ENV 790.30 - Time Series Analysis for Energy Data | Spring 2024 Assignment 3 - Due date 02/01/24

Cara Kuuskvere

Directions

You should open the .rmd file corresponding to this assignment on RStudio. The file is available on our class repository on Github.

Once you have the file open on your local machine the first thing you will do is rename the file such that it includes your first and last name (e.g., "LuanaLima_TSA_A02_Sp24.Rmd"). Then change "Student Name" on line 4 with your name.

Then you will start working through the assignment by **creating code and output** that answer each question. Be sure to use this assignment document. Your report should contain the answer to each question and any plots/tables you obtained (when applicable).

Please keep this R code chunk options for the report. It is easier for us to grade when we can see code and output together. And the tidy.opts will make sure that line breaks on your code chunks are automatically added for better visualization.

When you have completed the assignment, **Knit** the text and code into a single PDF file. Submit this pdf using Sakai.

Questions

Consider the same data you used for A2 from the spreadsheet "Table_10.1_Renewable_Energy_Production_and_Consumpt The data comes from the US Energy Information and Administration and corresponds to the December 2022 Monthly Energy Review. Once again you will work only with the following columns: Total Biomass Energy Production, Total Renewable Energy Production, Hydroelectric Power Consumption. Create a data frame structure with these three time series only.

R packages needed for this assignment: "forecast", "tseries", and "Kendall". Install these packages, if you haven't done yet. Do not forget to load them before running your script, since they are NOT default packages.\

```
#Load/install required package here
library(forecast)

## Registered S3 method overwritten by 'quantmod':
## method from
## as.zoo.data.frame zoo

library(tseries)
library(Kendall)
library(readr)
library(ggplot2)
library(cowplot)
```

```
#Importing data set
raw_energy_data <- read.csv(</pre>
  "Data/Table_10.1_Renewable_Energy_Production_and_Consumption_by_Source.csv",
  header=FALSE, skip=12)
#trim the table
energy_data <- raw_energy_data[,4:6] #want all rows</pre>
                                   #all columns from 4 to 6
n_energy_sources <- ncol(energy_data) #number of variables</pre>
n_obs <- nrow(energy_data) #number observations</pre>
#Adding column names
colnames(energy_data)=c("Total Biomass Energy Production (Trillion Btu)",
                             "Total Renewable Energy Production (Trillion Btu)",
                             "Hydroelectric Power Consumption (Trillion Btu)")
head(energy_data)
     Total Biomass Energy Production (Trillion Btu)
## 1
                                              129.824
## 2
                                              130.807
## 3
                                              118.091
## 4
                                              130.727
## 5
                                              126.583
## 6
                                              130.789
     Total Renewable Energy Production (Trillion Btu)
## 1
                                                220.755
## 2
                                                231.010
## 3
                                                210.188
## 4
                                                226.384
## 5
                                                223.218
## 6
                                                227.793
     Hydroelectric Power Consumption (Trillion Btu)
## 1
                                               90.131
## 2
                                               99.500
## 3
                                               91.476
## 4
                                               94.950
## 5
                                               95.969
## 6
                                               96.337
ts_energy_data <- ts(energy_data, start=c(1973,1), frequency = 12)
# frequency is 12 because it's monthly data, and months repeat every 12 entries!
# starts in year 1973
head(ts_energy_data)
            Total Biomass Energy Production (Trillion Btu)
## Jan 1973
                                                      129.824
## Feb 1973
                                                      130.807
## Mar 1973
                                                      118.091
## Apr 1973
                                                      130.727
## May 1973
                                                      126.583
## Jun 1973
                                                      130.789
```

```
Total Renewable Energy Production (Trillion Btu)
## Jan 1973
                                                       220.755
## Feb 1973
                                                       231.010
## Mar 1973
                                                       210.188
## Apr 1973
                                                       226.384
## May 1973
                                                       223.218
## Jun 1973
                                                       227.793
##
            Hydroelectric Power Consumption (Trillion Btu)
## Jan 1973
                                                      90.131
## Feb 1973
                                                      99.500
## Mar 1973
                                                      91.476
## Apr 1973
                                                      94.950
## May 1973
                                                      95.969
## Jun 1973
                                                      96.337
```

##Trend Component

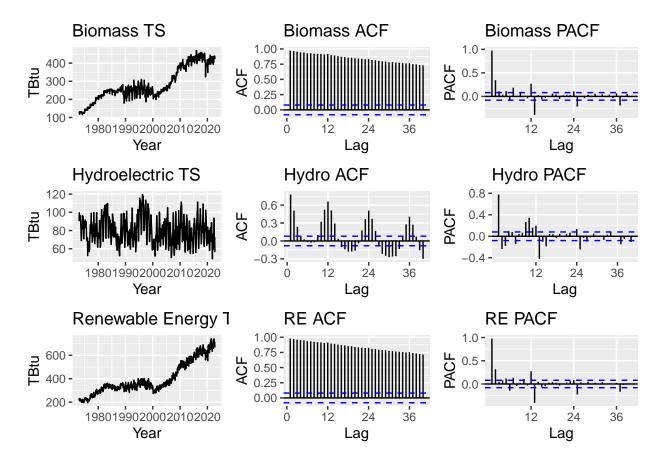
$\mathbf{Q}\mathbf{1}$

For each time series, i.e., Renewable Energy Production and Hydroelectric Consumption create three plots: one with time series, one with the ACF and with the PACF. You may use the some code form A2, but I want all the three plots side by side as in a grid. (Hint: use function plot_grid() from the cowplot package)

```
biomass_acf <- ggAcf(ts_energy_data[,1],lag.max=40)+
   labs(title="Biomass ACF")
#biomass_acf
hydro_acf <- ggAcf(ts_energy_data[,3],lag.max=40)+
   labs(title="Hydro ACF")
#hydro_acf
RE_acf <- ggAcf(ts_energy_data[,2],lag.max=40)+
   labs(title="RE ACF")
#RE_acf</pre>
```

```
biomass_pacf <- ggPacf(ts_energy_data[,1],lag.max=40)+
   labs(title="Biomass PACF")
#biomass_pacf
hydro_pacf <- ggPacf(ts_energy_data[,3],lag.max=40)+</pre>
```

```
labs(title="Hydro PACF")
#hydro_pacf
RE_pacf <- ggPacf(ts_energy_data[,2],lag.max=40)+
labs(title="RE PACF")
#RE_pacf</pre>
```



 $\mathbf{Q2}$

From the plot in Q1, do the series Total Biomass Energy Production, Total Renewable Energy Production, Hydroelectric Power Consumption appear to have a trend? If yes, what kind of trend?

Biomass and renewable energy production appear to have an increasing somewhat linear trend over time. The hydroelectric power consumption appears to have a strong seasonal component, which makes it hard to see if there is a small trend component.

$\mathbf{Q3}$

Use the lm() function to fit a linear trend to the three time series. Ask R to print the summary of the regression. Interpret the regression output, i.e., slope and intercept. Save the regression coefficients for further analysis.

```
t <- 1:n obs
biomass_linear_trend <- lm(energy_data[,1]~t)</pre>
RE_linear_trend <- lm(energy_data[,2]~t)</pre>
hydro_linear_trend <- lm(energy_data[,3]~t)
summary(biomass_linear_trend)
##
## Call:
## lm(formula = energy_data[, 1] ~ t)
##
## Residuals:
##
        Min
                  1Q
                       Median
                                     3Q
                                             Max
## -102.453 -24.240
                        6.106
                                32.219
                                          83.377
##
## Coefficients:
##
                Estimate Std. Error t value Pr(>|t|)
                            3.24250
                                       43.26
## (Intercept) 140.26864
                                               <2e-16 ***
## t
                 0.47527
                            0.00938
                                      50.67
                                               <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 39.6 on 596 degrees of freedom
## Multiple R-squared: 0.8116, Adjusted R-squared: 0.8113
## F-statistic: 2567 on 1 and 596 DF, p-value: < 2.2e-16
summary(RE_linear_trend)
##
## Call:
## lm(formula = energy_data[, 2] ~ t)
## Residuals:
##
       Min
                1Q
                   Median
                                3Q
                                       Max
## -148.05 -36.16
                     11.72
                             42.31
                                   143.58
##
## Coefficients:
##
                Estimate Std. Error t value Pr(>|t|)
## (Intercept) 187.25183
                            4.98485
                                      37.56
                                               <2e-16 ***
## t
                 0.70777
                            0.01442
                                      49.08
                                               <2e-16 ***
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
## Residual standard error: 60.87 on 596 degrees of freedom
## Multiple R-squared: 0.8017, Adjusted R-squared: 0.8013
## F-statistic: 2409 on 1 and 596 DF, p-value: < 2.2e-16
```

summary(hydro_linear_trend)

```
##
## Call:
## lm(formula = energy_data[, 3] ~ t)
##
## Residuals:
##
       Min
                10 Median
                                3Q
                                       Max
## -30.180 -10.665 -0.658
                             9.545
                                    39.409
##
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 83.02761
                           1.15464
                                     71.91 < 2e-16 ***
## t
               -0.01086
                           0.00334
                                     -3.25 0.00122 **
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
## Residual standard error: 14.1 on 596 degrees of freedom
## Multiple R-squared: 0.01741,
                                    Adjusted R-squared:
## F-statistic: 10.56 on 1 and 596 DF, p-value: 0.001219
```

The biomass linear trend has an intercept value of \sim 140 and a slope of .47, showing a positive linear trend with a strong correlation of a very small p-value.

The renewable energy linear trend has an intercept of ~ 187 and a slope of $\sim .7$, showing a positive linear trend with a strong correlation of a very small p-value.

The hydro linear trend has an intercept of ~ 83 with a very strong, small p value, but a small, weak, negative linear trend with slope -0.01 with a p value that is still less than 0.05. It also has a weaker r squared value than the other two trends.

$\mathbf{Q4}$

Use the regression coefficients from Q3 to detrend the series. Plot the detrended series and compare with the plots from Q1. What happened? Did anything change?

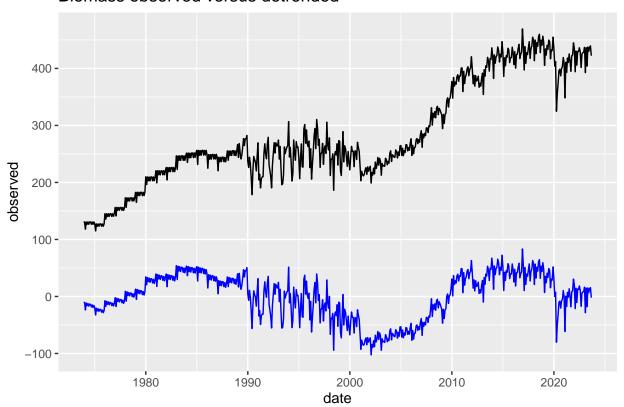
library(lubridate)

```
##
## Attaching package: 'lubridate'
## The following object is masked from 'package:cowplot':
##
## stamp

## The following objects are masked from 'package:base':
##
## date, intersect, setdiff, union

ym_date <- paste(raw_energy_data[,1])
ym_date <- ym(ym_date) #function my from package lubridate</pre>
```

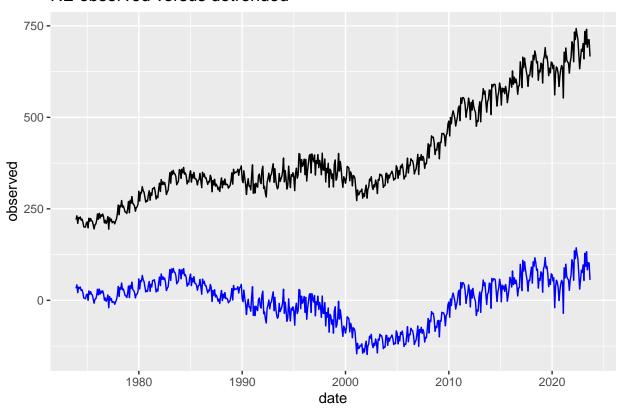
Biomass observed versus detrended



This plot shows the upward linear trend removed, as well as centered the mean around zero. It also shows a greater dip around the year 2000.

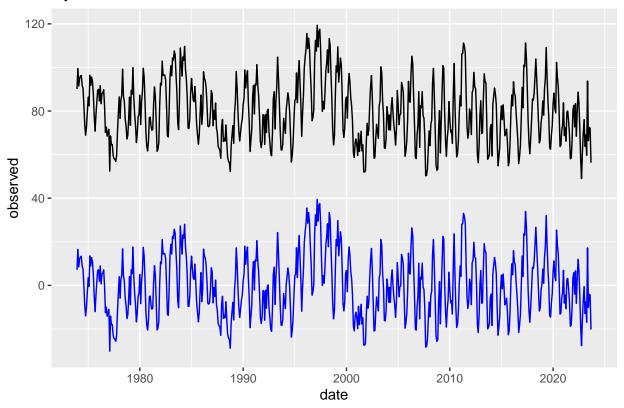
```
ggplot(df_RE_detrend, aes(x=date))+
  geom_line(aes(y=observed),color="black")+
  geom_line(aes(y=detrend),color="blue")+
  labs(title="RE observed versus detrended")
```

RE observed versus detrended



This plot removed the upward linear trend was removed and centered the mean at zero. It also shows a greater dip after 2000 relative to the rest of the data.

Hydro observed versus detrended



This plot did not change significantly beyond centering the mean at zero because there was very little trend component to this data.

$\mathbf{Q5}$

Plot ACF and PACF for the detrended series and compare with the plots from Q1. You may use plot_grid() again to get them side by side. nut mot mandatory. Did the plots change? How?

```
ts_biomass_detrend <- ts(biomass_detrend,start=c(1973,1),frequency = 12)
ts_RE_detrend <- ts(RE_detrend,start=c(1973,1),frequency = 12)
ts_hydro_detrend <- ts(hydro_detrend,start=c(1973,1),frequency = 12)</pre>
```

```
biomass_detrend_acf <- ggAcf(ts_biomass_detrend,lag.max=40)+
    labs(title="Biomass Detrended ACF")

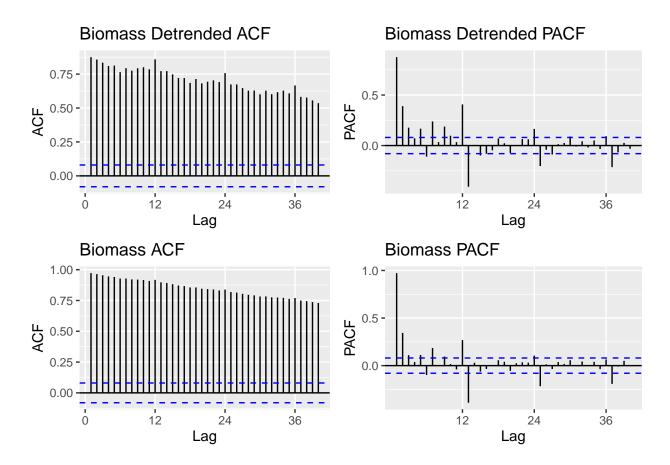
#biomass_detrend_acf
hydro_detrend_acf <- ggAcf(ts_hydro_detrend,lag.max=40)+
    labs(title="Hydro Detrended ACF")

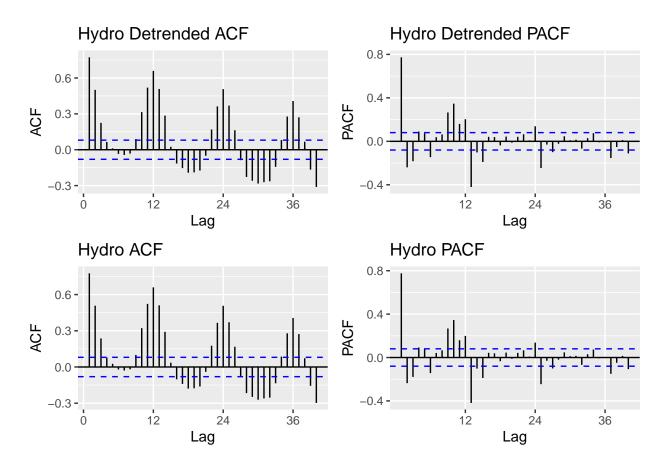
#hydro_detrend_acf
RE_detrend_acf <- ggAcf(ts_RE_detrend,lag.max=40)+
    labs(title="RE Detrended ACF")

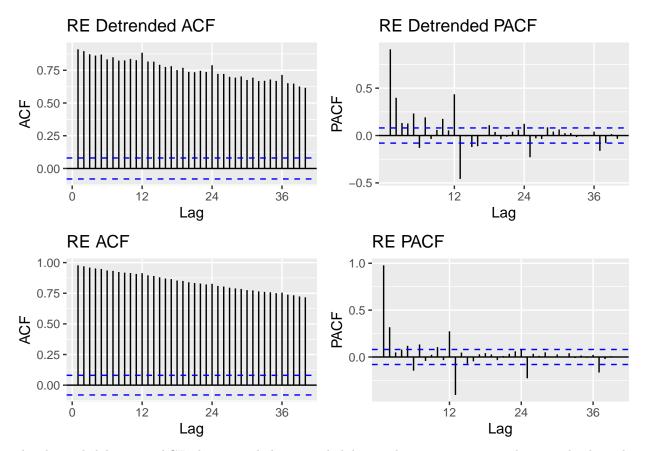
#RE_detrend_acf</pre>
```

```
biomass_detrend_pacf <- ggPacf(ts_biomass_detrend,lag.max=40)+
    labs(title="Biomass Detrended PACF")
#biomass_detrend_pacf</pre>
```

```
hydro_detrend_pacf <- ggPacf(ts_hydro_detrend,lag.max=40)+
    labs(title="Hydro Detrended PACF")
#hydro_detrend_pacf
RE_detrend_pacf <- ggPacf(ts_RE_detrend,lag.max=40)+
    labs(title="RE Detrended PACF")
#RE_detrend_pacf</pre>
```







The detrended biomass ACF shows much lower probability and connections over the periods than the detrended ACF, however the PACF shows some stronger probability on the detrended period and than on the original PACF.

The detrended hydro ACF and PACF looks very similar to the original hydro ACF and PACF because there was very little trend to remove of begin with, so this did not make a huge impact.

The detrended RE ACF and PACF demonstrates a similar change to the detrended biomass figures.

Seasonal Component

Set aside the detrended series and consider the original series again from Q1 to answer Q6 to Q8.

$\mathbf{Q6}$

Just by looking at the time series and the acf plots, do the series seem to have a seasonal trend? No need to run any code to answer your question. Just type in you answer below.

Just looking at the plots from Q1, hydro appears to have a strong seasonal trend. Biomass and RE appear to have what could be a weaker seasonal trend with their oscillating values at a somewhat regular period, with renewable energy appear to have more regular variations than biomass.

$\mathbf{Q7}$

Use function lm() to fit a seasonal means model (i.e. using the seasonal dummies) the two time series. Ask R to print the summary of the regression. Interpret the regression output. From the results which series have a seasonal trend? Do the results match you answer to Q6?

```
#Use seasonal means model
#Create the seasonal dummies
biomass_dummies <- seasonaldummy(ts_energy_data[,1])</pre>
#Fit a linear model to the seasonal dummies
biomass_seas_means_model <- lm(ts_energy_data[,1]~biomass_dummies)</pre>
summary(biomass_seas_means_model)
##
## Call:
## lm(formula = ts_energy_data[, 1] ~ biomass_dummies)
## Residuals:
##
      Min
              1Q Median
                             ЗQ
## -165.85 -55.24 -28.02
                          96.91 178.89
##
## Coefficients:
##
                    Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                    283.9706 13.0762 21.717 <2e-16 ***
## biomass_dummiesJan 6.4960 18.3998 0.353
                                                 0.724
## biomass_dummiesFeb 8.0013 18.3998 0.435
                                                 0.664
## biomass_dummiesMar -21.9534 18.3998 -1.193
                                                 0.233
                    0.6772 18.3998 0.037 0.971
## biomass_dummiesApr
## biomass_dummiesJun -4.5013 18.3998 -0.245
                                                0.807
## biomass_dummiesJul -9.9153 18.3998 -0.539
                                               0.590
## biomass_dummiesAug 6.0708 18.3998
                                       0.330 0.742
## biomass_dummiesSep 9.2018 18.3998
                                       0.500
                                                 0.617
## biomass_dummiesOct -3.6518
                               18.3998 -0.198
                                                 0.843
## biomass_dummiesNov
                      5.6767
                               18.4925
                                       0.307
                                                 0.759
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 91.53 on 586 degrees of freedom
## Multiple R-squared: 0.0101, Adjusted R-squared: -0.008486
## F-statistic: 0.5433 on 11 and 586 DF, p-value: 0.8739
#Store regression coefficients
biomass_beta_int <- biomass_seas_means_model$coefficients[1]</pre>
biomass_beta_coeff <- biomass_seas_means_model$coefficients[2:12]</pre>
```

The biomass coefficients demonstrate there is a seasonal component, but this is a weak driver of the values in the model as the r-squared value is very low.

```
#Use seasonal means model

#Create the seasonal dummies
RE_dummies <- seasonaldummy(ts_energy_data[,2])

#Fit a linear model to the seasonal dummies</pre>
```

```
RE_seas_means_model <- lm(ts_energy_data[,2]~RE_dummies)</pre>
summary(RE_seas_means_model)
##
## Call:
## lm(formula = ts_energy_data[, 2] ~ RE_dummies)
## Residuals:
##
      Min
               1Q Median
                               3Q
                                      Max
## -197.11 -85.79 -51.17 113.30 327.68
##
## Coefficients:
##
                Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                388.0347 19.6010 19.797
                                              <2e-16 ***
## RE_dummiesJan 16.4914
                            27.5811 0.598
                                               0.550
## RE_dummiesFeb 23.2065
                            27.5811
                                     0.841
                                               0.400
## RE_dummiesMar -14.5303
                            27.5811 -0.527
                                               0.599
## RE_dummiesApr 24.2156
                            27.5811
                                     0.878
                                               0.380
## RE_dummiesMay 11.5261
                            27.5811
                                    0.418
                                              0.676
## RE_dummiesJun 27.0403
                            27.5811
                                     0.980
                                               0.327
## RE_dummiesJul 16.1352
                            27.5811
                                      0.585
                                               0.559
## RE_dummiesAug 22.9346
                            27.5811
                                      0.832
                                               0.406
## RE_dummiesSep 15.3868
                            27.5811 0.558
                                               0.577
## RE dummiesOct -8.8250
                            27.5811 -0.320
                                               0.749
## RE_dummiesNov
                 0.3201
                            27.7200 0.012
                                               0.991
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 137.2 on 586 degrees of freedom
## Multiple R-squared: 0.009313,
                                   Adjusted R-squared:
                                                       -0.009283
## F-statistic: 0.5008 on 11 and 586 DF, p-value: 0.9031
#Store regression coefficients
RE_beta_int <- RE_seas_means_model$coefficients[1]</pre>
RE_beta_coeff <- RE_seas_means_model$coefficients[2:12]</pre>
```

The coefficients demonstrate that there are seasonal components that affect the renewable energy as well, but these are very week as noted by their low R squared value.

```
#Use seasonal means model

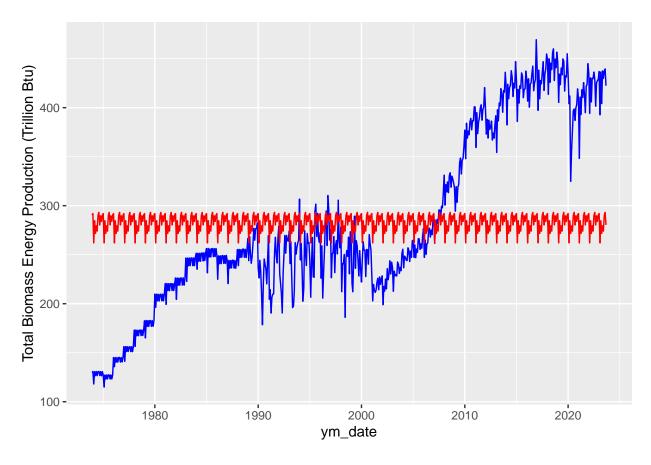
#Create the seasonal dummies
hydro_dummies <- seasonaldummy(ts_energy_data[,3])

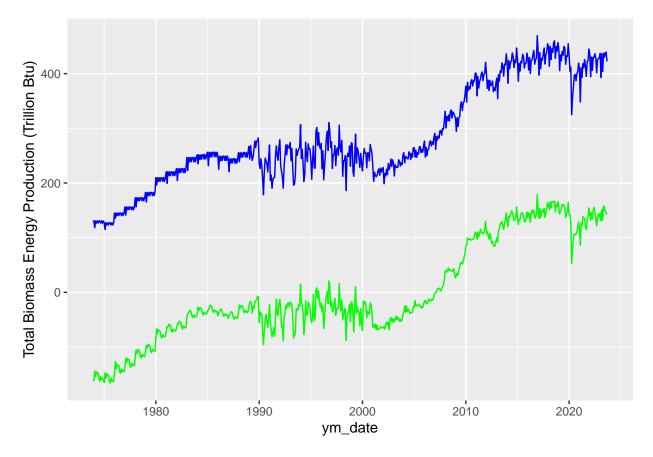
#Fit a linear model to the seasonal dummies
hydro_seas_means_model <- lm(ts_energy_data[,3]~hydro_dummies)
summary(hydro_seas_means_model)</pre>
```

```
##
## Call:
## lm(formula = ts_energy_data[, 3] ~ hydro_dummies)
```

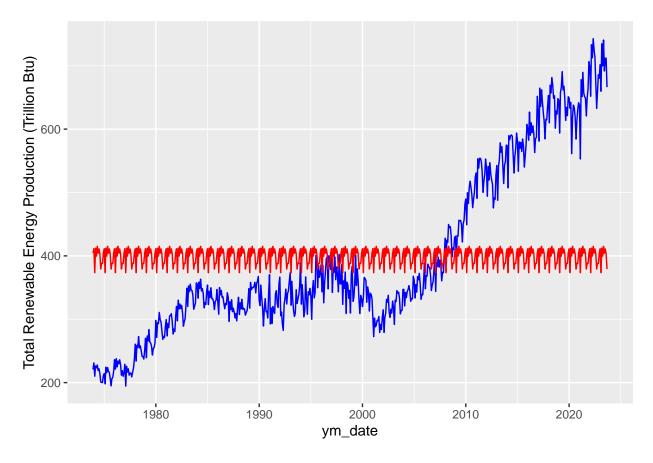
```
##
## Residuals:
##
      Min
                1Q Median
                                      Max
##
  -31.500 -5.842 -0.512
                            6.410
                                   32.314
##
## Coefficients:
                   Estimate Std. Error t value Pr(>|t|)
##
                                 1.496 46.389 < 2e-16 ***
## (Intercept)
                     69.404
## hydro_dummiesJan
                     10.878
                                 2.105
                                         5.167 3.26e-07 ***
## hydro_dummiesFeb
                     15.596
                                 2.105
                                         7.408 4.49e-13 ***
## hydro_dummiesMar
                      8.113
                                 2.105
                                         3.854 0.000129 ***
## hydro_dummiesApr
                     17.679
                                 2.105
                                         8.398 3.44e-16 ***
## hydro_dummiesMay
                     16.246
                                 2.105
                                        7.717 5.16e-14 ***
## hydro_dummiesJun
                     24.971
                                 2.105 11.862 < 2e-16 ***
                                 2.105 10.310 < 2e-16 ***
## hydro_dummiesJul
                     21.705
## hydro_dummiesAug
                     14.926
                                 2.105
                                         7.090 3.87e-12 ***
## hydro_dummiesSep
                                 2.105
                      5.234
                                         2.486 0.013182 *
## hydro dummiesOct
                      -5.830
                                 2.105 -2.769 0.005793 **
## hydro_dummiesNov
                     -5.573
                                 2.116 -2.634 0.008666 **
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 10.47 on 586 degrees of freedom
## Multiple R-squared: 0.467, Adjusted R-squared: 0.457
## F-statistic: 46.68 on 11 and 586 DF, p-value: < 2.2e-16
#Store regression coefficients
hydro beta int <- hydro seas means model$coefficients[1]
hydro beta coeff <- hydro seas means model$coefficients[2:12]
```

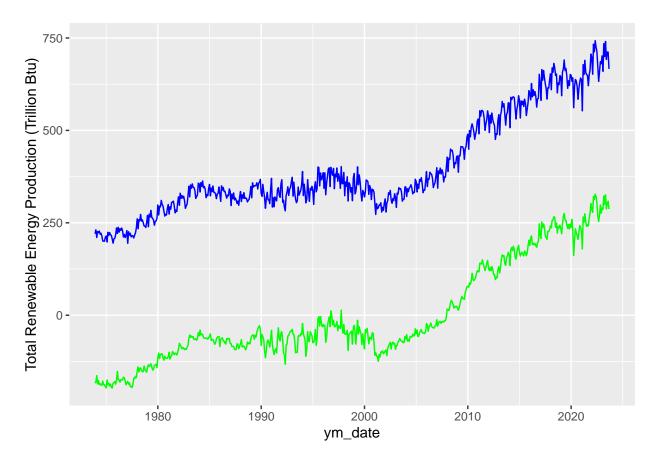
The coefficients indicate a very strong seasonal component to the data, with increased values in the summer and decreased values in the fall and winter months. These coefficients have a strong R square value and all have strong p values as well. This series has the most significant seasonal component of the three. ### Q8 Use the regression coefficients from Q7 to deseason the series. Plot the deseason series and compare with the plots from part Q1. Did anything change?



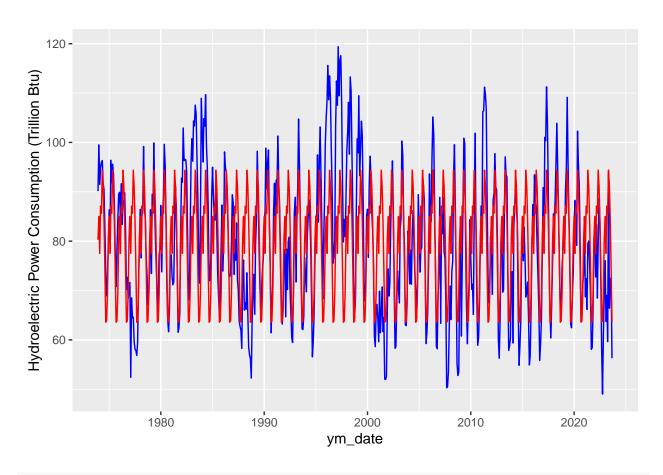


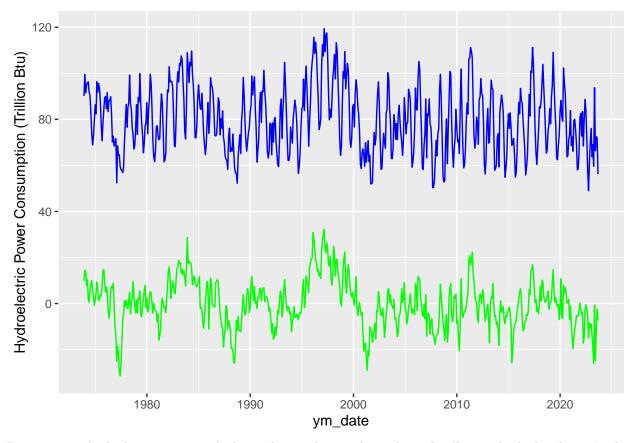
Biomass appears to have a very small seasonal trend that was removed through this process that smoothed out the regular variations year to year. De-seasoning the data also centered the mean at zero.





RE appears to have a very small seasonal trend that was removed through this process that smoothed out the regular variations year to year. De-seasoning the data also centered the mean at zero.





Deseasoning the hydro series smoothed out the regular yearly peaks and vallys in the hydro data. It also centered the mean at 0. This plot had the greatest change.

$\mathbf{Q}\mathbf{9}$

Plot ACF and PACF for the deseason series and compare with the plots from Q1. You may use plot_grid() again to get them side by side but not mandatory. Did the plots change? How?

```
ts_biomass_deseason <- ts(deseason_biomass_data,start=c(1973,1),frequency = 12)
ts_RE_deseason <- ts(deseason_RE_data,start=c(1973,1),frequency = 12)
ts_hydro_deseason <- ts(deseason_hydro_data,start=c(1973,1),frequency = 12)</pre>
```

```
biomass_deseason_acf <- ggAcf(ts_biomass_deseason,lag.max=40)+
    labs(title="Biomass Deseasoned ACF")

#biomass_season_acf
hydro_deseason_acf <- ggAcf(ts_hydro_deseason,lag.max=40)+
    labs(title="Hydro Deseasoned ACF")

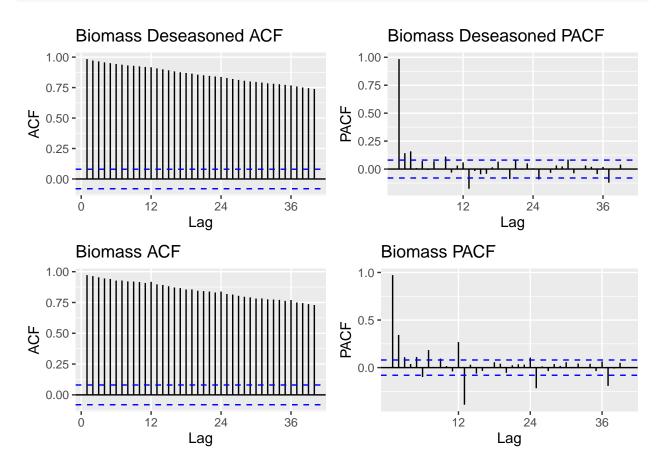
#hydro_season_acf

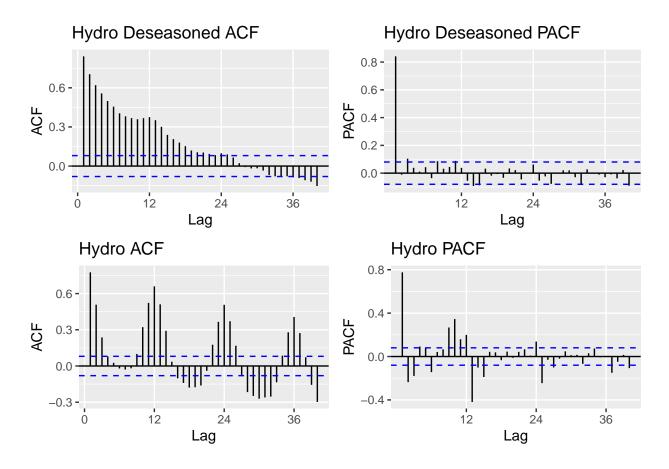
RE_deseason_acf <- ggAcf(ts_RE_deseason,lag.max=40)+
    labs(title="RE Deseasoned ACF")

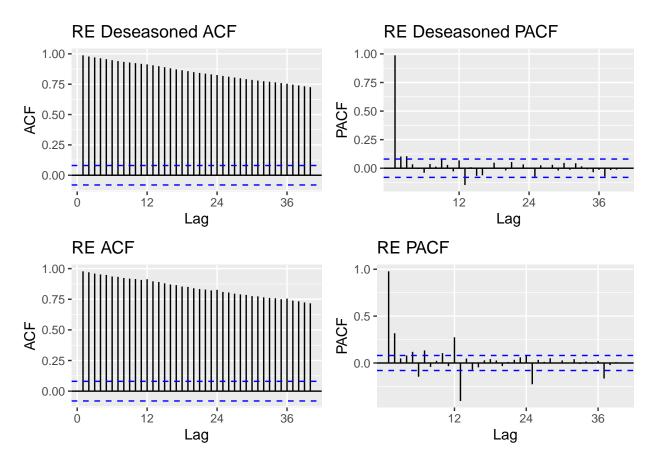
#RE_season_acf
```

```
biomass_deseason_pacf <- ggPacf(ts_biomass_deseason,lag.max=40)+
   labs(title="Biomass Deseasoned PACF")
#biomass_season_pacf</pre>
```

```
hydro_deseason_pacf <- ggPacf(ts_hydro_deseason,lag.max=40)+
    labs(title="Hydro Deseasoned PACF")
#hydro_season_pacf
RE_deseason_pacf <- ggPacf(ts_RE_deseason,lag.max=40)+
    labs(title="RE Deseasoned PACF")
#RE_season_pacf</pre>
```







The biomass and renewable energy PACF and ACFs look very similar to their deseasoned versions. However, the hydro deseasoned ACF shows far less correlation to previous data due to taking out the seasonal similarities, and the PACF has an even smaller statistical significance in probability the further along the lag goes. Taking out the seasonal component really helped the hydro data to be less dependent on many periods before it.