, Lucia, A. Rubio, Rev. Mod. Phys. **74**, 601 (2002)
 B. Farid, Phyl. Mag. B **79**, 1097 (1999) [arXiv 0004476 (2000)]
 B. Farid, Phyl. Mag. B **82**, 1413 (2002) [arXiv 0110481 (2002)]

Images Adapted from
 M. Gatti PhD thesis

QP complex energies



Example

$$G(\omega) = \sum_s \frac{R(s)}{\omega - s}$$

$$R(s) = \frac{1}{\pi} \frac{E_2}{(s - E_1)^2 + E_2^2}$$

$$G(z) = \frac{1}{z - (E_1 + iE_2)} \quad \Im(z) \neq 0$$

G. Onida, L. Reining, Lucia, A. Rubio, Rev. Mod. Phys. **74**, 601 (2002)

B. Farid, Phyl. Mag. B **79**, 1097 (1999) [arXiv 0004476 (2000)]

B. Farid, Phyl. Mag. B **82**, 1413 (2002) [arXiv 0110481 (2002)]

Images Adapted from
M. Gatti PhD thesis

The role of screening

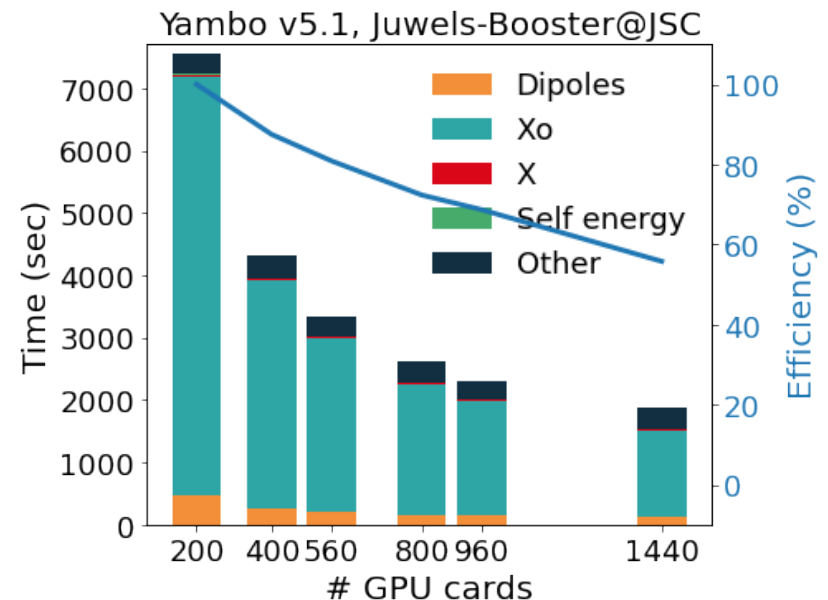
$$\Sigma^{xc}[G] = G \mathbf{W} \Gamma$$

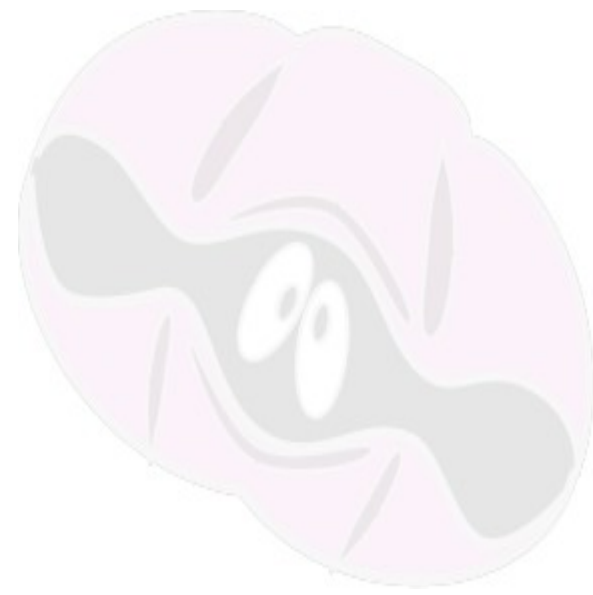
Screened
electron-hole interaction

$$\mathbf{W}^{RPA} = v + v \chi^{RPA} v$$

$$\chi_{GG'}^{RPA}(q, \omega)$$

$$\chi^{RPA} = \chi_0 + \chi_0 v \chi^{RPA}$$





Part III

Excitons:

The Bethe-Salpeter equation

Neutral excitations

1) Time ordered response function

$$L(1,2;3,4) = \langle \phi_0^N | T [\hat{\psi}(1) \hat{\psi}^+(2) \hat{\psi}(3) \hat{\psi}^+(4)] | \phi_0^N \rangle \quad 1 = (x, t)$$

Neutral excitations

1) Time ordered response function

$$L(1,2;3,4) = \langle \phi_0^N | T [\hat{\psi}(1) \hat{\psi}^\dagger(2) \hat{\psi}(3) \hat{\psi}^\dagger(4)] | \phi_0^N \rangle \quad 1 = (x, t)$$

2) Lehmann Representation

$$L(\omega) = \sum_{\lambda} \frac{[F_{\lambda}^N]^* F_{\lambda}^N}{\omega - (E_{\lambda}^N - E_0^N) + i\eta} - \frac{[F_{\lambda}^N]^* F_{\lambda}^N}{\omega + (E_{\lambda}^N - E_0^N) - i\eta} \quad (t_1 = t_2; t_3 = t_4)$$

Neutral excitations

1) Time ordered response function

$$L(1,2;3,4) = \langle \phi_0^N | T [\hat{\psi}(1) \hat{\psi}^+(2) \hat{\psi}(3) \hat{\psi}^+(4)] | \phi_0^N \rangle \quad 1 = (x, t)$$

2) Lehmann Representation

$$L(\omega) = \sum_{\lambda} \frac{[F_{\lambda}^N]^* F_{\lambda}^N}{\omega - (E_{\lambda}^N - E_0^N) + i\eta} - \frac{[F_{\lambda}^N]^* F_{\lambda}^N}{\omega + (E_{\lambda}^N - E_0^N) - i\eta} \quad (t_1 = t_2; t_3 = t_4)$$

3) Dyson like equation

$$L(\omega; \omega_1, \omega_2) = L^0(\omega; \omega_1, \omega_2) + L^0(\omega; \omega_1, \tilde{\omega}_1) K(\omega; \tilde{\omega}_1, \tilde{\omega}_2) L(\omega; \tilde{\omega}_2, \omega_2)$$

$$K^{Hxc}[G](1,2;3,4) = \frac{\delta \Sigma(1,2)}{\delta G(3,4)}$$

Bethe-Salpeter Equation

$$L^s = L^{qp} + L^{qp} K^{Hxc}(\omega=0) L^s$$

$$K^{Hxc}(\omega=0) = (v - W)$$

can be rewritten as an eigenvalue problem

$$\left[(\epsilon_{ck} - \epsilon_{vk-q}) + v_{cvk, c'v'k'} - W_{cvk, c'v'k'} \right] A_{c'v'k'}^{\lambda q} = \omega_{\lambda q} A_{cvk}^{\lambda q}$$

Bethe-Salpeter Equation

$$L^s = L^{qp} + L^{qp} K^{Hxc}(\omega=0) L^s$$

$$K^{Hxc}(\omega=0) = (v - W)$$

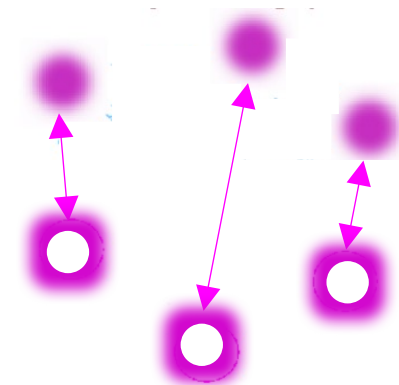
can be rewritten as an eigenvalue problem

$$\left[(\epsilon_{ck} - \epsilon_{vk-q}) + v_{cvk, c'v'k'} - W_{cvk, c'v'k'} \right] A_{c'v'k'}^{\lambda q} = \omega_{\lambda q} A_{cvk}^{\lambda q}$$

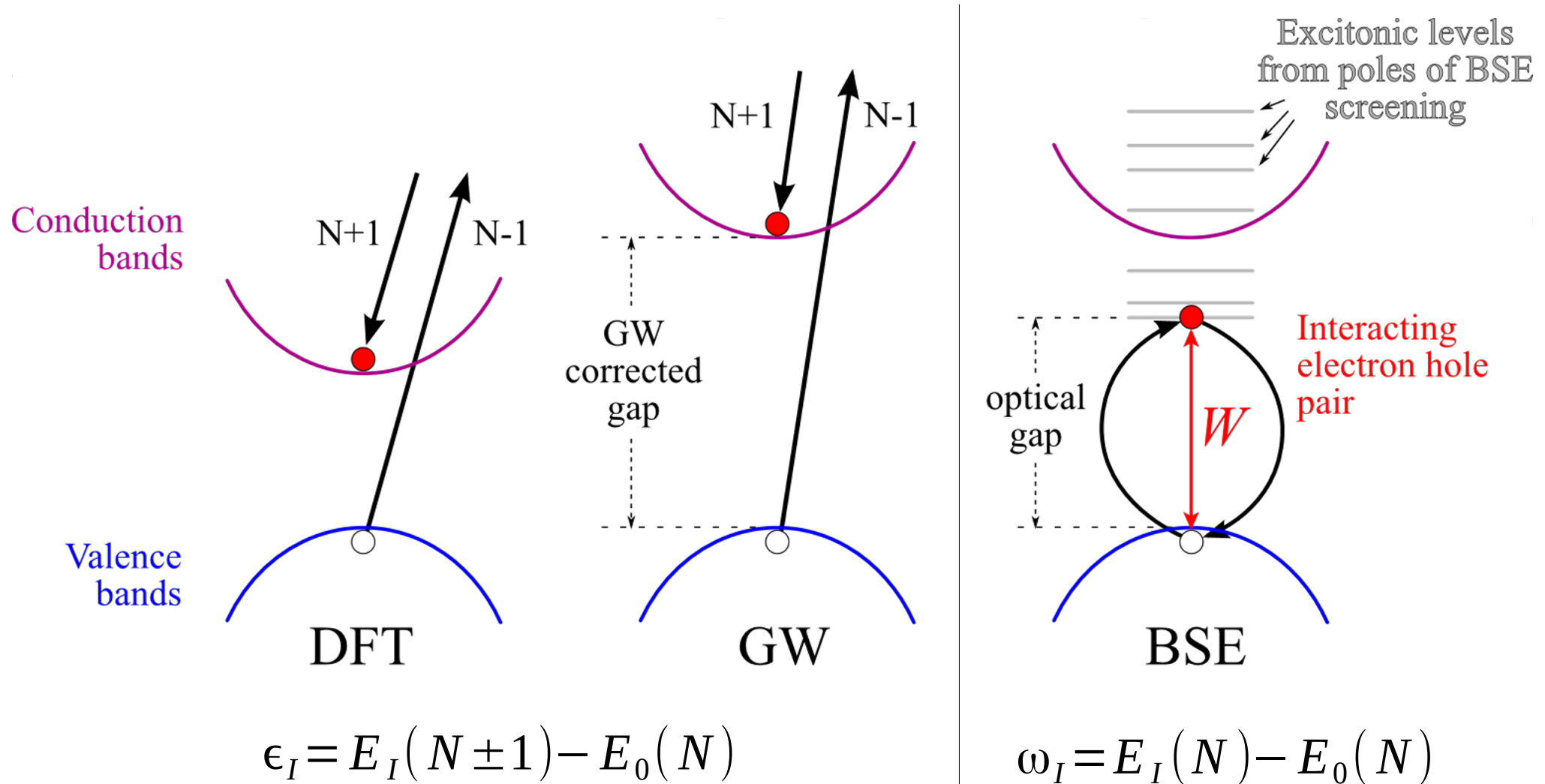
Excitation wave-function

$$\Psi^{\lambda q}(x_h, x_e) = \sum_{cvk} A_{cvk}^{\lambda q} \psi_{ck-q}^*(x_e) \psi_{vk}(x_h)$$

Strongly interacting
(quasi)electron – (quasi)hole



abinitio GW+BSE

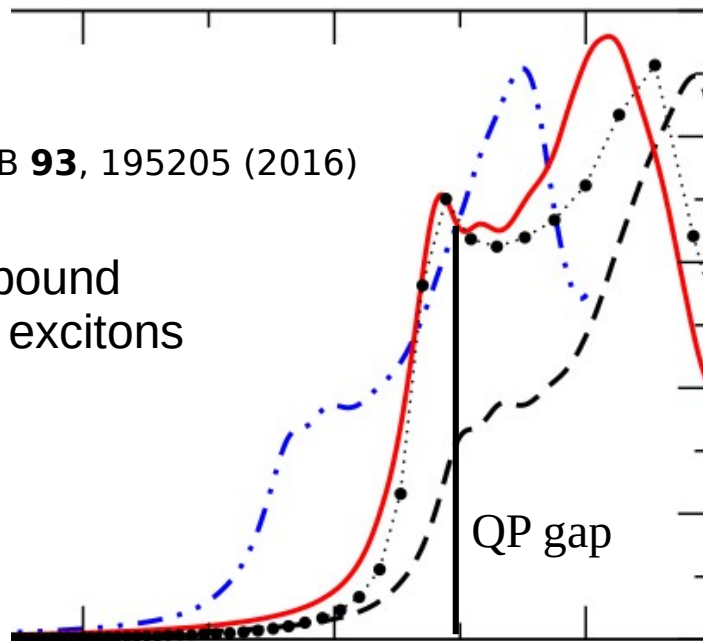


From Wannier to Frenkel excitons

bulk Si

Phys. Rev. B **93**, 195205 (2016)

Weakly bound
Wannier excitons



(b)

QP gap

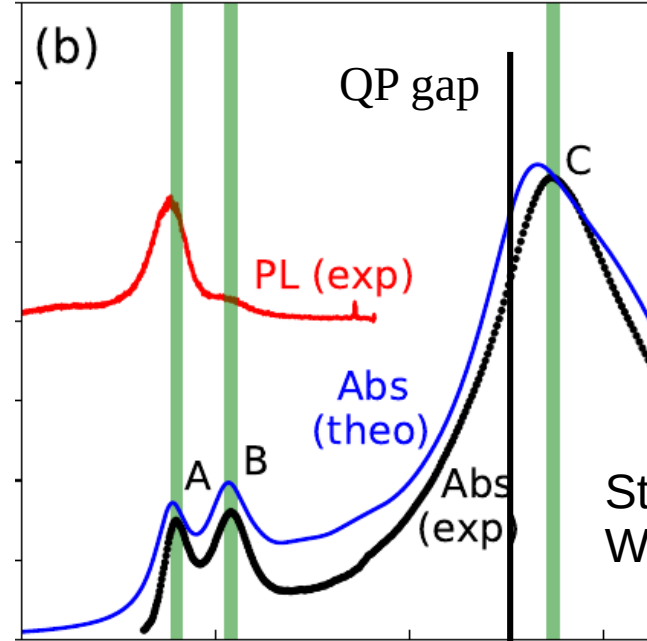
2D MoS2
ACS Nano **14**,
5700 (2020)

PL (exp)

Abs
(theo)

Abs
(exp)

Strongly bound
Wannier excitons



bulk LiF

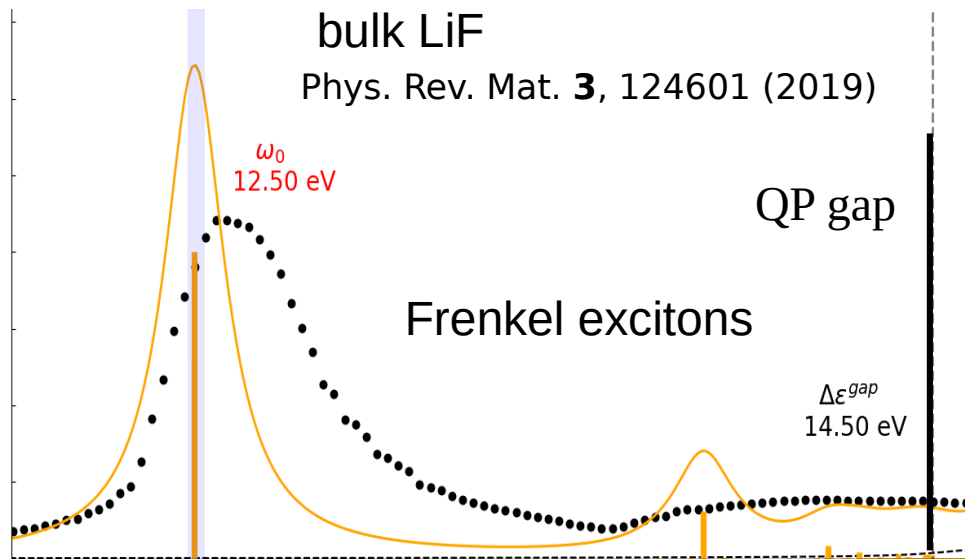
Phys. Rev. Mat. **3**, 124601 (2019)

ω_0
12.50 eV

QP gap

Frenkel excitons

$\Delta\epsilon^{gap}$
14.50 eV

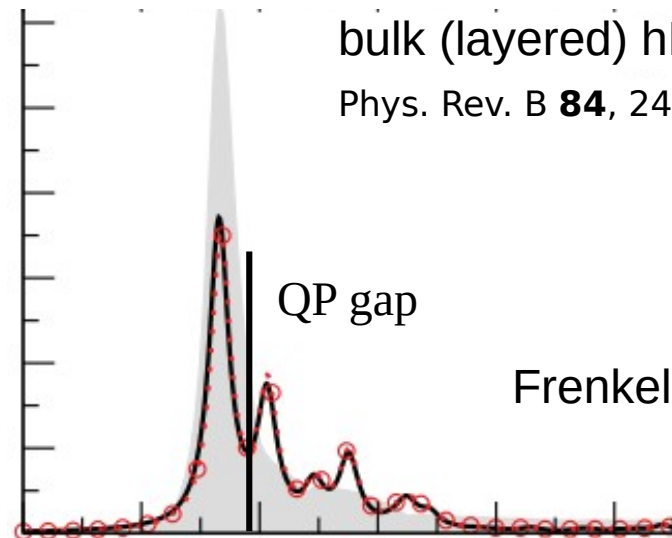


bulk (layered) hBN

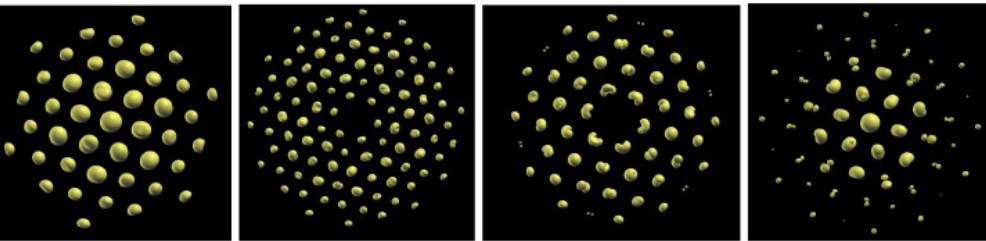
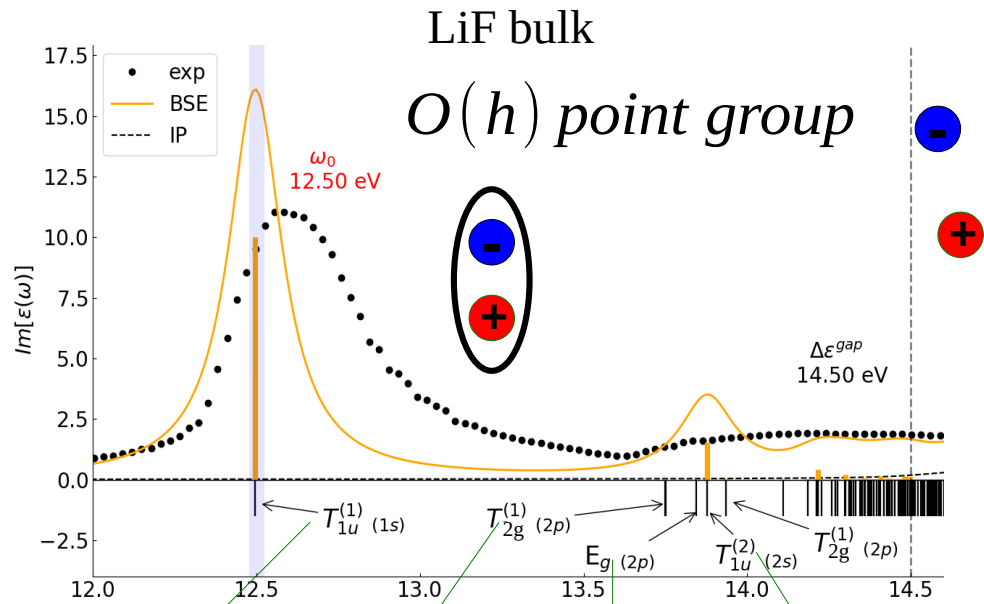
Phys. Rev. B **84**, 245110 (2011)

QP gap

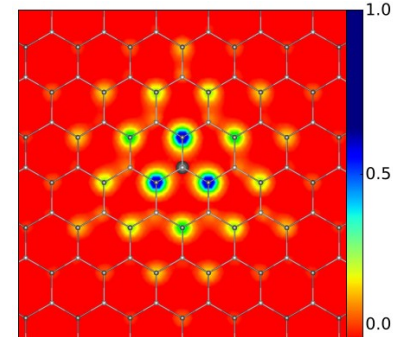
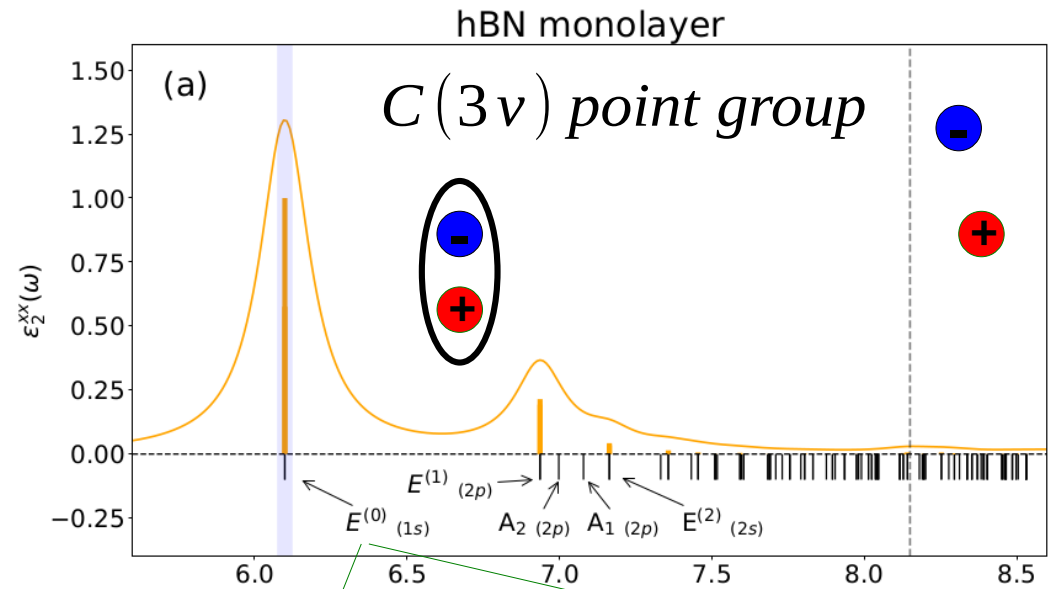
Frenkel excitons



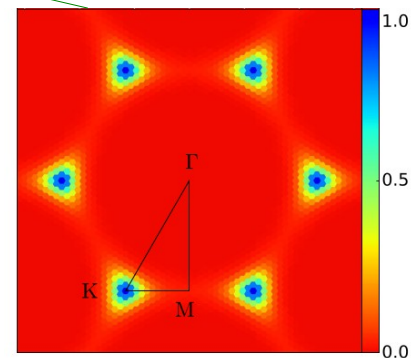
Exciton wave-functions



$$|\Psi^{\lambda q=0}(x_h^0, x)|^2$$



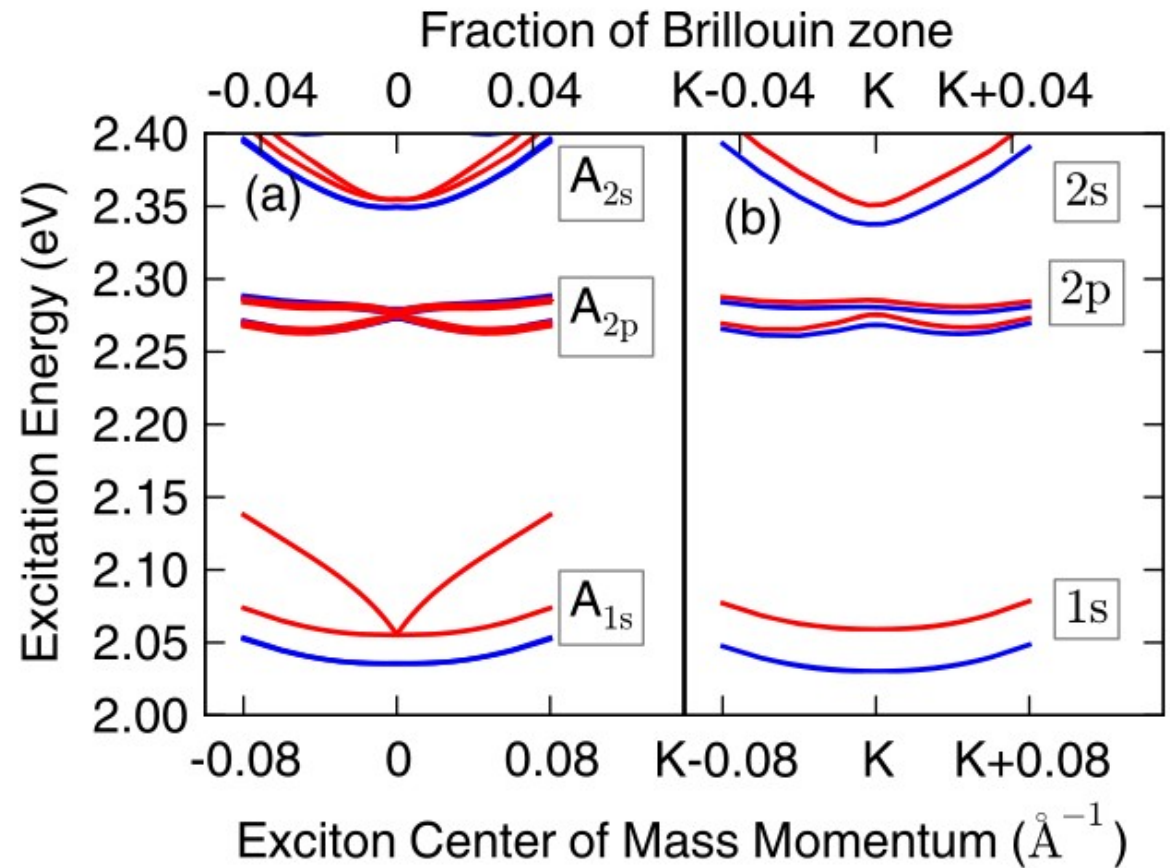
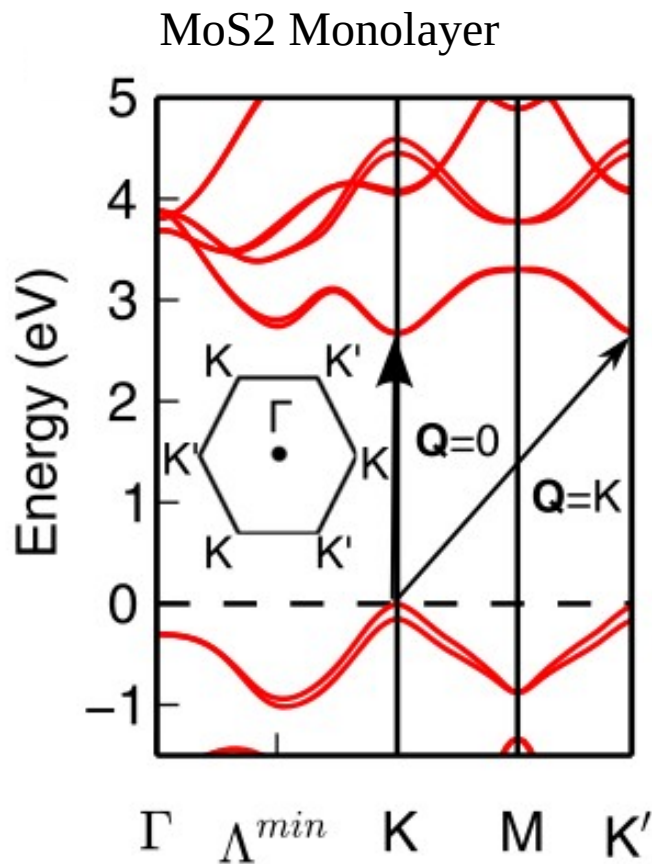
$$|\Psi^{\lambda q=0}(x_h^0, x)|^2$$



$$|\Psi^{\lambda q=0}(k)|^2$$

Exciton dispersion

$$\left[\left(\epsilon_{ck} - \epsilon_{vk-q} \right) + v_{cvk, c'v'k'} - W_{cvk, c'v'k'} \right] A_{c'v'k'}^{\lambda q} = \omega_{\lambda q} A_{cvk}^{\lambda q}$$



ACTIVE DEVELOPERS (alphabetic order)

- * Claudio Attaccalite
- * Miki Bonacci
- * Elena Cannuccia
- * Andrea Ferretti
- * Myrta Gruening
- * Alberto Guandalini
- * Conor Hogan
- * Dario Alejandro Leon-Valido
- * Andrea Marini
- * Alejandro Molina-Sánchez
- * Fulvio Paleari
- * Maurizia Palumbo
- * Davide Sangalli
- * Nicola Spallanzani
- * Daniele Varsano

FORMER DEVELOPERS

- * Ignacio Martin Alliati
- * Fabio Affinito
- * David Kammerlader
- * Ivan Marri
- * Antimo Marrazzo
- * Margherita Marsili
- * Pedro Melo
- * Henrique Miranda
- * Ryan McMillan



Thank you for your attention



the Yambo team

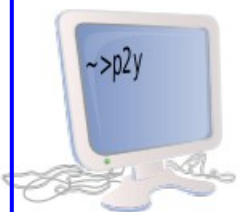
1. Many-body perturbation theory calculations using the yambo code
Journal of Physics: Condensed Matter 31, 325902 (2019)
2. Yambo: an ab initio tool for excited state calculations
Comp. Phys. Comm. 144, 180 (2009)

More slides

1. Many-body perturbation theory calculations using the yambo code
Journal of Physics: Condensed Matter 31, 325902 (2019)
2. Yambo: an ab initio tool for excited state calculations
Comp. Phys. Comm. 144, 180 (2009)

How the code works

1. Generate the core databases



2. Run setup

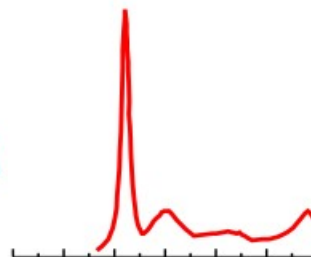


Import databases
from a previous
DFT simulation

3. Generate input

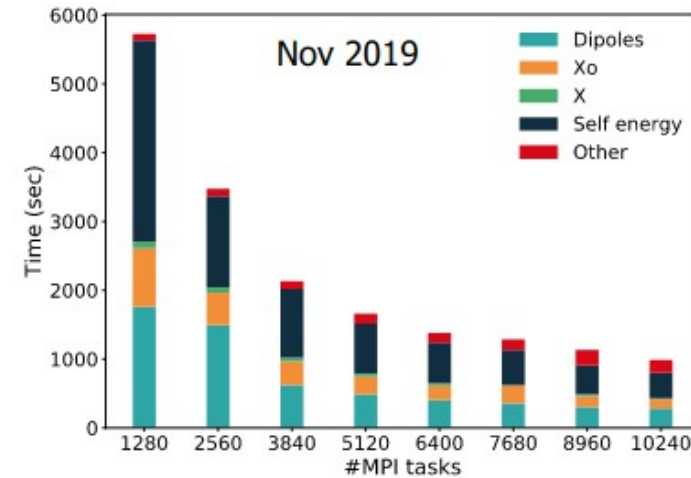
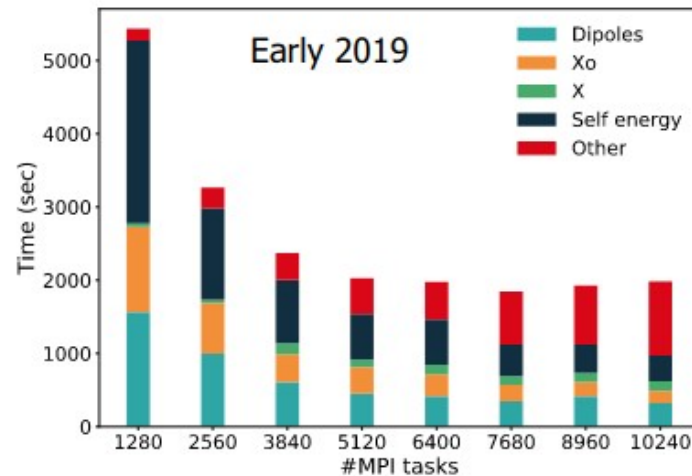


4. Run Yambo

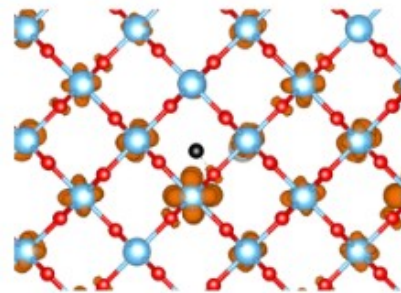


Yambo parallel performance

heterogeneous architectures: **MPI** + OpenMP + CUDA



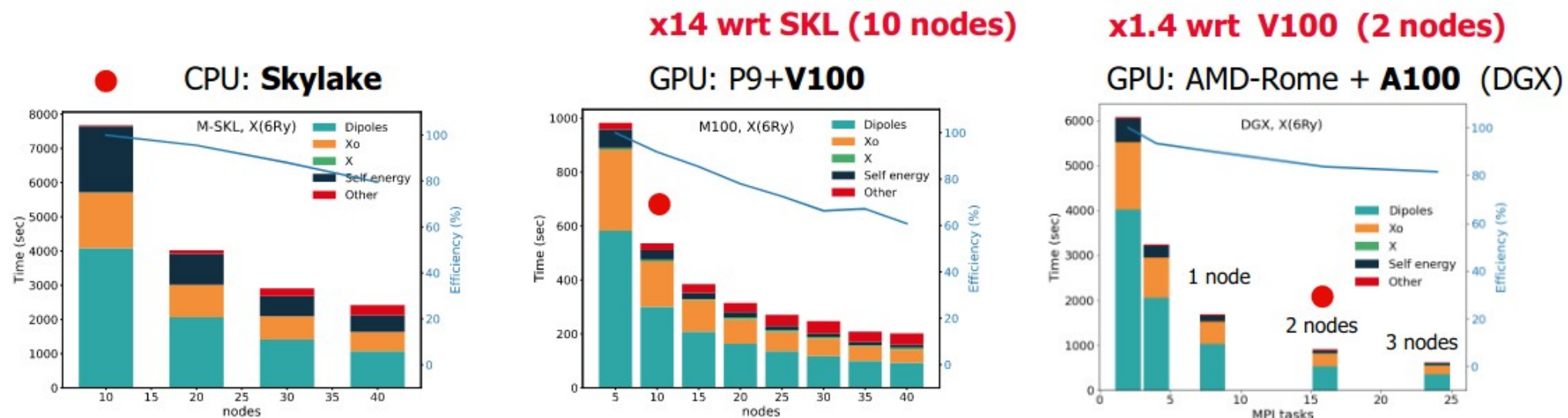
- **optimisation of MPI+OpenMP** parallelism
- working at scale (bottleneck identification and solution)



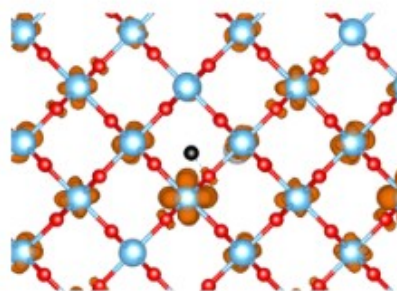
system size: 72+1 atoms, 2000 bands, 6 Ry for Xo repr (N=1317); ~290 occ states, 8 kpts.

data available at: <http://www.gitlab.com/max-centre/Benchmarks>

heterogeneous architectures: **MPI + OpenMP + CUDA**



- complete **GW workflow** for defected TiO₂ (rutile)
- small system, **stress test**
- 1 MPI task/GPU
- data obtained on Marconi100, 4 V100 GPUs/node
- and DGX arch, 8 A100 GPUs/node



system size: 72+1 atoms, 2000 bands,
6 Ry for Xo repr (N=1317); ~290 occ
states, 8 kpts.

data available at: <http://www.gitlab.com/max-centre/Benchmarks>