

i) 对于省间市场出清模型，将其原变量和对偶变量表示为：

$$\begin{aligned}
& \min \sum_{t=1}^T \left( \sum_{i=1}^I \sum_{k=1}^K \alpha_{i,k}^2 P_{i,t,k}^2 - \sum_{j=1}^J \sum_{k=1}^K \beta_{j,k}^2 D_{j,t,k}^2 \right) \\
& P_{r,t} = \sum_{i \in X_r} \sum_{k=1}^K P_{i,t,k}^2 - \sum_{j \in Y_r} \sum_{k=1}^K D_{j,t,k}^2 : \pi_{r,t}^2 \\
& - \sum_{l \in Z_r} \bar{P}_l^{Ex} \leq P_{r,t} \leq \sum_{l \in Z_r} \bar{P}_l^{Ex} : \tau_{r,t}^{Ex, \min}, \tau_{r,t}^{Ex, \max} \\
& 0 \leq P_{i,t,k}^2 \leq \bar{P}_{i,k}^2 : \zeta_{i,t,k}^{G2, \min}, \zeta_{i,t,k}^{G2, \max} \\
& 0 \leq D_{j,t,k}^2 \leq \bar{D}_{j,k}^2 : \zeta_{j,t,k}^{D2, \min}, \zeta_{j,t,k}^{D2, \max}
\end{aligned}$$

上述问题的形式为线性规划问题，其拉格朗日函数可以表示为：

$$\begin{aligned}
L = & \sum_{t=1}^T \left( \sum_{i=1}^I \sum_{k=1}^K \alpha_{i,k}^2 P_{i,t,k}^2 - \sum_{j=1}^J \sum_{k=1}^K \beta_{j,k}^2 D_{j,t,k}^2 \right) \\
& + \sum_{t=1}^T \sum_{r=1}^R \pi_{r,t}^2 (P_{r,t} - \sum_{i \in X_r} \sum_{k=1}^K P_{i,t,k}^2 + \sum_{j \in Y_r} \sum_{k=1}^K D_{j,t,k}^2) \\
& - \sum_{t=1}^T \sum_r \tau_{r,t}^{Ex, \min} (P_{r,t} + \sum_{l \in Z_r} \bar{P}_l^{Ex}) \\
& + \sum_{t=1}^T \sum_r \tau_{r,t}^{Ex, \max} (P_{r,t} - \sum_{l \in Z_r} \bar{P}_l^{Ex}) \\
& + \sum_{t=1}^T \sum_{i=1}^I \sum_{k=1}^K \zeta_{i,t,k}^{G2, \max} (P_{i,t,k}^2 - \bar{P}_{i,k}^2) \\
& + \sum_{t=1}^T \sum_{j=1}^J \sum_{k=1}^K \zeta_{j,t,k}^{D2, \max} (D_{j,t,k}^2 - \bar{D}_{j,k}^2) \\
& - \sum_{t=1}^T \sum_{i=1}^I \sum_{k=1}^K \zeta_{i,t,k}^{G2, \min} P_{i,t,k}^2 \\
& - \sum_{t=1}^T \sum_{j=1}^J \sum_{k=1}^K \zeta_{j,t,k}^{D2, \min} D_{j,t,k}^2
\end{aligned}$$

其最优性条件可以表示为：

（原始可行）：

$$\begin{aligned}
P_{r,t} &= \sum_{i \in X_r} \sum_{k=1}^K P_{i,t,k}^2 - \sum_{j \in Y_r} \sum_{k=1}^K D_{j,t,k}^2 \\
- \sum_{l \in Z_r} \bar{P}_l^{Ex} &\leq P_{r,t} \leq \sum_{l \in Z_r} \bar{P}_l^{Ex} \\
0 &\leq P_{i,t,k}^2 \leq \bar{P}_{i,k}^2 \\
0 &\leq D_{j,t,k}^2 \leq \bar{D}_{j,k}^2
\end{aligned}$$

（对偶可行）：

$$\alpha_{i,k}^2 - \pi_{r,t}^2 + \zeta_{i,t,k}^{G2, \max} - \zeta_{i,t,k}^{G2, \min} = 0$$

$$\begin{aligned}
-\beta_{j,k}^2 + \pi_{r,t}^2 + \zeta_{j,t,k}^{D2,\max} - \zeta_{j,t,k}^{D2,\min} &= 0 \\
\pi_{r,t}^2 - \tau_{r,t}^{Ex,\min} + \tau_{r,t}^{Ex,\max} &= 0 \\
\tau_{r,t}^{Ex,\min}, \tau_{r,t}^{Ex,\max} &\geq 0 \\
\zeta_{i,t,k}^{G2,\max}, \zeta_{i,t,k}^{G2,\min} &\geq 0 \\
\zeta_{j,t,k}^{D2,\max}, \zeta_{j,t,k}^{D2,\min} &\geq 0
\end{aligned}$$

(强对偶条件):

$$\begin{aligned}
&\sum_{t=1}^T (\sum_{i=1}^I \sum_{k=1}^K \alpha_{i,k}^2 P_{i,t,k}^2 - \sum_{j=1}^J \sum_{k=1}^K \beta_{j,k}^2 D_{j,t,k}^2) - \sum_{t=1}^T \sum_r \tau_r^{Ex,\min} \sum_{l \in Z_r} \bar{P}_{l,t}^{Ex} - \sum_{t=1}^T \sum_r \tau_r^{Ex,\max} \sum_{l \in Z_r} \bar{P}_{l,t}^{Ex} \\
&- \sum_{t=1}^T \sum_{i=1}^I \sum_{k=1}^K \zeta_{i,t,k}^{G2,\max} \bar{P}_{i,k}^2 - \sum_{t=1}^T \sum_{j=1}^J \sum_{k=1}^K \zeta_{j,t,k}^{D2,\max} \bar{D}_{j,k}^2 = 0
\end{aligned}$$

ii) 对于省内市场出清模型, 将其原变量和对偶变量表示为:

$$\begin{aligned}
\min &\sum_{t=1}^T (\sum_{i=1}^I \sum_{k=1}^K \alpha_{i,k}^1 P_{i,t,k}^1 - \sum_{j=1}^J \sum_{k=1}^K \beta_{j,k}^1 D_{j,t,k}^1) \\
P_{i,t} &= \sum_{k=1}^K P_{i,t,k}^1 + \sum_{k=1}^K P_{i,t,k}^2 : \chi_{i,t}^G \\
D_{j,t} &= \sum_{k=1}^K D_{j,t,k}^1 + \sum_{k=1}^K D_{j,t,k}^2 : \chi_{j,t}^D \\
\sum_{i \in \Psi_n} P_{i,t} - \sum_{j \in \Phi_n} D_{j,t} &= \sum_{l \in O_n} P_{l,t} - \sum_{l \in I_n} P_{l,t} + \sum_{l \in Co_n} P_{l,t}^{Ex} - \sum_{l \in Ci_n} P_{l,t}^{Ex} : \pi_{n,t}^1 \\
0 \leq P_{i,t,k}^1 &\leq \bar{P}_{i,k}^1 : \zeta_{i,t,k}^{G1,\min}, \zeta_{i,t,k}^{G1,\max} \\
0 \leq D_{j,t,k}^1 &\leq \bar{D}_{j,k}^1 : \zeta_{j,t,k}^{D1,\min}, \zeta_{j,t,k}^{D1,\max} \\
-P_i^{rp} \leq P_{i,t} - P_{i,t+1} &\leq P_i^{rp} : \eta_{i,t}^{\min}, \eta_{i,t}^{\max} \\
P_{l,t} &= \sum_{n=1}^N G_{l-n} (\sum_{i \in \Psi_n} P_{i,t} - \sum_{j \in \Phi_n} D_{j,t}) : \vartheta_{l,t} \\
-\bar{P}_l \leq P_{l,t} &\leq \bar{P}_l : \tau_{l,t}^{\min}, \tau_{l,t}^{\max}
\end{aligned}$$

类似地, 上述问题的形式同样为线性规划问题, 其拉格朗日函数可以表示为:

$$\begin{aligned}
L = & \sum_{t=1}^T \left( \sum_{i=1}^I \sum_{k=1}^K \alpha_{i,k}^1 P_{i,t,k}^1 - \sum_{j=1}^J \sum_{k=1}^K \beta_{j,k}^1 D_{j,t,k}^1 \right) \\
& + \sum_{t=1}^T \sum_{i=1}^I \chi_{i,t}^G (P_{i,t} - \sum_{k=1}^K P_{i,t,k}^1 - \sum_{k=1}^K P_{i,t,k}^2) \\
& + \sum_{t=1}^T \sum_{j=1}^J \chi_{j,t}^D (D_{j,t} - \sum_{k=1}^K D_{j,t,k}^1 - \sum_{k=1}^K D_{j,t,k}^2) \\
& + \sum_{t=1}^T \sum_{n=1}^N \pi_{n,t}^1 \left( \sum_{j \in \Phi_n} D_{j,t} - \sum_{i \in \Psi_n} P_{i,t} + \sum_{l \in O_n} P_{l,t} - \sum_{l \in I_n} P_{l,t} + \sum_{l \in Co_n} P_{l,t}^{Ex} - \sum_{l \in Ci_n} P_{l,t}^{Ex} \right) \\
& + \sum_{t=1}^T \sum_{l=1}^L \vartheta_{l,t} (P_{l,t} - \sum_{n=1}^N G_{l-n} (\sum_{i \in \Psi_n} P_{i,t} - \sum_{j \in \Phi_n} D_{j,t})) \\
& - \sum_{t=1}^T \sum_{i=1}^I \sum_{k=1}^K \zeta_{i,t,k}^{G1,\min} P_{i,t,k}^1 \\
& + \sum_{t=1}^T \sum_{i=1}^I \sum_{k=1}^K \zeta_{i,t,k}^{G1,\max} (P_{i,t,k}^1 - \bar{P}_{i,k}^1) \\
& - \sum_{t=1}^T \sum_{j=1}^J \sum_{k=1}^K \zeta_{j,t,k}^{D1,\min} D_{j,t,k}^1 \\
& + \sum_{t=1}^T \sum_{j=1}^J \sum_{k=1}^K \zeta_{j,t,k}^{D1,\max} (D_{j,t,k}^1 - \bar{D}_{j,k}^1) \\
& - \sum_{t=1}^T \sum_{i=1}^I \eta_{i,t}^{\min} (P_{i,t} - P_{i,t+1} + P_i^{rp}) \\
& + \sum_{t=1}^T \sum_{i=1}^I \eta_{i,t}^{\max} (P_{i,t} - P_{i,t+1} - P_i^{rp}) \\
& - \sum_{t=1}^T \sum_{l=1}^L \tau_{l,t}^{\min} (P_{l,t} + \bar{P}_l) \\
& + \sum_{t=1}^T \sum_{l=1}^L \tau_{l,t}^{\max} (P_{l,t} - \bar{P}_l)
\end{aligned}$$

其最优性条件可以表示为：

（原始可行）：

$$\begin{aligned}
P_{i,t} &= \sum_{k=1}^K P_{i,t,k}^1 + \sum_{k=1}^K P_{i,t,k}^2 \\
D_{j,t} &= \sum_{k=1}^K D_{j,t,k}^1 + \sum_{k=1}^K D_{j,t,k}^2 \\
\sum_{i \in \Psi_n} P_{i,t} - \sum_{j \in \Phi_n} D_{j,t} &= \sum_{l \in O_n} P_{l,t} - \sum_{l \in I_n} P_{l,t} + \sum_{l \in Co_n} P_{l,t}^{Ex} - \sum_{l \in Ci_n} P_{l,t}^{Ex} \\
0 &\leq P_{i,t,k}^1 \leq \bar{P}_{i,k}^1 \\
0 &\leq D_{j,t,k}^1 \leq \bar{D}_{j,k}^1
\end{aligned}$$

$$\begin{aligned}
-P_i^{rp} &\leq P_{i,t} - P_{i,t+1} \leq P_i^{rp} \\
P_{l,t} &= \sum_{n=1}^N G_{l-n} \left( \sum_{i \in \Psi_n} P_{i,t} - \sum_{j \in \Phi_n} D_{j,t} \right) \\
-\bar{P}_l &\leq P_{l,t} \leq \bar{P}_l
\end{aligned}$$

(对偶可行):

$$\begin{aligned}
\alpha_{i,k}^1 - \chi_{i,t}^G - \zeta_{i,t,k}^{G1,\min} + \zeta_{i,t,k}^{G1,\max} &= 0 \\
-\beta_{j,k}^1 - \chi_{j,t}^D - \zeta_{i,t,k}^{D1,\min} + \zeta_{i,t,k}^{D1,\max} &= 0 \\
\chi_{i,t}^G - \pi_{n,t}^1 - \sum_{l=1}^L \mathcal{G}_{l,t} G_{l-n} - \eta_{i,t}^{\min} + \eta_{i,t}^{\max} + \eta_{i,t-1}^{\min} - \eta_{i,t-1}^{\max} &= 0, i \in \Psi_n \\
\chi_{j,t}^D + \pi_{n,t}^1 + \sum_{l=1}^L \mathcal{G}_{l,t} G_{l-n} &= 0, j \in \Phi_n \\
\mathcal{G}_{l,t} + \pi_{x,t}^1 - \pi_{y,t}^1 - \tau_{l,t}^{\min} + \tau_{l,t}^{\max} &= 0, l \in O_x, l \in I_y \\
\zeta_{i,t,k}^{G1,\min}, \zeta_{i,t,k}^{G1,\max} &\geq 0 \\
\zeta_{j,t,k}^{D1,\min}, \zeta_{j,t,k}^{D1,\max} &\geq 0 \\
\eta_{i,t}^{\min}, \eta_{i,t}^{\max} &\geq 0 \\
\tau_{l,t}^{\min}, \tau_{l,t}^{\max} &\geq 0
\end{aligned}$$

(强对偶条件):

$$\begin{aligned}
&\sum_{t=1}^T \left( \sum_{i=1}^I \sum_{k=1}^K \alpha_{i,k}^1 P_{i,t,k}^1 - \sum_{j=1}^J \sum_{k=1}^K \beta_{j,k}^1 D_{j,t,k}^1 \right) + \sum_{t=1}^T \sum_{n=1}^N \pi_{n,t}^1 \left( \sum_{l \in Co_n} P_{l,t}^{Ex} - \sum_{l \in Ci_n} P_{l,t}^{Ex} \right) \\
&- \sum_{t=1}^T \sum_{i=1}^I \sum_{k=1}^K \zeta_{i,t,k}^{G1,\max} \bar{P}_{i,k}^1 - \sum_{t=1}^T \sum_{j=1}^J \sum_{k=1}^K \zeta_{j,t,k}^{D1,\max} \bar{D}_{j,k}^1 - \sum_{t=1}^T \sum_{i=1}^I \eta_{i,t}^{\min} P_i^{rp} - \sum_{t=1}^T \sum_{i=1}^I \eta_{i,t}^{\max} P_i^{rp} \\
&- \sum_{t=1}^T \sum_{l=1}^L \tau_{l,t}^{\min} \bar{P}_l - \sum_{t=1}^T \sum_{l=1}^L \tau_{l,t}^{\max} \bar{P}_l = 0
\end{aligned}$$

iii) 对于参与市场的策略型发电商  $i$ , 其在两个市场中的投标决策问题即可转化为 MPEC 问题, 目标函数为最大化自身效益, 约束条件为自身报价约束和两个市场最优性条件。该 MPEC 问题及其对偶变量可以表示为

$$\begin{aligned}
\min &\sum_{t=1}^T \left( \sum_{k=1}^K \lambda_{i,k} P_{i,t,k} - \pi_{i,t}^1 \sum_{k=1}^K P_{i,t,k}^1 - \pi_{i,t}^2 \sum_{k=1}^K P_{i,t,k}^2 \right) \\
0 &= \alpha_{i,0}^1 < \alpha_{i,1}^1 < \alpha_{i,2}^1 < \dots < \alpha_{i,K}^1 : \omega_{i,k}^{\alpha,1} \\
0 &= \alpha_{i,0}^2 < \alpha_{i,1}^2 < \alpha_{i,2}^2 < \dots < \alpha_{i,K}^2 : \omega_{i,k}^{\alpha,2} \\
P_{i,t} &= \sum_{k=1}^K P_{i,t,k} : \rho_{i,t}^G \\
0 &\leq P_{i,t,k} \leq \bar{P}_{i,k} : \omega_{i,t,k}^{G\min,0}, \omega_{i,t,k}^{G\max,0} \\
P_{r,t} &= \sum_{i \in X_r} \sum_{k=1}^K P_{i,t,k}^2 - \sum_{j \in Y_r} \sum_{k=1}^K D_{j,t,k}^2 : \rho_{r,t}^2
\end{aligned}$$

$$\begin{aligned}
& -\sum_{l \in Z_r} \bar{P}_l^{Ex} \leq P_{r,t} \leq \sum_{l \in Z_r} \bar{P}_l^{Ex} : \omega_{r,t}^{l \min, 2}, \omega_{r,t}^{l \max, 2} \\
& 0 \leq P_{i,t,k}^2 \leq \bar{P}_{i,k}^2 : \omega_{i,t,k}^{G \min, 2}, \omega_{i,t,k}^{G \max, 2} \\
& 0 \leq D_{j,t,k}^2 \leq \bar{D}_{j,k}^2 : \omega_{j,t,k}^{D \min, 2}, \omega_{j,t,k}^{D \max, 2} \\
& \alpha_{i,k}^2 - \pi_{r,t}^2 + \zeta_{i,t,k}^{G2, \max} - \zeta_{i,t,k}^{G2, \min} = 0 : \gamma_{i,t,k}^{G, 2} \\
& -\beta_{j,k}^2 + \pi_{r,t}^2 + \zeta_{j,t,k}^{D2, \max} - \zeta_{j,t,k}^{D2, \min} = 0 : \gamma_{j,t,k}^{D, 2} \\
& \pi_{r,t}^2 - \tau_{r,t}^{Ex, \min} + \tau_{r,t}^{Ex, \max} = 0 : \gamma_{r,t}^{Ex} \\
& \tau_{r,t}^{Ex, \min}, \tau_{r,t}^{Ex, \max} \geq 0 : \gamma_{r,t}^{Ex, \min}, \gamma_{r,t}^{Ex, \max} \\
& \zeta_{i,t,k}^{G2, \max}, \zeta_{i,t,k}^{G2, \min} \geq 0 : \gamma_{i,t,k}^{G2, \min}, \gamma_{i,t,k}^{G2, \max} \\
& \zeta_{j,t,k}^{D2, \max}, \zeta_{j,t,k}^{D2, \min} \geq 0 : \gamma_{j,t,k}^{D2, \min}, \gamma_{j,t,k}^{D2, \max} \\
& \sum_{t=1}^T (\sum_{i=1}^I \sum_{k=1}^K \alpha_{i,k}^2 P_{i,t,k}^2 - \sum_{j=1}^J \sum_{k=1}^K \beta_{j,k}^2 D_{j,t,k}^2) - \sum_{t=1}^T \sum_r \tau_r^{Ex, \min} \sum_{l \in Z_r} \bar{P}_{l,t}^{Ex} - \sum_{t=1}^T \sum_r \tau_r^{Ex, \max} \sum_{l \in Z_r} \bar{P}_{l,t}^{Ex} \\
& - \sum_{t=1}^T \sum_{i=1}^I \sum_{k=1}^K \zeta_{i,t,k}^{G2, \max} \bar{P}_{i,k}^2 - \sum_{t=1}^T \sum_{j=1}^J \sum_{k=1}^K \zeta_{j,t,k}^{D2, \max} \bar{D}_{j,k}^2 = 0 : \gamma^{DT, 2} \\
& P_{i,t} = \sum_{k=1}^K P_{i,t,k}^1 + \sum_{k=1}^K P_{i,t,k}^2 : \rho_{i,t}^{G'} \\
& D_{j,t} = \sum_{k=1}^K D_{i,t,k}^1 + \sum_{k=1}^K D_{i,t,k}^2 : \rho_{j,t}^{D'} \\
& \sum_{i \in \Psi_n} P_{i,t} - \sum_{j \in \Phi_n} D_{j,t} = \sum_{l \in O_n} P_{l,t} - \sum_{l \in I_n} P_{l,t} + \sum_{l \in Co_n} P_{l,t}^{Ex} - \sum_{l \in Ci_n} P_{l,t}^{Ex} : \rho_n^1 \\
& 0 \leq P_{i,t,k}^1 \leq \bar{P}_{i,k}^1 : \omega_{i,t,k}^{G \min, 1}, \omega_{i,t,k}^{G \max, 1} \\
& 0 \leq D_{j,t,k}^1 \leq \bar{D}_{j,k}^1 : \omega_{j,t,k}^{D \min, 1}, \omega_{j,t,k}^{D \max, 1} \\
& -P_i^{rp} \leq P_{i,t} - P_{i,t+1} \leq P_i^{rp} : \omega_{i,t}^{rp \min}, \omega_{i,t}^{rp \max} \\
& P_{l,t} = \sum_{n=1}^N G_{l-n} (\sum_{i \in \Psi_n} P_{i,t} - \sum_{j \in \Phi_n} D_{j,t}) : \rho_{l,t}^L \\
& -\bar{P}_l \leq P_{l,t} \leq \bar{P}_l : \omega_{l,t}^{L \min}, \omega_{l,t}^{L \max} \\
& \alpha_{i,k}^1 - \chi_{i,t}^G - \zeta_{i,t,k}^{G1, \min} + \zeta_{i,t,k}^{G1, \max} = 0 : \gamma_{i,t,k}^{G, 1} \\
& -\beta_{j,k}^1 - \chi_{j,t}^D - \zeta_{i,t,k}^{D1, \min} + \zeta_{i,t,k}^{D1, \max} = 0 : \gamma_{j,t,k}^{D, 1} \\
& \chi_{i,t}^G - \pi_{n,t}^1 - \sum_{l=1}^L \mathcal{G}_{l,t} G_{l-n} - \eta_{i,t}^{\min} + \eta_{i,t}^{\max} + \eta_{i,t-1}^{\min} - \eta_{i,t-1}^{\max} = 0, i \in \Psi_n : \gamma_{i,t}^G \\
& \chi_{j,t}^D + \pi_{n,t}^1 + \sum_{l=1}^L \mathcal{G}_{l,t} G_{l-n} = 0, j \in \Phi_n : \gamma_{j,t}^D \\
& \mathcal{G}_{l,t} + \pi_{x,t}^1 - \pi_{y,t}^1 - \tau_{l,t}^{\min} + \tau_{l,t}^{\max} = 0, l \in O_x, l \in I_y : \gamma_{l,t}^L \\
& \zeta_{i,t,k}^{G1, \min}, \zeta_{i,t,k}^{G1, \max} \geq 0 : \gamma_{i,t,k}^{G1, \min}, \gamma_{i,t,k}^{G1, \max} \\
& \zeta_{j,t,k}^{D1, \min}, \zeta_{j,t,k}^{D1, \max} \geq 0 : \gamma_{j,t,k}^{D1, \min}, \gamma_{j,t,k}^{D1, \max} \\
& \eta_{i,t}^{\min}, \eta_{i,t}^{\max} \geq 0 : \gamma_{i,t}^{rp, \min}, \gamma_{i,t}^{rp, \max}
\end{aligned}$$

$$\begin{aligned}
& \tau_{l,t}^{\min}, \tau_{l,t}^{\max} \geq 0 : \gamma_{l,t}^{L,\min}, \gamma_{l,t}^{L,\max} \\
& \sum_{t=1}^T \left( \sum_{i=1}^I \sum_{k=1}^K \alpha_{i,k}^1 P_{i,t,k}^1 - \sum_{j=1}^J \sum_{k=1}^K \beta_{j,k}^1 D_{j,t,k}^1 \right) + \sum_{t=1}^T \sum_{n=1}^N \pi_{n,t}^1 \left( \sum_{l \in Co_n} P_{l,t}^{Ex} - \sum_{l \in Ci_n} P_{l,t}^{Ex} \right) \\
& - \sum_{t=1}^T \sum_{i=1}^I \sum_{k=1}^K \zeta_{i,t,k}^{G1,\max} \bar{P}_{i,k}^1 - \sum_{t=1}^T \sum_{j=1}^J \sum_{k=1}^K \zeta_{j,t,k}^{D1,\max} \bar{D}_{j,k}^1 - \sum_{t=1}^T \sum_{i=1}^I \eta_{i,t}^{\min} P_i^{rp} - \sum_{t=1}^T \sum_{i=1}^I \eta_{i,t}^{\max} P_i^{rp} \\
& - \sum_{t=1}^T \sum_{l=1}^L \tau_{l,t}^{\min} \bar{P}_l - \sum_{t=1}^T \sum_{l=1}^L \tau_{l,t}^{\max} \bar{P}_l = 0 : \gamma^{DT,1}
\end{aligned}$$

iv) 对于每一个市场参与者（市场主体），可以建立其优化决策模型的拉格朗日函数，并列写其 KKT 条件：

（原始可行）：

$$\begin{aligned}
& 0 = \alpha_{i,0}^1 < \alpha_{i,1}^1 < \alpha_{i,2}^1 < \dots < \alpha_{i,K}^1 \\
& 0 = \alpha_{i,0}^2 < \alpha_{i,1}^2 < \alpha_{i,2}^2 < \dots < \alpha_{i,K}^2 \\
& \beta_{j,1}^1 > \beta_{j,2}^1 > \dots > \beta_{j,K}^1 > \beta_{j,0}^1 = 0 \\
& \beta_{j,1}^2 > \beta_{j,2}^2 > \dots > \beta_{j,K}^2 > \beta_{j,0}^2 = 0 \\
& P_{r,t} = \sum_{i \in X_r} \sum_{k=1}^K P_{i,t,k}^2 - \sum_{j \in Y_r} \sum_{k=1}^K D_{j,t,k}^2 \\
& - \sum_{l \in Z_r} \bar{P}_l^{Ex} \leq P_{r,t} \leq \sum_{l \in Z_r} \bar{P}_l^{Ex} \\
& 0 \leq P_{i,t,k}^2 \leq \bar{P}_{i,k}^2 \\
& 0 \leq D_{j,t,k}^2 \leq \bar{D}_{j,k}^2 \\
& \alpha_{i,k}^2 - \pi_{r,t}^2 + \zeta_{i,t,k}^{G2,\max} - \zeta_{i,t,k}^{G2,\min} = 0 \\
& -\beta_{j,k}^2 + \pi_{r,t}^2 + \zeta_{j,t,k}^{D2,\max} - \zeta_{j,t,k}^{D2,\min} = 0 \\
& \pi_{r,t}^2 - \tau_{r,t}^{Ex,\min} + \tau_{r,t}^{Ex,\max} = 0 \\
& \tau_{r,t}^{Ex,\min}, \tau_{r,t}^{Ex,\max} \geq 0 \\
& \zeta_{i,t,k}^{G2,\max}, \zeta_{i,t,k}^{G2,\min} \geq 0 \\
& \zeta_{j,t,k}^{D2,\max}, \zeta_{j,t,k}^{D2,\min} \geq 0 \\
& \sum_{t=1}^T \left( \sum_{i=1}^I \sum_{k=1}^K \alpha_{i,k}^2 P_{i,t,k}^2 - \sum_{j=1}^J \sum_{k=1}^K \beta_{j,k}^2 D_{j,t,k}^2 \right) - \sum_{t=1}^T \sum_r \tau_r^{Ex,\min} \sum_{l \in Z_r} \bar{P}_l^{Ex} - \sum_{t=1}^T \sum_r \tau_r^{Ex,\max} \sum_{l \in Z_r} \bar{P}_l^{Ex} \\
& - \sum_{t=1}^T \sum_{i=1}^I \sum_{k=1}^K \zeta_{i,t,k}^{G,\max} \bar{P}_{i,k}^2 - \sum_{t=1}^T \sum_{j=1}^J \sum_{k=1}^K \zeta_{j,t,k}^{D,\max} \bar{D}_{j,k}^2 = 0 \\
& P_{i,t} = \sum_{k=1}^K P_{i,t,k}^1 + \sum_{k=1}^K P_{i,t,k}^2 \\
& D_{j,t} = \sum_{k=1}^K D_{j,t,k}^1 + \sum_{k=1}^K D_{j,t,k}^2 \\
& \sum_{i \in \Psi_n} P_{i,t} - \sum_{j \in \Phi_n} D_{j,t} = \sum_{l \in O_n} P_{l,t} - \sum_{l \in I_n} P_{l,t} + \sum_{l \in Co_n} P_{l,t}^{Ex} - \sum_{l \in Ci_n} P_{l,t}^{Ex}
\end{aligned}$$

$$\begin{aligned}
0 &\leq P_{i,t,k}^1 \leq \bar{P}_{i,k}^1 \\
0 &\leq D_{j,t,k}^1 \leq \bar{D}_{j,k}^1 \\
-P_i^{rp} &\leq P_{i,t} - P_{i,t+1} \leq P_i^{rp} \\
P_{l,t} &= \sum_{n=1}^N G_{l-n} \left( \sum_{i \in \Psi_n} P_{i,t} - \sum_{j \in \Phi_n} D_{j,t} \right) \\
-\bar{P}_l &\leq P_{l,t} \leq \bar{P}_l \\
\alpha_{i,k}^1 - \chi_{i,t}^G - \zeta_{i,t,k}^{G1,\min} + \zeta_{i,t,k}^{G1,\max} &= 0 \\
-\beta_{j,k}^1 - \chi_{j,t}^D - \zeta_{j,t,k}^{D1,\min} + \zeta_{j,t,k}^{D1,\max} &= 0 \\
\chi_{i,t}^G - \pi_{n,t}^1 - \sum_{l=1}^L \mathcal{G}_{l,t} G_{l-n} - \eta_{i,t}^{\min} + \eta_{i,t}^{\max} + \eta_{i,t-1}^{\min} - \eta_{i,t-1}^{\max} &= 0, i \in \Psi_n \\
\chi_{j,t}^D + \pi_{n,t}^1 + \sum_{l=1}^L \mathcal{G}_{l,t} G_{l-n} &= 0, j \in \Phi_n \\
\mathcal{G}_{l,t} + \pi_{x,t}^1 - \pi_{y,t}^1 - \tau_{l,t}^{\min} + \tau_{l,t}^{\max} &= 0, l \in O_x, l \in I_y \\
\zeta_{i,t,k}^{G1,\min}, \zeta_{i,t,k}^{G1,\max} &\geq 0 \\
\zeta_{j,t,k}^{D1,\min}, \zeta_{j,t,k}^{D1,\max} &\geq 0 \\
\eta_{i,t}^{\min}, \eta_{i,t}^{\max} &\geq 0 \\
\tau_{l,t}^{\min}, \tau_{l,t}^{\max} &\geq 0 \\
\sum_{t=1}^T \left( \sum_{i=1}^I \sum_{k=1}^K \alpha_{i,k}^1 P_{i,t,k}^1 - \sum_{j=1}^J \sum_{k=1}^K \beta_{j,k}^1 D_{j,t,k}^1 \right) &+ \sum_{t=1}^T \sum_{n=1}^N \pi_{n,t}^1 \left( \sum_{l \in Co_n} P_{l,t}^{Ex} - \sum_{l \in Ci_n} P_{l,t}^{Ex} \right) \\
- \sum_{t=1}^T \sum_{i=1}^I \sum_{k=1}^K \zeta_{i,t,k}^{G1,\max} \bar{P}_{i,k}^1 - \sum_{t=1}^T \sum_{j=1}^J \sum_{k=1}^K \zeta_{j,t,k}^{D1,\max} \bar{D}_{j,k}^1 - \sum_{t=1}^T \sum_{i=1}^I \eta_{i,t}^{\min} P_i^{rp} - \sum_{t=1}^T \sum_{i=1}^I \eta_{i,t}^{\max} P_i^{rp} \\
- \sum_{t=1}^T \sum_{l=1}^L \tau_{l,t}^{\min} \bar{P}_l - \sum_{t=1}^T \sum_{l=1}^L \tau_{l,t}^{\max} \bar{P}_l &= 0
\end{aligned}$$

(对偶可行):

$$\begin{aligned}
\frac{\partial L}{\partial P_{i,t,k}} &= \lambda_{i,k} - \rho_{i,t}^G - \omega_{i,t,k}^{G\min,0} + \omega_{i,t,k}^{G\max,0} = 0 \\
\frac{\partial L}{\partial P_{i,t,k}^1} &= -\pi_{i,t}^1 - \rho_{i,t}^{G'} - \omega_{i,t,k}^{G\min,1} + \omega_{i,t,k}^{G\max,1} + \alpha_{i,k}^1 \gamma^{DT,1} = 0 \\
\frac{\partial L}{\partial P_{i,t,k}^2} &= -\pi_{i,t}^2 - \rho_{i,t}^{r,2} - \rho_{i,t}^{G'} - \omega_{i,t,k}^{G\min,2} + \omega_{i,t,k}^{G\max,2} + \alpha_{i,k}^2 \gamma^{DT,2} = 0 \\
\frac{\partial L}{\partial \alpha_{i,k}^1} &= -\omega_{i,k}^{\alpha,1} + \omega_{i,k-1}^{\alpha,1} + \sum_{t=1}^T \gamma_{i,t,k}^{G,1} + \gamma^{DT,1} \sum_{t=1}^T P_{i,t,k}^1 = 0 \\
\frac{\partial L}{\partial \alpha_{i,k}^2} &= -\omega_{i,k}^{\alpha,2} + \omega_{i,k-1}^{\alpha,2} + \sum_{t=1}^T \gamma_{i,t,k}^{G,2} + \gamma^{DT,2} \sum_{t=1}^T P_{i,t,k}^2 = 0 \\
\frac{\partial L}{\partial D_{j,t,k}} &= -\mu_{j,k} - \rho_{j,t}^D - \omega_{j,t,k}^{D\min,0} + \omega_{j,t,k}^{D\max,0} = 0
\end{aligned}$$

$$\begin{aligned}
\frac{\partial L}{\partial D_{j,t,k}^1} &= \pi_{j,t}^1 - \rho_{i,t}^{D'} - \omega_{i,t,k}^{D\min,1} + \omega_{i,t,k}^{G\max,1} - \beta_{i,k}^1 \gamma^{DT,1} = 0 \\
\frac{\partial L}{\partial D_{j,t,k}^2} &= \pi_{i,t}^2 + \rho_{r,t}^2 - \rho_{i,t}^{D'} - \omega_{j,t,k}^{D\min,2} + \omega_{j,t,k}^{D\max,2} - \beta_{j,k}^2 \gamma^{DT,2} = 0 \\
\frac{\partial L}{\partial \beta_{j,k}^1} &= \omega_{j,k}^{\beta,1} - \omega_{j,k-1}^{\beta,1} - \sum_{t=1}^T \gamma_{j,t,k}^{D,1} - \gamma^{DT,1} \sum_{t=1}^T D_{j,t,k}^1 = 0 \\
\frac{\partial L}{\partial \beta_{j,k}^2} &= \omega_{j,k}^{\beta,2} + \omega_{j,k-1}^{\beta,2} - \sum_{t=1}^T \gamma_{j,t,k}^{D,2} - \gamma^{DT,2} \sum_{t=1}^T D_{j,t,k}^2 = 0 \\
\frac{\partial L}{\partial \pi_{n,t}^1} &= -\sum_{k=1}^K P_{i,t,k}^1 - \sum_{k=1}^K \gamma_{i,t,k}^G + \sum_{l=O_n} \gamma_{l,t}^L - \sum_{l=I_n} \gamma_{l,t}^L + \gamma^{DT,1} (\sum_{l \in Co_n} P_{l,t}^{Ex} - \sum_{l \in Ci_n} P_{l,t}^{Ex}) = 0, i \in \Psi_n \\
\frac{\partial L}{\partial \pi_{n,t}^1} &= \sum_{k=1}^K D_{j,t,k}^1 - \sum_{k=1}^K \gamma_{j,t,k}^D + \sum_{l=O_n} \gamma_{l,t}^L - \sum_{l=I_n} \gamma_{l,t}^L + \gamma^{DT,1} (\sum_{l \in Co_n} P_{l,t}^{Ex} - \sum_{l \in Ci_n} P_{l,t}^{Ex}) = 0, j \in \Phi_n \\
\frac{\partial L}{\partial \pi_{r,t}^2} &= -\sum_{k=1}^K P_{i,t,k}^2 - \sum_{k=1}^K \gamma_{i,t,k}^{G,2} + \gamma_{r,t}^{Ex} = 0, i \in \Psi_r \\
\frac{\partial L}{\partial \pi_{r,t}^2} &= \sum_{k=1}^K D_{j,t,k}^2 + \sum_{k=1}^K \gamma_{j,t,k}^{D,2} + \gamma_{r,t}^{Ex} = 0, i \in \Phi_r \\
\frac{\partial L}{\partial P_{i,t}} &= \rho_{i,t}^G + \rho_{i,t}^{G'} + \rho_{n,t}^1 + \omega_{i,t}^{rp\min} - \omega_{i,t}^{rp\max} - \sum_{l \in O_n \text{ or } l \in I_n} \rho_{l,t}^L G_{l-n} = 0 \\
\frac{\partial L}{\partial D_{j,t}} &= \rho_{j,t}^D + \rho_{j,t}^{D'} - \rho_{n,t}^1 + \sum_{l \in O_n \text{ or } l \in I_n} \rho_{l,t}^L G_{l-n} = 0 \\
\frac{\partial L}{\partial P_{r,t}} &= \rho_{r,t}^2 - \omega_{r,t}^{l\min,2} + \omega_{r,t}^{l\max,2} = 0 \\
\frac{\partial L}{\partial \zeta_{i,t,k}^{G2,\max}} &= \gamma_{i,t,k}^{G,2} - \gamma_{i,t,k}^{G2,\max} - \gamma^{DT,2} \bar{P}_{i,k}^2 = 0 \\
\frac{\partial L}{\partial \zeta_{i,t,k}^{G2,\min}} &= -\gamma_{i,t,k}^{G,2} - \gamma_{i,t,k}^{G2,\min} = 0 \\
\frac{\partial L}{\partial \zeta_{j,t,k}^{D2,\max}} &= \gamma_{j,t,k}^{D,2} - \gamma_{j,t,k}^{D2,\max} - \gamma^{DT,2} P \bar{D}_{j,k}^2 = 0 \\
\frac{\partial L}{\partial \zeta_{j,t,k}^{D2,\min}} &= -\gamma_{j,t,k}^{D,2} - \gamma_{j,t,k}^{D2,\min} = 0 \\
\frac{\partial L}{\partial \tau_{r,t}^{Ex,\max}} &= \gamma_{r,t}^{Ex} - \gamma_{r,t}^{Ex,\max} - \gamma^{DT,2} \sum_{l \in Z_r} \bar{P}_{l,t}^{Ex} = 0 \\
\frac{\partial L}{\partial \tau_{r,t}^{Ex,\min}} &= -\gamma_{r,t}^{Ex} - \gamma_{r,t}^{Ex,\min} - \gamma^{DT,2} \sum_{l \in Z_r} \bar{P}_{l,t}^{Ex} = 0 \\
\frac{\partial L}{\partial P_{l,t}} &= \rho_{l,t}^L + \rho_{l,t}^1 - \rho_{y,t}^1 - \omega_{l,t}^{L\min} + \omega_{l,t}^{L\max} = 0, l \in O_x, l \in I_y
\end{aligned}$$



$$\begin{aligned}
\frac{\partial L}{\partial \chi_{i,t}^G} &= -\sum_{k=1}^K \gamma_{i,t,k}^{G,1} + \gamma_{i,t}^G = 0 \\
\frac{\partial L}{\partial \chi_{j,t}^D} &= -\sum_{k=1}^K \gamma_{j,t,k}^{D,1} + \gamma_{j,t}^D = 0 \\
\frac{\partial L}{\partial \zeta_{i,t,k}^{G1,\min}} &= -\gamma_{i,t,k}^{G,1} - \gamma_{i,t,k}^{G1,\min} = 0 \\
\frac{\partial L}{\partial \zeta_{i,t,k}^{G1,\max}} &= \gamma_{i,t,k}^{G,1} - \gamma_{i,t,k}^{G1,\max} - \gamma^{DT,1} \bar{P}_{i,k}^1 = 0 \\
\frac{\partial L}{\partial \zeta_{j,t,k}^{D1,\min}} &= -\gamma_{j,t,k}^{D,1} - \gamma_{j,t,k}^{D1,\min} = 0 \\
\frac{\partial L}{\partial \zeta_{j,t,k}^{D1,\max}} &= \gamma_{j,t,k}^{D,1} - \gamma_{j,t,k}^{D1,\max} - \gamma^{DT,1} \bar{D}_{j,k}^1 = 0 \\
\frac{\partial L}{\partial \eta_{i,t}^{\min}} &= -\gamma_{i,t}^G + \gamma_{i,t-1}^G - \gamma_{i,t}^{rp,\min} - \gamma^{DT,1} P_i^{rp} = 0 \\
\frac{\partial L}{\partial \eta_{i,t}^{\max}} &= \gamma_{i,t}^G - \gamma_{i,t-1}^G - \gamma_{i,t}^{rp,\max} - \gamma^{DT,1} P_i^{rp} = 0 \\
\frac{\partial L}{\partial \mathfrak{g}_{l,t}} &= \sum_{n=1}^N G_{l-n} \left( \sum_{j \in \Phi_n} \gamma_{j,t}^D - \sum_{i \in \Psi_n} \gamma_{i,t}^G \right) + \gamma_{l,t}^L = 0 \\
\frac{\partial L}{\partial \tau_{l,t}^{\min}} &= -\gamma_{l,t}^L - \gamma_{i,t}^{rp,\min} - \gamma^{DT,1} \bar{P}_l = 0 \\
\frac{\partial L}{\partial \tau_{l,t}^{\max}} &= \gamma_{l,t}^L - \gamma_{i,t}^{rp,\max} - \gamma^{DT,1} \bar{P}_l = 0
\end{aligned}$$

(互补松弛条件):

$$\begin{aligned}
\alpha_{i,k-1}^1 &\leq \alpha_{i,k-1}^1 \perp \omega_{i,k}^{\alpha,1} \geq 0 \\
\alpha_{i,k-1}^2 &\leq \alpha_{i,k-1}^2 \perp \omega_{i,k}^{\alpha,2} \geq 0 \\
\beta_{i,k-1}^1 &\geq \beta_{i,k-1}^1 \perp \omega_{i,k}^{\beta,1} \geq 0 \\
\beta_{i,k-1}^2 &\geq \beta_{i,k-1}^2 \perp \omega_{i,k}^{\beta,2} \geq 0 \\
0 &\leq P_{i,t,k} \perp \omega_{i,t,k}^{G\min,0} \geq 0 \\
P_{i,t,k} &\leq \bar{P}_{i,k} \perp \omega_{i,t,k}^{G\max,0} \geq 0 \\
-\sum_{l \in Z_r} \bar{P}_l^{Ex} &\leq P_{r,t} \perp \omega_{r,t}^{l\min,2} \geq 0 \\
P_{r,t} &\leq \sum_{l \in Z_r} \bar{P}_l^{Ex} \perp \omega_{r,t}^{l\max,2} \geq 0 \\
0 &\leq P_{i,t,k}^2 \perp \omega_{i,t,k}^{G\min,2} \geq 0 \\
P_{i,t,k}^2 &\leq \bar{P}_{i,k}^2 \perp \omega_{i,t,k}^{G\max,2} \geq 0 \\
0 &\leq D_{j,t,k}^2 \perp \omega_{j,t,k}^{D\min,2} \geq 0 \\
D_{j,t,k}^2 &\leq \bar{D}_{j,k}^2 \perp \omega_{j,t,k}^{D\max,2} \geq 0
\end{aligned}$$

$$\begin{aligned}
& \tau_{r,t}^{Ex,min} \geq 0 \perp \gamma_{r,t}^{Ex,min} \geq 0 \\
& \tau_{r,t}^{Ex,max} \geq 0 \perp \gamma_{r,t}^{Ex,max} \geq 0 \\
& \zeta_{i,t,k}^{G2,min} \geq 0 \perp \gamma_{i,t,k}^{G2,min} \geq 0 \\
& \zeta_{i,t,k}^{G2,max} \geq 0 \perp \gamma_{i,t,k}^{G2,max} \geq 0 \\
& \zeta_{j,t,k}^{D2,min} \geq 0 \perp \gamma_{j,t,k}^{D2,min} \geq 0 \\
& \zeta_{j,t,k}^{D2,max} \geq 0 \perp \gamma_{j,t,k}^{D2,max} \geq 0 \\
& 0 \leq P_{i,t,k}^1 \perp \omega_{i,t,k}^{Gmin,1} \geq 0 \\
& P_{i,t,k}^1 \leq \bar{P}_{i,k}^1 \perp \omega_{i,t,k}^{Gmax,1} \geq 0 \\
& 0 \leq D_{j,t,k}^1 \perp \omega_{j,t,k}^{Dmin,1} \geq 0 \\
& D_{j,t,k}^1 \leq \bar{D}_{j,k}^1 \perp \omega_{j,t,k}^{Dmax,1} \geq 0 \\
& -P_i^{rp} \leq P_{i,t} - P_{i,t+1} \perp \omega_{i,t}^{rp,min} \geq 0 \\
& P_{i,t} - P_{i,t+1} \leq P_i^{rp} \perp \omega_{i,t}^{rp,max} \geq 0 \\
& -\bar{P}_l \leq P_{l,t} \perp \omega_{l,t}^{L,min} \geq 0 \\
& P_{l,t} \leq \bar{P}_l \perp \omega_{l,t}^{L,max} \geq 0 \\
& \zeta_{i,t,k}^{G1,min} \geq 0 \perp \gamma_{i,t,k}^{G1,min} \geq 0 \\
& \zeta_{i,t,k}^{G1,max} \geq 0 \perp \gamma_{i,t,k}^{G1,max} \geq 0 \\
& \zeta_{j,t,k}^{D1,min} \geq 0 \perp \gamma_{j,t,k}^{D1,min} \geq 0 \\
& \zeta_{j,t,k}^{D1,max} \geq 0 \perp \gamma_{j,t,k}^{D1,max} \geq 0 \\
& \eta_{i,t}^{min} \geq 0 \perp \gamma_{i,t}^{rp,min} \geq 0 \\
& \eta_{i,t}^{max} \geq 0 \perp \gamma_{i,t}^{rp,max} \geq 0 \\
& \tau_{l,t}^{min} \geq 0 \perp \gamma_{l,t}^{L,min} \geq 0 \\
& \tau_{l,t}^{max} \geq 0 \perp \gamma_{l,t}^{L,max} \geq 0
\end{aligned}$$

通过上述模型转化，建立了对应的 EPEC 模型，理论上求解该模型即可获得在策略型竞价模式下，市场参与者（市场主体）的最优行为。然而，在 EPEC 模型的转化过程中，引入了大量的变量相乘和互补松弛约束，导致 EPEC 模型的实际求解存在较大困难。