

# Introduction to Expressions

As part of Week 3, Unit 3  
CC4 Data Structures and Algorithms  
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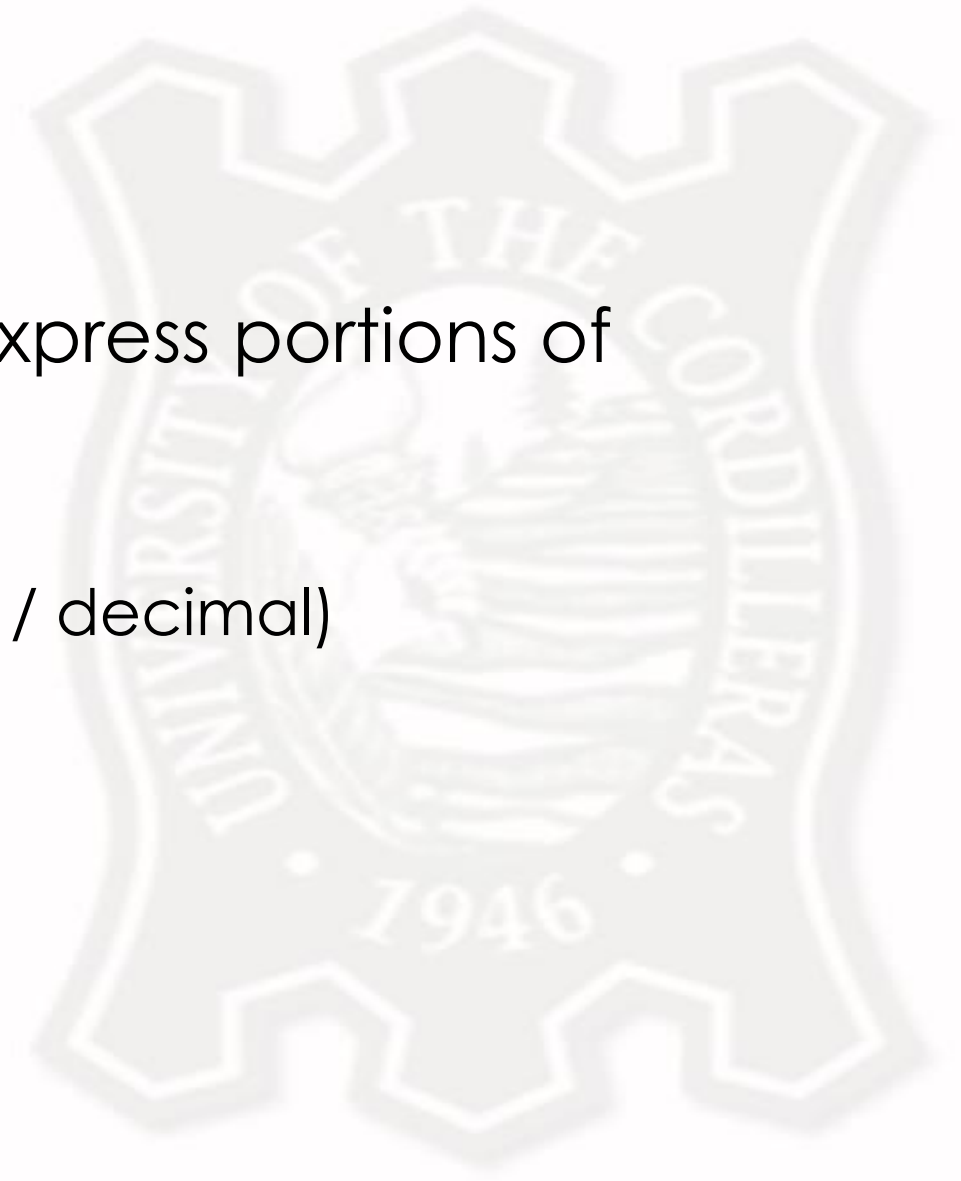
# Introduction to Expressions

What are expressions? | Parts of an expression | Expressions in this unit



# What are Expressions?

- A combination of symbols used to express portions of mathematical equations
- Symbols can be:
  - Numbers (positive / negative, absolute / decimal)
  - Variables (expressed in letters)
  - Operators (arithmetic or comparison)
  - Punctuations (groupings)
- Mathematical expressions can be:
  - Arithmetic (numbers only)
  - Algebraic (numbers and constants)
  - Comparison (uses comparison symbols)



# Parts of an Expression

## Operator

- Symbol(s) that decide(s) which operation is to be performed
- Arithmetic (+, -, \*, /, %)
- Comparison (<, >, ==, <=, >=)

## Operand

- Symbol(s) that represents an entity on which the operation is performed
- Numbers (0, -1, 1.2)
- Variables (a, b, x)
- Constants (log, e)



# Expressions in this Unit

- Limited to binary expressions
  - Utilizes operations that would require two operands
  - Arithmetic and comparison operations may be used
  - Increment and decrement operations are not to be used
  - Unary / ternary operators are possible for use in expressions
- Limited to arithmetic operations
  - Comparison operations may be used, and may appear in activities
  - All examples will be limited to arithmetic operations and the equal sign (=)



# Infix Expressions

What is an infix expression? | Examples of infix expressions |  
Precedence and associativity | Importance of prefix and postfix  
expressions



# What is an Infix Expression?

- Usual way on how humans express mathematical expressions
- Notation where the operators are placed in-between the operands
- Requires specific precedence and associativity rules





# Examples of Infix Expressions

- $a + b$

- $c + d * 2$

- $3 - e + 1$

- $(x + y) * (z - 5)$



# Precedence and Associativity

## Precedence

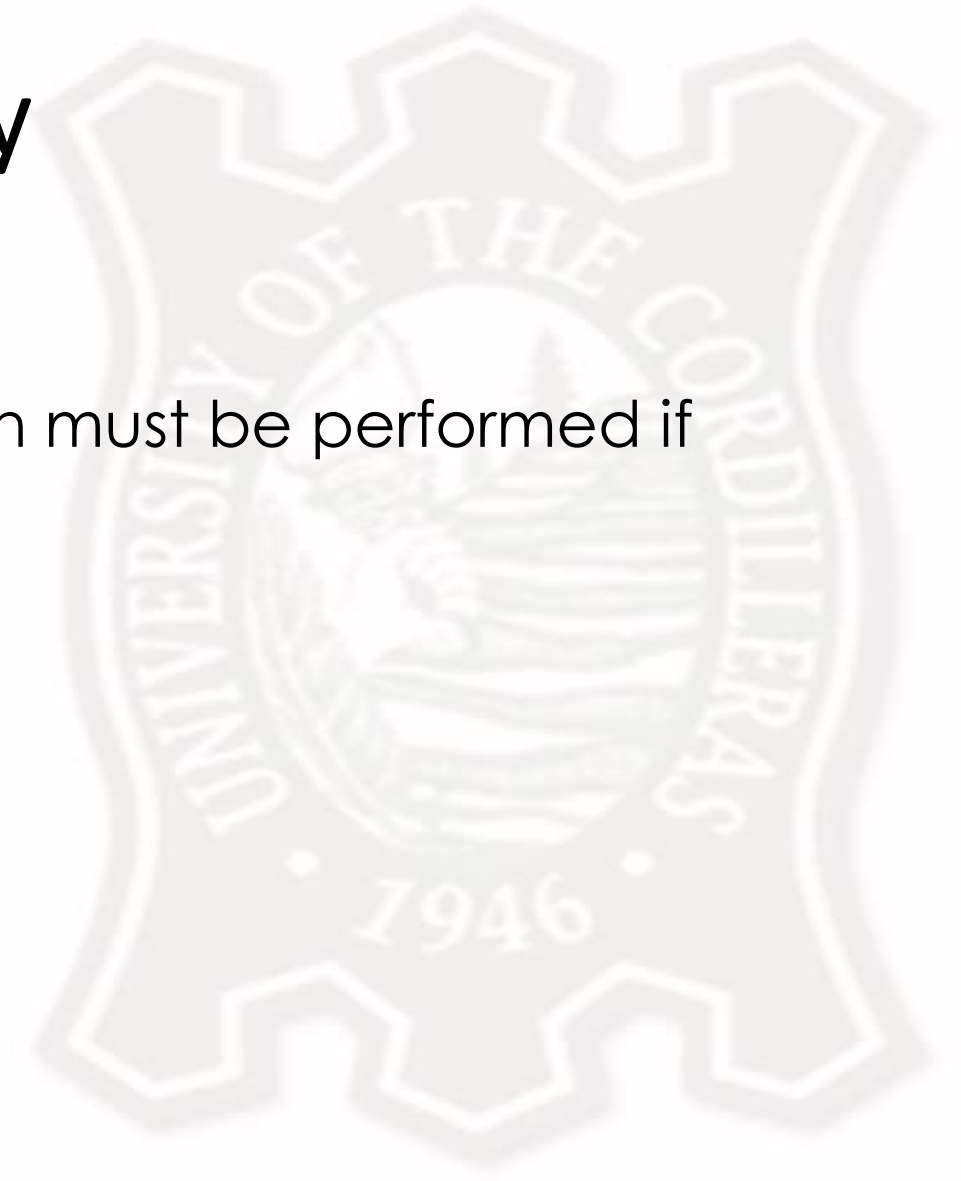
- Determines the order of what operation must be performed first in comparison to other operations
- Parenthesis, Multiplication and Division, Addition and Subtraction
- Example:  $c + d * 2, (x + y) * (z - 5)$



# Precedence and Associativity

## Associativity

- Determines the order of what operation must be performed if they are in the same precedence
- Left to right precedence
- Example:  $3 - e + 1$



# Prefix and Postfix Expressions

- Infix expressions are easily understood for humans, but not for machines
  - There are a lot of rules and regulations that cannot be easily translated into machine code
- Prefix and postfix expressions are notations that are understood better by machines
  - All rules on precedence and associativity are removed
  - All symbols can be placed on a stack
  - Increases overall efficiency of the code
  - Less understood by humans



# Postfix Expressions

What is a postfix expression? | Steps – infix to postfix | Postfix expression – examples



# What is a Postfix Expression?

- Notation for expressions where:
  - Operators are placed on the right side (after)
  - Operands are placed on the left side (before)
- Order of evaluation of expressions is always left to right
- Brackets cannot be used to change the order
- More commonly used for machine code
  - Translation from infix expression is much easier



# Steps – Infix to Postfix

- Determine the order of operations using the rules from infix expressions
- First operands that must be evaluated are placed at the leftmost portion of the notation
- First operator that must be evaluated are placed after the operands
- Next operators and/or operands are placed at the left side of the notation
- Last operator must be at the rightmost side of the notation



# Postfix Expression - Examples

- $a + b = \mathbf{a\ b\ +}$

- $c + d * 2 = \mathbf{c\ d\ 2\ *\ +}$

- $3 - e + 1 = \mathbf{3\ e\ -\ 1\ +}$

- $(x + y) * (z - 5) = \mathbf{x\ y\ +\ z\ 5\ -\ *}$





# Prefix Expressions

What is a prefix expression? | Steps – infix to prefix | Prefix expression – examples



# What is a Prefix Expression?

- Notation where the operators are written before the operands
- Operators act on the two nearest values on the right
  - Technically evaluated from left to right
  - The order changes depending whether or not elements to the right would be used



# Steps – Infix to Prefix

- Determine the order of operations using the rules from infix expressions
- First operands that must be evaluated are placed at the rightmost portion of the notation
- First operator that must be evaluated are placed before the operands
- Next operators and/or operands are placed at the right side of the notation
- Last operator must be at the leftmost side of the notation



# Prefix Expression - Examples

- $a + b = + a b$

- $c + d * 2 = + c * d 2$

- $3 - e + 1 = - 3 + e 1$

- $(x + y) * (z - 5) = * + x y - z 5$

