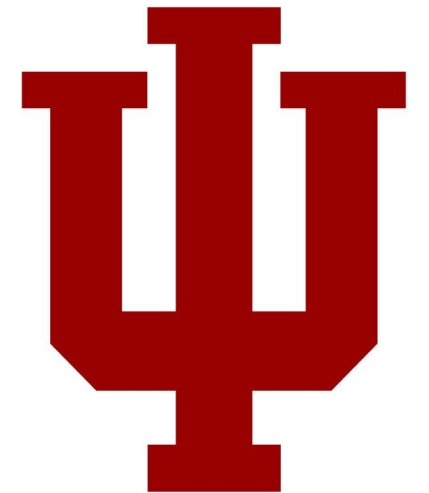


Max Austin Michael Clare

Grant Chris Will Jack Trey Yifan

# 07 True Random Number Generators (TRNGs)

Engr 399/599: Hardware Security  
Andrew Lukefahr  
*Indiana University*



Adapted from: Mark Tehranipoor of University of Florida

Course Website

engr599.github.io

Room  
2-3-5  
Pass code:

Write that down!

# Project 1: Hardware Trojan

Shareable  
board in  
14

(Firmware  
JTAG)

- Goal: “Corrupt” a working DES implementation
- We give you DES in HW
- You need to:
  - Deploy DES
  - Corrupt DES

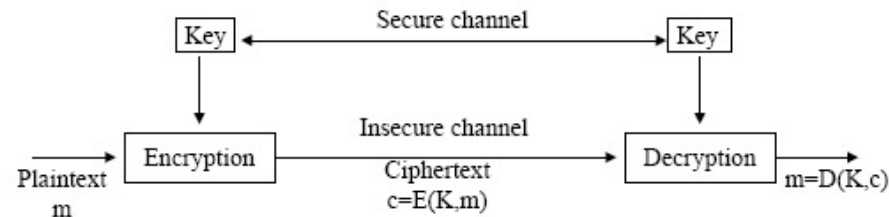
# Group Assignments

- Chris Sozio
- Will Fleming
- Clare Barnes
  
- Austin Parkes
- Max Harms
- Michael Foster
  
- Trey Peterson
- Yifan Zhang
- Jack Ruocco

Due next  
Wednesday 

# Symmetric and Asymmetric Cryptosystems (1)

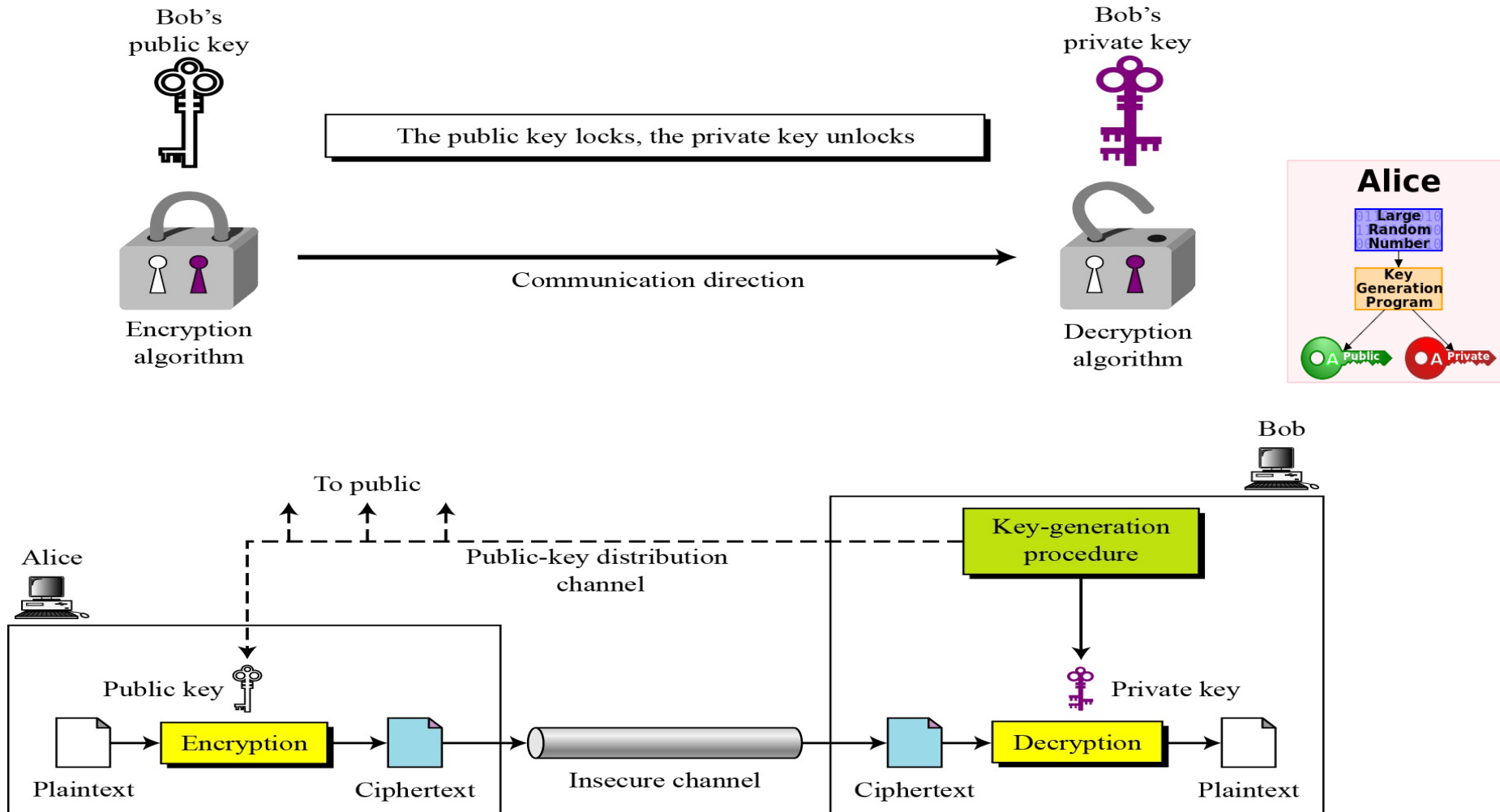
- Symmetric encryption = **secret key encryption**
  - $K_E = K_D$  — called a **secret key** or a **private key**
  - Only sender S and receiver R know the key



[cf. J. Leiwo]

- As long as the key remains secret, it also provides **authentication** (= proof of sender's identity)

# Asymmetric Security



# Attacks

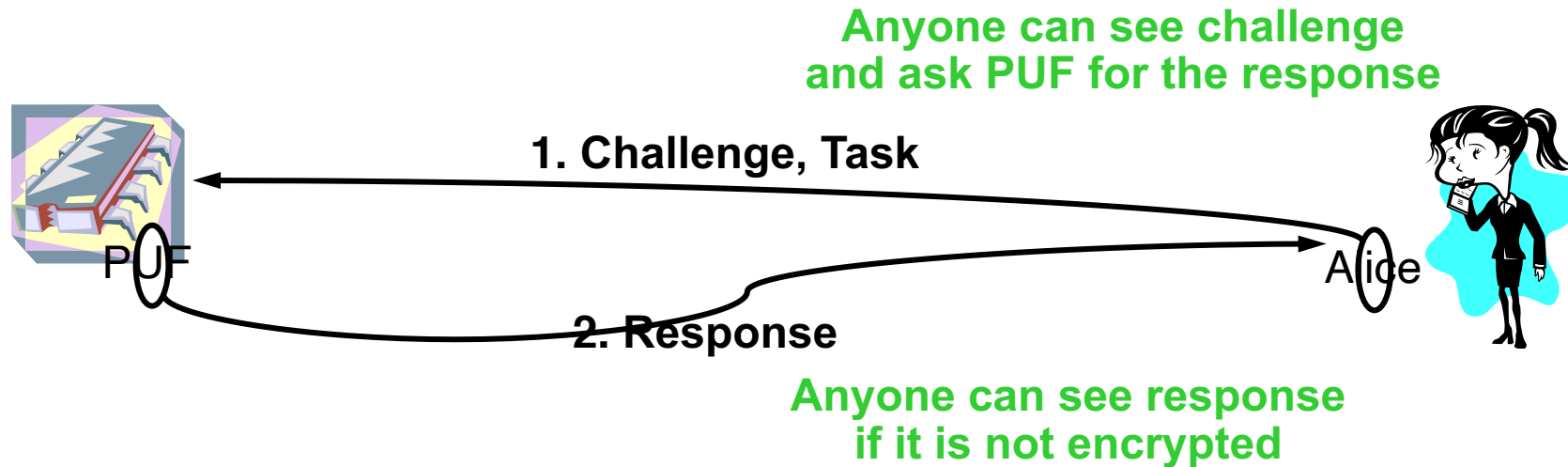
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Software-only protection is not enough. Non-volatile memory technologies are vulnerable to invasive attack as secrets always exist in digital form

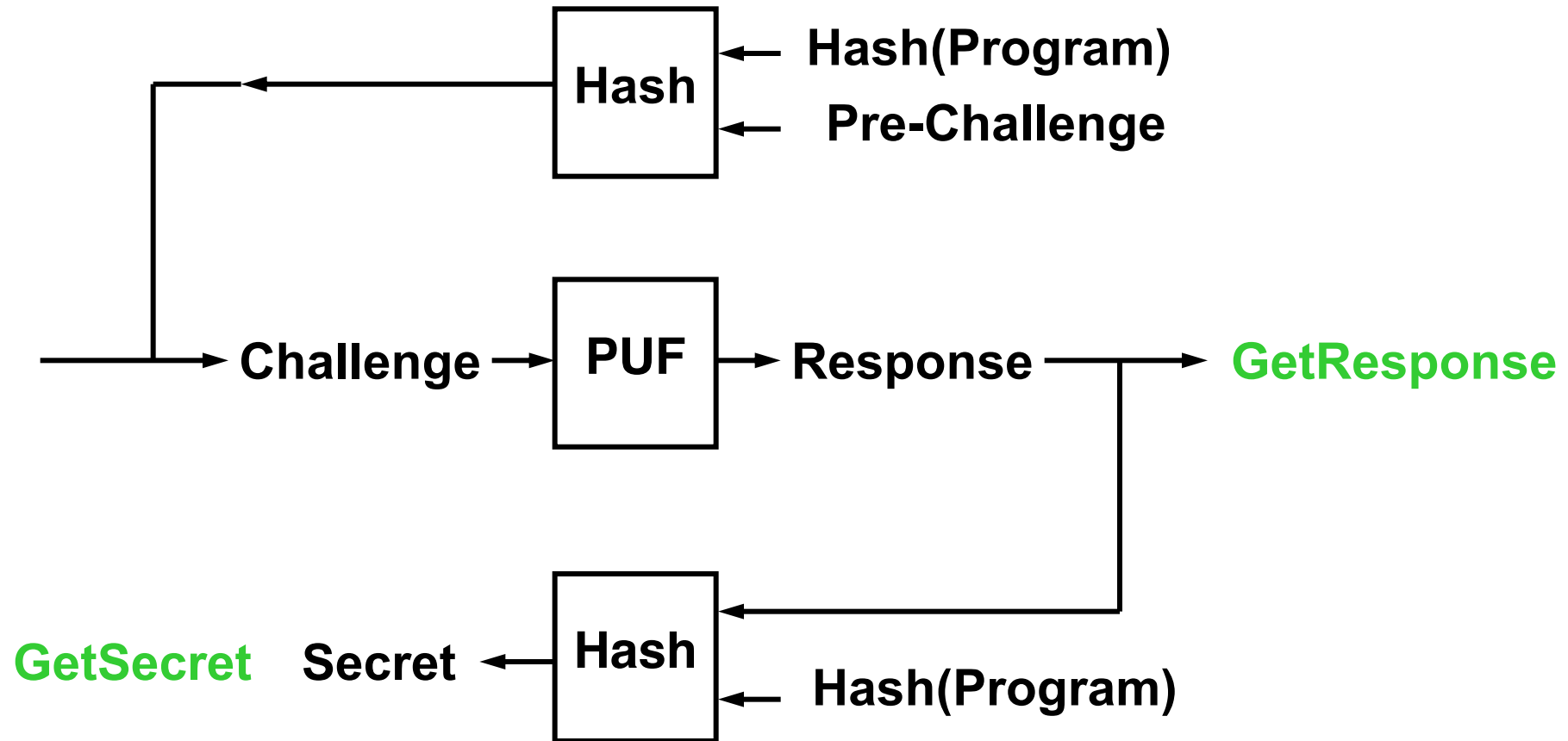
# Sharing a Secret with a Silicon PUF

Suppose Alice wishes to share a secret with the silicon PUF  
She has a challenge response pair that no one else knows,  
which can authenticate the PUF  
She asks the PUF for the response to a challenge

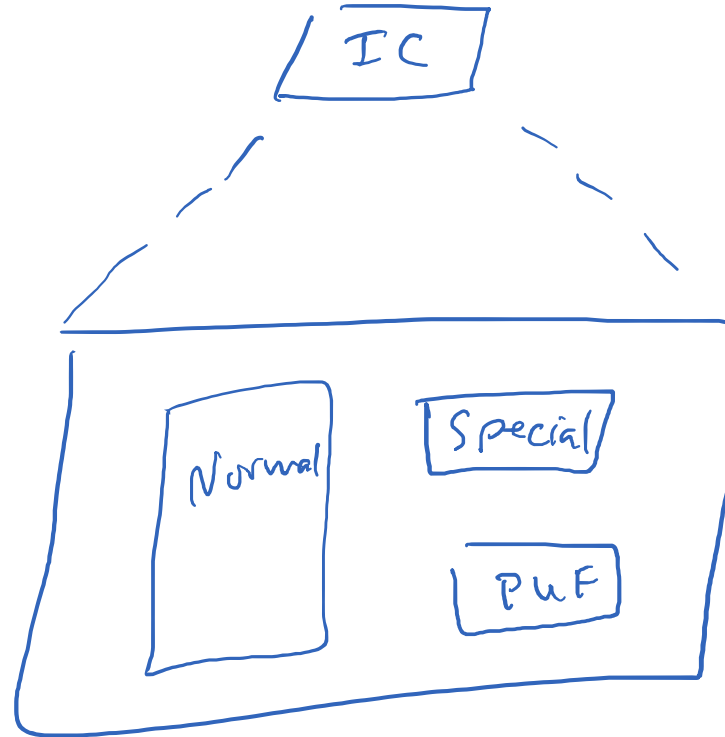




# Controlled PUF Implementation



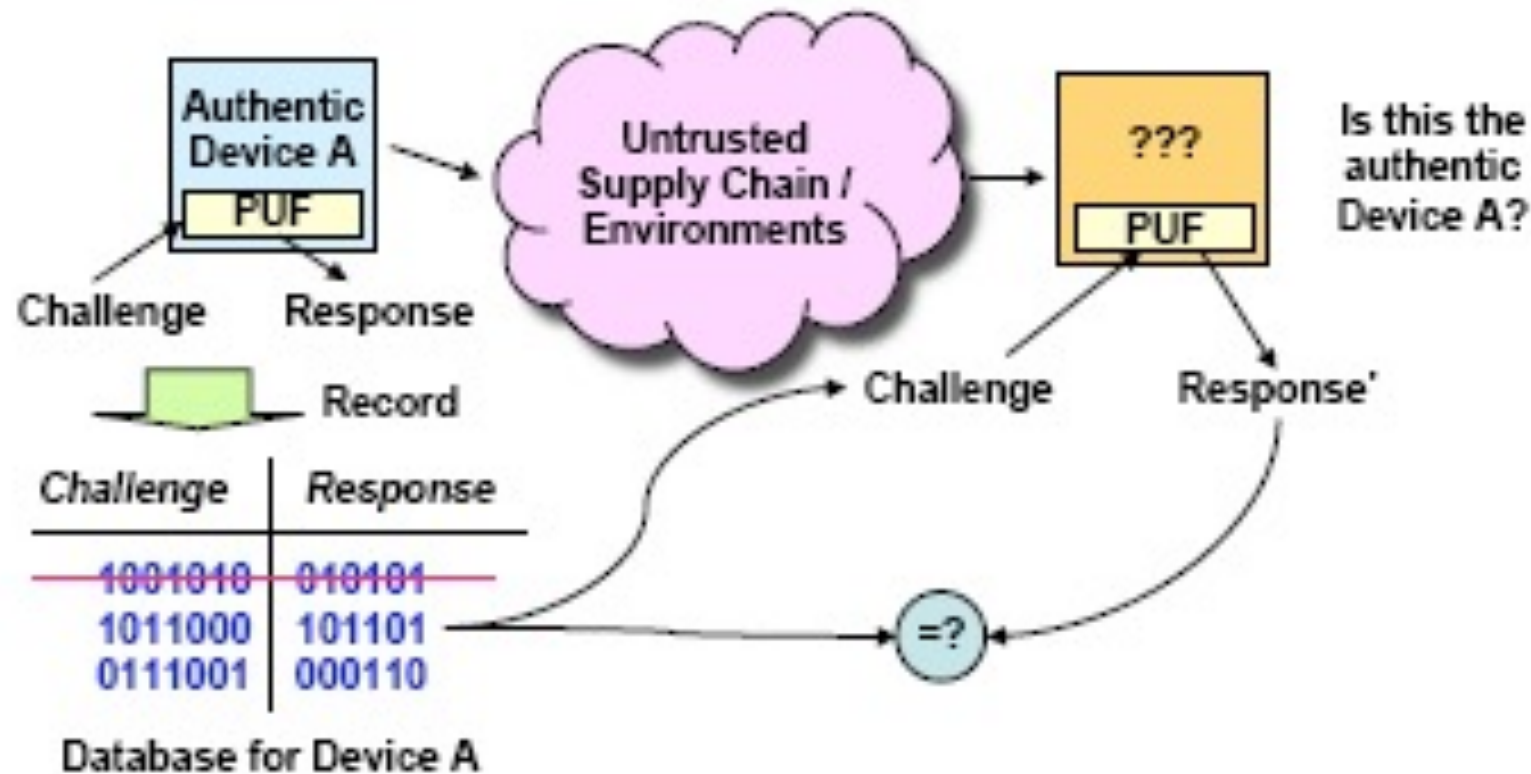
# Software Licensing



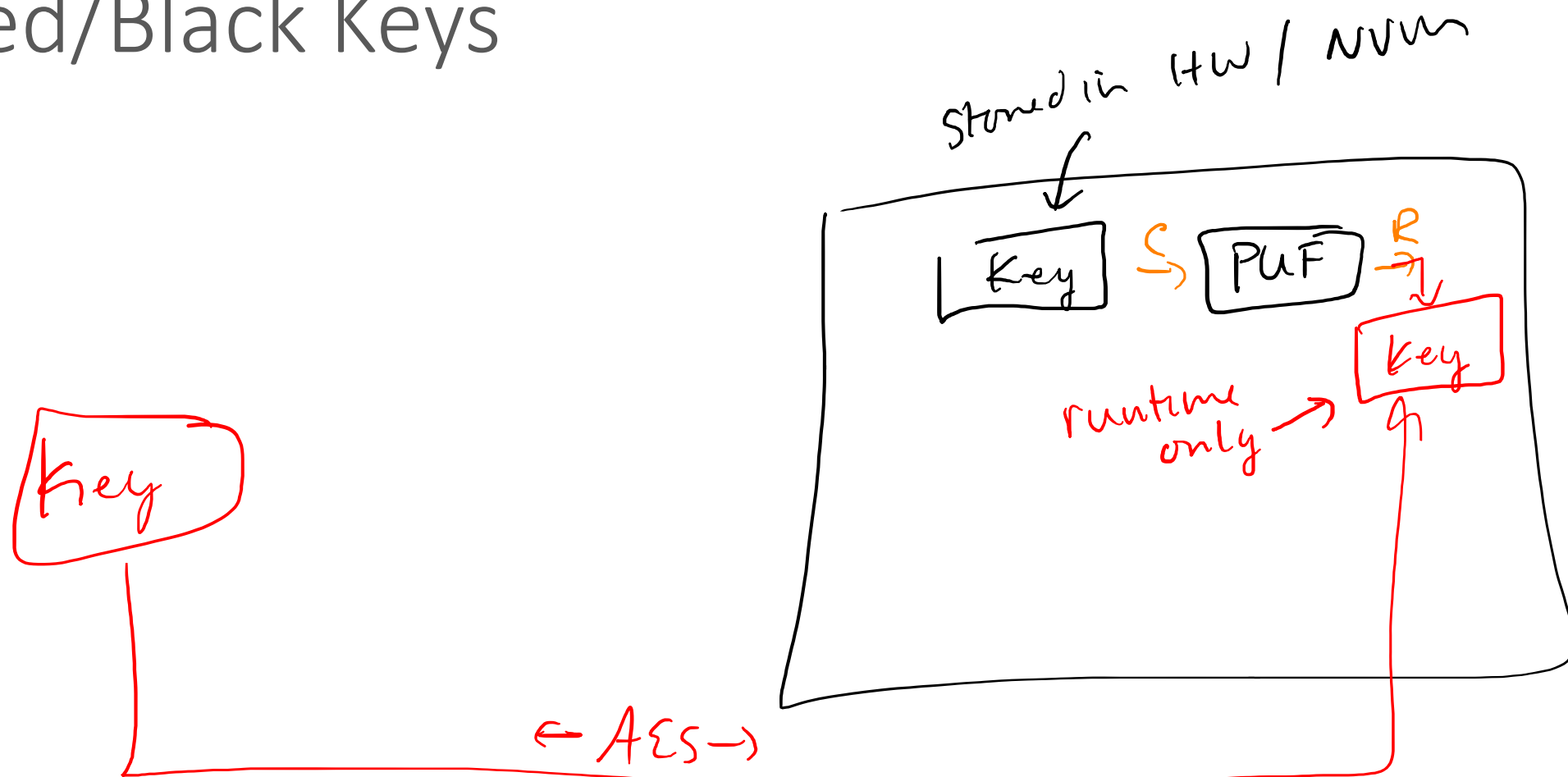
Challenge → Response  
Color → flower

# Applications – Authentication

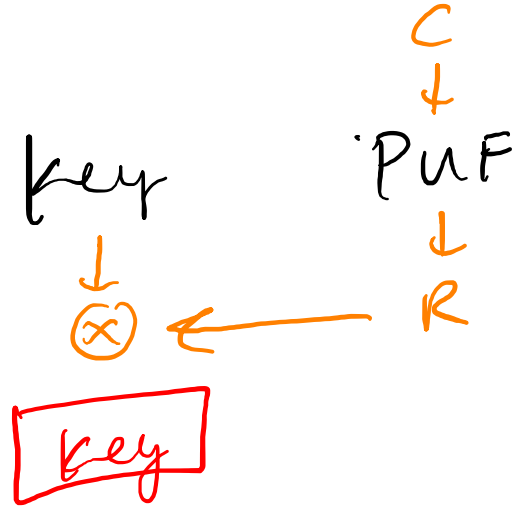
- Same challenges should not be used to prevent the man-in-the-middle attacks



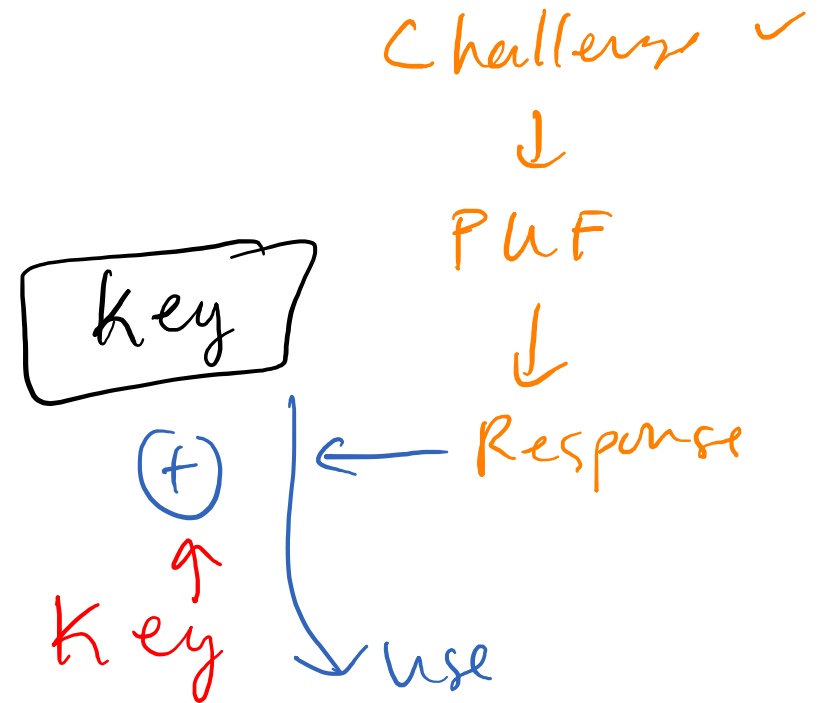
# Red/Black Keys



# Problems with PUFs



program



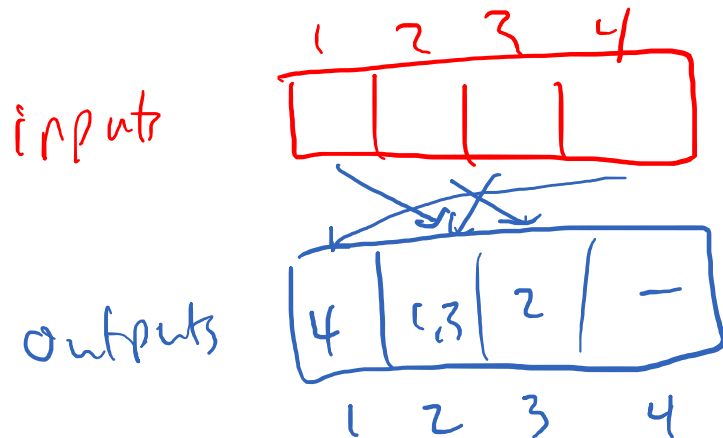
# Put Problems

challenge → response

color → "strawberry"

ice-cream → strawberry

fruit → strawberry



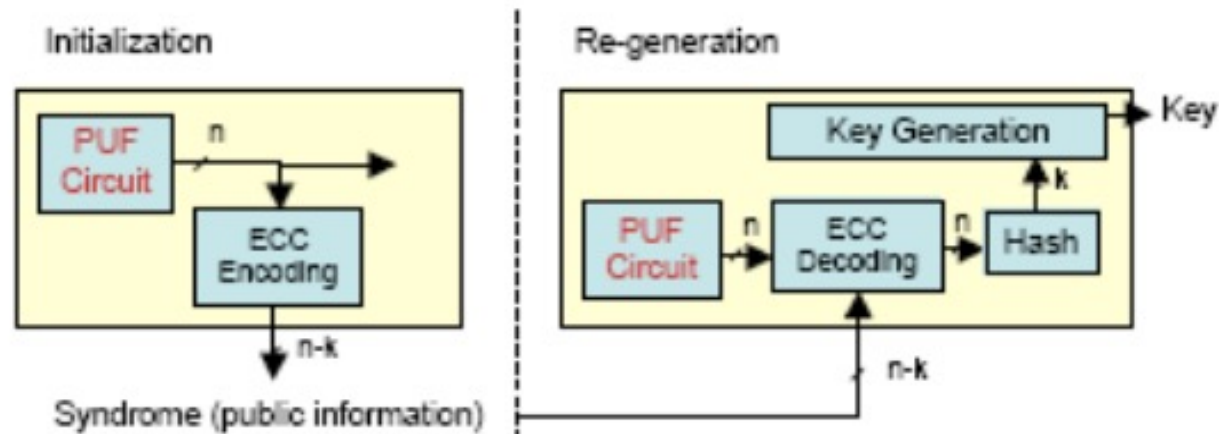
→ similar answers across puts

→ similar answers with put

→ dissimilar responses with put

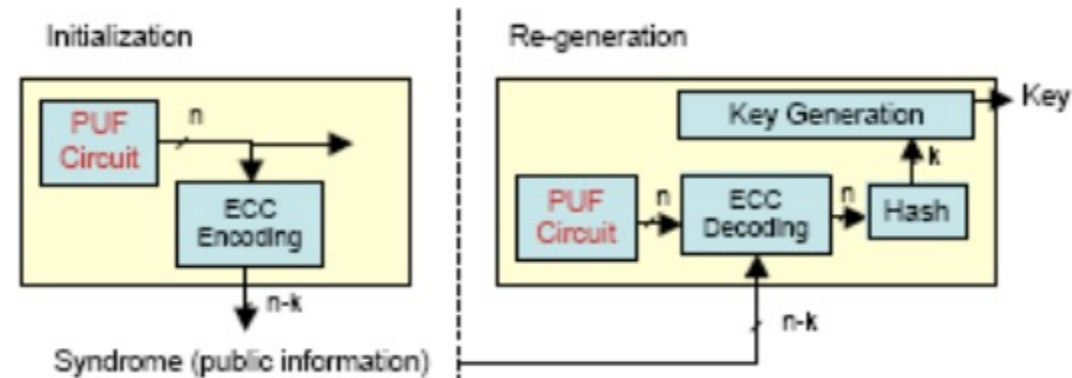
# Application – Cryptographic Key Generation

- The unstability is a problem
- Some crypto protocols (e.g., RSA) require specific mathematical properties that random numbers generated by PUFs do not have
- How can we use PUFs to generate crypto keys?
  - Error correction process: initialization and regeneration
  - There should be a one-way function that can generate the key from the PUF output



# Crypto Key Generation

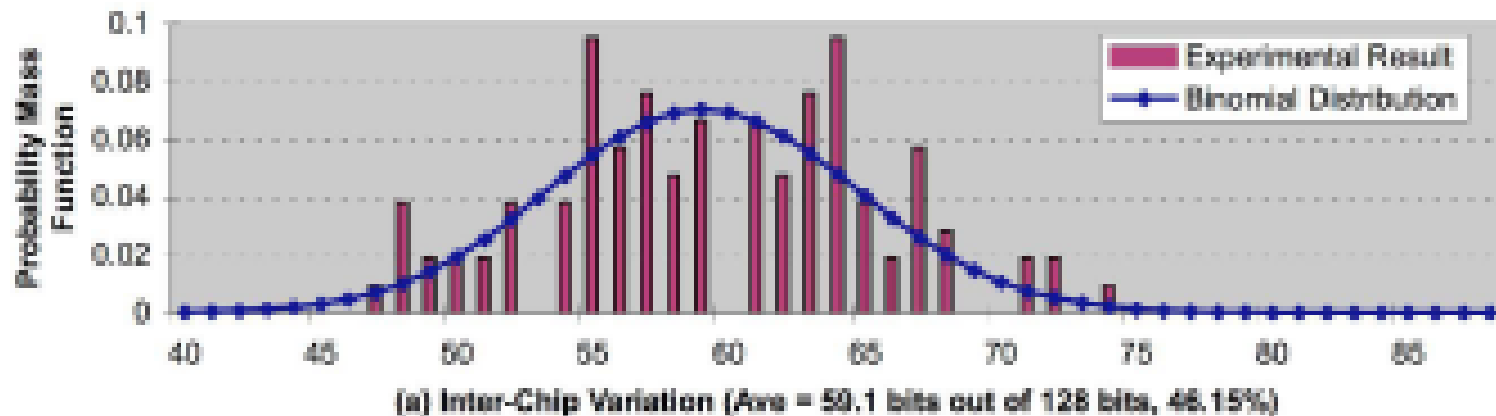
- Initialization: a PUF output is generated and error correcting code (e.g., BCH) computes the syndrome (public info)
- Regeneration: PUF uses the syndrome from the initial phase to correct changes in the output
- Clearly, the syndrome reveals information about the circuit output and introduces vulnerabilities





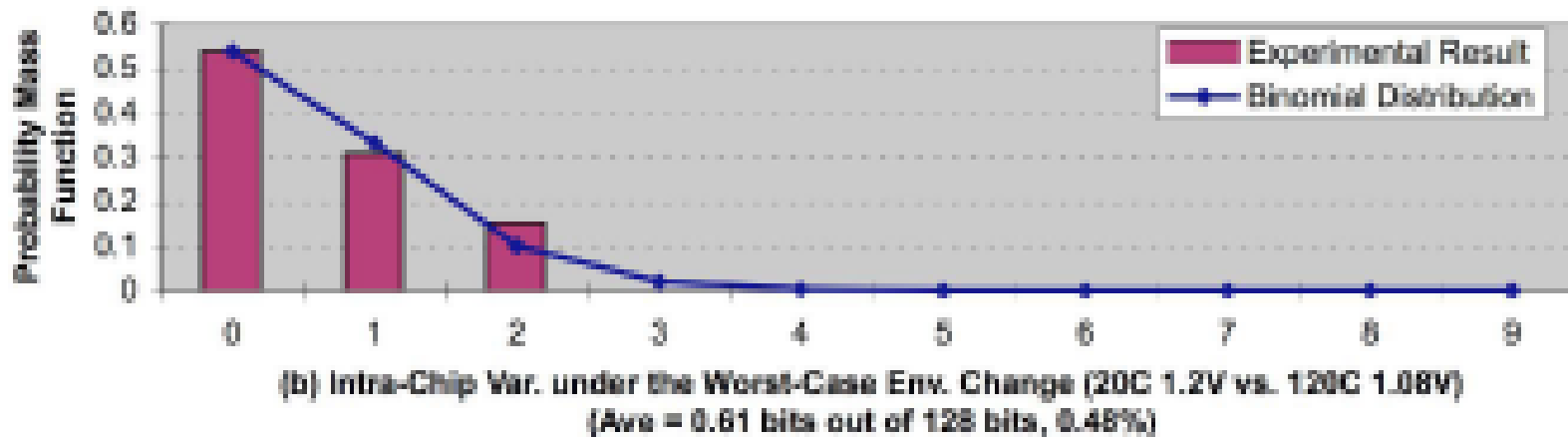
# The Probability Distribution for Inter-chip Variations

- 128 bits are produced from each PUF
- x-axis: number of PUF o/p bits different b/w two FPGAs; y-axis: probability
- Purple bars show the results from 105 pair-wise comparisons
- Blue lines show a binomial distribution with fitted parameters ( $n=128$ ,  $p=0.4615$ )
- Average inter-chip variations  $0.4615 \sim 0.5$



# The Probability Distribution for Intra-chip Variations

- PUF responses are generated at two different conditions and compared
- Changing the temperature from 20°C to 120°C and the core voltage from 1.2 to 1.08 altered the PUF o/p by ~0.6 bits (0.47%)
- Intra-chip variations is much lower than inter-chip – the PUF o/p did not change from small to moderate



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# True Random Number Generator



# Random Numbers in Cryptography

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- The keystream in the one-time pad
- The secret key in the DES encryption
- The prime numbers  $p$ ,  $q$  in the RSA encryption
- Session keys
- The private key in digital signature algorithm (DSA)
- The initialization vectors (IVs) used in ciphers

# Pseudo-random Number Generator

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- **Pseudo-random number generator:**

- A polynomial-time computable function  $f(x)$  that expands a short random string  $x$  into a long string  $f(x)$  that appears random

- **Not truly random in that:**

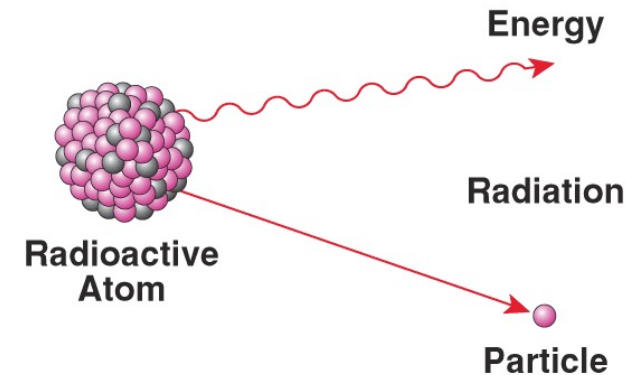
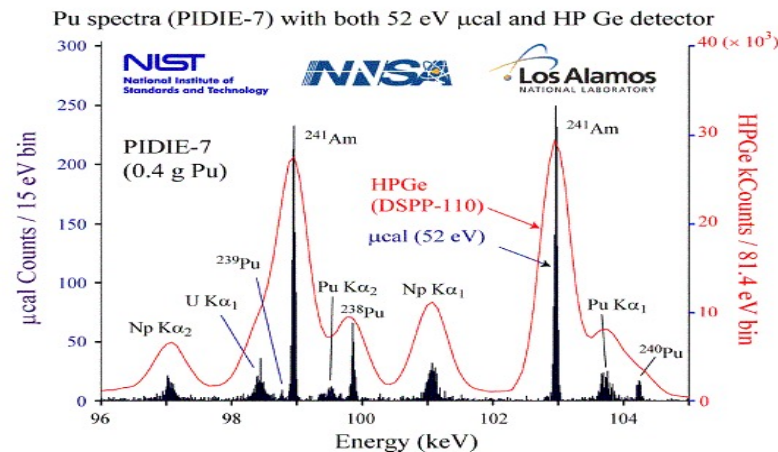
- Deterministic algorithm
- Dependent on initial values (seed)

- **Objectives**

- Fast
- Secure

# Sources

- The only truly random number sources are those related to physical phenomena such as **the rate of radioactive decay** of an element or the **thermal noise** of a semiconductor.



- Randomness is bound to natural phenomena. It is impossible to algorithmically generate truly random numbers.

Microcalorimeter (black) and high-purity germanium (red) spectra of a mixture of plutonium isotopes. Minimal thermal noise is achieved at 100 mK. High sensitivity is due to use of a superconducting quantum interference device.

# Good TRNG Design

## ■ Entropy Source:

- ❑ Randomness present in physical processes such as thermal and shot noise in circuits, brownian motion, or nuclear decay.

## ■ Harvesting Mechanism:

- ❑ The mechanism that does not disturb the physical process but collects as much entropy as possible.

## ■ Post-Processing (optional):

- ❑ Applied to mask imperfections in entropy sources or harvesting mechanism or to provide tolerance in the presence of environmental changes and tampering.

# Set of Requirements

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- ❑ The Design Should be purely digital
- ❑ The harvesting mechanism should be simple.
  - The unpredictability of the TRNG should not be based on the complexity of the harvesting mechanism, but only on the unpredictability of the entropy source.
- ❑ No correction circuits are allowed
- ❑ Compact and efficient design (high throughput per area and energy spent).
- ❑ The design should be sufficiently simple to allow rigorous analysis.

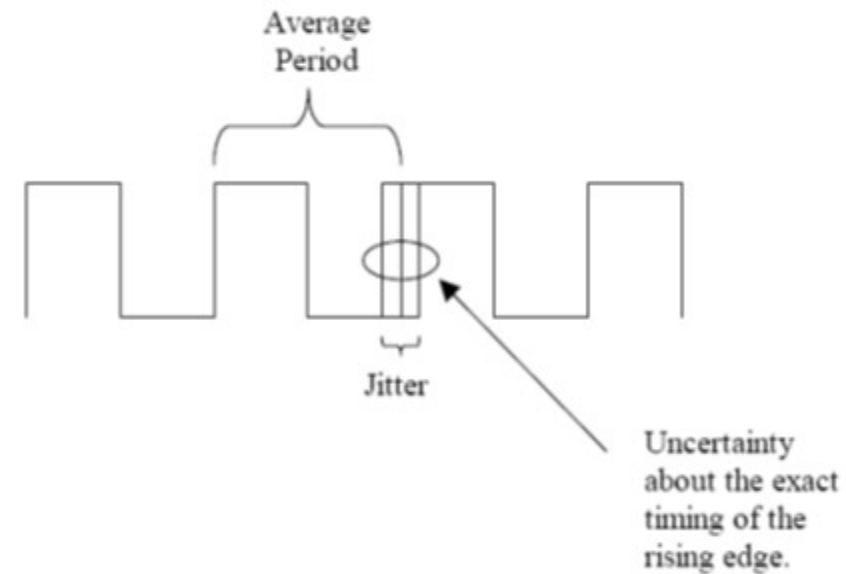


# Method : Clock Jitter

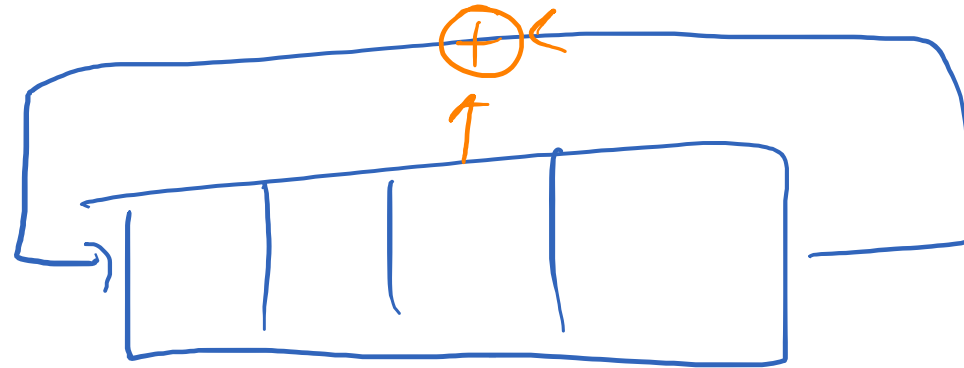
- Jitter is variations in the significant instants of a clock
- Jitter is nondeterministic (random)

- **Sources of Jitter:**

- Semiconductor noise
- Cross-talk
- Power supply variations
- Electromagnetic fields



# Linear Feedback Shift Register



1 2 3 4

← original

4 1 2 3

← shift

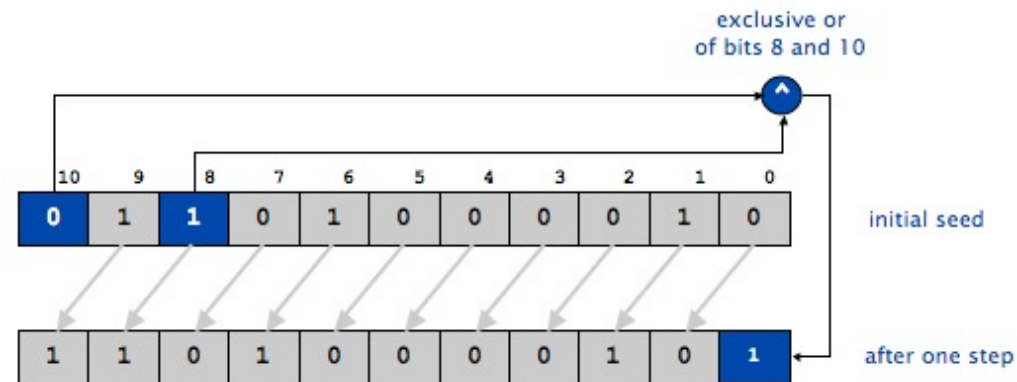
4 ⊕ 3 1 2 3

7 1 2 3

linear  
feedback  
shift

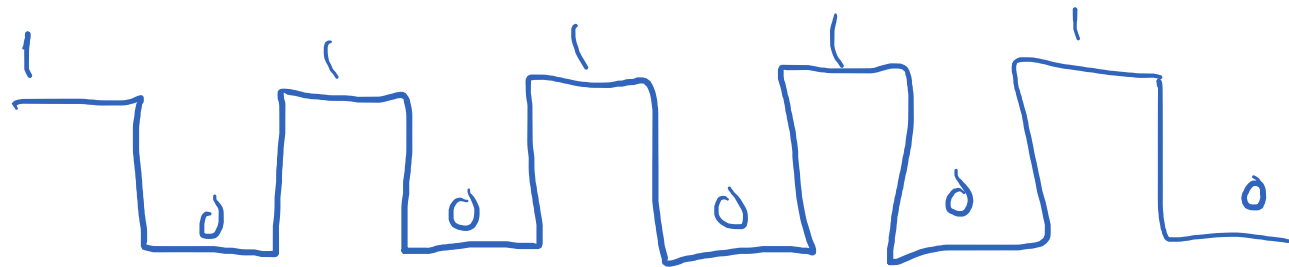
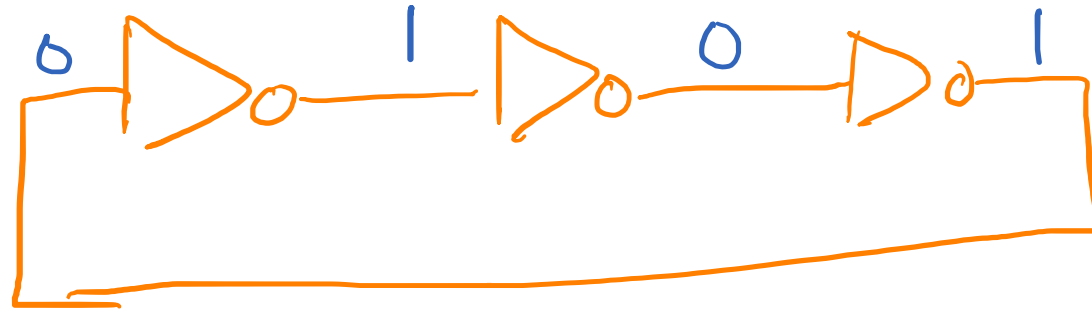
$$\begin{array}{r} 100 \\ \oplus 011 \\ \hline 111 \end{array}$$

# Linear Feedback Shift Register



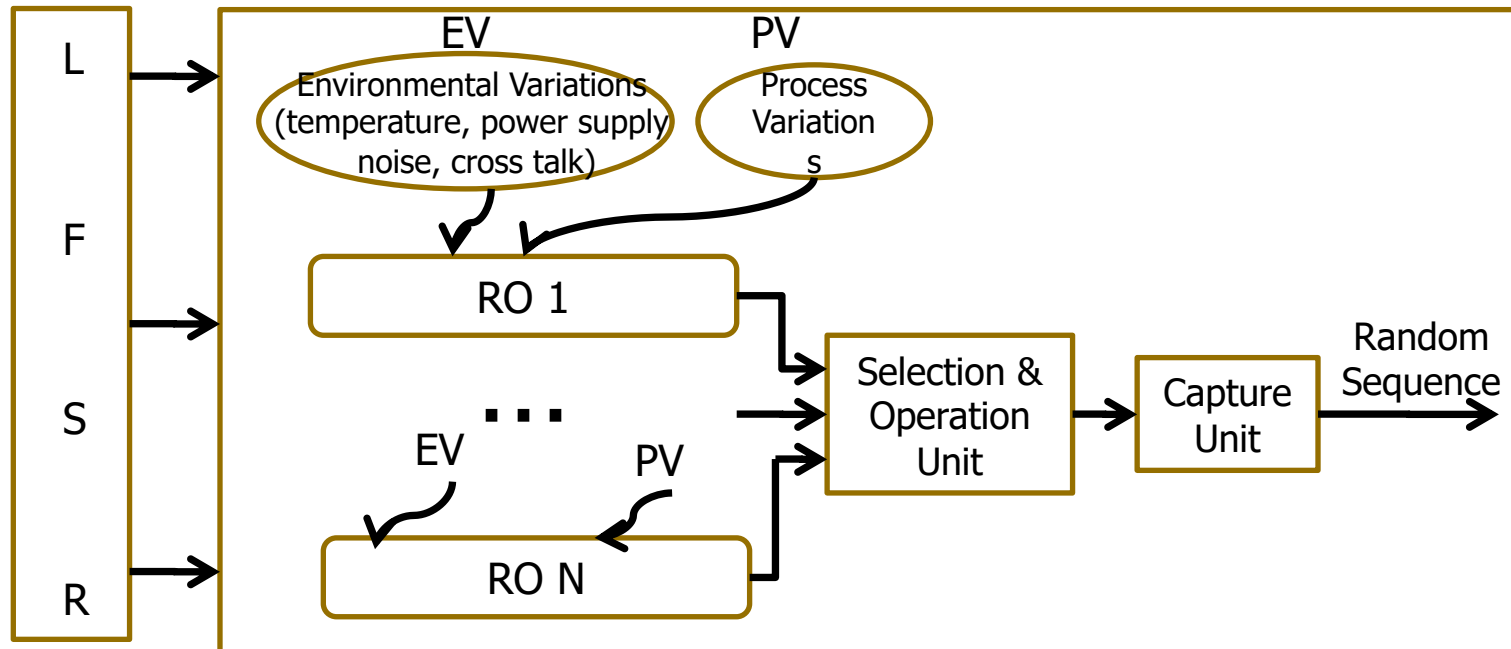
One step of an 11-bit LFSR with initial seed 01101000010 and tap at position 8

# Ring Oscillator



# TRNG Structure

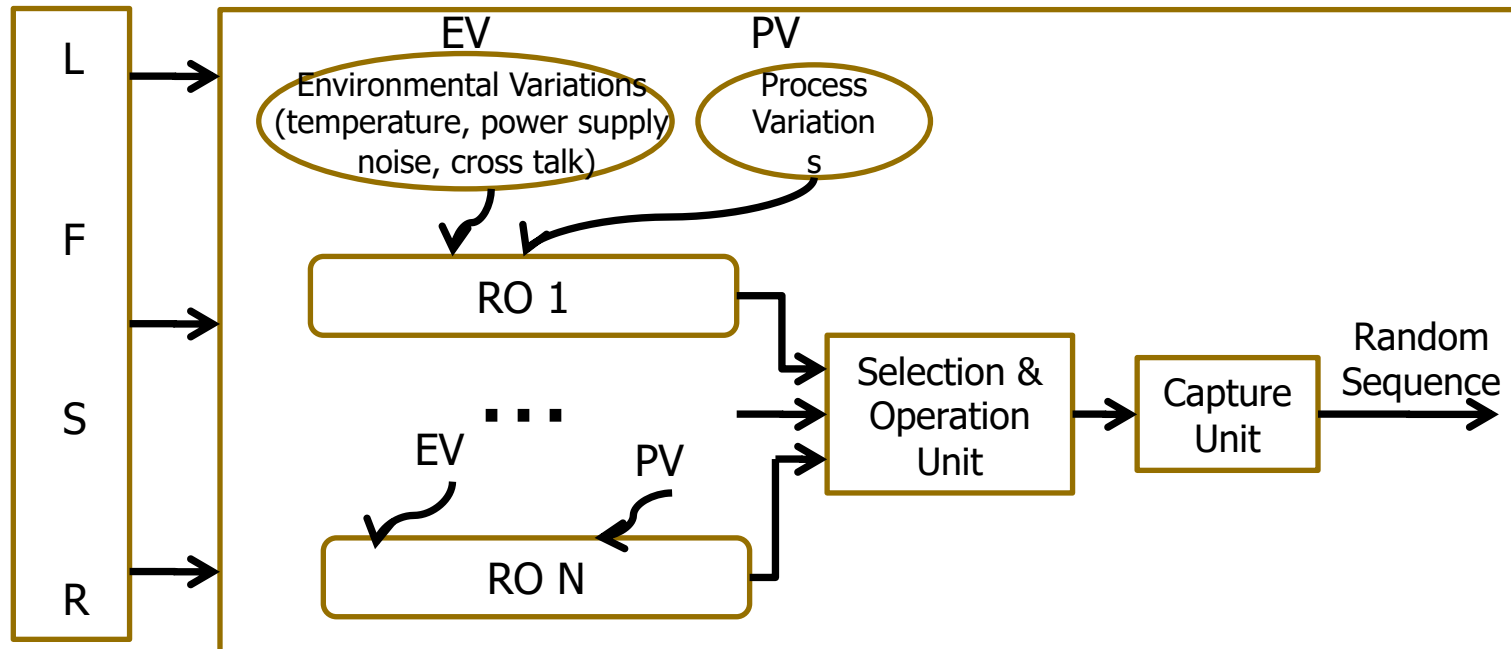
- ❑ **LFSR**: Generate random patterns, causing random switching noise



# TRNG Structure

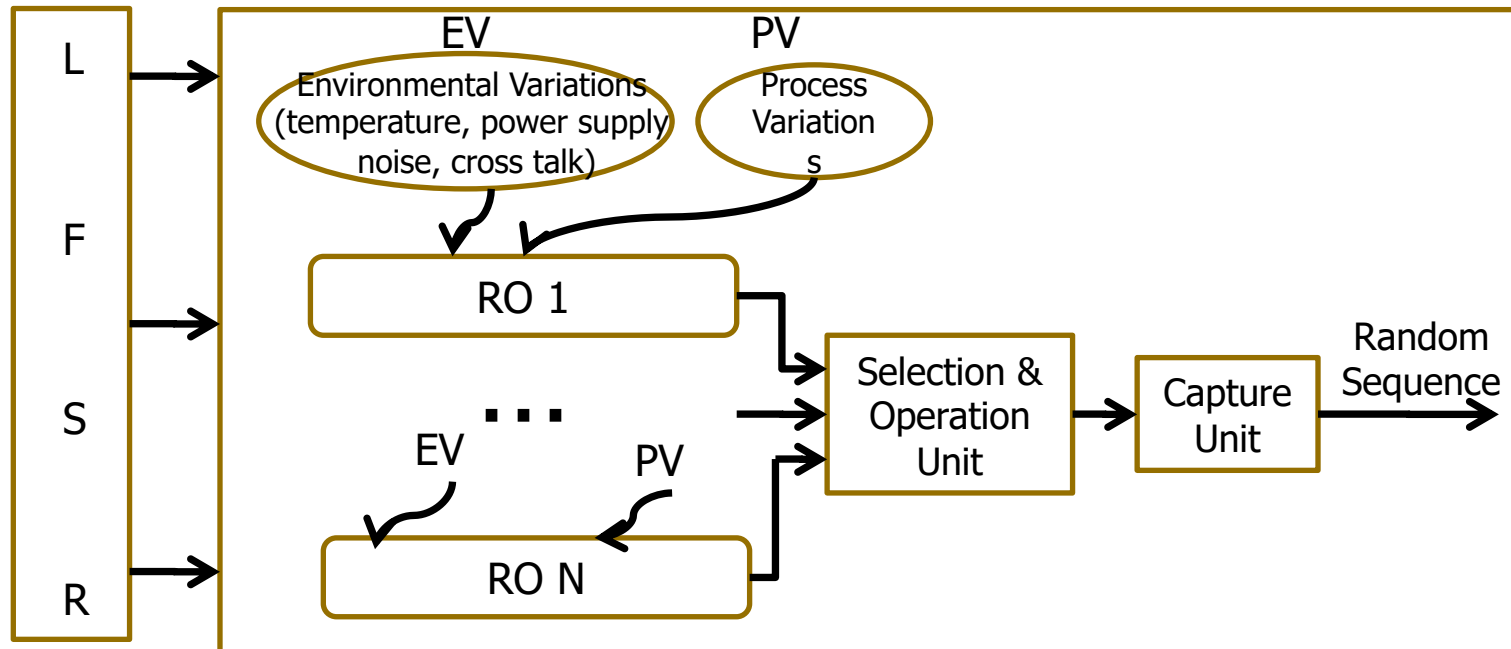
## □ Ring Oscillators

- Process variations & environmental variations
- Random phase jitter



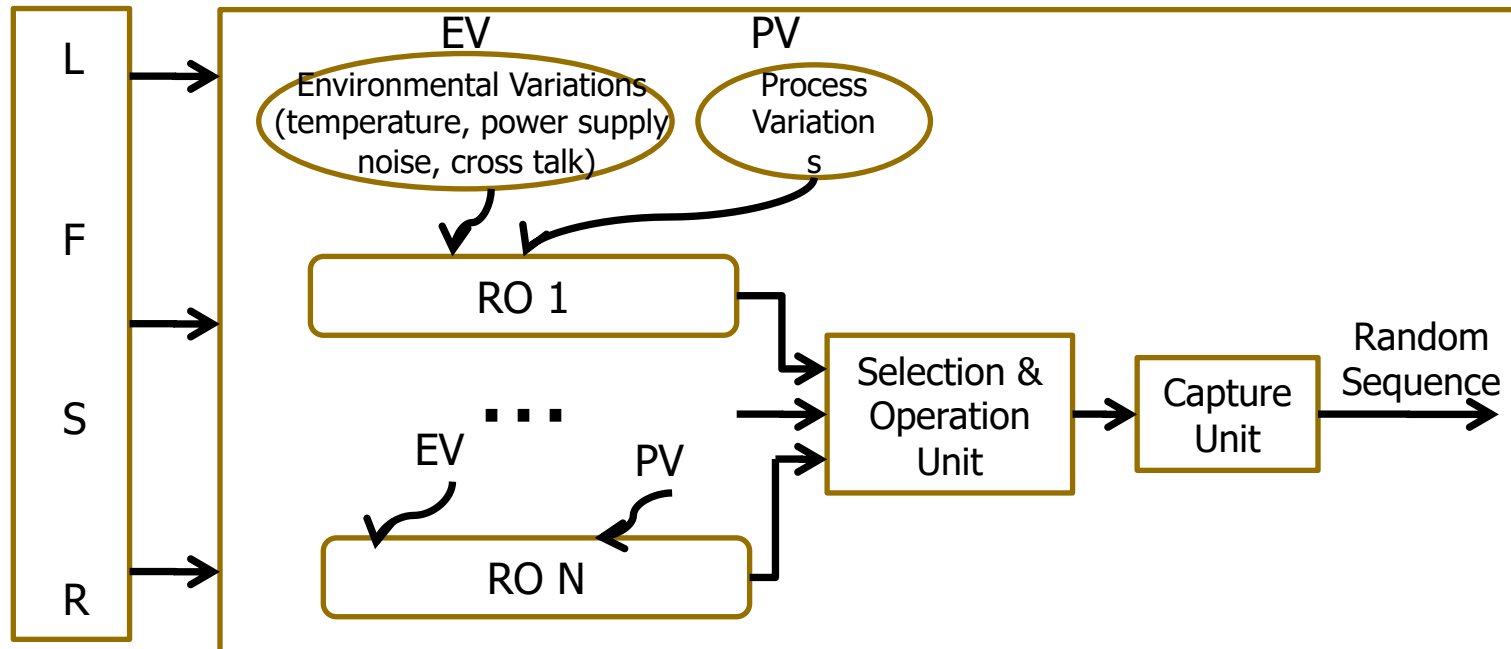
# TRNG Structure

- ❑ **Selection & Operation Unit:** The random phase of ring oscillators could be translated into digital values by this unit, such as XOR operation



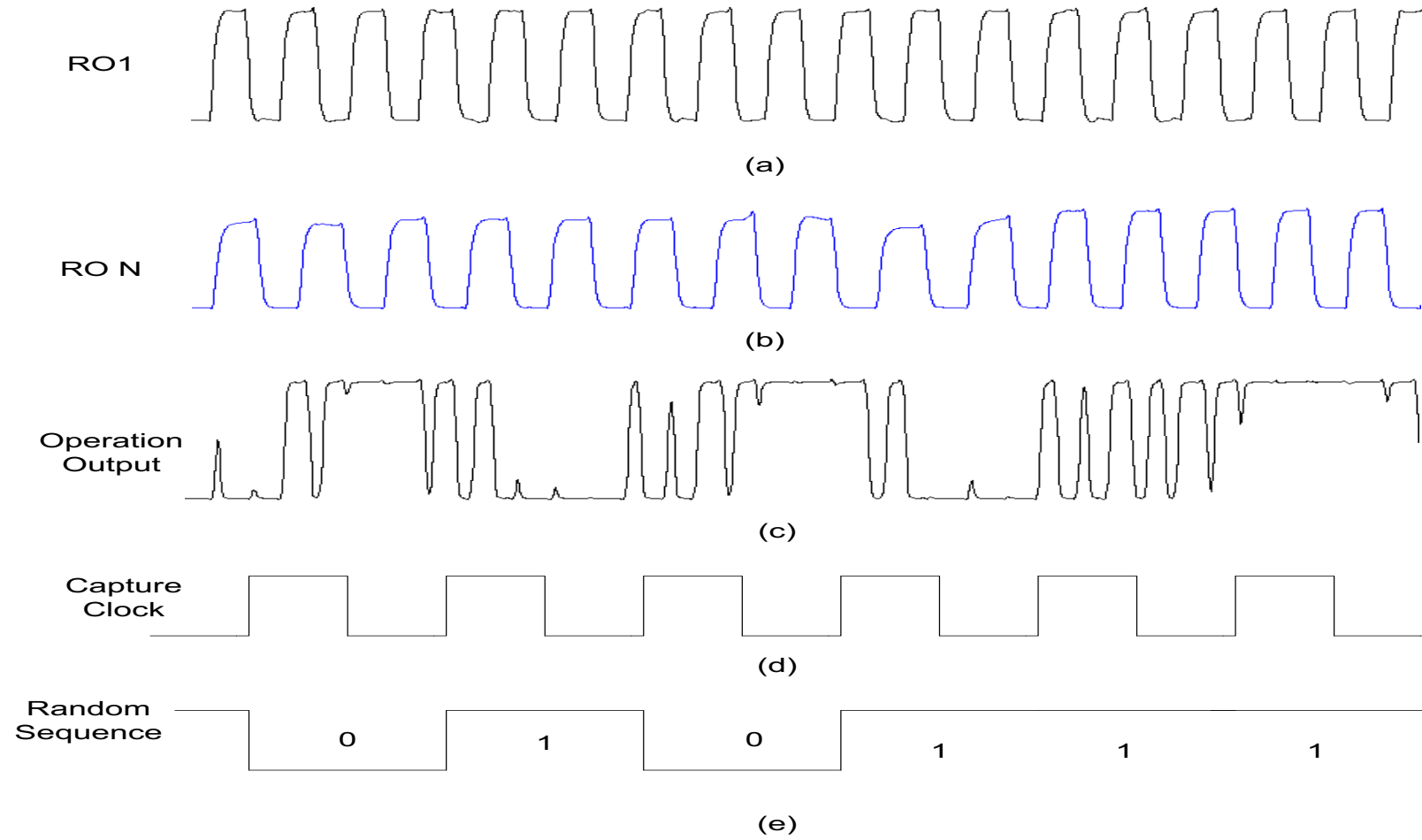
# TRNG Structure

- ❑ **Capture Unit:** Make sure the digital value is sampled with the frequency of the required true random number.





# TRNG Output



# References

- [1]Suh, G.E., Devadas, S.: Physical unclonable functions for device authentication and secret key generation. In: Design Automation Conference, pp. 9{14. ACM Press, New York, NY, USA (2007)
- [2]Gassend, B., Lim, D., Clarke, D., van Dijk, M., Devadas, S.: Identification and authentication of integrated circuits: Research articles. Concurr. Comput. : Pract. Exper.16(11), 1077-1098.
- [3]Gassend, B., Clarke, D., van Dijk, M., Devadas, S.: Controlled physical random functions. In: ACSAC '02: Proceedings of the 18th Annual Computer Security Applications Conference, p. 149. IEEE Computer Society, Washington, DC, USA (2002)
- [4]B. Gassend, D. Clarke, M. van Dijk, and S. Devadas. Silicon physical random functions. In Proceedings of the Computer and Communication Security Conference , November 2002.
- [5] Dinesh Ganta, Vignesh Vivekraja, Kanu Priya and Leyla Nazhandali, “A Highly Stable Leakage-Based Silicon Physical Unclonable Functions”

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- [6] A. Maiti and P. Schaumont, “Improved ring oscillator puf: An fpga-friendly secure primitive,” J. Cryptology, vol. 24, no. 2, pp. 375–397.,2011.
- [7] B. Sunar, W. J. Martin, D. R. Stinson. A Provably Secure True Random Number Generator with Built-in Tolerance to Active Attacks. IEEE Transactions on Computers, vol 58, no 1, pages 109-119, January 2007.