

$$A) \frac{Y(s)}{R(s)} = \frac{\frac{100}{s^2}}{1 + K_f \left(\frac{100}{s^2} \right)} = \frac{\frac{100}{s^2}}{1 + \frac{100K_f}{s^2}} = \frac{100}{s^2(1 + \frac{100K_f}{s^2})}$$

~~(= \frac{100}{s^2 + 100K_f s^2})~~

~~W1 = 10 & 2 * W1 = 100K_f~~

$$B) \frac{Y(s)}{R(s)} = \frac{\frac{100}{s^2}}{1 + ((1s+1)(\frac{100}{s^2}))} = \boxed{\frac{100}{s^2 + 100ks + 100}}$$

$$\rightarrow \omega_n^2 = 10 \quad \& \quad 2\zeta\omega_n = 100k \Rightarrow \zeta = 5k$$

$$B) M_p = 0,2 = e^{-\frac{\pi f_s}{Vf - g^2}} = e^{-\frac{\pi 5k}{Vf - g^2}}$$

$$\rightarrow -1,61 = \frac{-\pi 5k}{Vf - g^2} \rightarrow 1,61 \sqrt{1 - (\frac{\pi 5k}{Vf - g^2})^2} = \pi 5k$$

$$\rightarrow 2,54(1 - 25k^2) = \pi^2 5^2 \rightarrow 2,54 - 64,76k^2 = \pi^2 5^2$$

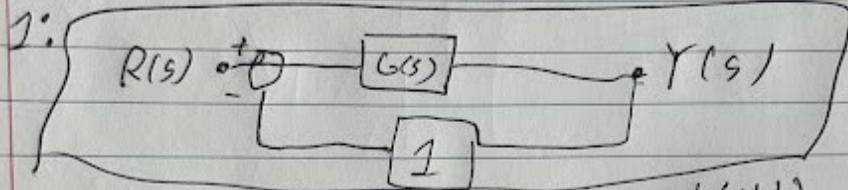
$$\rightarrow 64,76k^2 \pm \pi^2 5^2 = 2,54 \xrightarrow{\text{Quadratic}} \boxed{k = 0,113}$$

$$C) G = \zeta\omega_n = 5(0,091)10 = 4,55$$

$$\rightarrow \text{for } T_s \quad T_s = \frac{4,6}{4,55} = \boxed{1,011s}$$

Problem 2:

$$G(s) = \frac{k(s+1)}{s(s+2)(s^2+s+4)}$$



$$\rightarrow \frac{R(s)}{\cancel{R(s)}} \frac{Y(s)}{R(s)} = \frac{G(s)}{1 + G(s)} = \frac{\frac{k(s+1)}{s(s+2)(s^2+s+4)}}{1 + \frac{k(s+1)}{s(s+2)(s^2+s+4)}}$$

$$= \frac{k(s+1)}{s(s+2)(s^2+s+4) + k(s+1)}$$

$$= \frac{k(s+1)}{s^4 + 3s^3 + 6s^2 + (k+8)s + k}$$

characteristic equation

$$\begin{array}{c|ccc} s^4 & 1 & 6 & k \\ s^3 & 3 & (k+8) & 0 \\ s^2 & \frac{10-k}{3} & k & 0 \\ s^1 & \frac{-k^2-7k+80}{10-k} & 0 & 0 \\ s^0 & k & 0 & N \end{array}$$

$$\rightarrow \text{for stability: } \frac{10-k}{3} > 0 \Rightarrow \cancel{k < 10}$$

$$\& \frac{k^2 - 7k + 80}{10-k} > 0 \Rightarrow -13.1 < k < 6.1$$

$$\rightarrow \cancel{-13.1 < k < 6.1}$$

$$\& k > 0$$

