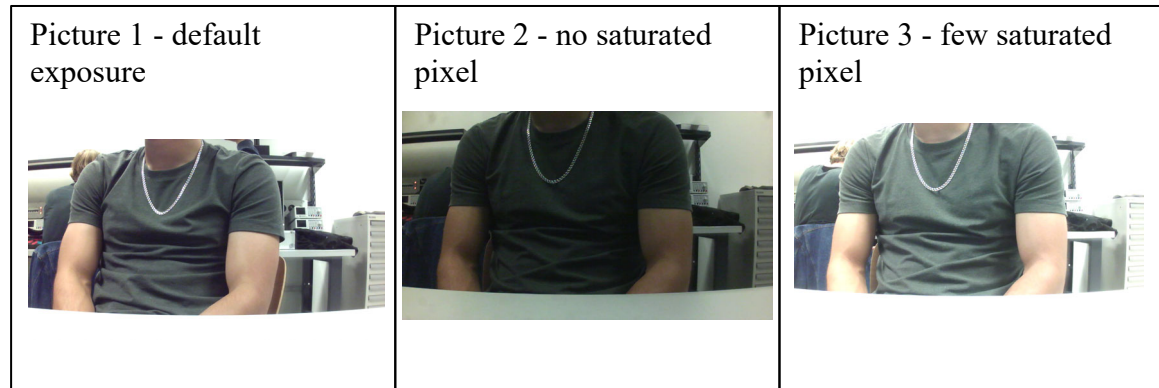


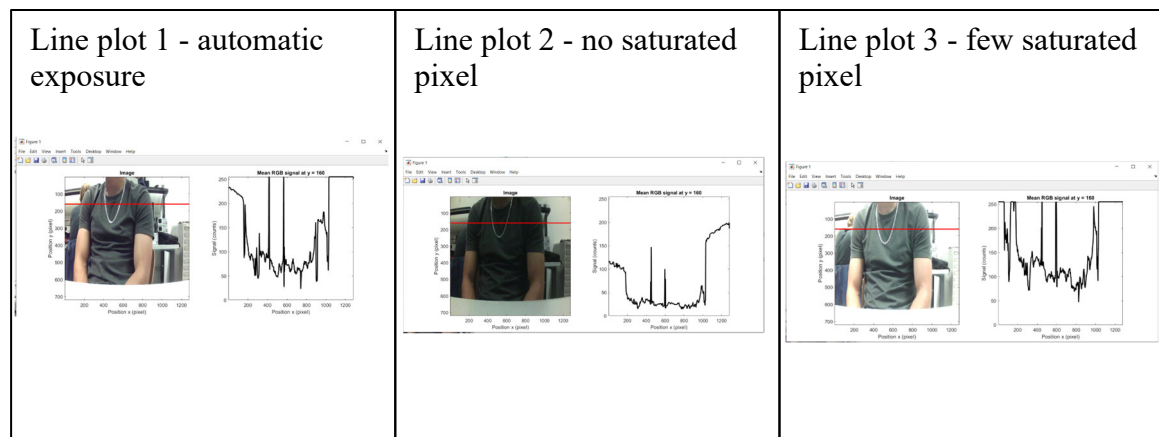
## TP 01: Imaging

### 1. Saturation and intensity adjustment of the camera

Take an image of the same scene at different exposure levels: one with default  
Make line plots at areas where automatic exposure gave saturation and compare the plots



for the three exposure conditions.

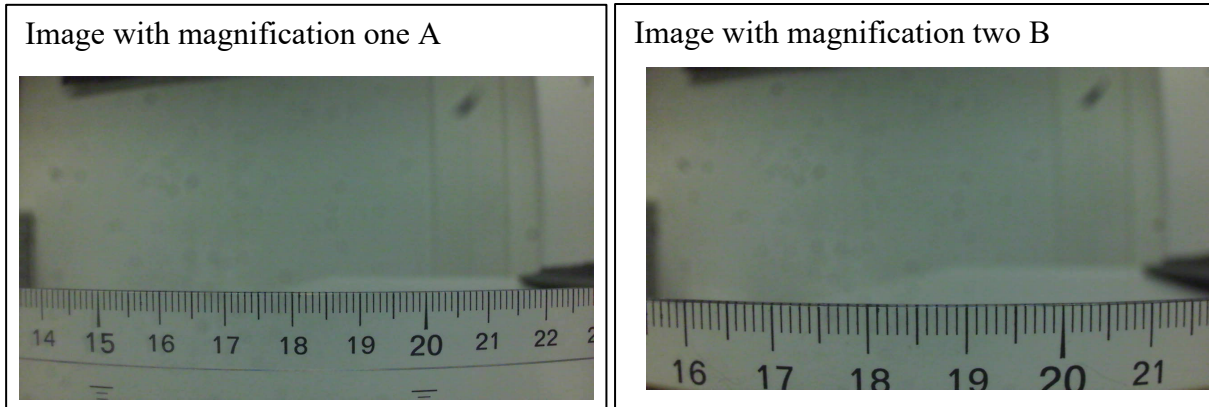


#### Comments:

We notice that the auto exposure is quite smart and will allow some saturation without letting too much information be lost to have a better contrast for the darker part of the image. As we can see in the non saturated image, there are no saturated region but image is quite dark because the brightest region is the necklace and the rest has to scale accordingly. While in the third image we can see a lot of saturation in the background while having a better contrast in the darker region of the tshirt.

## 2 Procedure to measure the focal lengths

Show your two images with different magnifications.



$$m_A = 3.888[\text{mm}] / 93[\text{mm}] = 0.0418$$

$$m_B = 3.888[\text{mm}] / 63.5[\text{mm}] = 0.0612$$

Determine the focal length and show the numbers used for the calculation. ( $d_{IA} = 0.5$  mm for one turn of the objective)

$$f = \frac{\Delta d_I}{(m_B - m_A)} = \frac{0.125 [\text{mm}]}{(0.0612 - 0.0418)} = 6.4432 [\text{mm}]$$

Make an error estimation (see “Uncertainties and Error Propagation.pdf”) assuming no error is made on  $d_{IA}$  and  $d_{IB}$ .

Give the steps to obtain the formula for  $\Delta f$  :

assuming we turned the objective by exactly a quarter of a turn, the only factor of error left is the measured length of the image. we assume the worse error is  $\pm 1$  [mm]

$$\Delta m_b = \frac{h_i}{h_{ob}^2} \Delta h_{ob} = \frac{3.888[\text{mm}]}{63.5^2[\text{mm}^2]} * (\pm 1[\text{mm}]) = \pm 0.96423$$

$$\Delta m_a = \frac{h_i}{h_{oa}^2} \Delta h_{oa} = \frac{3.888[\text{mm}]}{93^2[\text{mm}^2]} * (\pm 1[\text{mm}]) = \pm 0.449532$$

$$f = \frac{d_{ib} - d_{ia}}{x_1 - x_2}$$

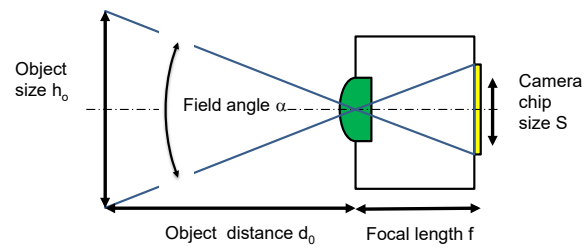
$$df = \frac{0 - (d_{ib} - d_{ia})}{(x_1 - x_2)^2} dm_b + \frac{0 + (d_{ib} - d_{ia})}{(x_1 - x_2)^2} dm_a$$

$$\Delta f = \left| \frac{\partial f}{\partial m_b} \right| * \Delta m_b + \left| \frac{\partial f}{\partial m_a} \right| * \Delta m_a = \frac{d_{ib} - d_{ia}}{(m_b - m_a)^2} (\Delta m_b + \Delta m_a)$$

$$\Delta f = \frac{0.125[\text{mm}]}{(0.0612 - 0.0418)^2} (0.96423 + 0.449532) = \pm 0.469551[\text{mm}]$$

$$f \pm \Delta f = (6.4432[\text{mm}] \pm 0.469551[\text{mm}])$$

### 3 Measurement of the field of view (angle of view)



Measure  $h_o$  and  $d_o$ . Calculate the angle of view (field of view) and make an error estimation.

$$\alpha = 2 \arctan \frac{S}{2f} = 2 \arctan \frac{h_o}{2d_o} \approx \frac{h_o}{d_o} \Rightarrow$$

Give the steps to obtain the formula for  $\Delta\alpha$ :

we measured :

$$d_o = 68[mm]$$

$$h_o = 64[mm]$$

$$\Delta h_o = \pm 2[mm]$$

$$\Delta d_o = \pm 2[mm]$$

we can deduce

$$s = h_o \pm dh_o$$

$$2f = 2d_o \pm d(d_o)$$

$$\alpha = 2 * \arctan\left(\frac{S}{2f}\right) = 2 * \arctan\left(\frac{h_o}{2d_o}\right) \approx \frac{h_o}{d_o} = 1.0625[rad]$$

$$d\alpha = 2 \frac{2d_o}{h_o^2 + 4d_o^2} dh_o - 2 \frac{2h_o}{h_o^2 + 4d_o^2} dd_o$$

$$\Delta\alpha = \left| \frac{\partial\alpha}{\partial h_o} \right| dh_o + \left| \frac{\partial\alpha}{\partial d_o} \right| dd_o = \frac{4}{h_o^2 + 4d_o^2} (d_o * d(h_o) + h_o * d(d_o))$$

$$\Delta\alpha = \frac{1}{d_o^2} (d_o \Delta h_o + h_o \Delta d_o)$$

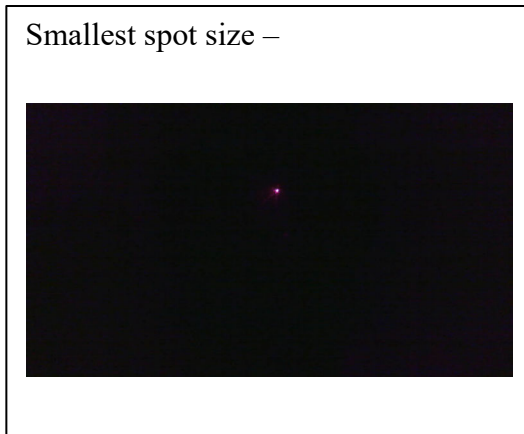
thus :

$$\Delta\alpha = \frac{1}{(68[mm])^2} (68[mm] * 2[mm] + 64[mm] * 2[mm]) = \pm 0.05709[rad]$$

$$\alpha \pm \Delta\alpha = 1.0625[rad] \pm 0.05709[rad]$$

#### 4 Measurement of the F# number.

A picture of the smallest spot size.



Fill the table below with your measurements of luminous disc size versa relative focusing position (min 5 measurements).

No.	relative position	Spot size in pixel (from image)	Spot size in micron	Angle u	NA	F#
1	0	10	30			
2	0.125[mm]	12	36	8.19°	0.1425	3.508
3	0.25[mm]	34	102	11.53°	0.1998	2.501
4	0.375[mm]	38	114	8.64°	0.1503	3.327
5	0.5[mm]	40	120	6.84°	0.1191	4.196
6						

Calculate the averaged values

$$u = 8.8^\circ$$

$$NA = 0.152925$$

$$F\# = 3.383$$

## Comments:

On remarque qu'en changeant le focus, le point diminue, atteint un minimum puis grandit à nouveau. Et bien que cette variation de taille n'est pas négligeable et dont la mesure du nombre de pixel est bruitée elle permet tout de fois d'approximer le F number en faisant une moyenne sur suffisamment d'échantillon.

## 5 Example from real world

Find an example on the internet of **one photographic lens** with small F# number. Try to find something that not all your classmates have. You might look at websites of well-known lens producers such as Nikon, Canon, Leica, Zeiss, Rodenstock, Fuji, etc. You can also include c-mount lenses (used for automated machine vision) in your search. Add a photo **of** the objective!

Photo of your objective



Leica Noctilux-M 1:0.95/50mm ASPH.

Ref: <https://www.arducam.com/product/arducam-2-8-12mm-varifocal-c-mount-lens-for-raspberry-pi-hq-camera-with-c-cs-adapter/>

(the F number vary between 1 and 1.6 depending on the settings)

**(Optional) Personal feedback:**

Was the amount of work adequate?

Yes. It took a bit longer than 4 hours in total

What is difficult to understand?

No except for the F number

What did you like about it?

Is very practical

How can we do better?

Find a way to ensure the measure data vary less. Expose the common factor of variation between students.