



# TIME SERIES ANALYSIS AND APPLICATIONS

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# Let's start with introductions...



- Originally from Brazil
- B.Sc. & MS. , Electrical Engineering

FEDERAL UNIVERSITY OF ITAJUBÁ, Brazil, 2005 & 2007

*Electrical Power Systems*



- Ph.D., Operations Research and Industrial Engineering

UNIVERSITY OF TEXAS, Austin, TX, 2011



*Modeling and Forecast of Brazilian Reservoir Inflows via Dynamic Linear Models under Climate Change Scenarios*

- Joined the Nicholas School in Jan 2018 and the EI/NIEES in July 2019
- **Recent courses:** Time Series Analysis for Energy Data, Environmental Data Analytics, Modeling for Energy Systems, Economics of Modern Power Systems
- **Research and work experience:** Renewable energy development and integration, Co-Optimization of Water & Energy Systems, Power System Economics, Climate Change effect on energy production



# Agenda



- Intro to Time Series Analysis
  - ▣ Background and motivation
  - ▣ TS Definition and Components
  - ▣ Examples of TS Models
  - ▣ Applications to Energy
- Time Series Decomposition
  - ▣ Trend component and seasonal component
  - ▣ How to identify/estimate components
  - ▣ Case Study
- Forecasting

# Intro to Time Series Analysis

Background and Motivation

TS Models

# What is a Time Series (TS)?

- Sequence of observations on a variable collected over time
  - ▣ Ex: stock prices, interest rate, retail sales, electric power consumption
- Mathematical representation
  - ▣ TS is defined by the values  $Y_1, Y_2, \dots$  of a variable  $Y$  at times  $t_1, t_2, \dots$  Thus,

$$Y = F(t)$$

# Causes of Variation in TS data

- **Calendar:** seasons, holidays, weekends
- **Example**

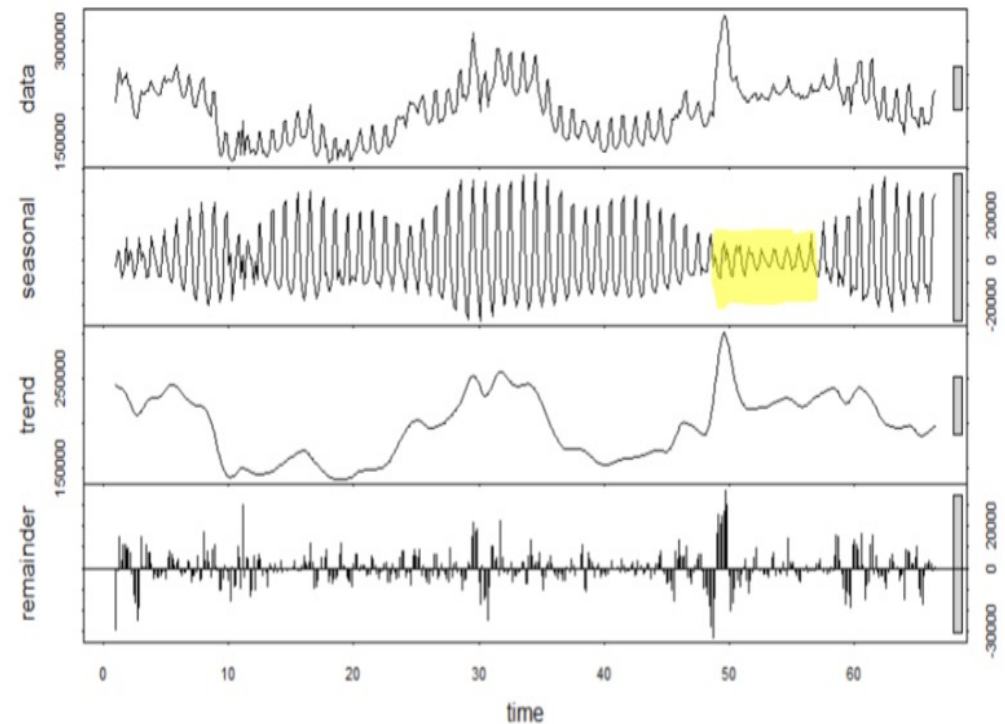
## Interest

- Trend of usage over time
- Popularity of games
- Weekly cycle of usage

## Knowledge

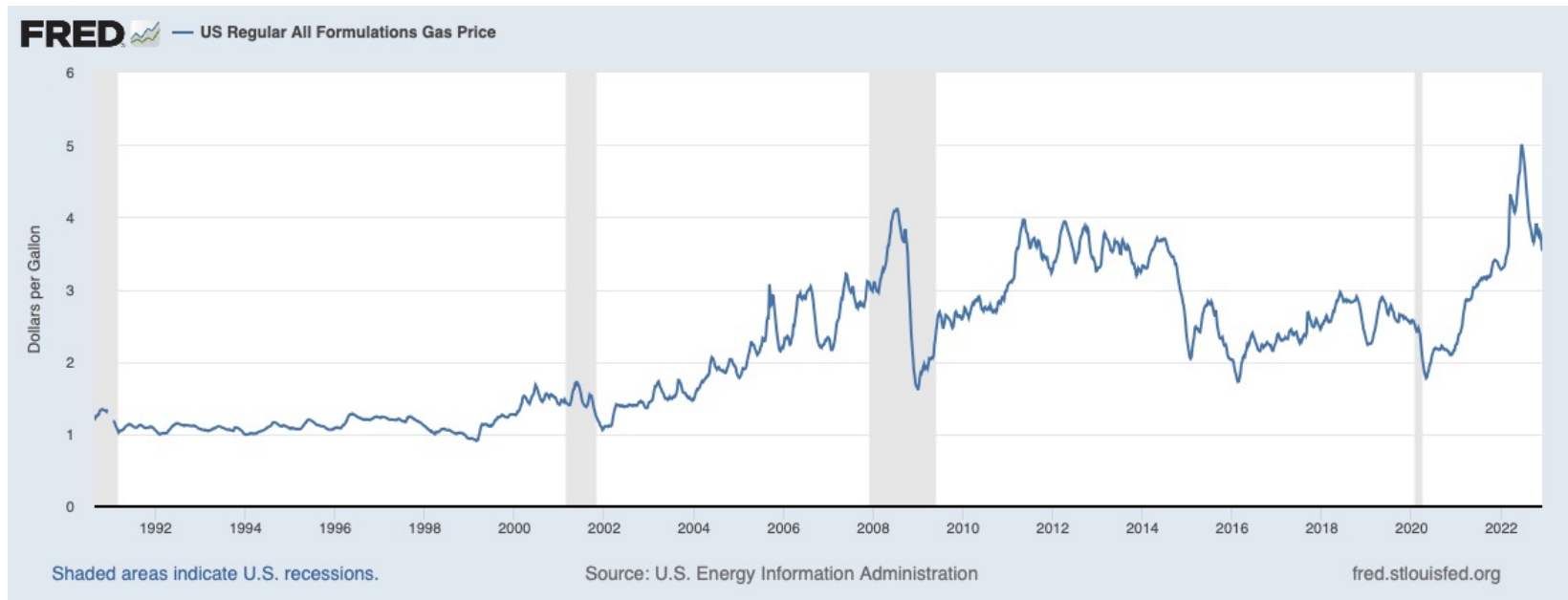
- Usage up on the weekend and down during the week
- Increased usage during holidays
- Summer time: weekdays/weekends blend together

**Video game usage over time – daily basis**



# Causes of Variation in TS data

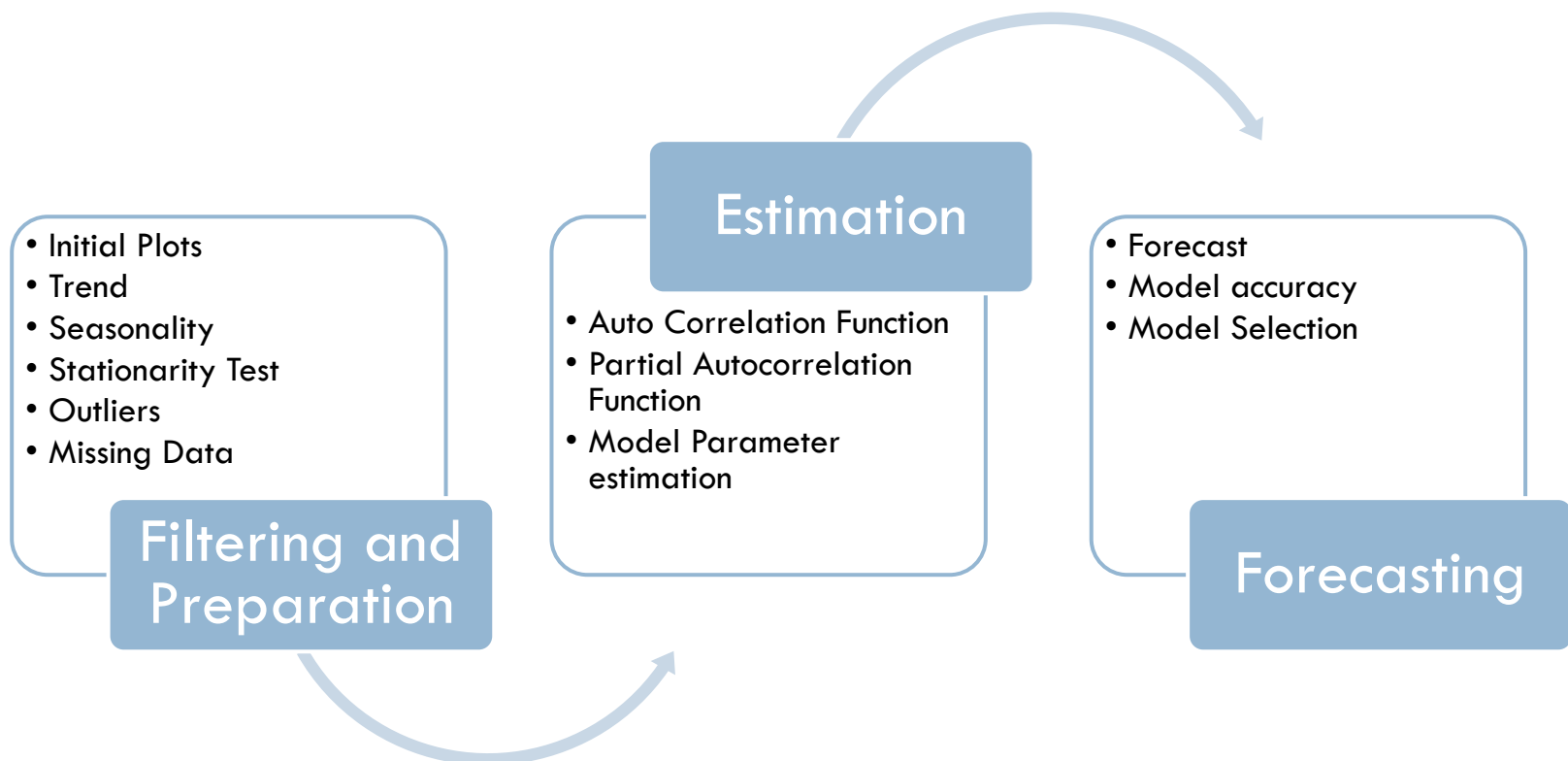
- **Natural calamities:** earthquake, epidemic, flood, drought
- **Human:** Political movements or changes, policies, war
- **Example**



Source: <https://fred.stlouisfed.org/series/GASREGW#>

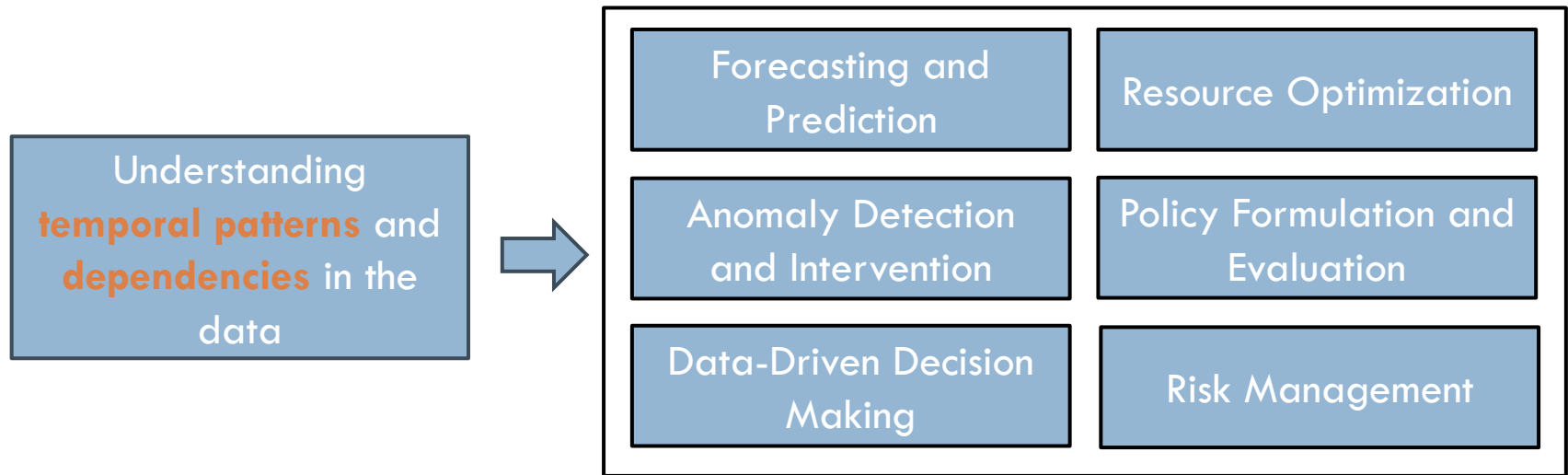
# What is Time Series Analysis (TSA)?

- In TSA, we analyze the past behavior of a variable in order to predict its future behavior





# Why Learn Time Series Analysis?



- ❑ Critical skill in today's **data-driven world**
- ❑ Widely applicable across various industries and domains

# Examples of Time Series Models

- Autoregressive Integrated Moving Average (ARIMA)
  - ▣ combines three components: autoregression (AR), differencing (I), and moving average (MA)
- Seasonal Autoregressive Integrated Moving Average (SARIMA)
  - ▣ extension of ARIMA that incorporates seasonal components
- Exponential Smoothing Models: Exponential
  - ▣ Simple Exponential Smoothing (SES), Holt's Linear Exponential Smoothing, and Holt-Winters' Seasonal Exponential Smoothing
- Seasonal Decomposition of Time Series (STL): STL is a method that decomposes a time series into seasonal, trend, and residual components

# TSA Applications to Energy

- **Energy demand** forecasting for resource planning, load balancing, and infrastructure development
- **Renewable energy** forecasting to facilitate solar and wind power grid integration
- Forecasting **energy prices** to inform trading strategies and risk management
- **Energy storage** optimal sizing and dispatch strategies for energy storage systems
- Identifying **abnormal energy consumption or production** patterns that may indicate equipment malfunction or faults
- **Load profiling** for dynamic pricing structures and personalized tariffs/rates to incentivize energy efficiency



# Time Series Decomposition

Trend Component

Seasonal Component

# Time Series Components

- A time series may have the following components:

Trend  
Component

Seasonal  
Component

**Decomposing the Time Series means separating trend/cycle, seasonal and random components.**

Cyclical  
Component

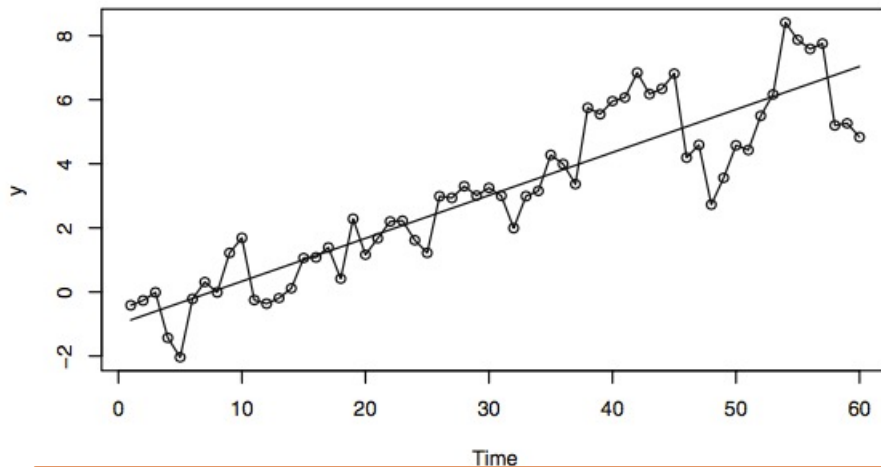
Random  
Component

**TSA will find and exploit predictable patterns/components.**

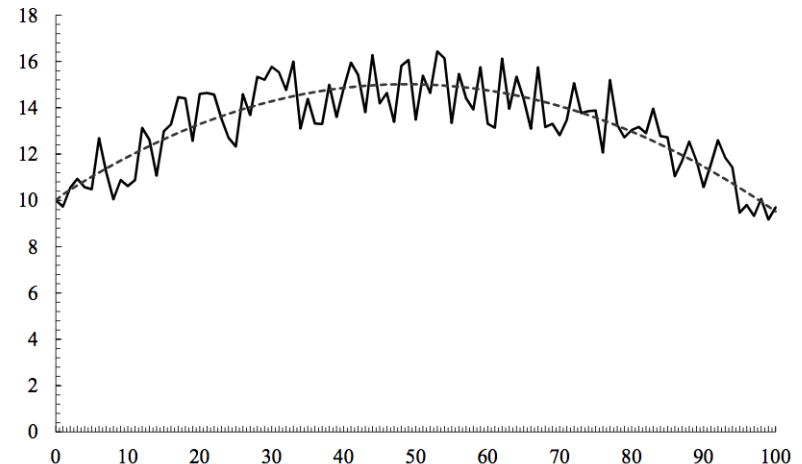
# Trend Component

- Long-term tendency
  - ▣ Increase (upward movement) or
  - ▣ Decrease (downward movement)
- Trend can be linear or non-linear

Ex: Upward Linear Trend



Ex: Quadratic Trend



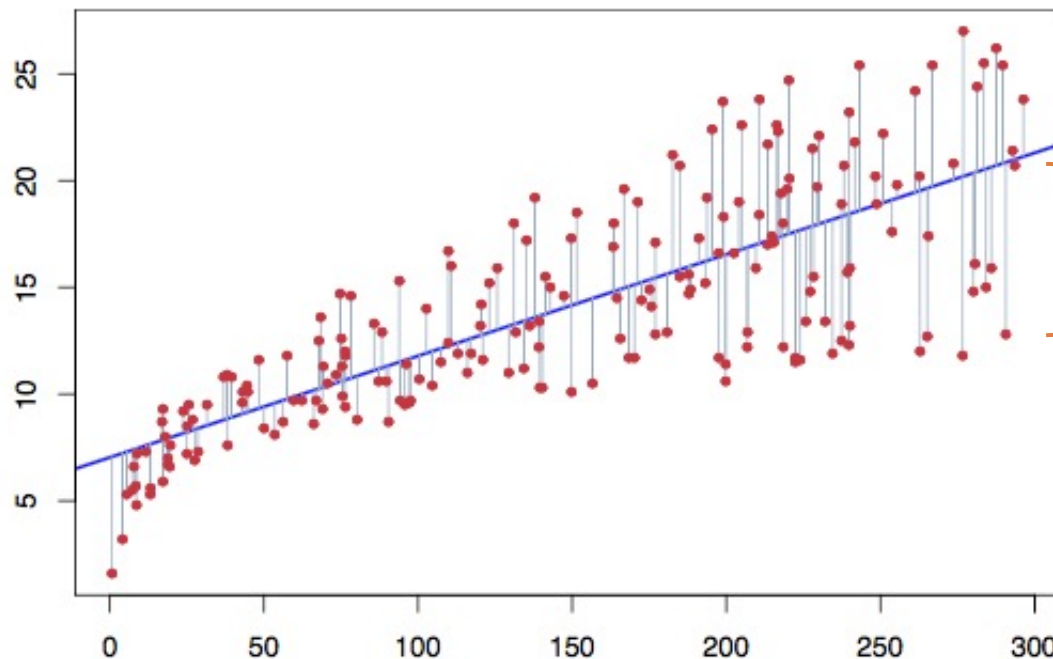
**Most of the time we assume a rolling average to simplify the analysis**

# Linear Trend Component

- For a linear trend we can write

$$Y_i = \beta_0 + \beta_1 t_i + \varepsilon_i$$

- **Slope** ( $\beta_1$ ) and the **intercept** ( $\beta_0$ ) are the unknown parameters, and  $\varepsilon_i$  is the **error term**



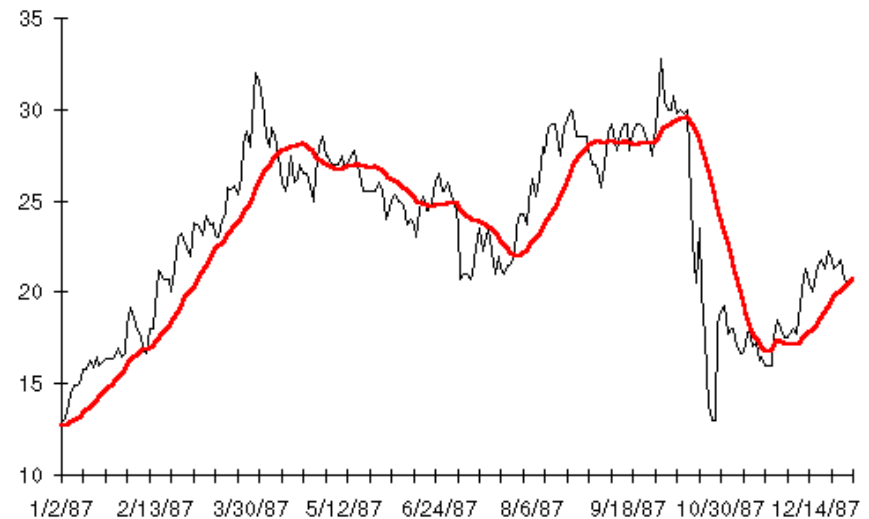
$$\hat{Y}_i = \beta_0 + \beta_1 t_i$$

The error term or residual  
is the distance from point  
 $Y_i$  to the estimate  $\hat{Y}_i$

$$\varepsilon_i = Y_i - \hat{Y}_i$$

# Non-Linear Trend Estimation: Moving Average

- Smooth out the trend with something like a rolling average
  - ▣ A moving average trendline smooth out fluctuations in data to show a pattern or trend more clearly
  - ▣ Which order to use for the moving average?
- Looking at the rolling average makes it easier to tell how the trend is moving underneath the noise

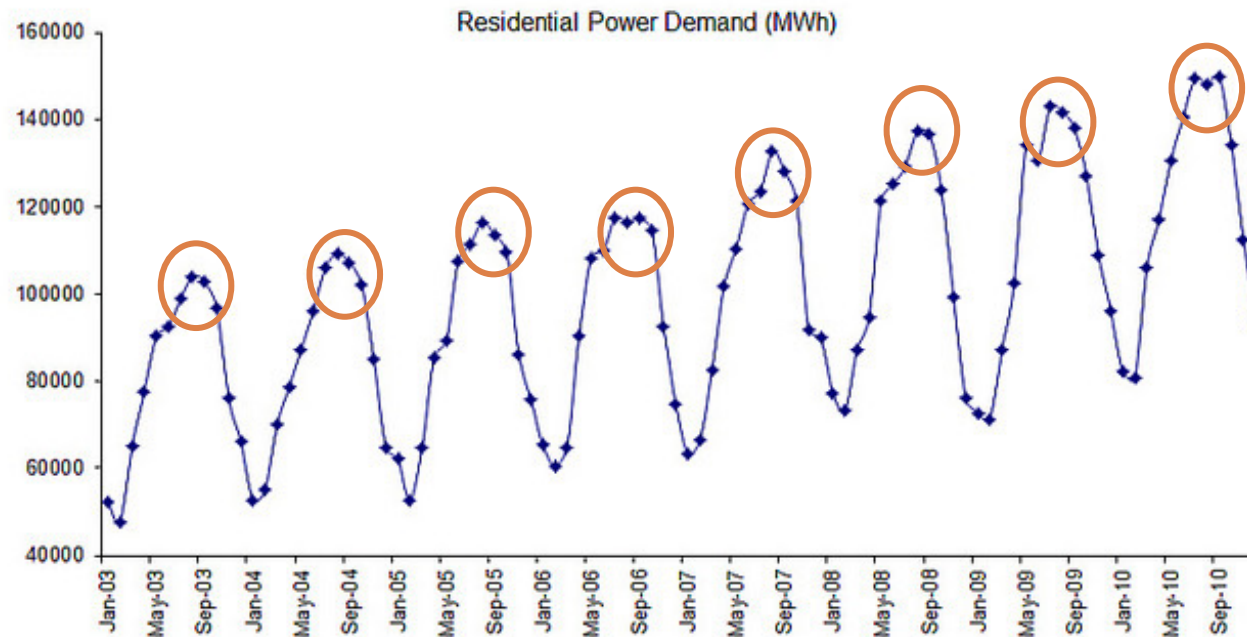




# Seasonal Component

- Short-term regular wave-like patterns
  - ▣ Observed within 1 year - monthly or quarterly
  - ▣ Equally spaced peaks and troughs

**Calendar  
Related**



**Peaks in the  
Summer months  
Jun/Jul/Ago**

# Decomposition: Trend Component

## 1. Smooth the trend with a moving average

- Find  $Y_{trend}$

## 2. De-trend the series

### ■ Additive Model

- take original series and **subtract** the smoothed trend

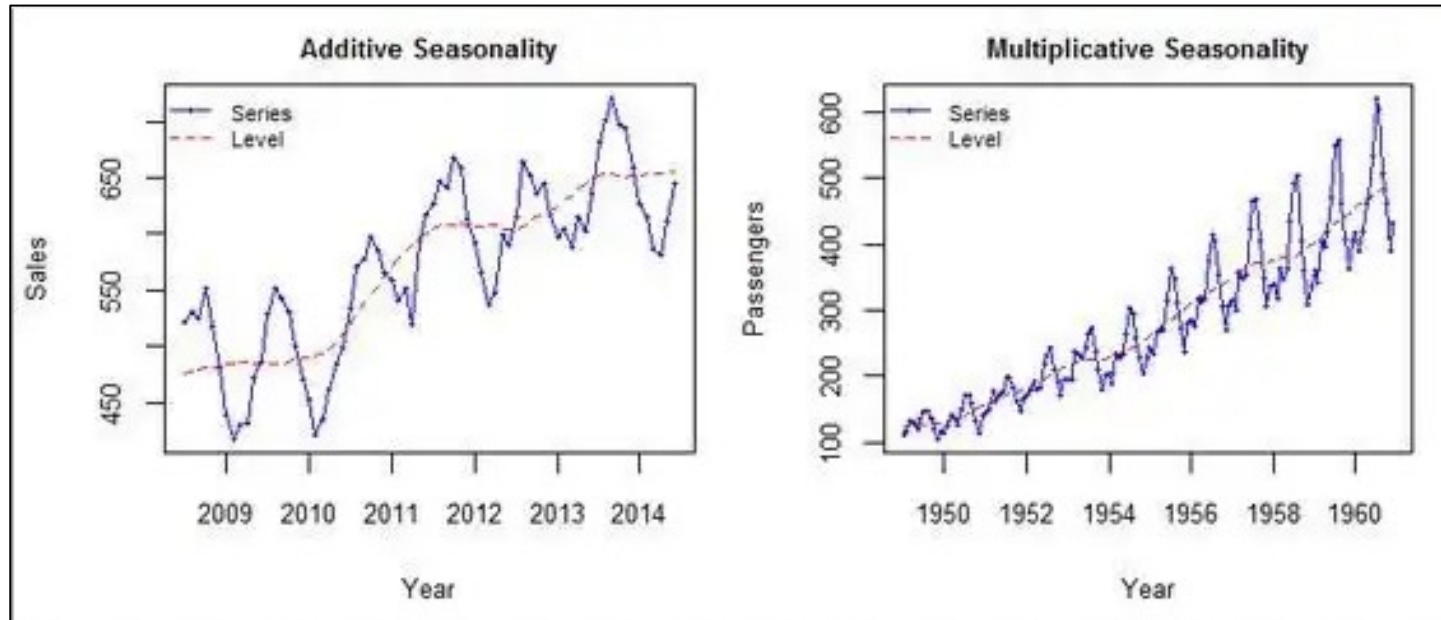
$$Y_{seasonal} = Y - Y_{trend}$$

### ■ Multiplicative model

- scales the size of the seasonal component as the trend rises or falls
- take original series and **divide** the original data by the trend

$$Y_{seasonal} = \frac{Y}{Y_{trend}}$$

# Additive vs Multiplicative Model



- In the **additive model** the magnitude of seasonality does not change in relation to time
- In the **multiplicative model** the magnitude of the seasonal pattern depends on the magnitude/level of the data.

# Decomposition: Seasonal Component

3. Assume the observed detrended series can be **represented** as

$$Y_{seasonal_t} = \sum_{s=1}^{12} \beta_s D_{s,t} + \epsilon_t \quad \text{where } E[\epsilon_t] = 0$$

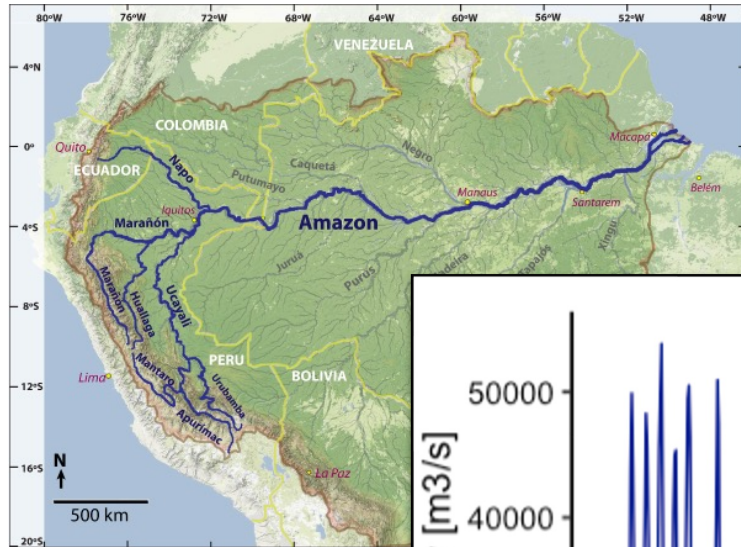
$$D_{s,t} = \begin{cases} 1 & \text{if } t \text{ belongs to season } s \\ 0 & \text{o.w.} \end{cases} \quad \text{for } s = 1, 2, \dots, 12$$

4. **Estimate** the parameters  $\beta_1, \beta_2, \dots, \beta_{12}$  by regression

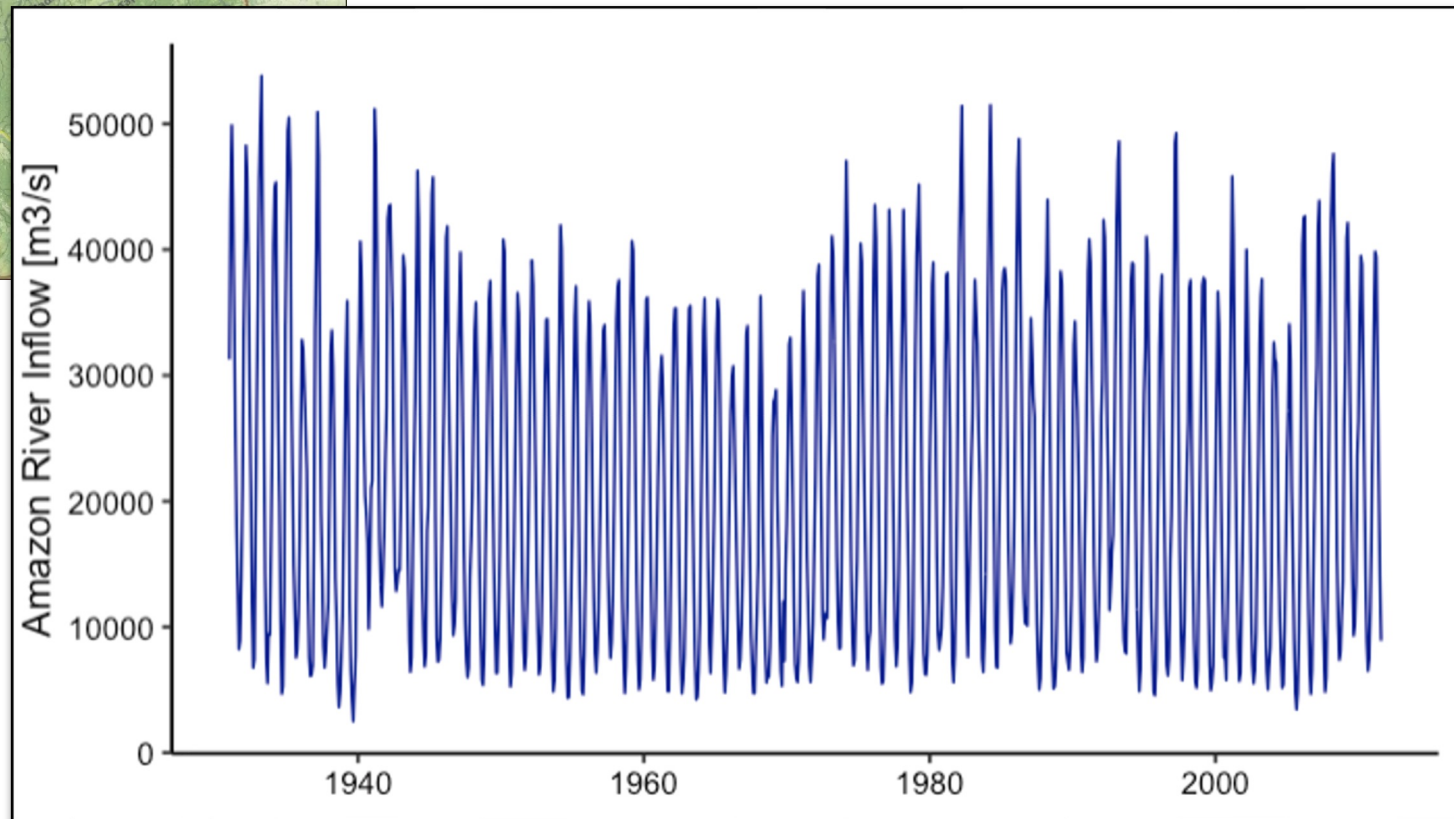


# Example: Inflow Data

# Amazon River Inflow in $\text{m}^3/\text{s}$

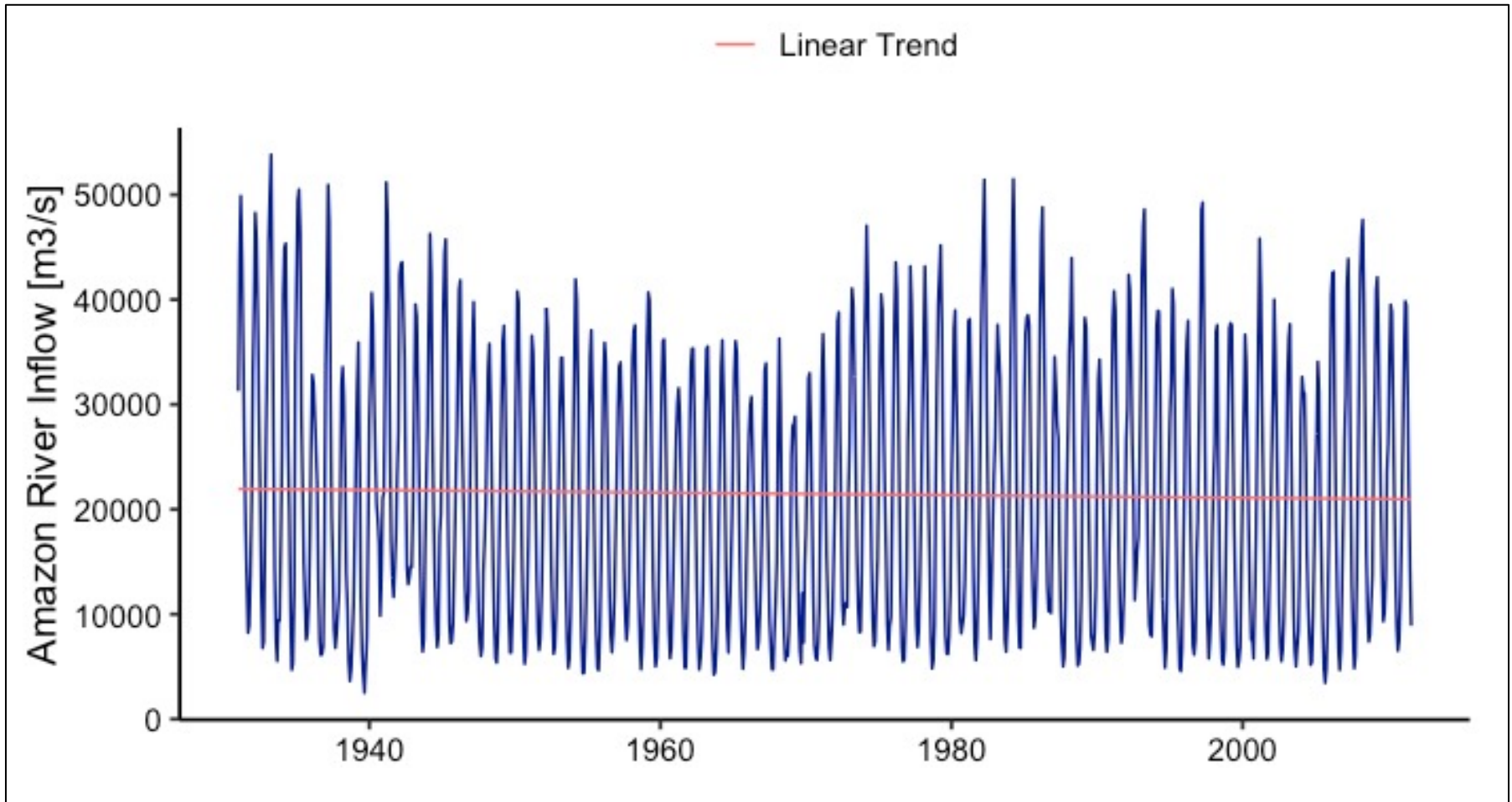


Which components/patterns can you see in this series?



# Linear Trend visualization

$$Y_{trend_t} = \beta_0 + \beta_1 t$$



# Linear Trend regression results

$$Y_{trend_t} = \beta_0 + \beta_1 t$$

Call:

```
lm(formula = inflow ~ t, data = data)
```

Residuals:

Min	1Q	Median	3Q	Max
-19337	-11555	-1483	10061	31900

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	21949.403	797.962	27.507	<2e-16 ***
t	-1.024	1.427	-0.718	0.473

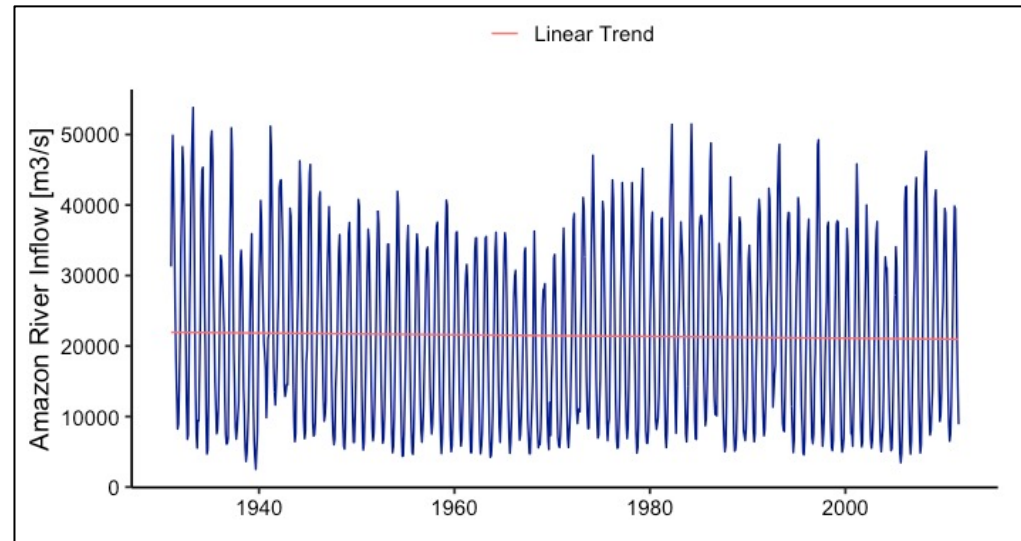
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Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 12400 on 966 degrees of freedom

Multiple R-squared: 0.0005328, Adjusted R-squared: -0.0005018

F-statistic: 0.515 on 1 and 966 DF, p-value: 0.4732

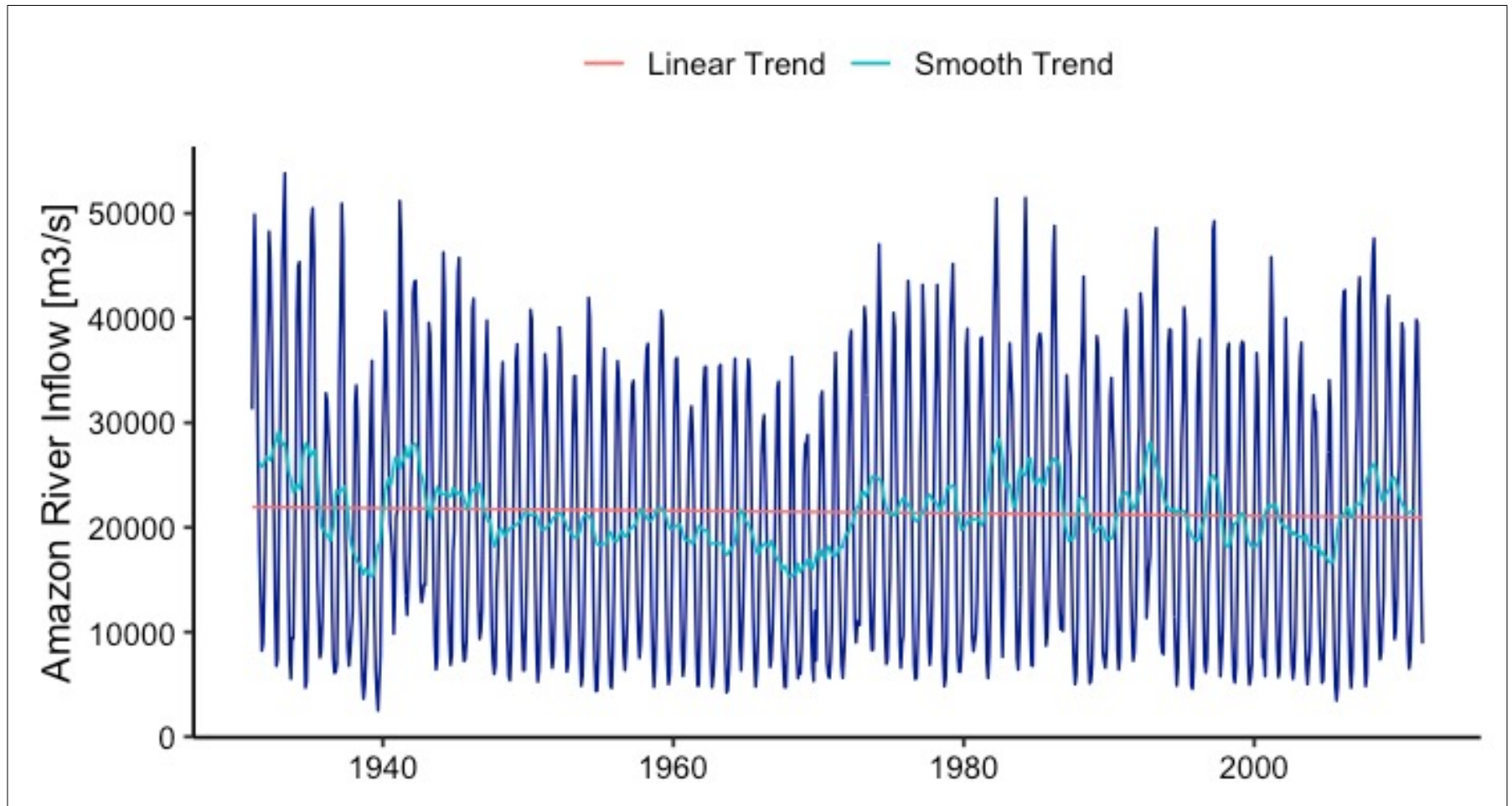


**p-value > 0.05**  
**Coefficient  $\beta_1$  not significant**



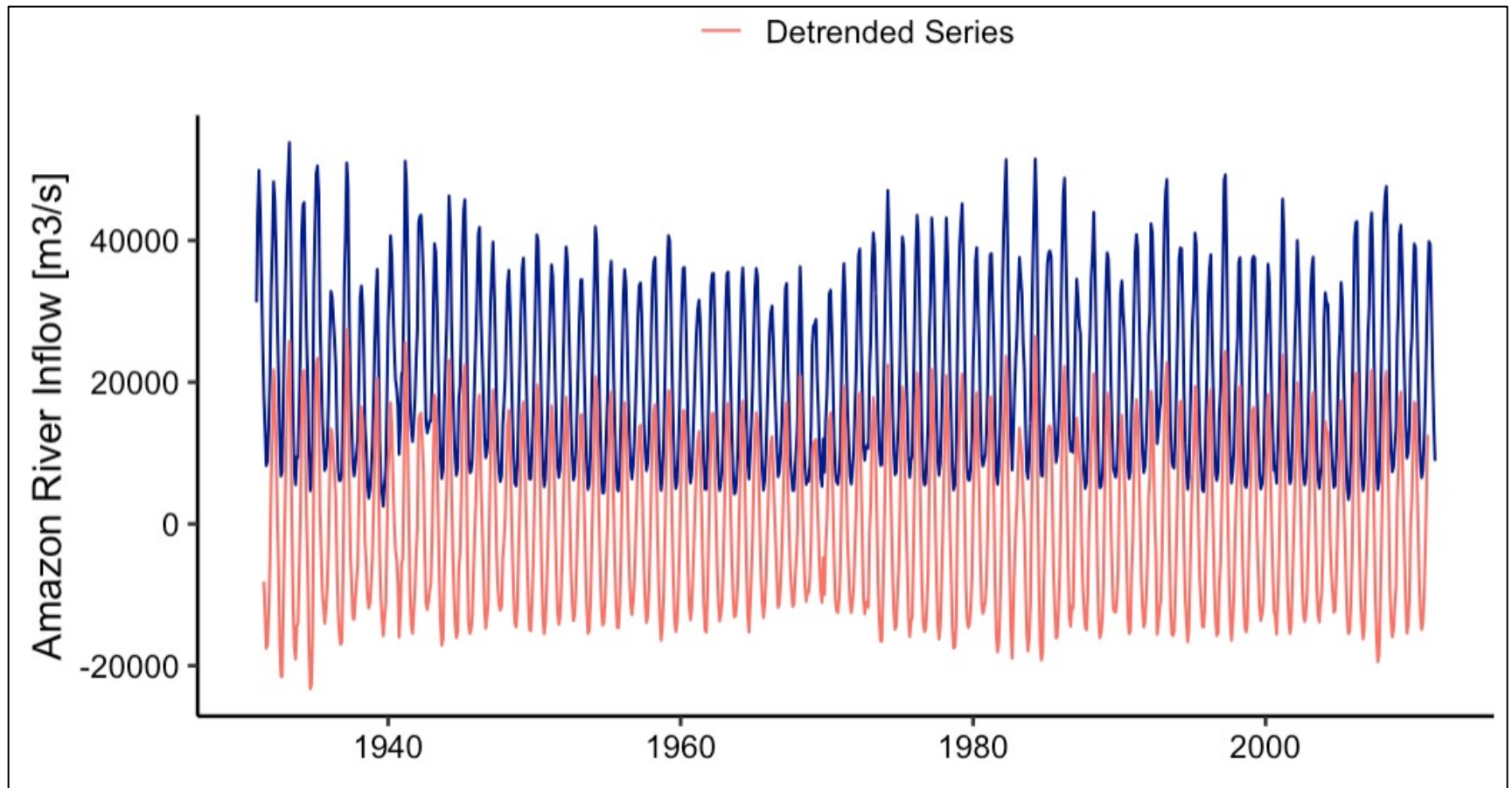
# Smooth Trend: MA(6)

$$Y_{trend_t} = average(Y_{t-6} + Y_{t-5} + \dots + Y_t + \dots + Y_{t+5} + Y_{t+6})$$

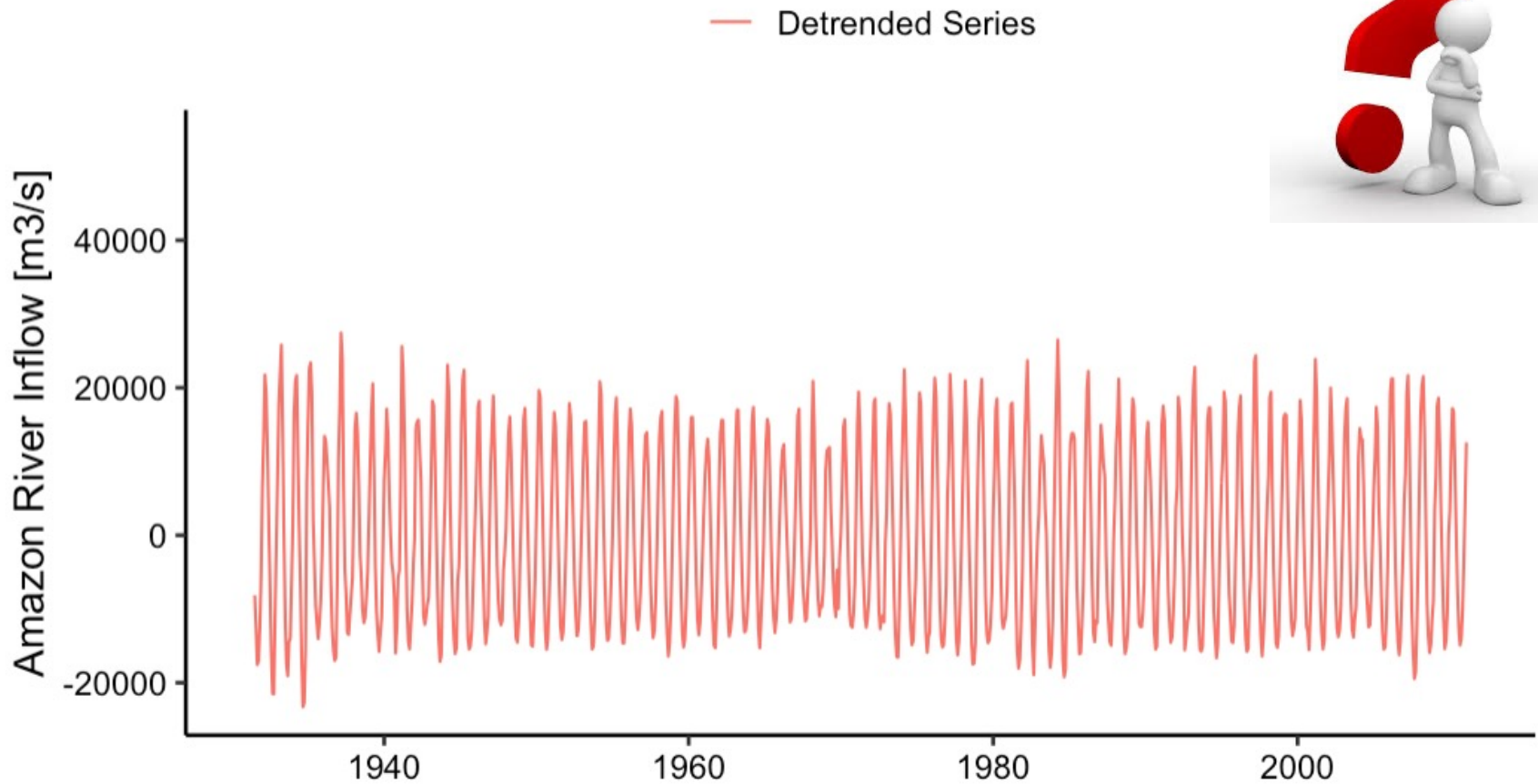


# Detrended Series with Additive Model

$$Y_{detrend_t} = Y_t - Y_{trend_t}$$



# Do you still see any patterns?



# Seasonal Component Regression Results

$$Y_{\text{seasonal}_t} = \sum_{s=1}^{12} \beta_s D_{s,t} + \epsilon_t$$

Call:

```
lm(formula = detrend_smooth ~ dummies)
```

Residuals:

Min	1Q	Median	3Q	Max
-9430	-1552	-50	1654	10797

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	-3545.7	307.4	-11.533	<2e-16 ***
dummiesJan	8131.5	434.8	18.702	<2e-16 ***
dummiesFeb	15948.6	434.8	36.682	<2e-16 ***
dummiesMar	21556.7	436.2	49.424	<2e-16 ***
dummiesApr	20984.3	436.2	48.112	<2e-16 ***
dummiesMay	12870.3	436.2	29.508	<2e-16 ***
dummiesJun	3959.1	436.2	9.077	<2e-16 ***
dummiesJul	-3731.7	434.8	-8.583	<2e-16 ***
dummiesAug	-8994.6	434.8	-20.688	<2e-16 ***
dummiesSep	-11306.9	434.8	-26.006	<2e-16 ***
dummiesOct	-10378.9	434.8	-23.872	<2e-16 ***
dummiesNov	-6515.4	434.8	-14.986	<2e-16 ***

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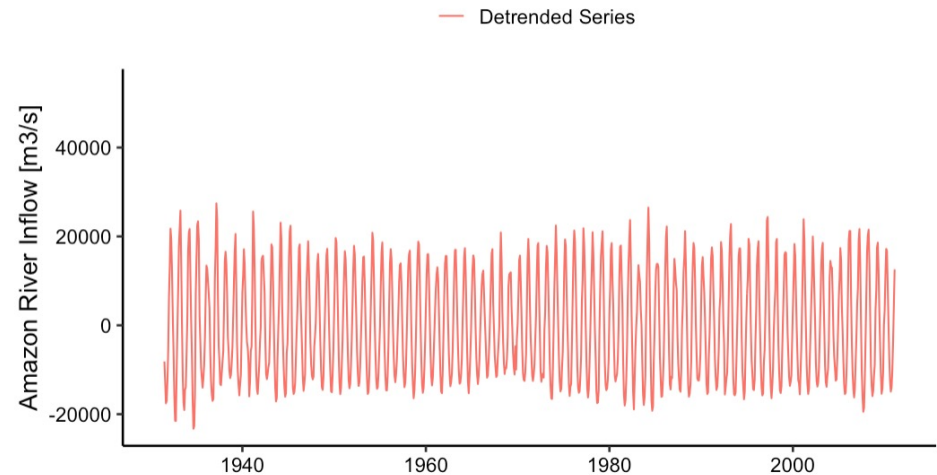
Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 2750 on 944 degrees of freedom

(12 observations deleted due to missingness)

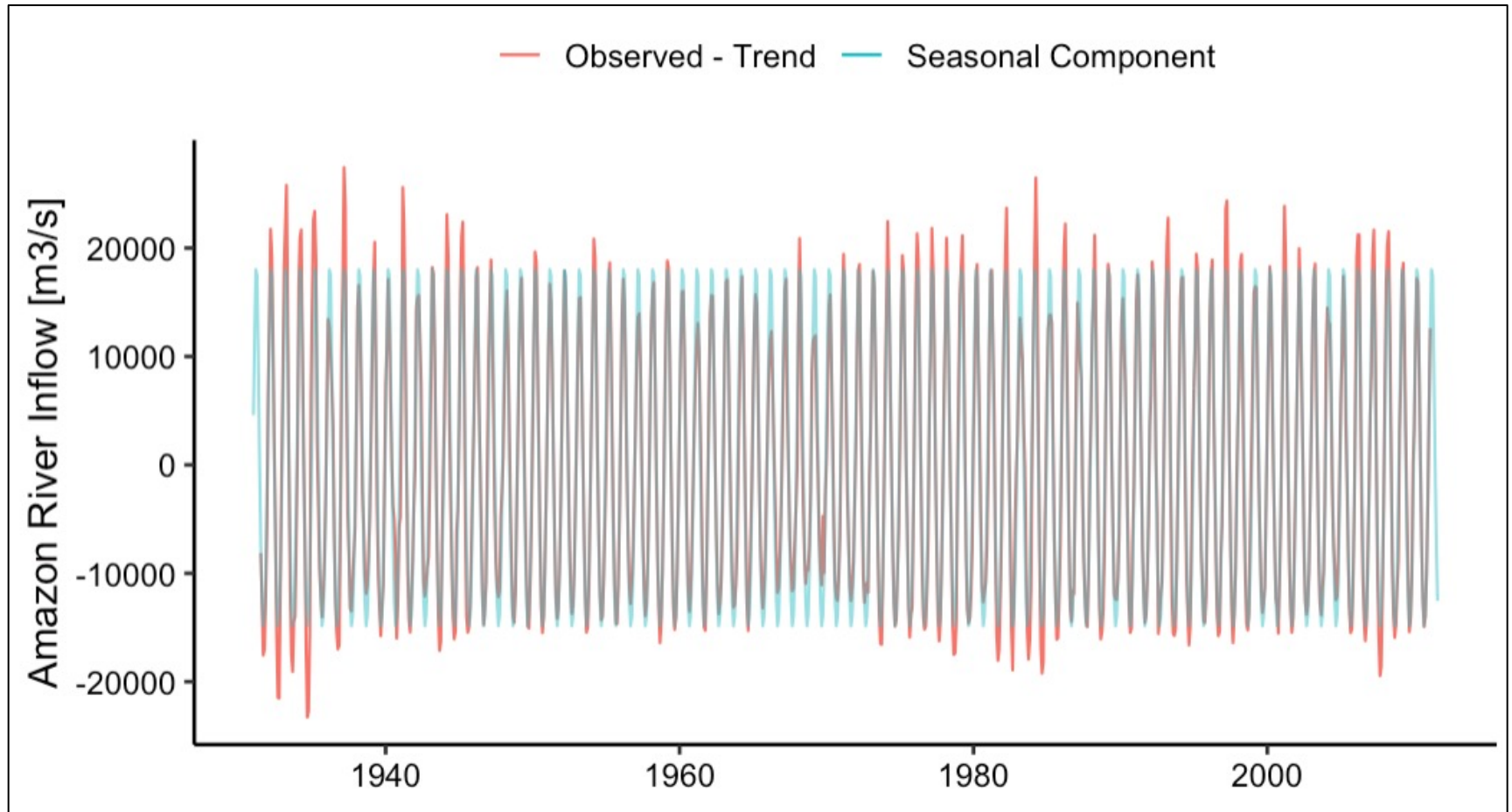
Multiple R-squared: 0.9478, Adjusted R-squared: 0.9472

F-statistic: 1558 on 11 and 944 DF, p-value: < 2.2e-16

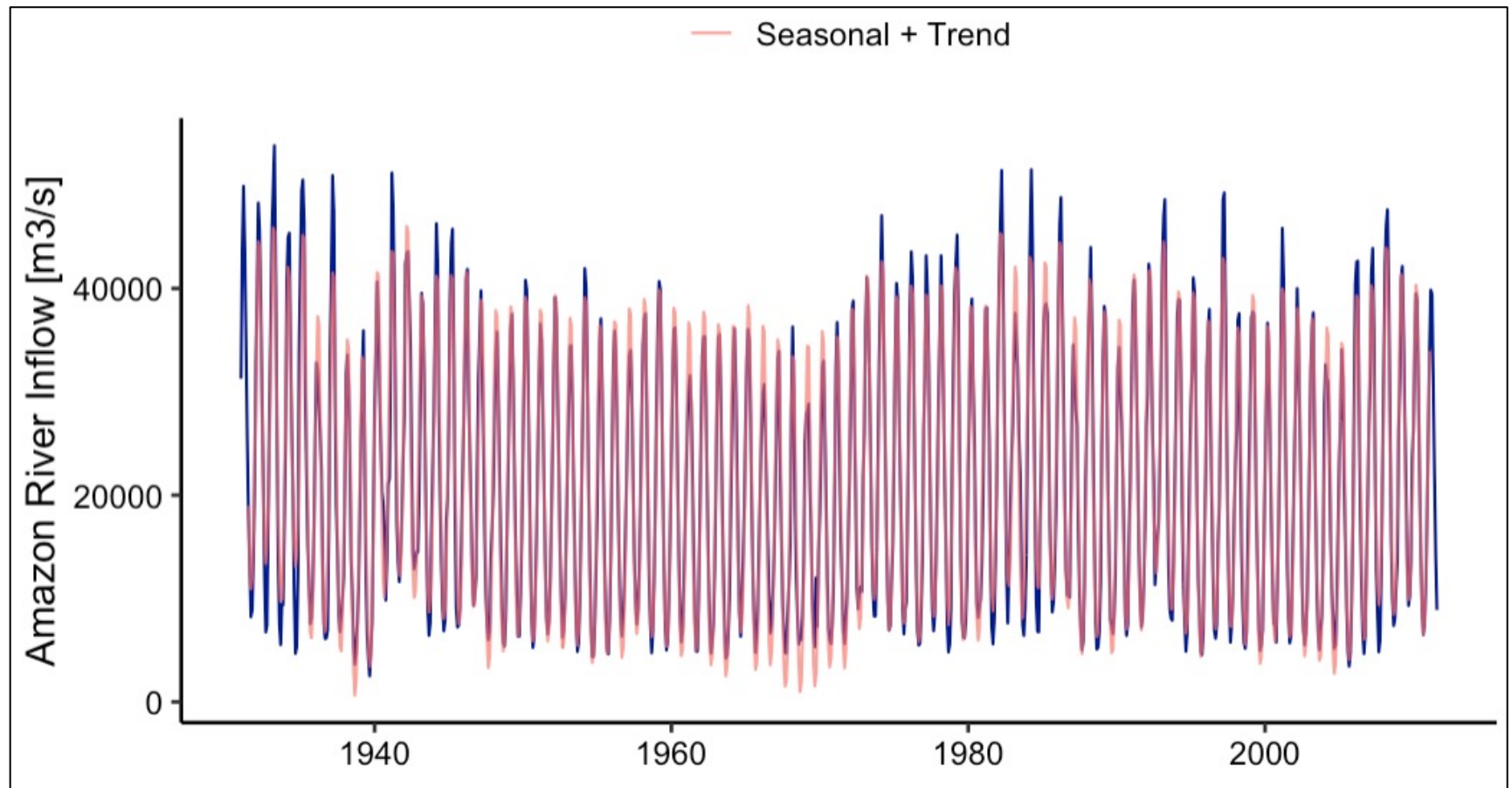


**Seasonality explains most of the variability**

# Seasonal Component Visualization



# Seasonal + Trend Model of Inflow

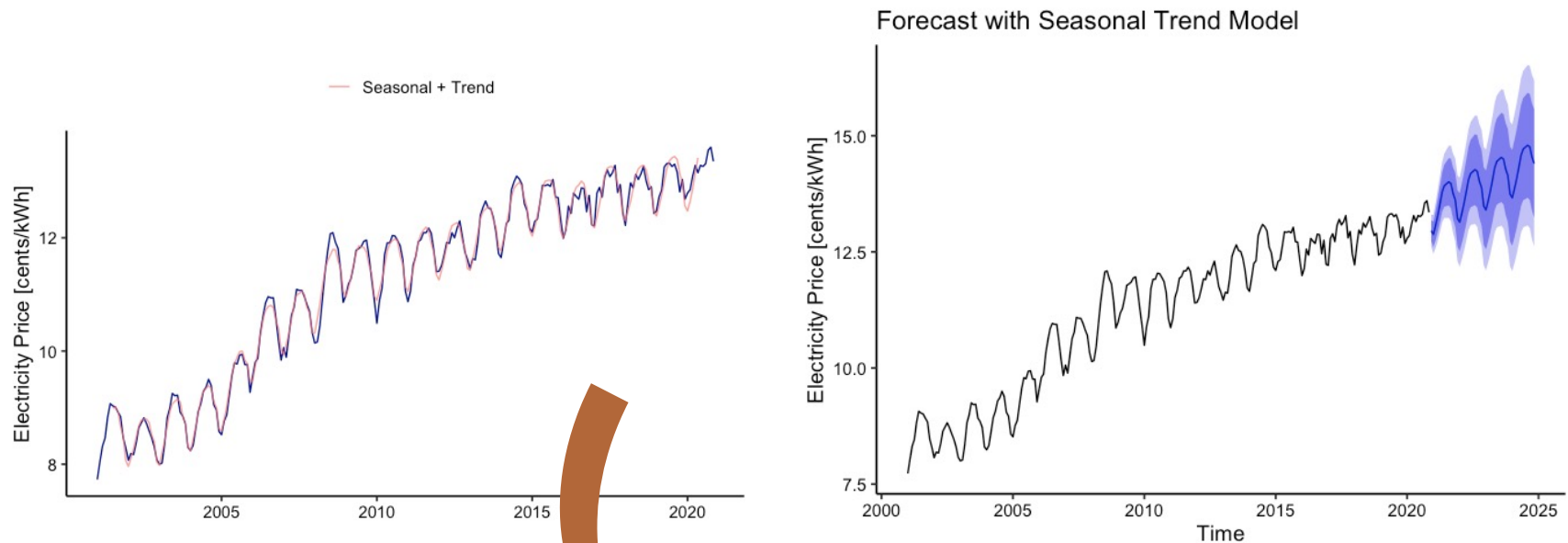


Recall dark blue line represents observed data



# More Examples

## □ Electricity Price – STL model



Please visit: [https://github.com/ENV790/TSA\\_Intro\\_EDAL](https://github.com/ENV790/TSA_Intro_EDAL)



# Forecasting and Model Selection



# Time Series Forecasting

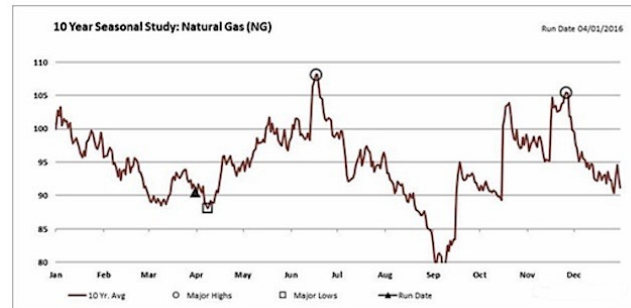
- **Forecast/Projection** ➡ statement about the future value/probability distribution of a variable of interest
  - ▣ Forecasts are often used for weather, demand, and resource availability
  - ▣ Important element in making informed decisions
  - ▣ uses past values of a time series to estimate future values of the same time series



# Two Important Aspects of Forecasts

## □ Expected **level**

- Ex: the level of demand may be a function of some structural variation such as trend or seasonal variation



## □ **Accuracy**

- Related to the potential size of forecast error



Calculating Forecast Error



# Features Common to All Forecasts

- Techniques assume some underlying **causal system that existed in the past will persist into the future**
- Forecasts are **not perfect**
  - ▣ Probability density function: provide an indication of the extent to which the forecast might deviate from the forecasted value
- Forecasts for **groups of items are more accurate** than those for individual items
- Forecast **accuracy decreases as the forecasting horizon increases**



# Model Selection



***“Unsolved” problem in statistics: there are no magic procedures to get you the “best model” (Kadane and Lazar)***

- With a limited number of predictors, it is possible to search all possible models
- But when we have many predictors, it can be difficult to find “best” model (many possibilities)
- How do we select models?
  - ▣ We need a criteria or benchmark to compare two models
  - ▣ We need a search strategy

# Model Selection

Which models best explain the observed data?

- Backward-looking assessment
  - **Residual Analysis:** describes the difference between actual historical data and the fitted values generated by a statistical model
  - **Akaike Information Criterion (AIC):** balance goodness of fit and the simplicity of the model

Which models give the best predictions of future observations?

- Forward-looking assessment
  - **Forecast accuracy** is an important forecasting technique selection criterion
$$\text{Error} = \text{Actual} - \text{Forecast}$$

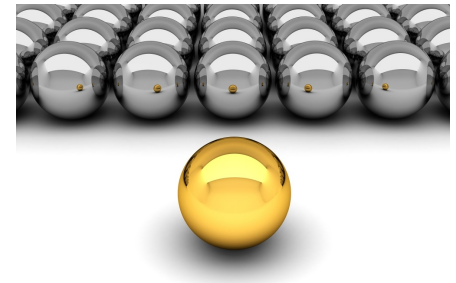
Observed value
  - **Root Mean Squared Error (RMSE)**
  - **Mean Absolute Percentage Error (MAPE)**
  - Need to hold-out some observed data to test forecast accuracy



**Always combine metrics!**

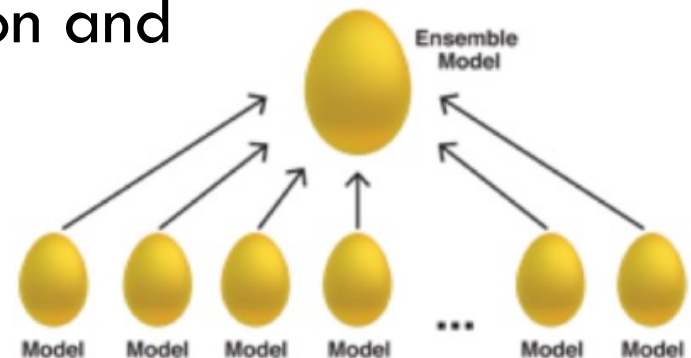
# How to choose the best model?

- Build a set of candidate models and use **model selection/performance criteria** to pick one



- To improve forecasting accuracy, **combine forecasts** derived from models that differ in construction and predictor variables

**ENSEMBLE**



# Additional Resources

- Time Series Analysis for Energy and Environment Applications
  - ▣ Spring 2023 Course website: <https://env790.github.io>
- Environmental Data Analytics
  - ▣ Spring 2023 Course website: <https://env872.github.io>



# THANK YOU !

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