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# Stochastic modelling of particles in turbulent flows with neural networks

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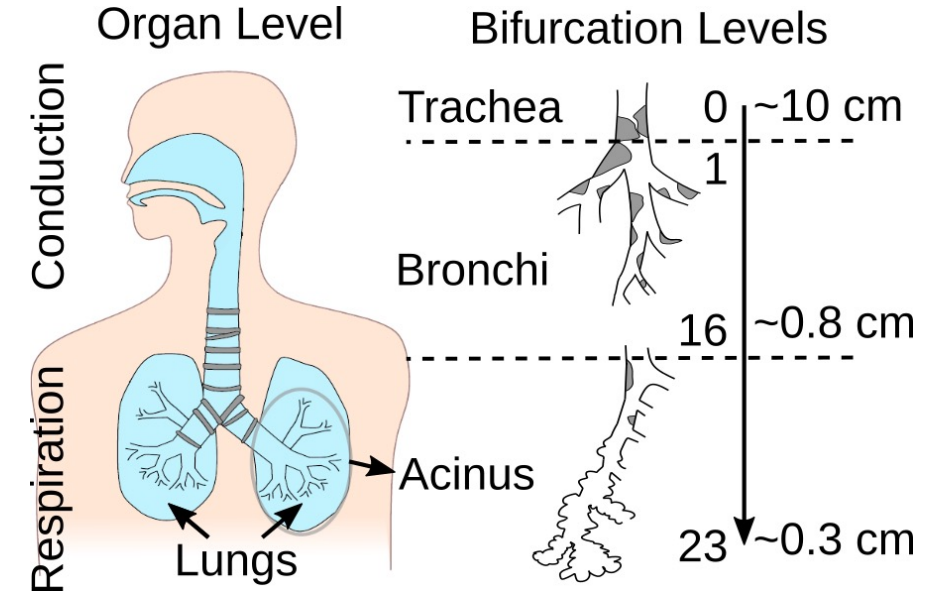
<sup>2</sup> School of Engineering and Physical Sciences, Heriot-Watt University, UK

# Overview

- Motivation and context
- Fluid and particle modelling
- Data generation, neural network training, implementing in OpenFOAM.
- Results
- Conclusions and lessons learned

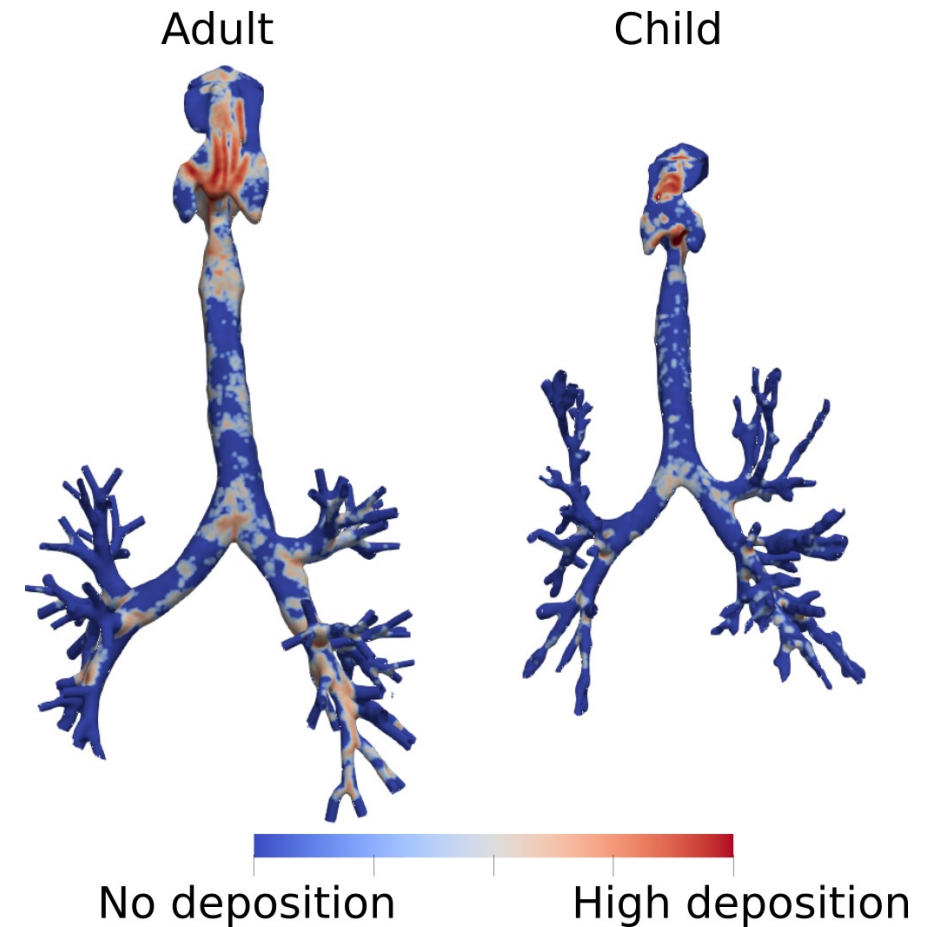
# Motivation and context

- 1 billion patients worldwide suffer from chronic respiratory disease <sup>[1]</sup>.



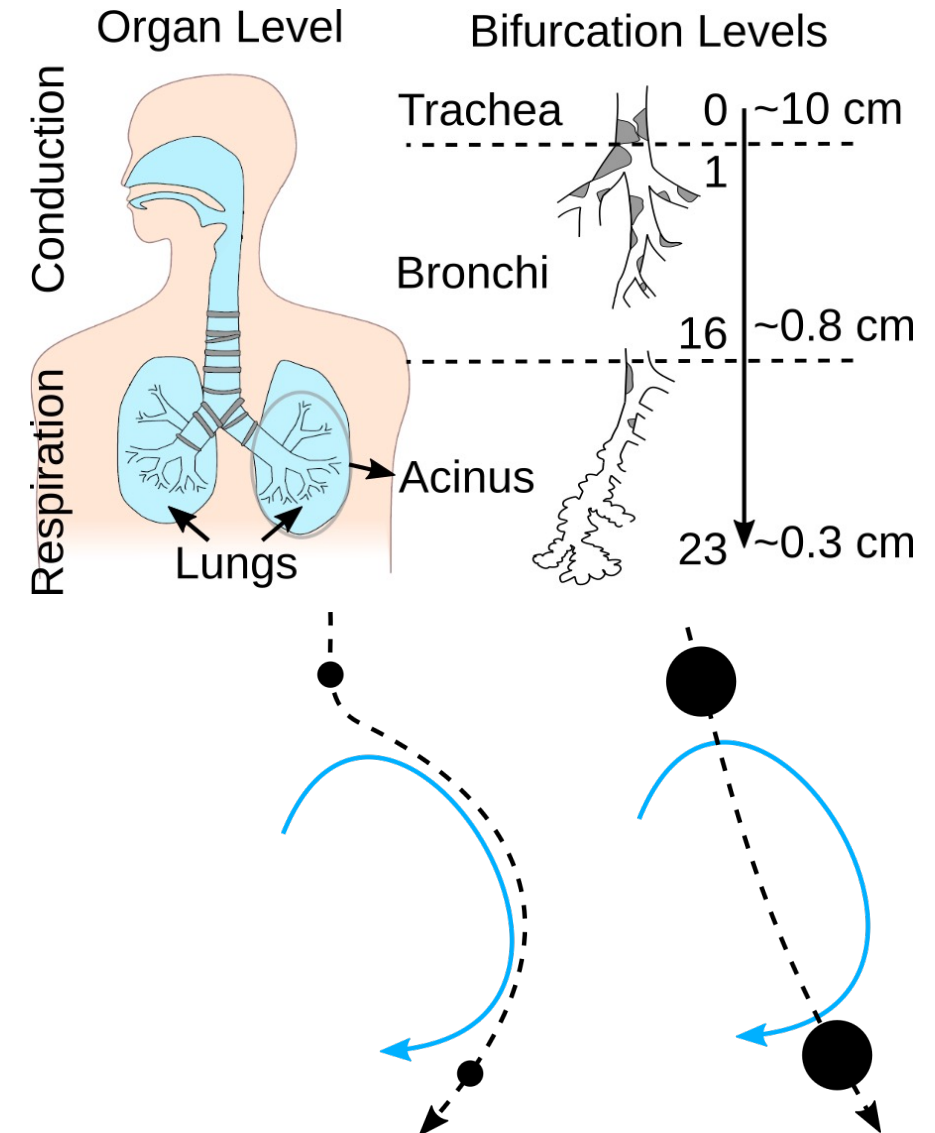
# Motivation and context

- 1 billion patients worldwide suffer from chronic respiratory disease <sup>[1]</sup>.
- Treatment efficacy varies across patients <sup>[2]</sup>.
  - Lung and airway shape.
  - Disease in different part of the lungs.
  - Patients breathe differently.



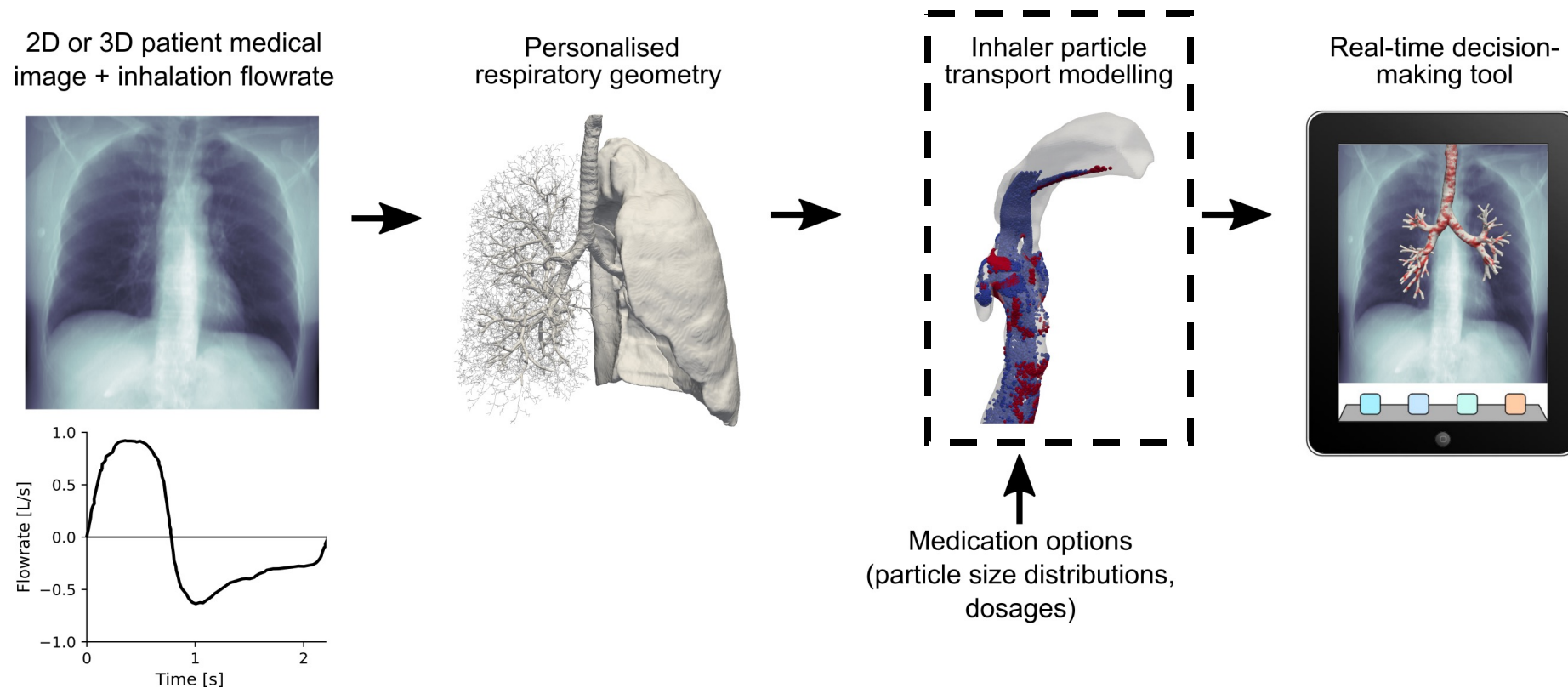
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  - Patients breathe differently.
- Deposition depends on particle size.



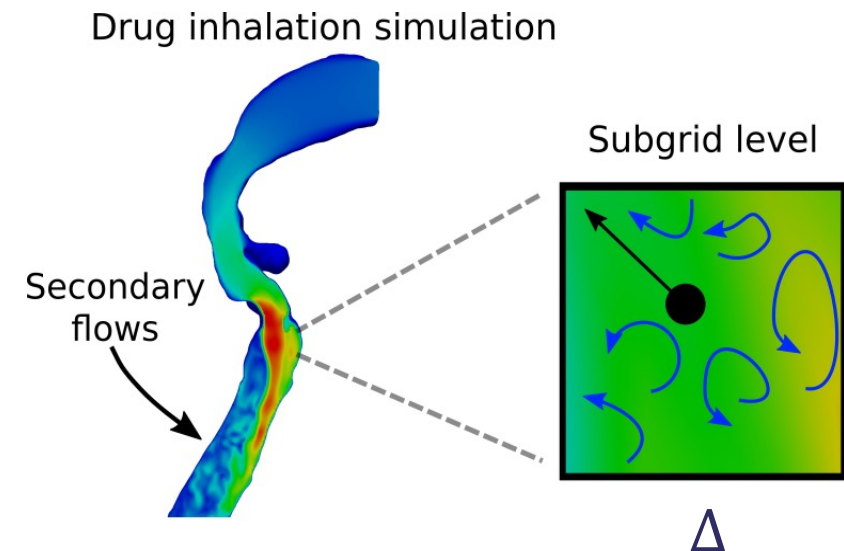
# Image-based modelling as a solution

- **Main motivation:** use modelling to predict and optimise drug deposition.
- Large range of length and time-scales (**turbulence**, particle interactions etc).



# Fluid modelling framework

- Cannot resolve all length scales.  $\mathbf{u}_f = \tilde{\mathbf{u}}_f + \mathbf{u}_{sgs}$ .
- *Filtered* incompressible Navier-Stokes (large eddy simulation, LES).
- Eddy viscosity model for  $\tau_{sgs}$ .<sup>[1]</sup>
- $k_{sgs}$  and  $\varepsilon_{sgs}$  based on mesh size and local velocity gradients.
- Use MPPICFoam with 1-way coupling.<sup>[2]</sup>

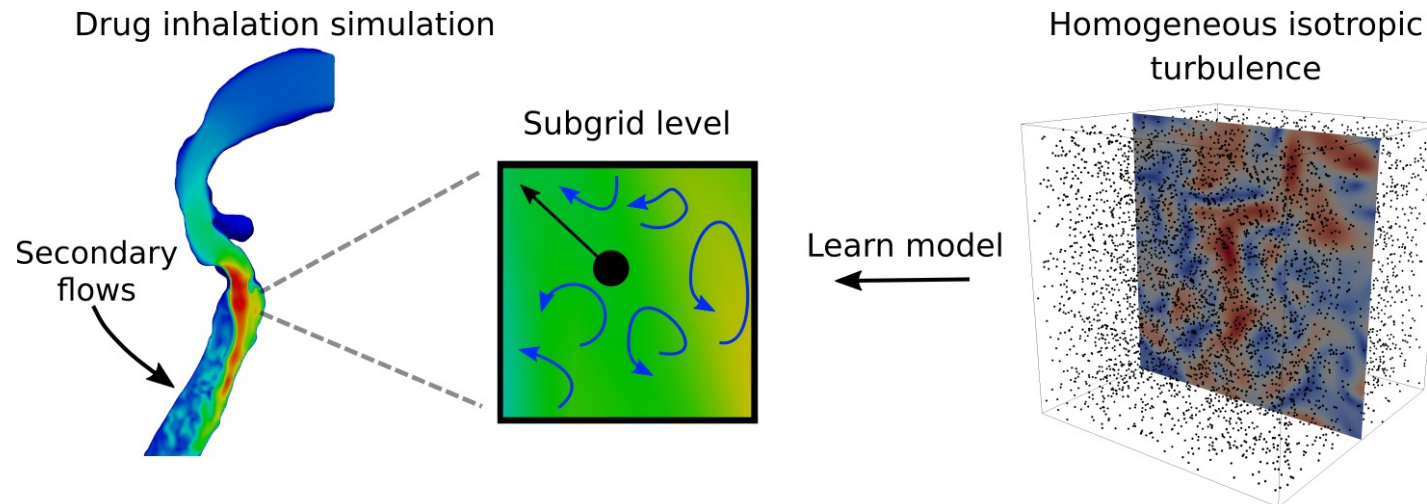


[1] Germano, M. et al., 1991. *Physics of Fluids*.

[2] Kleinstreuer, C. and Zhang, Z., 2010. *Annual Review of Fluid Mechanics*.

# Modelling turbulent fluctuations

- Turbulent fluctuations ( $u_{sgs}$ ) may influence deposition [1].
- Existing stochastic models [1] not consistent with near-wall or decaying flow [2].
- **Our aim: learn stochastic turbulence model from highly resolved simulations.**
- Current model limited to homogeneous flows (*proof of concept*).





# Stochastic particle modelling

- Newton's equation of motion:

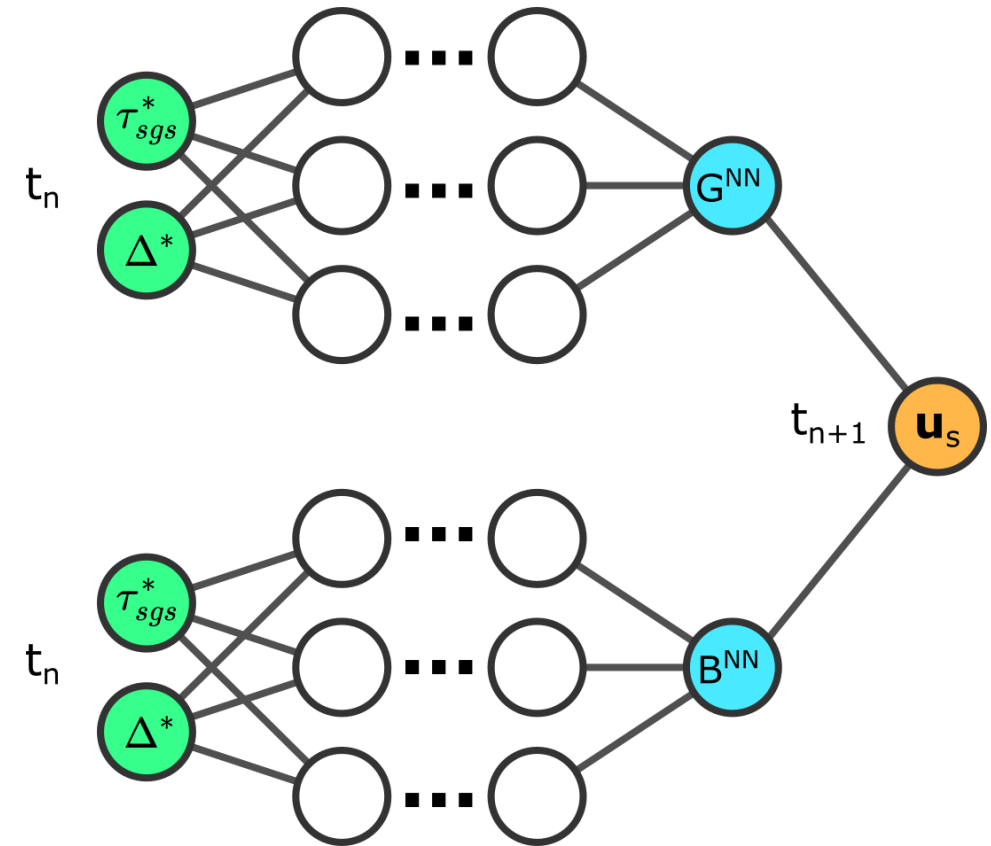
$$d\mathbf{u}_p = \frac{\mathbf{u}_s - \mathbf{u}_p}{\tau_p} dt \quad \text{and} \quad \tau_p = \frac{\rho_p}{\rho_f} \frac{4 d_p}{3 C_D |\mathbf{u}_s - \mathbf{u}_p|}$$

- We can use a Langevin-type model for  $\mathbf{u}_s^{[1]}$ :

$$d\mathbf{u}_s = -G^{NN}(\mathbf{u}_s - \tilde{\mathbf{u}}_f) dt + B^{NN} d\mathbf{w}$$

$$G^{NN} = 1/T^{NN}$$

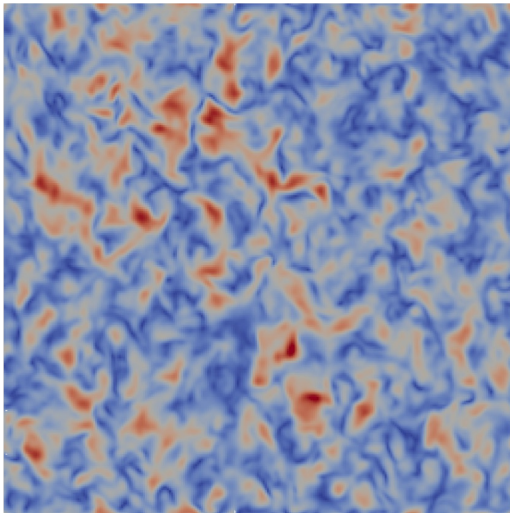
All fluid properties interpolated to particle.



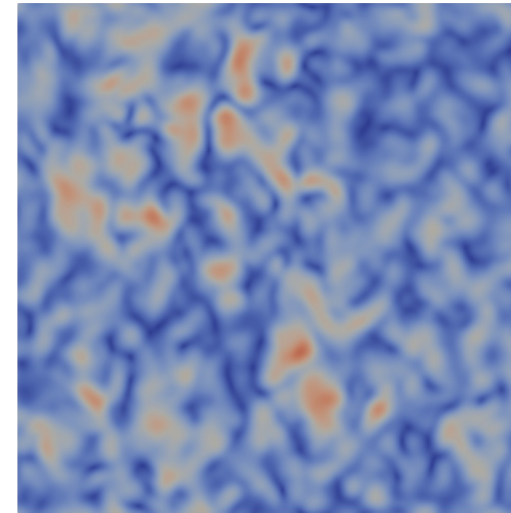
# Simulation configuration

- Decaying homogeneous isotropic turbulence at  $Re_\lambda^0 = \{9, 33, \mathbf{105}\}$ .
- Ground truth has  $256^3$  cells.  $St^0 = 0.1$ ,  $N_p = 10^4$ .
- Top-hat filter width  $\{3\Delta, 5\Delta, 7\Delta, 9\Delta\}^{[1]}$ . Extract subgrid variables  $k_{sgs}, \varepsilon_{sgs}$ .

Direct numerical simulation  
(fine mesh)



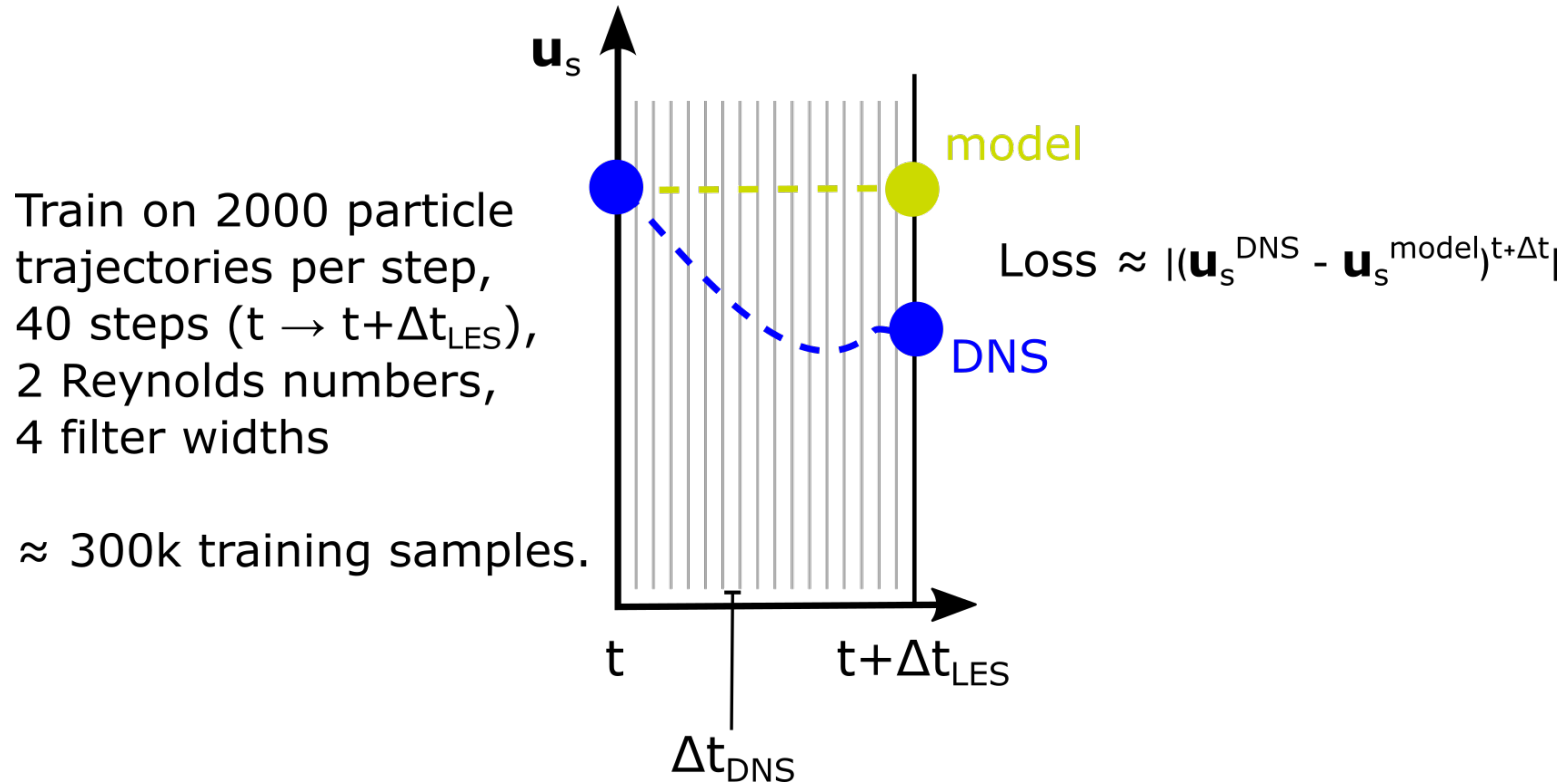
Large eddy simulation  
(coarse mesh,  $9\Delta$ )



←  
Langevin model

# Neural network training

- Feed-forward neural network (4 hidden layers, 120 neurons per layer).



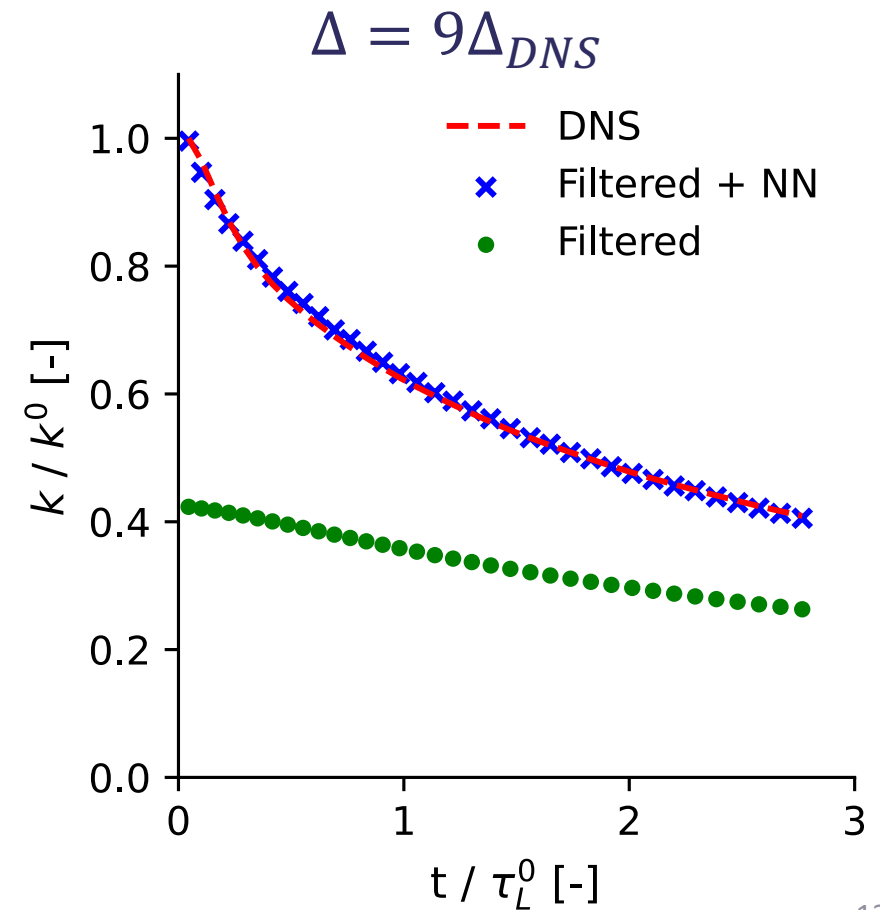
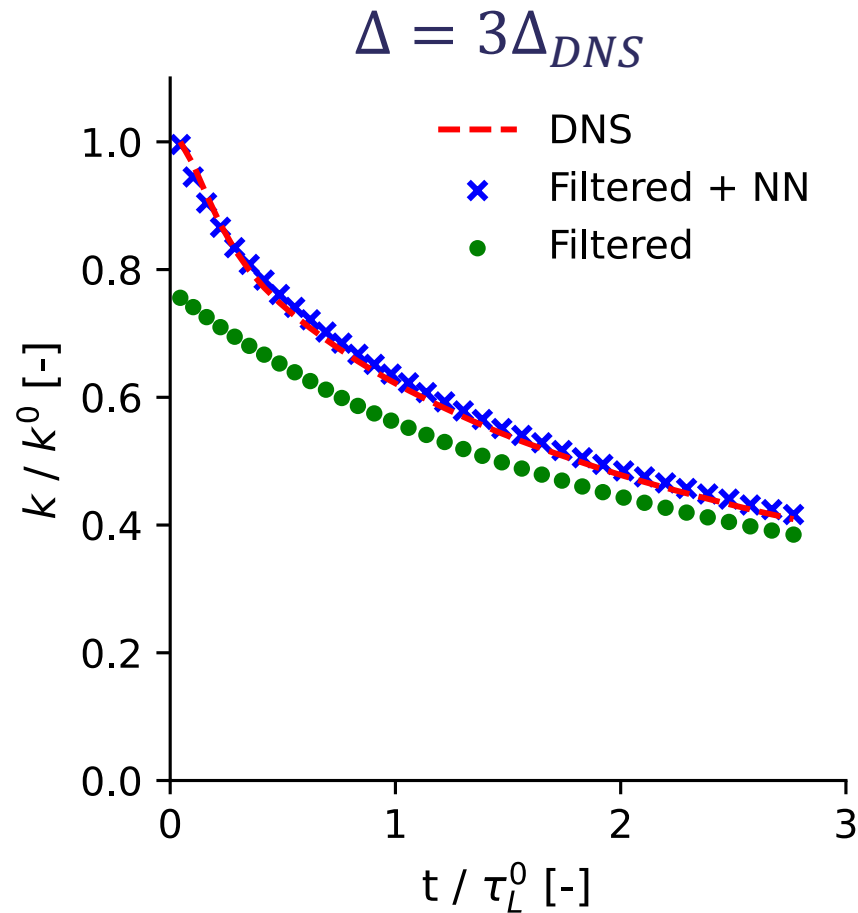
# Using in OpenFOAM

- Save Tensorflow architecture as JSON, parameters as HDF5. Write to readable ASCII format.
- Keras2cpp repository, read weights and perform forward pass.
  - Limited features, not been updated in around 6 years...
- Tried other repositories, but not really lightweight or user-friendly.

```
layers 12
layer 0 Convolution2D
4 1 3 3 same
[ 0.13240439 -0.39469701 -0.05886053]
[-0.16273086 0.27228925 0.70811206]
[-0.0382412 0.91429299 0.72160912]
[ 0.41376248 -0.13718128 -0.55548537]
[ 0.06595665 -0.43903521 0.04035483]
[ 0.34481722 0.63220054 0.07781094]
[ 0.41419399 -0.13306008 0.72000468]
[ 0.28247169 0.10319189 0.50113165]
[-0.14225948 0.33037826 -0.4037863 ]
[ 0.21228614 -0.69273335 0.45505175]
[ 0.63414061 -0.75804955 -0.62078679]
[-0.5811435 -0.20503305 0.65040439]
[ 0.04864343 -0.02648391 -0.00558628 0.06567492]
layer 1 Activation
relu
```

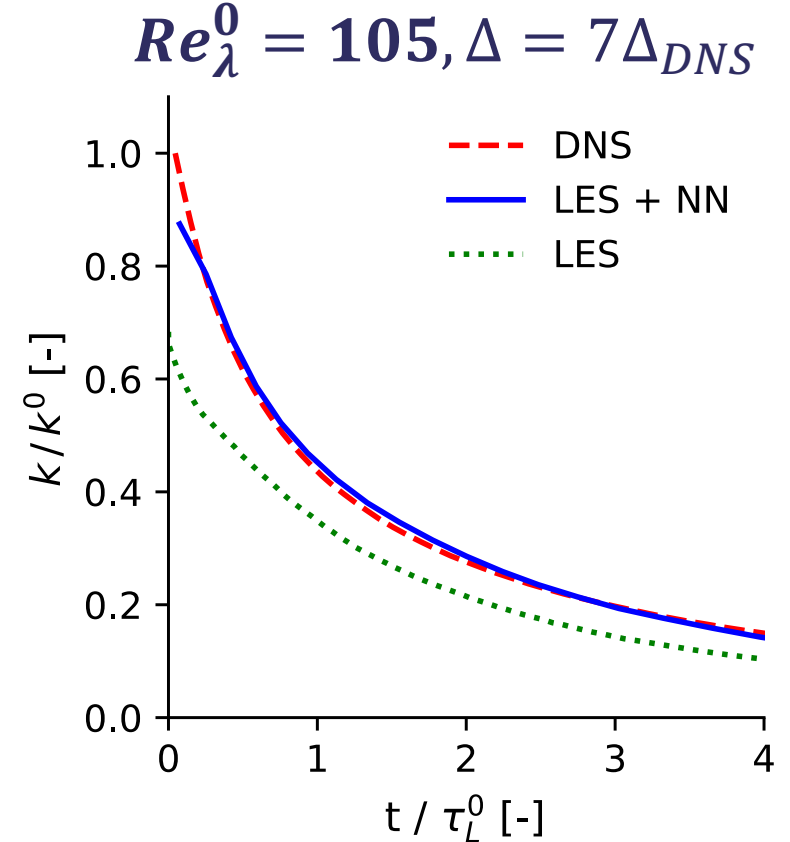
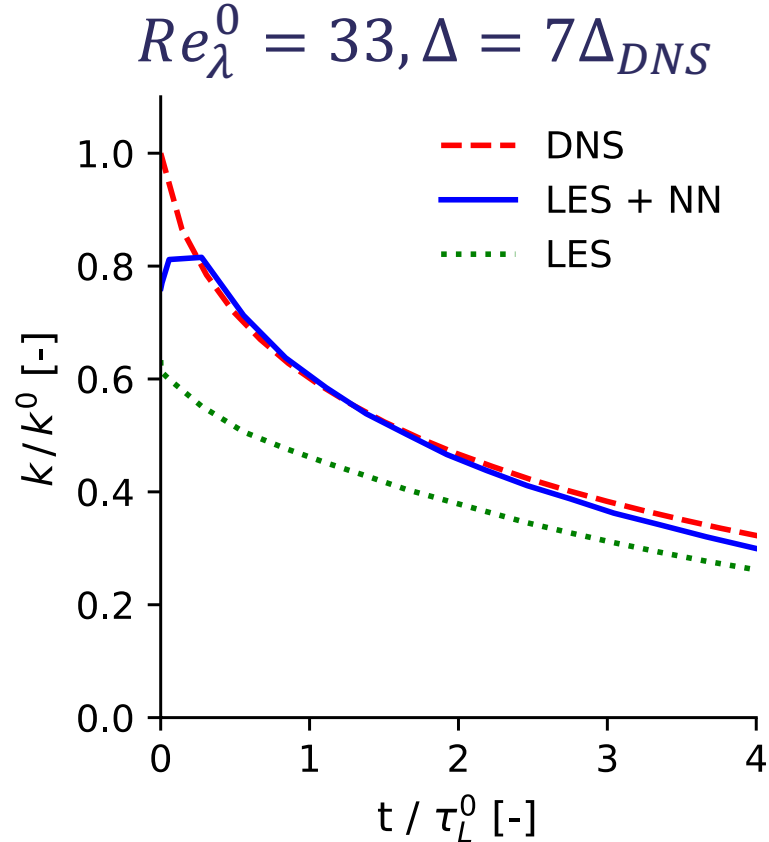
# Tracer velocity statistics (*a priori*)

$$k = \text{tr}(\mathbf{u}_s \otimes \mathbf{u}_s)/2, Re_\lambda^0 = 33$$



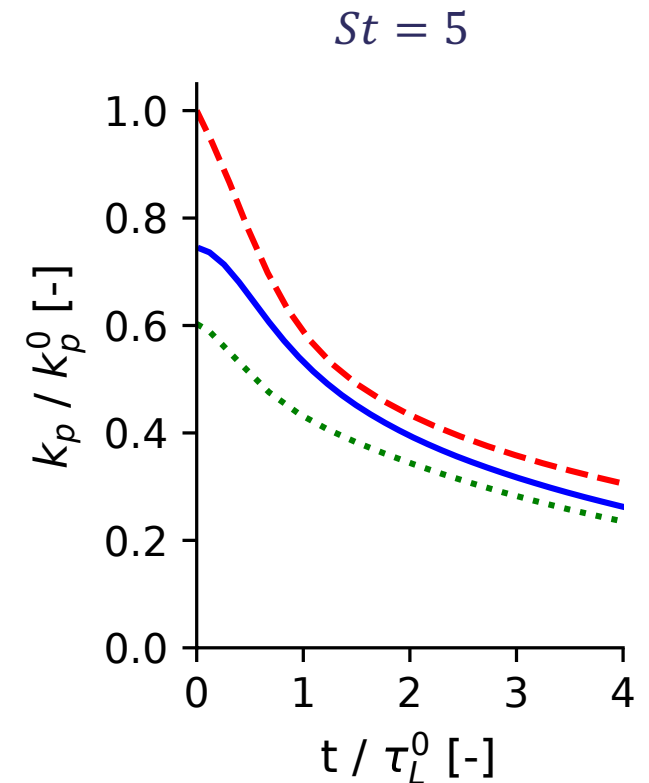
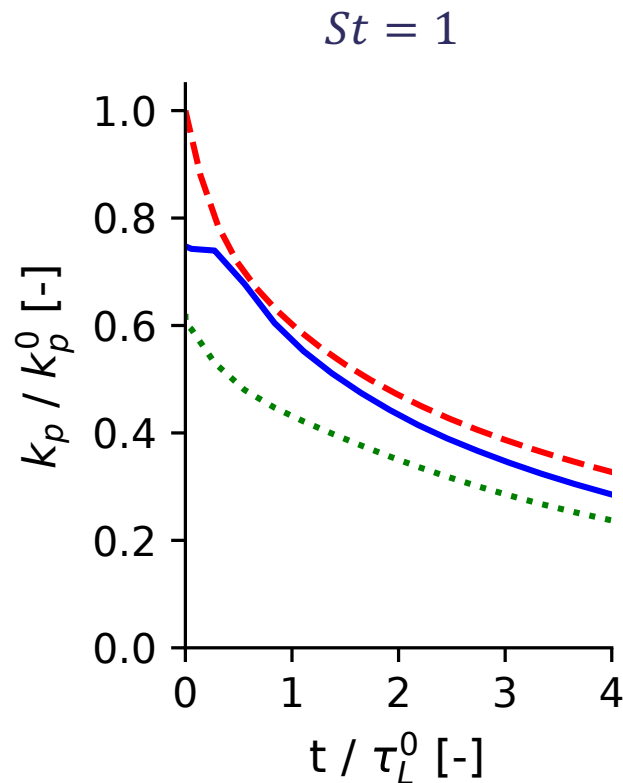
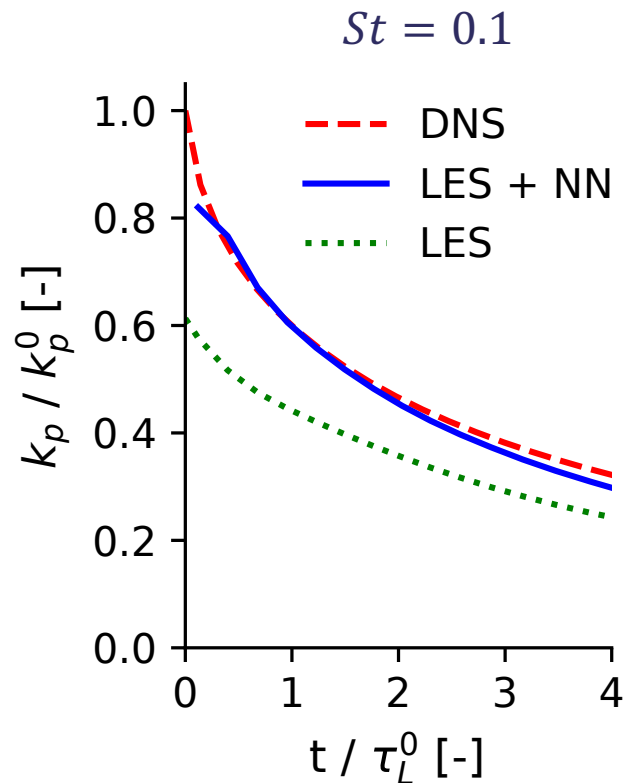
# Tracer velocity statistics (*a posteriori*)

Initial condition  $\mathbf{u}_p^0 = \mathbf{u}_f^0$ , but in LES we only have filtered fields. So,  $\tilde{\mathbf{u}}_f^0 + \sqrt{2k_{sgs}/3}\xi$



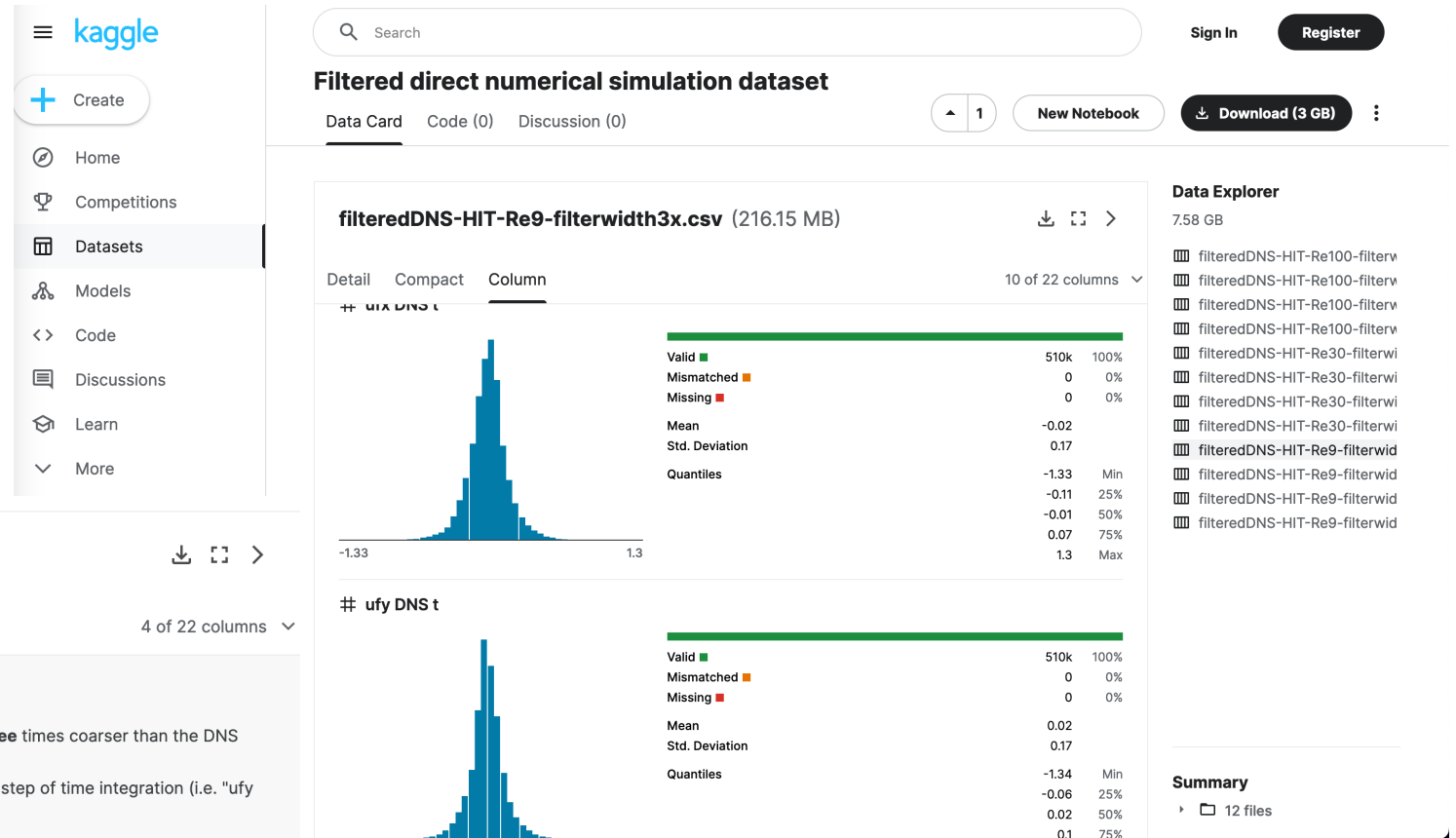
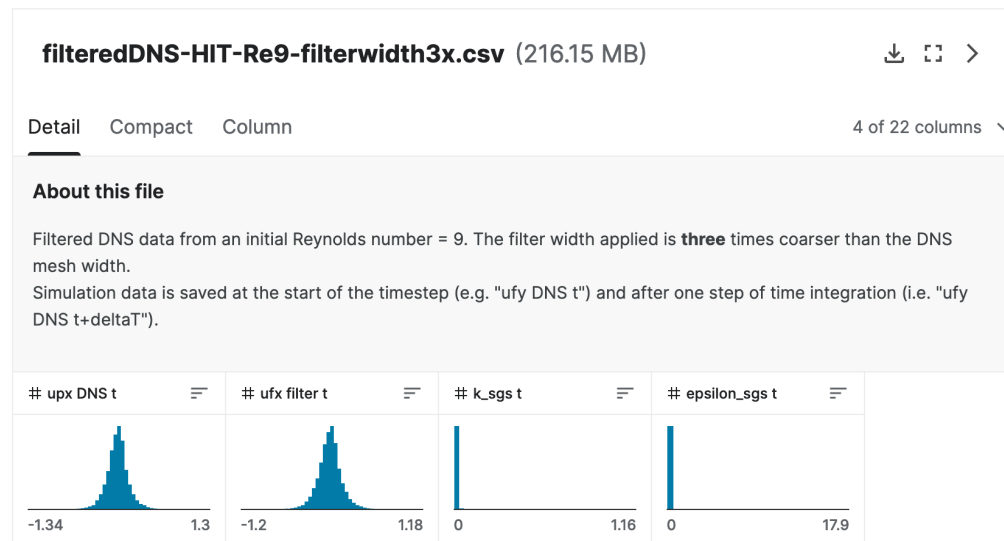
# Inertial particle kinetic energy

Parameters:  $k_p = \frac{1}{2} \text{tr}(\mathbf{u}_p \otimes \mathbf{u}_p)^2$ ,  $Re_\lambda^0 = 33$ ,  $N_{cell} = 36^3$ ,  $St = \tau_p / \tau_L^0$ .



# Open science

- Data shared on Kaggle.
- Python + OpenFOAM code on Github.
- Integrated platform for code + data?





# Conclusions

- Developed approach for data-driven modelling based on highly-resolved simulation data.
- NN model improves predictions of particle velocity in unbounded flows.
- Include complex physics (data-driven models for collisions, cohesion, etc).
- Code + pre-trained model shared on Github, data shared on Kaggle (seems rare).
- How to share best-practices? CFD has e.g. OpenFOAM workshop, not much in ML for fluid dynamics.
- **Take home message:** Data-driven modelling can provide more efficient and faster simulations (coarser mesh).

# Acknowledgements

- Dr Uwe Wolfram and Dr Ali Ozel (HWU).
- Carnegie-Trust for the Universities of Scotland (PhD scholarship).
- Open Clouds for Research Environments (cloud computing credits).



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# Thank you

Physics of Fluids

ARTICLE

[scitation.org/journal/phf](https://scitation.org/journal/phf)

## Neural stochastic differential equations for particle dispersion in large-eddy simulations of homogeneous isotropic turbulence

Cite as: Phys. Fluids **34**, 113315 (2022); doi: [10.1063/5.0121344](https://doi.org/10.1063/5.0121344)

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**Twitter:** [@joshwill\\_96](https://twitter.com/joshwill_96)

**Website:** [jvwilliams23.github.io](https://jvwilliams23.github.io)

All code available!

# Forward pass code, keras2cpp

```
//define model objects and compute prediction for drift_flux
keras::KerasModel DFnnModel_("Model/DFkerasParameters.nnet", false);
keras::DataChunkFlat dataChunk( num_features, 0.0);
vector<float>& features = dataChunk.get_1d_rw();
float scaled_dimless_drift_flux = 1.0e-6;
float drift_flux = 1.0e-6;
//collect features and normalize the features using mean and std input
unsigned int index = 0;
features.clear();
features.push_back((Reynolds_number - means_[index])/stds_[index]);
++index;
features.push_back((dimless_filter_size - means_[index])/stds_[index]);
++index;
features.push_back((scaled_solid_volume_fraction - means_[index])/stds_[index]);
++index;
features.push_back((dimless_grad_P - means_[index])/stds_[index]);
++index;
features.push_back((dimless_slip_velocity - means_[index])/stds_[index]);

//compute prediction
vector<float> prediction = DFnnModel_.compute_output( &dataChunk );
```