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2.67 Unbalanced machine seperti gambar.

Mass $\rightarrow 120$ kg

Out of balance $\rightarrow 374$ W

amount stiffness $\rightarrow 800$ kN/m

at running speed $\rightarrow 3000$ rev/min

damping value $\rightarrow 500$ kg/s

a) Amplitude karena out of balance

$$M_0 e = \frac{F_0}{\omega r^2}$$

$$M = 120$$

$$F_0 = 374$$

$$C = 500$$

$$k = 800 \cdot 1000$$

$$\omega r = 100 \cdot 1$$

$$\omega_n = \sqrt{\frac{k}{m}} \quad \zeta = \frac{C}{2\sqrt{k m}} \quad k = 8 \cdot 10^5$$

$$r = \frac{\omega r}{\omega_n} \quad \omega_n = 81,65 \quad r = 3,848 \quad \zeta = 0,025$$

$$X = \frac{F_0}{\omega r^2 \cdot m} \cdot \frac{r^2}{\sqrt{(1-r^2)^2 + (2\zeta \cdot r)^2}} \quad X = 3,386 \cdot 10^{-5}$$

$$b) M_0 e = m_0 e \omega r^2$$

$$e = \frac{F_0}{\omega r^2 (0,01 \text{ m})}$$

$$e = 3,158 \cdot 10^{-3}$$

2.68 Plot response 2.57

$$M = 120 \quad k = 120 \quad C = 500 \quad F_0 = 379$$

$$\omega_n = \sqrt{\frac{k}{m}}$$

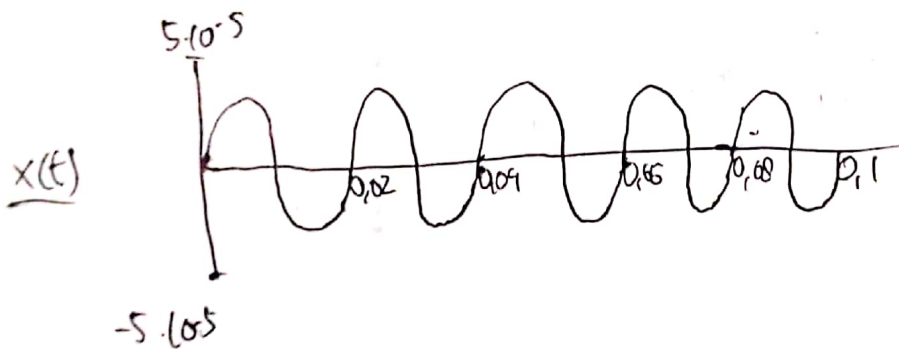
$$\omega_r = \frac{3000 \text{ Hz}}{60}$$

$$r = \frac{\omega_r}{\omega_n} \quad \zeta = \frac{C}{2\sqrt{mk}}$$

$$X = \frac{F_0}{\omega_r^2 m} \cdot \frac{r^2}{\sqrt{(1-r^2)^2 + (2\zeta r)^2}}$$

$$\theta = \arctan\left(\frac{2\zeta r}{1-r^2}\right)$$

$$x(t) = X \sin(\omega_r t - \theta)$$



2.51 Diket: $m = 50 \text{ kg}$ $e = 0.1 \text{ m}$ $\omega_0 = 7.5 \text{ rad/s}$
 $m_0 = 5$ $f = 0.06$ $\omega_r = 30 \text{ rad/s}$
 $r = \frac{\omega_r}{\omega_0} = 4$

Dit: Amplitudo

Jawab:

$$x = \frac{m_0 e}{m} \frac{r^2}{\sqrt{(1-r^2)^2 + (2f r)^2}} = \frac{(5)(0.1)}{50} \frac{4^2}{\sqrt{(1-4^2)^2 + (2(0.06)(4))^2}}$$

$$x = \frac{(5)(0.1)}{50} \frac{16}{\sqrt{(1-16)^2 + [2(0.06)(4)]^2}}$$

$$x = 0.011 \text{ m}$$

$$x = 1.1 \text{ cm}$$



2.62 Diket: $x = 1 \text{ mm}$ Fixed
 $x = 10 \text{ mm}$

Dit: ζ / Damping ratio

Jawab: $x = \frac{m_0 e}{m} \frac{r^2}{\sqrt{1-r^2} + (2\zeta r)^2}$

at resonance $x = 10 \text{ mm} = \frac{m_0 e}{m} \frac{1}{2\zeta}$

$$10 \text{ mm} = \frac{1}{\frac{m_0 e}{m} 2\zeta}$$

when r is very large, λm and $\lambda = 1 \text{ mm}$
 $\frac{m}{m_0 e}$

$$\frac{m}{m_0 e} = 1$$

therefore, $10 (1) = \frac{1}{2\zeta}$

$$\zeta = 0.05$$



2-63 Diket: $m_0 = 12 \text{ kg}$

$$m = 100 \text{ kg}$$

$$k = 3000 \text{ N/m}$$

$$e = 0.1$$

$$\omega_r = 1800 \text{ RPM} = 188.5 \text{ rad/s}$$

Dit: Amplitudo of forced vibration.

Jawab ~

$$\omega_0 = \sqrt{(3000/100)} = 5.4772 \text{ rad/s}$$

$$r = \frac{\omega_r}{\omega_0} = \frac{188.5}{5.4772} = 34.415$$

$$x = \left(\frac{(m_0 \cdot e)}{m} \right) \left(\frac{r^2}{|1 - r^2|} \right) = 0.01201$$

2.6a)

$$x = 0,05 \text{ m}$$

$$m = 10 \text{ kg}$$

$$\zeta = 0,1$$

$$e = 0,1 \text{ m}$$

$$k = 3200 \text{ N/m}$$

$$r = \frac{\frac{2\pi \times 1800}{60}}{\left(\sqrt{3200/100}\right)} = 2\pi\sqrt{30} = 39,414$$

Rotation unbalance

$$e = \left(\frac{m x}{m_0}\right) \frac{\sqrt{(1-r^2)^2 + (2\zeta)^2}}{r^2} = \frac{10 \times 0,05 \times \sqrt{(1-(39,414)^2)^2 + (2 \times 0,1 \times 39,414)^2}}{(39,414)^2}$$

$$= \boxed{0,49950 \text{ m}}$$

2.65)

$$m\ddot{x} + c\dot{x} + kx = m_0 e \omega^2 \sin(\omega t + \theta)$$

- Steady state solution

$$x(t) = \frac{m_0 e}{m} \frac{r^2}{\sqrt{(1-r^2)^2 + (2\zeta r)^2}} \sin \omega t$$

- Force transmitted to the ground

$$F(t) = kx + c\dot{x} = \frac{m_0 e}{m} \frac{k r^2}{\sqrt{(1-r^2)^2 + (2\zeta r)^2}} \sin \omega t + \frac{m_0 e}{m} \frac{c \omega r^2}{\sqrt{(1-r^2)^2 + (2\zeta r)^2}} \cos \omega t$$

- Magnitude of the force transmitted

$$F_0 = \frac{m_0 e}{m} \frac{r^2 \sqrt{k^2 + c^2 \omega^2}}{\sqrt{(1-r^2)^2 + (2\zeta r)^2}} = m_0 e \omega \frac{\sqrt{1 + (2\zeta r)^2}}{\sqrt{(1-r^2)^2 + (2\zeta r)^2}}$$

- Magnitude of the force generated by the rotating mass

$$F_r = m_0 e \omega^2$$

$$F_0 = 0,1 F_r$$

$$\Rightarrow m_0 e \omega^2 \frac{\sqrt{1 + (2\zeta r)^2}}{\sqrt{(1-r^2)^2 + (2\zeta r)^2}} = 0,1 m_0 e \omega^2$$

$$\zeta = 0,2$$

$$\Rightarrow r^4 - 17,84 r^2 - 99 = 0$$

$$\Rightarrow r^2 = 22,28 = \frac{\omega^2}{k/m} \Rightarrow \frac{k}{m} = \left(\frac{10000 \times 2\pi}{60} \right)^2 \frac{1}{22,28}$$

$$\Rightarrow k = 95 \left(\frac{10000 \times 2\pi}{60} \right)^2 \frac{1}{22,28} = \boxed{2,21 \times 10^6 \text{ N/m}}$$

2-66)

$$\chi_m(\zeta, r) = \frac{r^2}{\sqrt{(1-r^2)^2 + (2-\zeta r)^2}}$$

