

# ENVX2001 - Model selection

## Learning Outcomes

In this lab, you will work towards achieving learning outcomes

## Lab Objectives

In this lab, we will:

- []
- []



Tip

Please work on this exercise by creating your own R Markdown file.

## Exercise 1: Model quality - multiple vs adjusted $r^2$

Data: *California\_streamflow* spreadsheet

Import the “California\_streamflow” sheet into R.

CODE

```
# Load library if needed
library(readxl)
# Load data
stream_data <- read_xlsx("data/california_streamflow.xlsx", "streamflow")
```

in this exercise we will use the same data as last week. To jog your memory, the dataset contains 43 years of annual precipitation measurements (in mm) taken at (originally) 6 sites in the Owens Valley in California. Through model selection via partial F-test we have the final model as below:

```
CODE
fit <- lm(runoff_volume ~ rock_creek + pine_creek, data = stream_data)
```

We will now add a totally useless variable to the dataset. This variable is a random number generated from a normal distribution with mean 3 and standard deviation 2. We use the `set.seed()` function to make sure that everybody gets the same random values.

```
CODE
set.seed(100) # to make sure everybody gets the same results

# this generates the random number into the dataset
stream_data$random_no <- rnorm(n = nrow(stream_data), mean = 3, sd = 2)
```

We will see the impact of including a totally useless variable, such as this random variable, has on measures of model quality,  $r^2$  and adjusted  $r^2$  values.

**Task: create two regression models:**

1. `runoff_volume ~ rock_creek + pine_creek`
2. `runoff_volume ~ rock_creek + pine_creek + random_no`

## Question 2

Compare each in terms of their multiple  $r^2$  and adjusted  $r^2$  values. Which performance measure (multiple  $r^2$  or adj  $r^2$ ) would you use to identify which predictors to use in your model?

## Answer

There is only a small difference in the multiple  $r^2$  and adj  $r^2$  between the models, but one goes up and the other goes down. Since the random number is a totally useless value, this demonstrates that the adjusted  $r^2$  is the better performance measure to use.

```
CODE
mod_rand1 <- lm(runoff_volume ~ rock_creek + pine_creek, data = stream_data)
summary(mod_rand1)
```

### OUTPUT

```
Call:
lm(formula = runoff_volume ~ rock_creek + pine_creek, data = stream_data)

Residuals:
    Min       1Q   Median       3Q      Max
-0.09832 -0.02350  0.01076  0.03291  0.08568

Coefficients:
```

```

              Estimate Std. Error t value Pr(>|t|)
(Intercept)  3.35762    0.10547  31.835 < 2e-16 ***
rock_creek   0.44437    0.08925   4.979 1.26e-05 ***
pine_creek   0.21051    0.06861   3.068 0.00385 **
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 0.04937 on 40 degrees of freedom
Multiple R-squared:  0.8749,    Adjusted R-squared:  0.8686
F-statistic: 139.8 on 2 and 40 DF,  p-value: < 2.2e-16

```

#### CODE

```

mod_rand2 <- lm(runoff_volume ~ rock_creek + pine_creek + random_no ,data = stream_data)
summary(mod_rand2)

```

#### OUTPUT

```

Call:
lm(formula = runoff_volume ~ rock_creek + pine_creek + random_no,
    data = stream_data)

Residuals:
    Min       1Q   Median       3Q      Max
-0.10327 -0.02401  0.01220  0.03179  0.08056

Coefficients:
              Estimate Std. Error t value Pr(>|t|)
(Intercept)  3.359356    0.106303  31.602 < 2e-16 ***
rock_creek   0.442795    0.089956   4.922 1.6e-05 ***
pine_creek   0.207234    0.069324   2.989 0.00482 **
random_no    0.003213    0.005077   0.633 0.53055
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 0.04974 on 39 degrees of freedom
Multiple R-squared:  0.8761,    Adjusted R-squared:  0.8666
F-statistic: 91.96 on 3 and 39 DF,  p-value: < 2.2e-16

```

## Exercise 2: Fish productivity

Fish communities were surveyed in lakes across a eutrophication gradient to investigate the relationship between productivity and fish diversity.

The datasheet has the following variables:

- `lake_id` Unique identifier for each lake
- `chl_a` Log-transformed Chlorophyll a
- `richness` Log-transformed species richness
- `evenness` Log-transformed Pielou's evenness

- abundance Log-transformed abundance per unit effort (NPUE)
- biomass Log-transformed biomass per unit effort (BPUE)
- productivity Log-transformed productivity proxy

```
CODE
#Load library if necessary
library(tidyverse)

#Read in data
fish_data <- read_csv("data/fish_communities.csv")
```

```
OUTPUT
Rows: 39 Columns: 7
— Column specification —————
Delimiter: ","
chr (1): lake_id
dbl (6): chl_a, richness, evenness, abundance, biomass, productivity

i Use `spec()` to retrieve the full column specification for this data.
i Specify the column types or set `show_col_types = FALSE` to quiet this message.
```

```
CODE
#Have a look at the structure of the data
str(fish_data)
```

```
OUTPUT
spc_tbl_ [39 × 7] (S3: spec_tbl_df/tbl_df/tbl/data.frame)
 $ lake_id      : chr [1:39] "FTH" "XLH" "HGH" "LH" ...
 $ chl_a       : num [1:39] 4.61 4.53 3.84 3.71 2.43 ...
 $ richness    : num [1:39] 2.64 2.89 1.99 2.94 2.37 ...
 $ evenness    : num [1:39] -0.356 -0.67 -0.423 -0.405 -0.589 ...
 $ abundance   : num [1:39] 2.24 3.34 1.24 2.67 1.12 ...
 $ biomass     : num [1:39] 4.96 6.03 4.67 6.52 5.32 ...
 $ productivity: num [1:39] 3.47 4.47 2.71 4.47 3.24 ...
- attr(*, "spec")=
.. cols(
..   lake_id = col_character(),
..   chl_a = col_double(),
..   richness = col_double(),
..   evenness = col_double(),
..   abundance = col_double(),
..   biomass = col_double(),
..   productivity = col_double()
.. )
- attr(*, "problems")=<externalptr>
```

Explore the data on your own before making any models. (*Hint: remember that we are only interested in the numeric variables for our linear models*)

## Question 1

Are there any obvious relationships between the response variable (productivity) and the other variables?

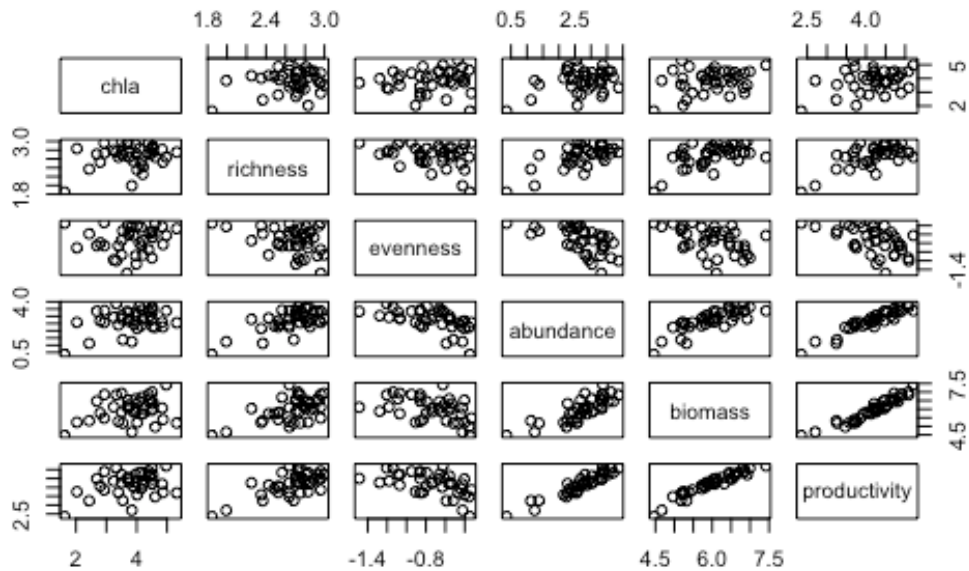
## Answer

```
CODE
#correlation matrix
cor(fish_data[,1])
```

OUTPUT

	chla	richness	evenness	abundance	biomass	productivity
chla	1.0000000	0.2388845	0.0872381	0.3449158	0.2809369	0.3406440
richness	0.2388845	1.0000000	-0.3295238	0.6585895	0.5704803	0.6611413
evenness	0.0872381	-0.3295238	1.0000000	-0.5553243	-0.4396433	-0.5162017
abundance	0.3449158	0.6585895	-0.5553243	1.0000000	0.8089680	0.9379798
biomass	0.2809369	0.5704803	-0.4396433	0.8089680	1.0000000	0.9571907
productivity	0.3406440	0.6611413	-0.5162017	0.9379798	0.9571907	1.0000000

```
CODE
#Plot the variables
pairs(fish_data[,1])
```



Productivity has a strong relationship with biomass and abundance

## Question 2

Are there any other patterns or potential issues you can see from the exploratory plots?

## **Answer**

Biomass is also highly correlated with abundance, so collinearity might be an issue.

## **Take home exercise:**

## **Review**

## **Attribution**