

$$A) \frac{Y(s)}{R(s)} = \frac{100/s^2}{1 + K(s) \cdot \frac{100}{s^2}} = \frac{100/s^2}{1 + \frac{100K}{s}} = \frac{100}{s^2(1 + 100K/s)}$$

$$= \frac{100}{s^2 + 100Ks}$$

~~$$\frac{Y(s)}{R(s)} = \frac{100/s^2}{1 + K(s) \cdot \frac{100}{s^2}} = \frac{100}{s^2 + 100Ks}$$~~

$$a) \frac{Y(s)}{R(s)} = \frac{100/s^2}{1 + (1s+1)(100/s^2)} = \boxed{\frac{100}{s^2 + 100Ks + 100}}$$

$$\rightarrow \omega_n = 10 \text{ \& } 2\zeta\omega_n = 100K \rightarrow \zeta = 5K$$

$$b) M_p = 0.2 = e^{-\frac{\pi\zeta}{\sqrt{1-\zeta^2}}} = e^{-\frac{\pi 5K}{\sqrt{1-(5K)^2}}}$$

$$\rightarrow -1.61 = \frac{-\pi 5K}{\sqrt{1-(5K)^2}} \rightarrow 1.61\sqrt{1-(5K)^2} = \pi 5K$$

$$\rightarrow 2.54(1-25K^2) = \pi^2 5^2 K^2 \rightarrow 2.54 - 64.76K^2 = 78.5K^2$$

~~$$\rightarrow 64.76K^2 + 78.5K^2 - 2.54 = 0 \xrightarrow{\text{Quadratic}} K = 0.113$$~~

~~$$c) \zeta = 5\omega_n \rightarrow 0 = (\pi^2 5^2 + 2.54 \cdot 75)K^2 - 2.54$$~~

~~$$\rightarrow \boxed{0.041 = K}$$~~

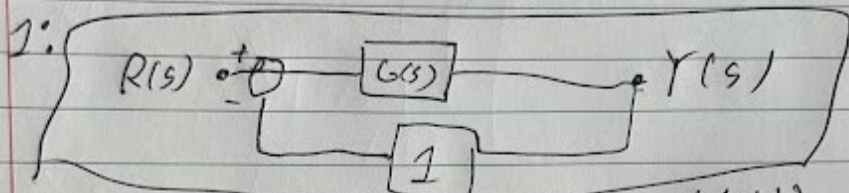
$$c) \zeta = 5\omega_n = 5(0.041)10 = 4.55$$

$$\rightarrow \text{for 1\%, } T_s = \frac{4.6}{4.55} = \boxed{1.011 \text{ s}}$$



Problem 2:

$$G(s) = \frac{k(s+1)}{s(s+2)(s^2+s+4)}$$



$$\rightarrow \frac{Y(s)}{R(s)} = \frac{G(s)}{1+G(s)} = \frac{\frac{k(s+1)}{s(s+2)(s^2+s+4)}}{1 + \frac{k(s+1)}{s(s+2)(s^2+s+4)}}$$

$$= \frac{k(s+1)}{s(s+2)(s^2+s+4) + k(s+1)}$$

$$= \frac{k(s+1)}{s^4 + 3s^3 + 6s^2 + (k+8)s + k}$$

characteristic equation

$s^4$	1	6	k
$s^3$	3	(k+8)	0
$s^2$	$\frac{10-k}{3}$	k	0
$s^1$	$\frac{-k^2-7k+80}{10-k}$	0	0
$s^0$	k	0	0

$$\rightarrow \text{for stability: } \frac{10-k}{3} > 0 \Rightarrow k < 10$$

$$\& \frac{k^2-7k+80}{10-k} > 0 \Rightarrow -13.1 < k < 6.1$$

$$\rightarrow \boxed{-13.1 < k < 6.1} \quad \& k > 0$$

