

Leyes de logaritmos

$$1. \log_a AB = \log_a A + \log_a B$$

$$2. \log_a \frac{A}{B} = \log_a A - \log_a B$$

$$3. \log_a B^n = n \log_a B$$

Sustituciones trigonométricas

$$1. \sqrt{a^2 - u^2}, \quad u = a \sin \theta$$

$$2. \sqrt{a^2 + u^2}, \quad u = a \tan \theta$$

$$3. \sqrt{u^2 - a^2}, \quad u = a \sec \theta$$

Integración por partes

$$\int f'(x) g(x) dx = (fg)(x) - \int g'(x) f(x) dx$$

Derivadas

$$1. [(f \pm g)(x)]' = f'(x) \pm g'(x)$$

$$2. [(fg)(x)]' = f'(x) g(x) + g'(x) f(x)$$

$$3. \left[\left(\frac{f}{g} \right)(x) \right]' = \frac{f'(x) g(x) - g'(x) f(x)}{[g(x)]^2}$$

$$4. [(f \circ g)(x)]' = [(f' \circ g)(x)] g'(x)$$

$$5. [u^n]' = n u^{n-1} u'$$

$$6. [\ln u]' = \frac{1}{u} u'$$

$$7. [e^u]' = e^u u'$$

$$8. [\sin u]' = \cos u u'$$

$$9. [\cos u]' = -\sin u u'$$

$$10. [\tan u]' = \sec^2 u u'$$

$$11. [\cot u]' = -\csc^2 u u'$$

$$12. [\sec u]' = \sec u \tan u u'$$

$$13. [\csc u]' = -\csc u \cot u u'$$

$$14. [\arcsin u]' = \frac{1}{\sqrt{1-u^2}} u'$$

$$15. [\arccos u]' = \frac{-1}{\sqrt{1-u^2}} u'$$

$$16. [\arctan u]' = \frac{1}{1+u^2} u'$$

$$17. [\operatorname{arccot} u]' = \frac{-1}{1+u^2} u'$$

$$18. [\operatorname{arcsec} u]' = \frac{1}{|u|\sqrt{u^2-1}} u'$$

$$19. [\operatorname{arccsc} u]' = \frac{-1}{|u|\sqrt{u^2-1}} u'$$

$$4a. f(x) = g(h(x))$$

$$f'(x) = g'(h(x)) h'(x)$$

$$6a. f(x) = \log_a u$$

$$f'(x) = \frac{u'}{u} \left(\frac{1}{\ln a} \right)$$

$$7a. f(x) = a^u$$

$$f'(x) = u' a^u \ln a$$

Integrales

$$1. \int k dx = kx + c, k \in \mathbb{R}$$

$$2. \int (f \pm g)(x) dx = \int f(x) dx \pm \int g(x) dx$$

$$3. \int k f(x) dx = k \int f(x) dx, k \in \mathbb{R}$$

$$4. \int x^n dx = \frac{x^{n+1}}{n+1} + c, n \neq -1$$

$$5. \int \frac{dx}{x} = \ln|x| + c$$

$$6. \int e^x dx = e^x + c$$

$$7. \int \sin x dx = -\cos x + c$$

$$8. \int \cos x dx = \sin x + c$$

$$9. \int \tan x dx = \ln|\sec x| + c$$

$$10. \int \cot x dx = \ln|\sin x| + c$$

$$11. \int \sec x dx = \ln|\sec x + \tan x| + c$$

$$12. \int \csc x dx = \ln|\csc x - \cot x| + c$$

$$13. \int \sec^2 x dx = \tan x + c$$

$$14. \int \csc^2 x dx = -\cot x + c$$

$$15. \int \sec x \tan x dx = \sec x + c$$

$$16. \int \csc x \cot x dx = -\csc x + c$$

$$17. \int \frac{dx}{\sqrt{a^2 - x^2}} = \arcsin \frac{x}{a} + c$$

$$18. \int \frac{dx}{a^2 + x^2} = \frac{1}{a} \arctan \frac{x}{a} + c$$

$$19. \int \frac{dx}{x\sqrt{x^2 - a^2}} = \frac{1}{a} \operatorname{arcsec} \frac{x}{a} + c$$