

# Project 6: Arithmetic Logic Unit

E210/B441

Version 2022.0

**Demo Due: 4.30pm, Friday March 11th**

## Overview

You will design and implement an 8-bit **Arithmetic Logic Unit (ALU)**. You can use the same design procedure to expand to a functionally complete 16-, or 32-bit ALU. You will also get to implement a basic **D Flip-Flop**. Flip Flops are used to add state to your digital systems.

## Background

### Arrays

For the last project, we expressed the `d` outputs of the decoder separately:

```
module decoder(  
    input a, b, c,  
    output d0, d1, d2, d3, d4, d5, d6, d7  
);
```

However, it is also possible to combine them into a single array of wires:

```
module decoder(  
    input a, b, c,  
    output [7:0] d  
);
```

Note that the array definition is of the form:

```
type [mostSignificantIndex:leastSignificantIndex] name;
```

Thus, the big index goes on the left, and the smaller index (typically 0) on the right. *It is possible to create arrays differing from this convention, but we do not recommend it.*

Individual wires can be accessed with the standard array syntax “[]” that you’ve seen from C or Python:

```
assign d[1] = ~a && ~b && c;
wire wire1 = d[0] ^ d[1];
```

You can also access groups of bits from within an array using the semicolon similar to Python. For example, this will access bits 5,4, and 3 from d and assign them to bits 2,1, and 0 of other\_wire2.

```
wire [2:0] wire2 = d[5:3];
```

A few other useful array operations are concatenation and static assignment. Concatenation lets you join multiple signals together to create an array using curly-brackets. The following example joins three wires (a, b, and c) to make a 3-wire array wire3.

```
wire [2:0] wire3 = { a, b, c }; //concatenation
```

Static assignment lets you fix a wire to a given logical value, for example 1. The “’h” prefix is Verilog’s method of specifying hexadecimal. Recall that C uses the “0x” prefix. You can also use ’b to specify a binary number.

```
wire wire4 = 'h0; // static assignment
wire [2:0] wire5 = 'b010; //also static assignment
wire [2:0] wire6 = { 'b0, 'b1, 'b0 } ; //static + concatenation
```

Sometimes it’s helpful to specify the number of bits for a number. You can do this by placing the number of bits for a number ahead of the ’h. In the following example, we specify that the first number is two bits wide, and the second number is only 1 bit wide.

```
wire [2:0] wire6 = { 2'b1, 1'b0 } ; // binary 01 & 1
```

## Case Statements

Another piece of new Verilog for this lab is the case statement. Just like C, verilog lets you use case statements. The syntax looks something like this:

```
case(sel)

    2'b00: out = input[0]; //set out = input[0] when sel = 00
    2'b01: out = input[1]; //set out = input[1] when sel = 01
    2'b10: out = input[2];
```

```
    2'b11: out = input[3];  
    default: out = input[0]; //you usually want a default case  
  
endcase
```

## Combinational Always Blocks

Unfortunately, you cannot use `case` statements with `assign`, it must be inside a special block called `always_comb`. The `comb` is short for combinational. `always_comb` blocks look like this:

```
always_comb  
begin  
    out = input[2];  
end
```

`always_comb` blocks run all of the commands between `begin/end` every time something on the right-hand side of any contained equation changes. In the above block, the right-hand-side is shown in bold. That means whenever anything changes, Verilog will re-evaluate *all* the block's assignments. The above block is functionally equivalent to `assign out = input[2];`

As Verilog is an odd language, and you cannot assign a value to a 'wire' inside an `always` block. Therefore we declare `out` as a 'logic' type. There are subtle differences between wire and logic, but for now just remember that everything inside an `always` block must be declared 'logic'.

If we put the `always` block and the `case` statement together, we get something that looks like this:

```
logic out; //must be logic (or reg) for always blocks  
  
always_comb  
begin  
    out = 1'h0; //default  
    case(sel)  
  
        2'b00: out = input[0];  
        2'b01: out = input[1];  
        2'b10: out = input[2];  
    endcase  
end
```

```
        2'b11: out = input[3];
    endcase
end
```

This lets us set `out` to one of 4 values based on the value of `sel` (or `select`). This is one way to build a 4-1 multiplexer.

## Flip-Flop Always Blocks

One final piece is how to build D Flip Flops in Verilog. Here again we make use of an `always` block, but this one looks a little different.

```
wire clk, D; //input signals
logic Q, Qbar; //must be logic (or reg) for always blocks

//D Flip Flop
always_ff @(posedge clk)
begin
    Q    <= D;
    Qbar <= ~D; //optional
end
```

Notice this `always` block is an `always_ff`, “ff” is short for “flip-flop”. It also includes `@(posedge clk)` or “at the positive edge of clock”. This means only the positive (rising) edge of `clk` will cause signals inside the `always` block to change. A positive edge is when a signal which was 0 (a low voltage) rises to 1 (a high voltage). Thus, there is a “positive” or “rising” edge in the waveform. Unless `clk` is rising (going from 0 to 1), none of the outputs will change. This is what makes this block into a flip flop. As `Q` and `Qbar` can hold state, they must be declared as `logic` or the older `reg`. Also, notice the use of the **non-blocking assignment** (`<=`). We’ll discuss this more in class, but the rule is:

**`always_comb` is for combinational logic and  
ONLY USES BLOCKING ASSIGNMENTS (`=`)**

**`always_ff @(posedge ...)` is for sequential logic and  
ONLY USES NON-BLOCKING ASSIGNMENTS (`<=`)**

# ***DEBUGGING PAIN WILL RESULT IF YOU BREAK THE ABOVE RULE!!!***

Verilog being an odd language, the tools will not check for this, and are more than happy to let you do whatever you want. Then you won't understand why your FPGA does not behave as expected. If you get a warning that says "inferring latch", you broke the rule!

There are several other `always` blocks in Verilog. For now, don't use them.

## Flip-Flop Always Blocks with Enable

The previous flip-flop block always updated its state on every rising edge of `clk`. However, often you want to control that slightly, so that it only updates the value when you enable it. For that, we add a little more logic to the `always_ff` block:

```
wire clk, D; //input signals
wire e; //enable input
logic Q, Qbar; //must be logic (or reg) to retain state

//D Flip Flop
always_ff @(posedge clk)
begin
    if (e) begin //only update if enabled
        Q    <= D;
        Qbar <= ~D; //optional
    end
end
```

## ALU

You will build an ALU that takes two inputs, `a` and `b`, and produces three outputs, `r`, `c` and `v`. Additionally, another input `s` will select which type of operation should be performed. Your ALU will be capable of both Arithmetic and Logical operations.

## Arithmetic

Your ALU should be capable of both **addition** and **subtraction**. We'll assume you've seen digital addition before. Subtraction in the digital world can be implemented using addition and 2's complement.

$$r = a - b = a + \bar{b} + 1$$

Thus, by inverting  $b$  and adding 1, we can implement subtraction. Now that we are also doing subtraction, we have chosen to express the result as  $r$  rather than  $s$  for sum.

There are a number of different ways to build adders. **In practice, it is typically easiest to use the built-in Verilog addition operator (+) or subtraction operator (-) and let the tools figure it out.** Unfortunately, Verilog's built-in addition operator, by default, assumes an 8-bit addition results in an 8-bit sum. However, we want the carry-out, so we need a 9-bit sum. **The solution is to prepend a 1-bit 0 to your 8-bit value to form a 9-bit value.** We can use the concatenation operator in Verilog to achieve this.

```
wire [7:0] a = 8'hff;
wire [8:0] a9 = { 1'h0, a }; //concatenation of inputs

wire [7:0] r;
wire r9;
{r9,r} = a9; //concatenation of outputs
```

Notice for  $a9$  we're mashing the `wire` declaration and the `assign`-ment statement together into a single line.

In addition, your ALU should be capable of several other helpful functions:

**Transfer:**  $r = a$   
**Test:**  $r = (a == 0)$

## Logic

Your ALU should also be capable of 4 basic bitwise logic operations, **AND**, **OR**, **NOT**, and **XOR**. These are computed to all bits of  $a$  and  $b$ .

## Operation Encoding

To select which operand your ALU should perform, you will need to read in a 4-bit “operation select” value ( here named  $s$ ). The mapping of  $s$  values to operations is given below.

$s$	Operation	Result
1110	AND	$r = a \& b$
1101	OR	$r = a   b$
1100	NOT	$r = \bar{a}$
1011	XOR	$r = a \oplus b$
1010	Addition	$r = a + b$
1001	Subtraction	$r = a - b$
1000	Transfer	$r = a$
0111	Test	$r = (a == 0)$

## Carry

Recall that 8-bit unsigned addition can result in a 9-bit sum. Therefore, the highest bit should be returned in the  $c$  bit, short for Carry. This bit must be 0 for transfer, test and all logic operations.

## Overflow

Additionally, signed arithmetic can result in overflows. This can occur when adding two positive numbers, and receiving a negative result. Or when adding two negative numbers resulting in a positive number. This overflow condition should be captured in a  $v$  bit, short for oVerflow. This bit must be correct for addition and subtraction and is undefined for all other operations. If a signal is undefined, you can set it to whatever you want.

SP'21: The autograder now sets  $c$  and  $v$  to 0 for all operations other than Addition or Subtraction.

There are two ways to calculate overflow. The one discussed in class is using an XOR gate between the carry-out and the last internal carry bit of the addition/subtraction. For an 8-bit

addition, this would be  $v = c_{out} \oplus c_7$ . Unfortunately, if you use the Verilog subtraction operator,  $-$ , you will not have a  $c_7$ .

The second way is to look at both the inputs and the result. If you construct a truth table for  $a[7]$ ,  $b[7]$ ,  $c[7]$ ,  $c_{out}$  and  $r(result)$ , it will look something like this:

Inputs		ALU			Overflow
$a[7]$	$b[7]$	$c[7]$	$c_{out}$	$r$	$c[7] \wedge c_{out}$
0	0	0	0	0	0
<u>0</u>	<u>0</u>	1	0	<u>1</u>	<u>1</u>
0	1	0	0	1	0
0	1	1	1	0	0
1	0	0	0	1	0
1	0	1	1	0	0
<u>1</u>	<u>1</u>	0	1	<u>0</u>	<u>1</u>
1	1	1	1	1	0

Recall the  $v = c[7] \wedge c_{out}$ . Which means it is true whenever  $c[7]$  and  $c_{out}$  differ. Notice, there are two cases above where  $c[7]$  and  $c_{out}$  differ, highlighted in red above. Those two cases are shown in red above. The first case occurs when  $a[7] == 0$ ,  $b[7] == 0$ , and  $result[7] == 1$ . This occurs when we are adding two positive numbers, and the result is negative. The second case occurs when  $a[7] == 1$ ,  $b[7] == 1$ , and  $result[7] == 0$ . Now we are adding two negative numbers and getting a positive result. We can write a Verilog expression to capture these two cases:

```
wire oVerflowAdd = ~a[7] & ~b[7] & r[7] | a[7] & b[7] & ~r[7];
```

Recall with subtraction that  $A - B = A + \overline{B} + 1$ . Therefore, Verilog will flip the bits of  $b$  to form  $\sim b$ . It will then perform  $\{c_{out}, result[7]\} = a[7] + \sim b[7] + c[7]$ . As part of the project, you will need to compute a similar overflow equation for subtraction:

```
wire oVerflowSubtract = ??? ;
```



Hint: the solution can be found in the textbook.

## Assignment Description

### 8-bit ALU

Create a Verilog file named `alu.sv` which defines a module as follows:

```
module alu(  
    input      [7:0] a, //operand  
    input      [7:0] b, //operand  
  
    input      [3:0] s, //operation Select  
  
    output logic [7:0] r, //the Result value  
    output logic      c, //for unsigned Carry  
    output logic      v  //for signed oVerflow  
);
```

The `logic` keyword is optional and can be omitted.

Your task is to implement the ALU as per the specifications above.

### Top-Level

Please use the following `top.sv`.

```
`timescale 1ns / 1ps  
  
module top(  
    input      CLK100MHZ,  
    input  [15:0] sw, //operands a,b,s  
    input      btnC, //  
    output  [15:0] LED //results c,v  
);  
  
    logic  [7:0] a;  
  
    always @(posedge CLK100MHZ) begin  
        if (btnC)  
            a <= sw[7:0];  
    end
```

```

alu alu0(
    .a(a),
    .b(sw[7:0]),
    .s(sw[11:8]),
    .r(LED[7:0]),
    .c(LED[8]),
    .v(LED[9])
);

assign LED[15:12] = 5'b0;

endmodule

```

This module includes an 8-bit value that stores the value of `a` in flip flops.

```

logic [7:0] a; //a state-holding register for a

```

This module incorporates flip-flops that capture `sw[7:0]` and stores it to `a[7:0]` when the `btnC` button is pressed. This will capture the first input (`a`) for the ALU and store it, allowing you to reset `sw[7:0]` for the second input to the ALU (`b`).

You will then need to reconfigure `sw[7:0]` for the second input, and set the select inputs to perform the appropriate ALU operation.

As some of the `LED` values are unused, we assign them to 0 (off).

*Remember to select “System Verilog” from the “File Type” drop-down menu.*

## Testbench

For this project, you only need to create a testbench for your ALU. It should be named `alu_tb.sv`.

*Remember to select “System Verilog” from the “File Type” drop-down menu.*

## Constraints

We recommend you copy the default constraints file from here:

[Basys3 Constraints](#)

You will also need to reconfigure your file to align with the top-level module declaration. The names should line up properly by default.

## Evaluation

The evaluation will have two steps, first submission of your source code and testbench to the autograder. Second, you will need to synthesize your design, download it to the FPGA and do a demonstration for the TA.

### Autograder (70% )

Log on to <https://autograder.sice.indiana.edu> and submit your code as per previous projects.

You should submit:

- `alu.sv`
- `alu_tb.sv`
- `top.sv`

### Demonstration (30%)

Program your FPGA with your demultiplexer and demonstrate your working system to the TA. You will not receive full points until the TA has approved your demonstration.