

# AUTOMATIQUE ET COMMANDE NUMERIQUE

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Fall 2023

**Why are we interested in feedback control systems ?**

**Feedback is everywhere : Biology, Economics and  
ENGINEERING**

- Body temperature control
- Glucose control
- Inflation control
- Grasping by hand
- Shower temperature control
- Water level control
- Driving a car
- Robotics
- Electrical networks
- Communication networks

# Body Temperature Control

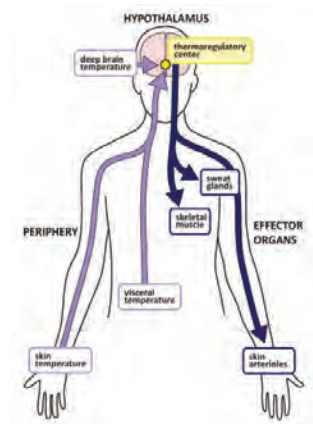
**Objective :** Keep the body temperature at  $37^{\circ}$ .

**Process :** The body balances its heat budget by metabolic activity, conduction and radiation.

**Measurements :** Thermo-receptors in the skin

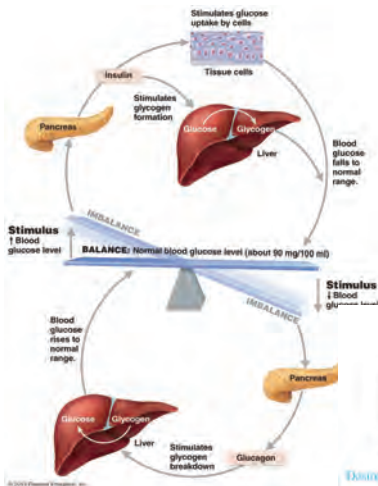
**Controller :** Hypothalamus

**Actuators :** Sweating, Shivering, ...

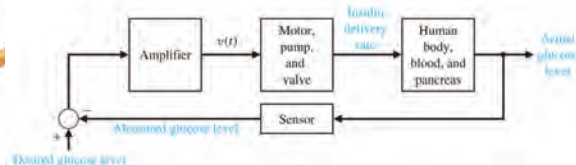


# Glucose Control

**Objective :** Keep the blood glucose in an appropriate level.



## Insulin Delivery System (Artificial pancreas)



# Inflation Rate Control

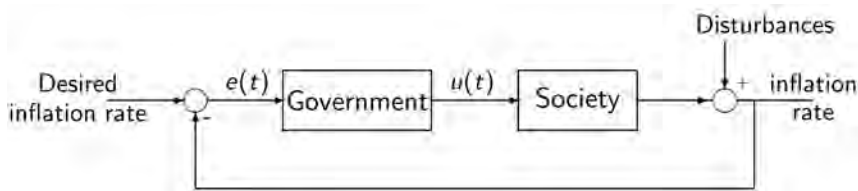
**Objective :** Keep the inflation rate at the desired value.

**Process :** The society (the relation between interest rate, direct taxes, government spending, etc and inflation rate)

**Measurements :** The general level of prices during a given period

**Controller :** Government

**Actuators :** Interest rate, taxes, ...



# Grasping by Hand

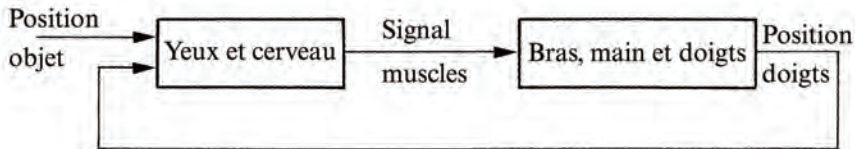
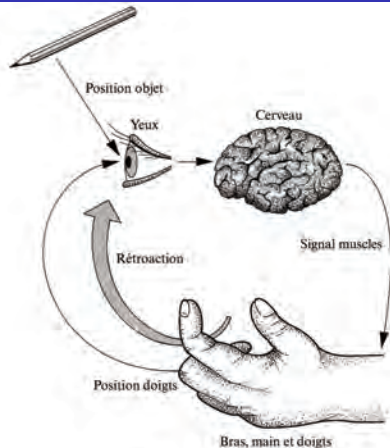
**Objective :** Grasping a pencil.

**Process :** Arm, hand and fingers

**Measurements :** By eyes (image processing)

**Controller :** Brain

**Actuators :** Muscles



# Shower Temperature Control

**Objective :** Taking shower with desired water temperature

**Process :** Shower

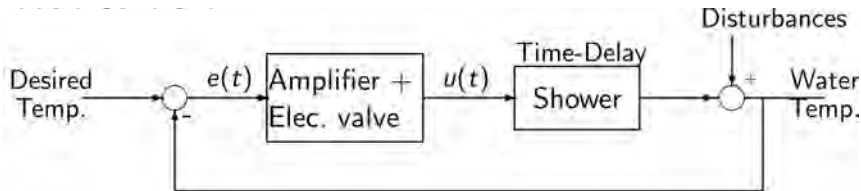
**Measurements :** By hand sensors

**Controller :** Brain

**Actuators :** Fingers, valve



**Automatic Control :**



# Water Level Control

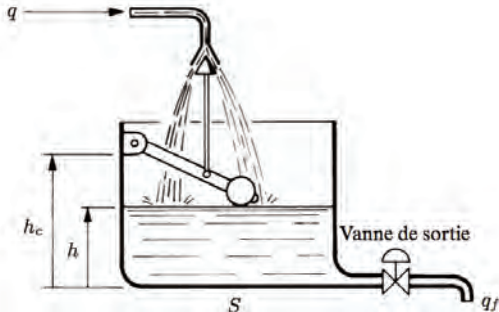
**Objective :** Keeping the water level at a desired value

**Process :** Water tank

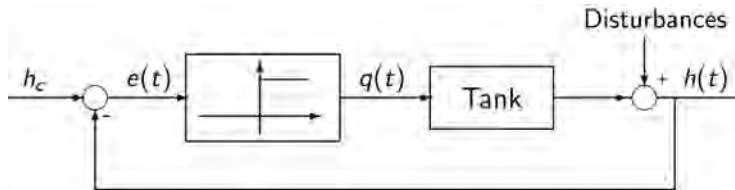
**Measurements :** By floater

**Controller :** on-off

**Actuators :** Valve



**Block diagram :**





# Driving a Car

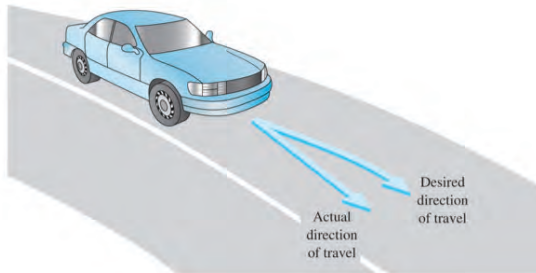
**Objective :** Driving in a desired direction

**Process :** Automobile

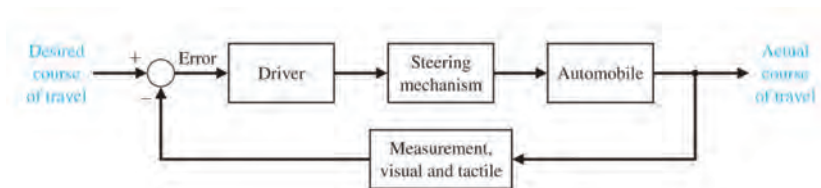
**Measurements :** Visual

**Controller :** Driver

**Actuators :** Steering mechanism



**Block diagram :**



## Automatic Driving



There are more than 500 feedback loops in a conventional car !

# Robotics

**Objective** : Position control in a robotic arm

**Process** : Robotic arm

**Measurements** : Position sensors (encoders)

**Controller** : Computer

**Actuators** : Joint Servomotors



**Robots in action :**



# Electrical Networks

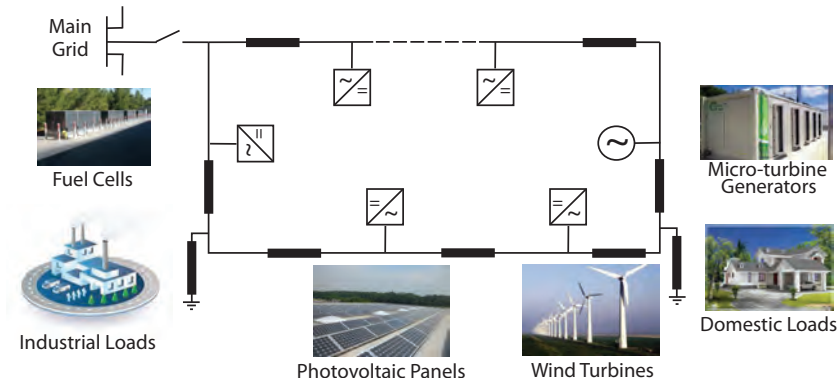
**Objective :** Voltage control of a microgrid in islanded mode

**Process :** Microgrid

**Measurements :** Voltage sensors

**Controller :** Computer

**Actuators :** Power electronic converters



# Communication Networks

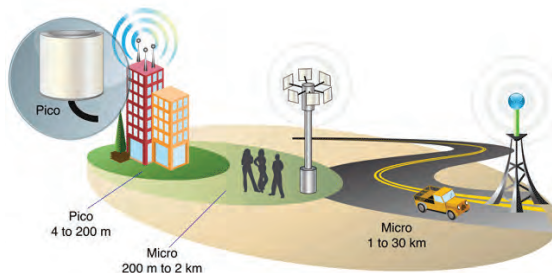
**Objective** : Signal quality control in mobile phones

**Process** : Mobile phones

**Measurements** : Signal quality (signal to noise ratio)

**Controller** : Computer

**Actuators** : Signal amplifier



There are more than 10 feedback loops in each mobile phone  
(Frequency control, gain control, transmission power control, etc.)

# Components of Feedback Control Systems

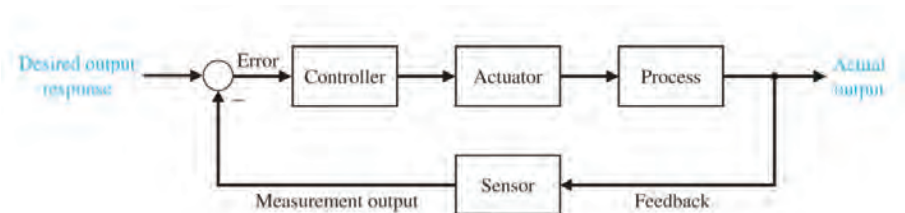
All Feedback Control systems have four components :

**Process** : The system to be controlled.

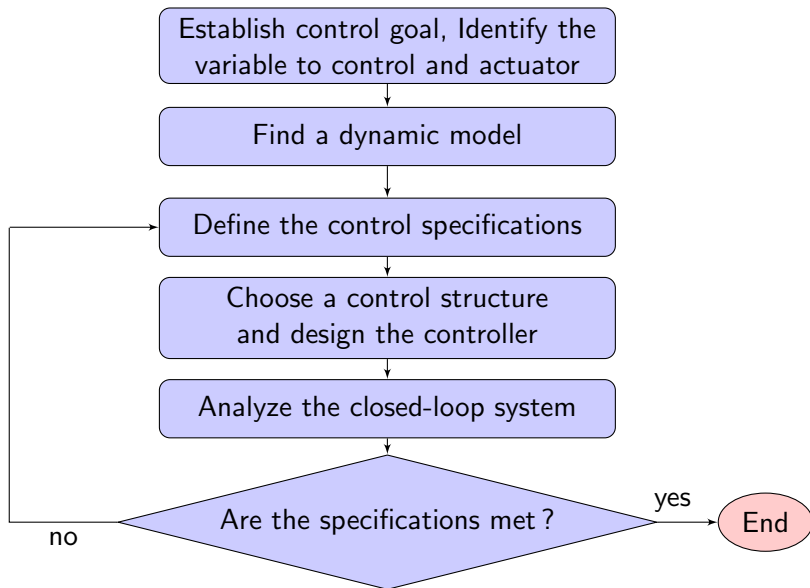
**Sensor** : Measures the system output (the variable to be controlled).

**Actuator** : Apply the command to the process.

**Controller** : An algorithm that makes the closed-loop system to behave as we wish.



# Control System Design Procedure



## **Objective :**

Analysis and Synthesis of Linear Feedback Control Systems

## **Learning Outcomes :**

- Represent a linear dynamic system with a transfer function or a state-space model,
- Analyze a linear dynamical system (continuous- and discrete-time),
- Assess the stability, performance and robustness of a closed-loop system,
- Design PID or lead-lag controllers by loop-shaping method,
- Design optimal state-space controllers,
- Design digital RST controllers.



# Teaching Method

## Lectures : Question/Answer with Clickers and Written Exercises



[www.responseware.eu](http://www.responseware.eu)

# Teaching Method

## Written Exercises :

6 series of exercises with solutions. 6h of exercise sessions for answering the questions.



## Computer Exercises :

Control of a flexible joint using different control strategies. It includes 5 Modules (10h).

The students will work in groups (three students) and their reports will be graded.

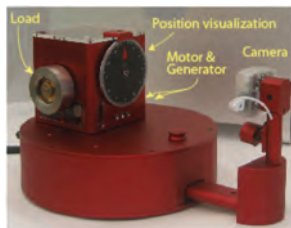


**Using Jupyter Notebook**

# Teaching Method

## Hands-on Laboratory (Travaux Pratiques) :

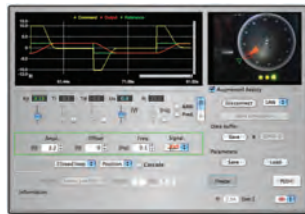
5 Sessions (10h) in MED 21120 (MOOC available)

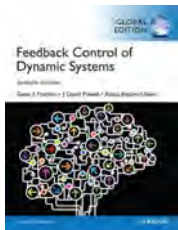


**Responsible :** Dr Christophe Salzmann

**Objective :** Control of a Servomechanism

TP sessions (1-4) can be done remotely  
(5th session needs the presence of students).





## Strongly Recommended

### Feedback Control of Dynamic Systems

by Franklin, Powell and Emami-Naeini,

Global Edition, 7th Edition, 2017.

Chapter 1 : Introduction

Chapter 2 : Modeling of Dynamic Systems

Chapter 3 : Analysis of Dynamic Systems

Chapter 4 : Feedback Control Systems

Chapter 5 : The Root-Locus Design Methods

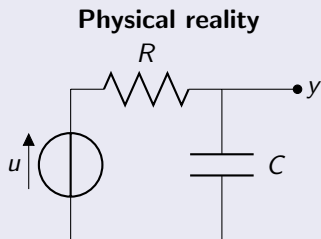
Chapter 6 : The Frequency-Response Methods

Chapter 7 : The State-Space Methods

Chapter 8 : Digital Control

# Course Content

## Chapter 2 : Modeling of Dynamic Systems



### Model

- Variable of interest :  $y$
- Independent variable :  $u$
- Mathematical model :

$$y(t) = u(t) - RC \frac{dy}{dt}$$

**Transfer Function :**  $Y(s) = U(s) - RCsY(s) \Rightarrow G(s) = \frac{Y(s)}{U(s)} = \frac{1}{RCs + 1}$

## Chapter 3 : Analysis of Dynamic Systems

**Analysis :** Compute the output  $y(t)$  for any input  $u(t)$  (step response, impulse response, etc)

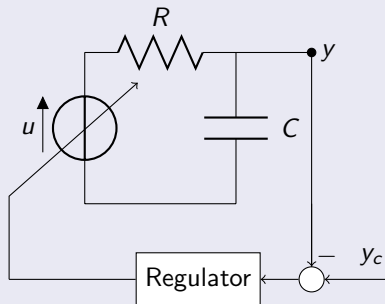
$$y(t) = \mathcal{L}^{-1}[Y(s)] = \mathcal{L}^{-1}[G(s)U(s)]$$

**Stability**

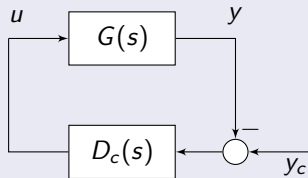
**Performance**

## Chapter 4 : Feedback Control Systems

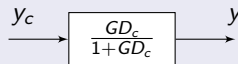
**Physical reality  
(voltage regulator)**



**Closed-loop System**



**Simplifying block diagrams**

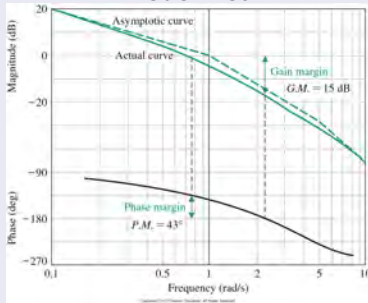


**Analysis :** Computing all closed-loop signals for any external input, closed-loop stability, closed-loop performance.

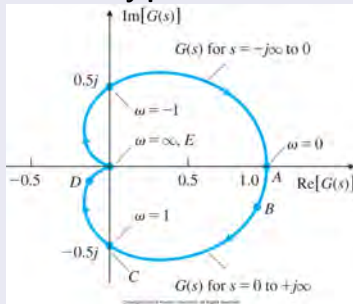
**Synthesis :** Design of the regulator, controller,  $D_c(s)$  for the PID structure.

## Chapter 6 : The Frequency Response Methods

### Bode Plot



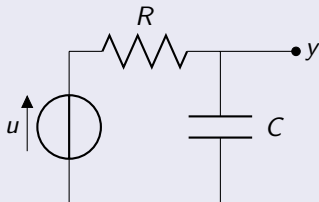
### Nyquist Plot



- Sketching Bode and Nyquist plots; Extracting information from the plots.
- Nyquist stability criterion, Gain, Phase and Modulus margins.
- Designing PID and Lead-Lag Controllers in the frequency domain (Loop Shaping Method).

## Chapter 7 : The State-Space Methods

### Transfer Function Model



$$y(t) = u(t) - RC \frac{dy}{dt}$$

$$G(s) = \frac{Y(s)}{U(s)} = \frac{1}{RCs + 1}$$

### State-Space Model

- Variable of interest :  $y$
- Independent variable :  $u$
- State Variable :  $x$

$$\dot{x}(t) = \frac{-1}{RC}x(t) + \frac{1}{RC}u(t)$$

$$y(t) = x(t)$$

### General Representation

$$\dot{\mathbf{x}}(t) = \mathbf{A}\mathbf{x}(t) + \mathbf{B}u(t)$$

$$y(t) = \mathbf{C}\mathbf{x}(t)$$

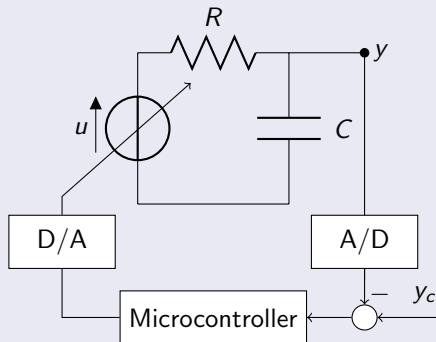
**Analysis :** State-space modeling, converting TF to SS and vis-versa, Controllability, Observability.

**Synthesis :** Designing **optimal** state feedback controller  $u(t) = \mathbf{K}\mathbf{x}(t)$  and state observer.



## Chapter 8 : Digital Control

### Discrete-time System



### Digital Control System

- Controller is implemented on a computer (microcontroller).
- Controller sees the physical system as a digital system.
- The digital system is represented by a difference equation :
$$y(k) = -ay(k-1) + bu(k)$$
- The z-transform is used instead of the Laplace transform.

**Analysis :** Analysis of discrete-time models using the z-transform and its inverse ; stability and performance of discrete-time systems.

**Synthesis :** Design of digital RST controller using the pole placement technique.

# Course Schedule

	Wednesday (CM3)		Thursday (CM4)	Friday (CM3)
Date	13:15-15:00		10:15-12:00	10:15-12:00
20-22 sep.	Introduction		Chapter 2	Chapter 2
27-29 sep.	Chapter 3		Chapter 3	Chapter 3
4-6 oct.	CE1-A	TP1-B	Chapter 3	Chapter 4
11-13 oct.	TP1-A	CE1-B	Chapter 4	Chapter 4
18-20 oct.	Written Ex 2-3		Chapter 4	Chapter 6
25-27 oct.	TP2-A	CE2-B	Chapter 6	Chapter 6
1-3 nov.	CE2-A	TP2-B	Chapter 6	Chapter 6
8-10 nov.	Written Ex 4-6		Chapter 7	Chapter 7
15-17 nov.	CE3-A	TP3-B	Chapter 7	Chapter 7
22-24 nov.	TP3-A	CE3-B	Chapter 8	Chapter 8
29 nov.- 1 dec.	Mid-term Exam		Chapter 8	Chapter 8
6-10 dec.	TP4-A	CE4-B	Chapter 8	Chapter 8
13-15 dec.	CE4-A	TP4-B	Chapter 8	Chapter 8
20-22 dec.	Written Ex 7-8		CE5-A TP5-B	TP5-A CE5-B

TP in MED 21120 , CE in BC 07 and BC 08

Written Ex. Group A in MED 21120, Group B in BC 07 and BC 08

**Report on computer exercises :** Five Jupyter Notebook reports should be submitted in due times by each group of three students ( $1.5+1.5+2+2.5+2.5=10$  points).

## Written exam :

- Mid-term exam : Chapters 2, 3, 4 and 6 (40 points).
- Final exam : Only Chapter 7 and 8 (40 points),  
One question on TP (10 points).

**Problems similar to the Written Exercises, One A4 Cheatsheet, nonprogrammable calculator**

## Grading :

Points	96-100	91-95	...	56-60	51-55	...	6-10	1-5	0
Grade	6.00	5.75	...	4.00	3.75	...	1.50	1.25	1.00

## Available on Moodle :

- Information about TP and Computer Exercises, Course slides
- Written Exercises with solutions (Ed discussion forum is available)

Goto [www.responseware.eu](http://www.responseware.eu), Session ID : [Automatique](#)

## House heating system

Provide a block diagram for closed-loop temperature control in a house using a thermostat and a gas furnace.

## Question

What is the process? what is the actuator?

- A Gas furnace
- B House
- C Thermostat
- D Heat

## Question

What is the output of the process

- A the exit door of the house,
- B the inside temperature of the house
- C the outside temperature
- D The heat generated by the furnace

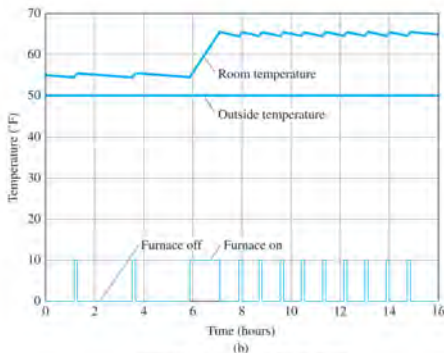
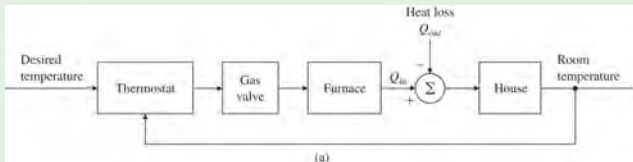
## Question

What is the reference signal

- A the entrance door,
- B the outside temperature of the house
- C heat
- D desired temperature

# Exercise

## Example (Household Temperature Control)



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