

KNN-Averaging for Noisy Multi-Objective Optimisation

Stefan Klikovits^{*}, Paolo Arcaini



ERATO MMSD Hasuo Project
National Institute of Informatics, Tokyo

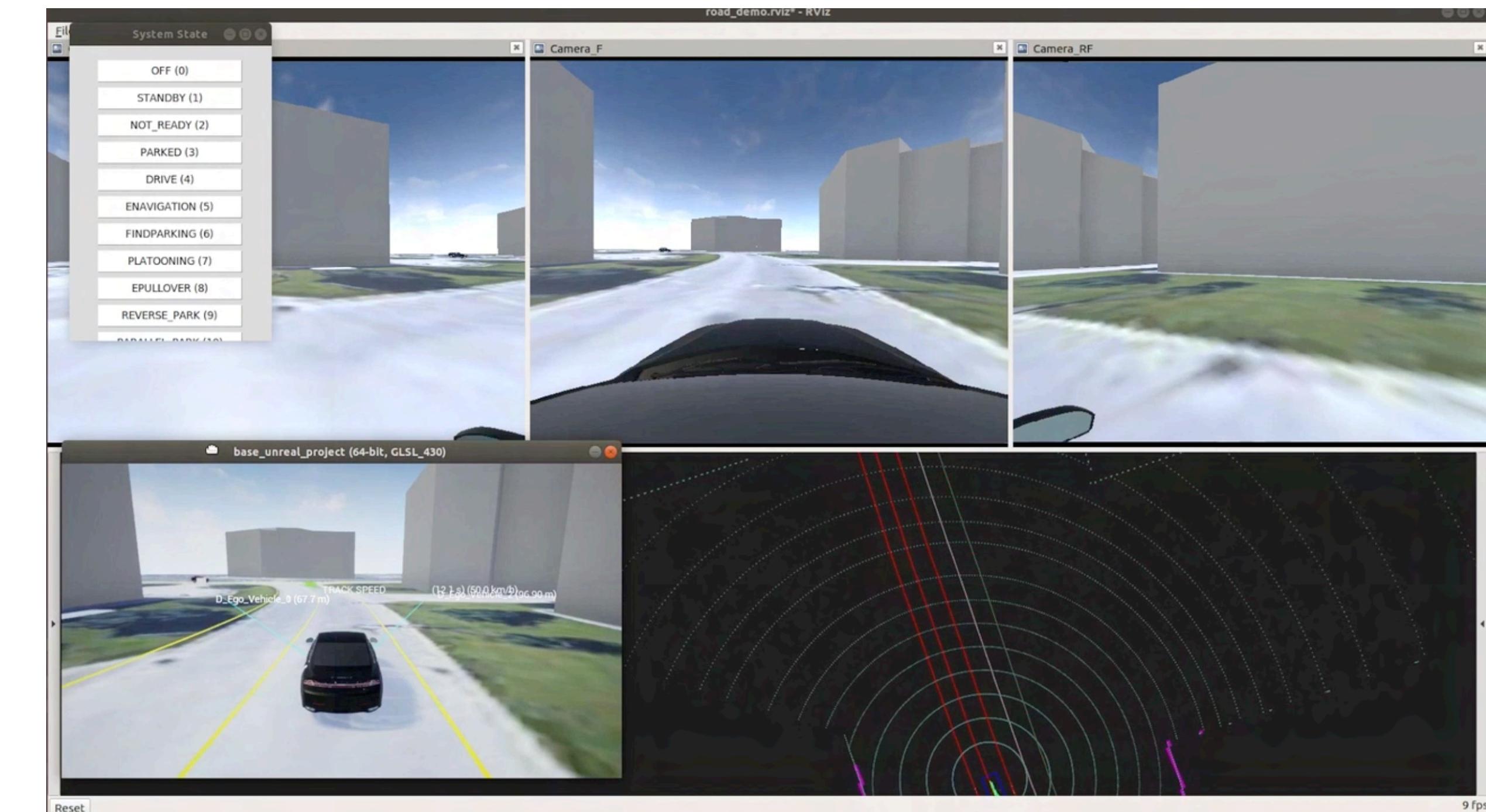
^{*}supported by JSPS Kakenhi Grant-in-Aid JP20K23334

Autonomoose ADS & Simulator

Self-Driving Vehicle

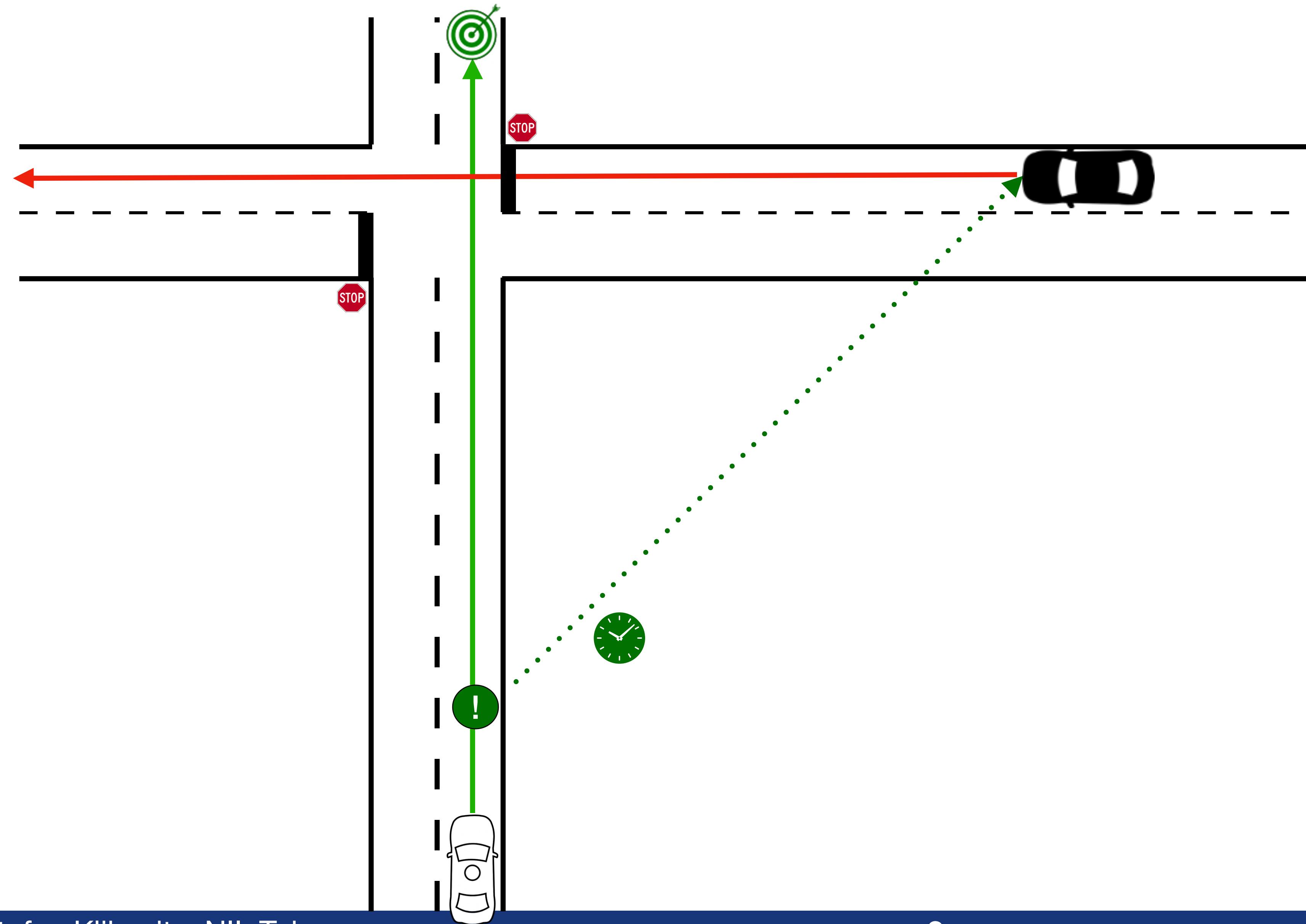


Simulation Platform

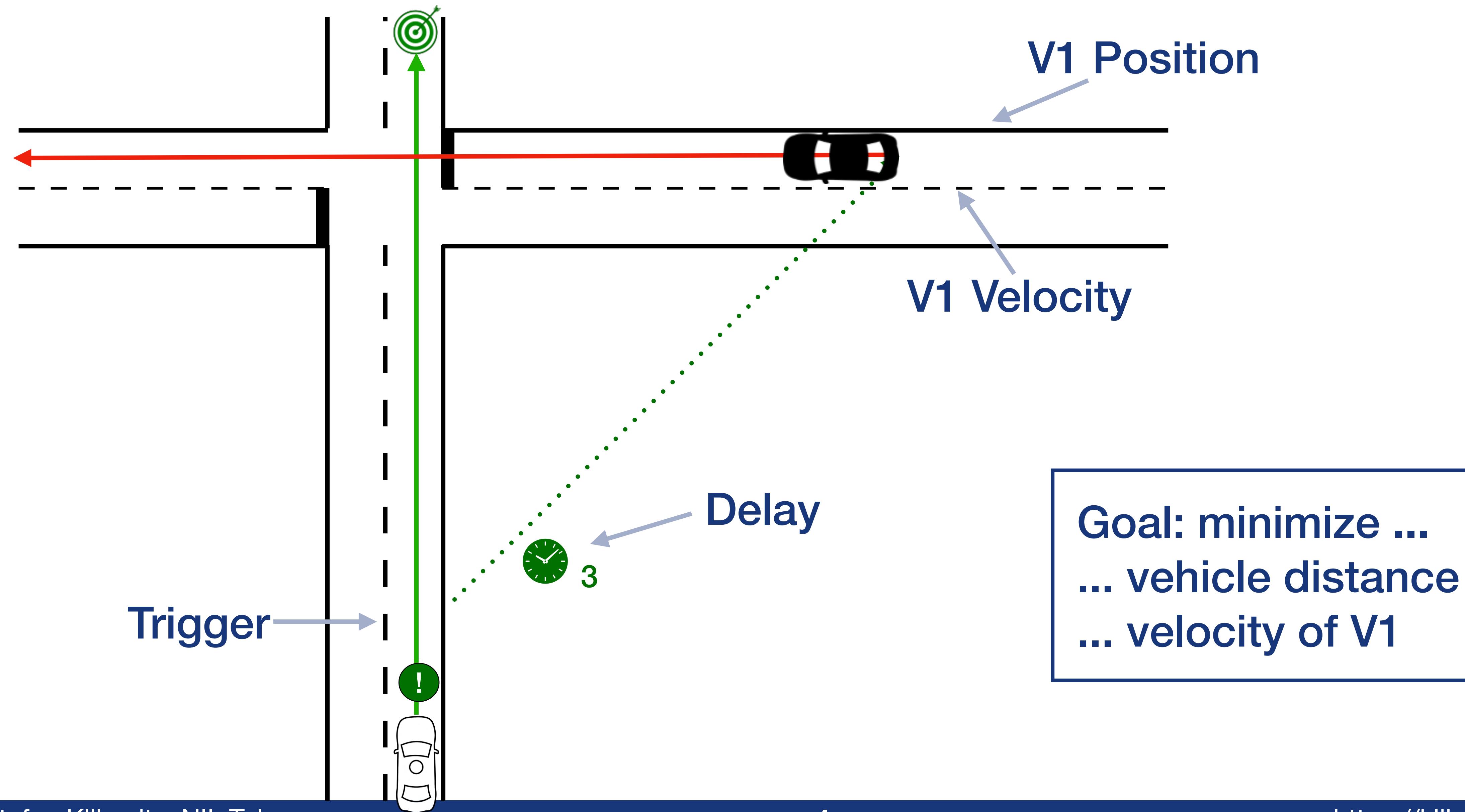


<https://www.youtube.com/watch?v=KjQosq-DIMg>

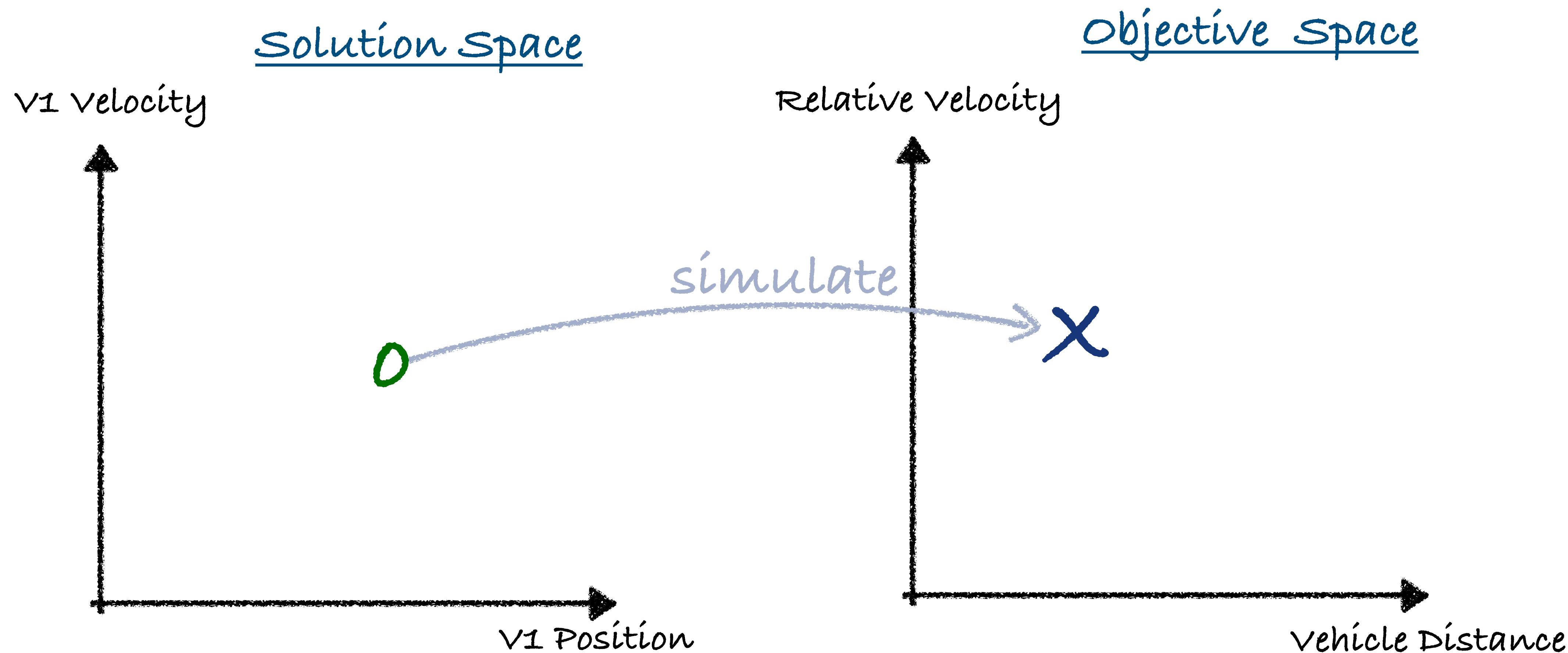
Scenario Search-Based Testing



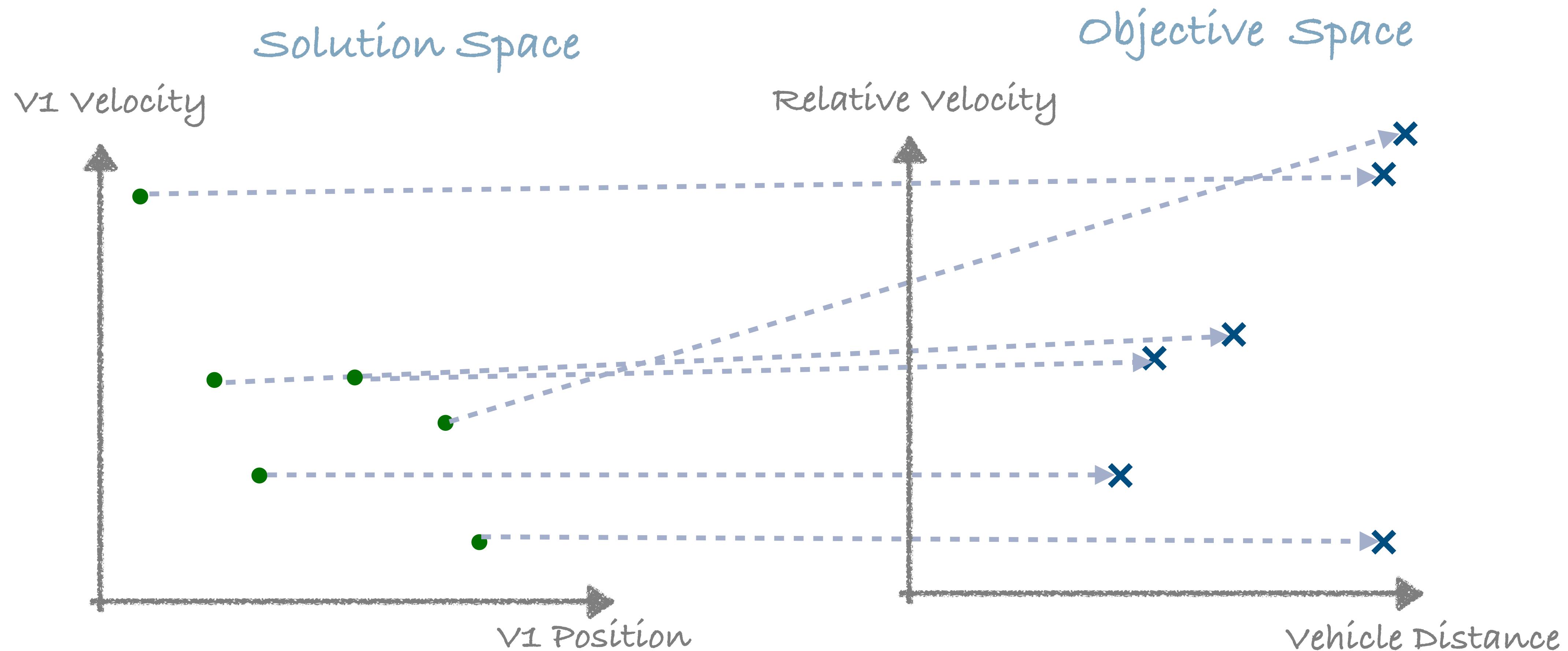
Scenario Search-Based Testing



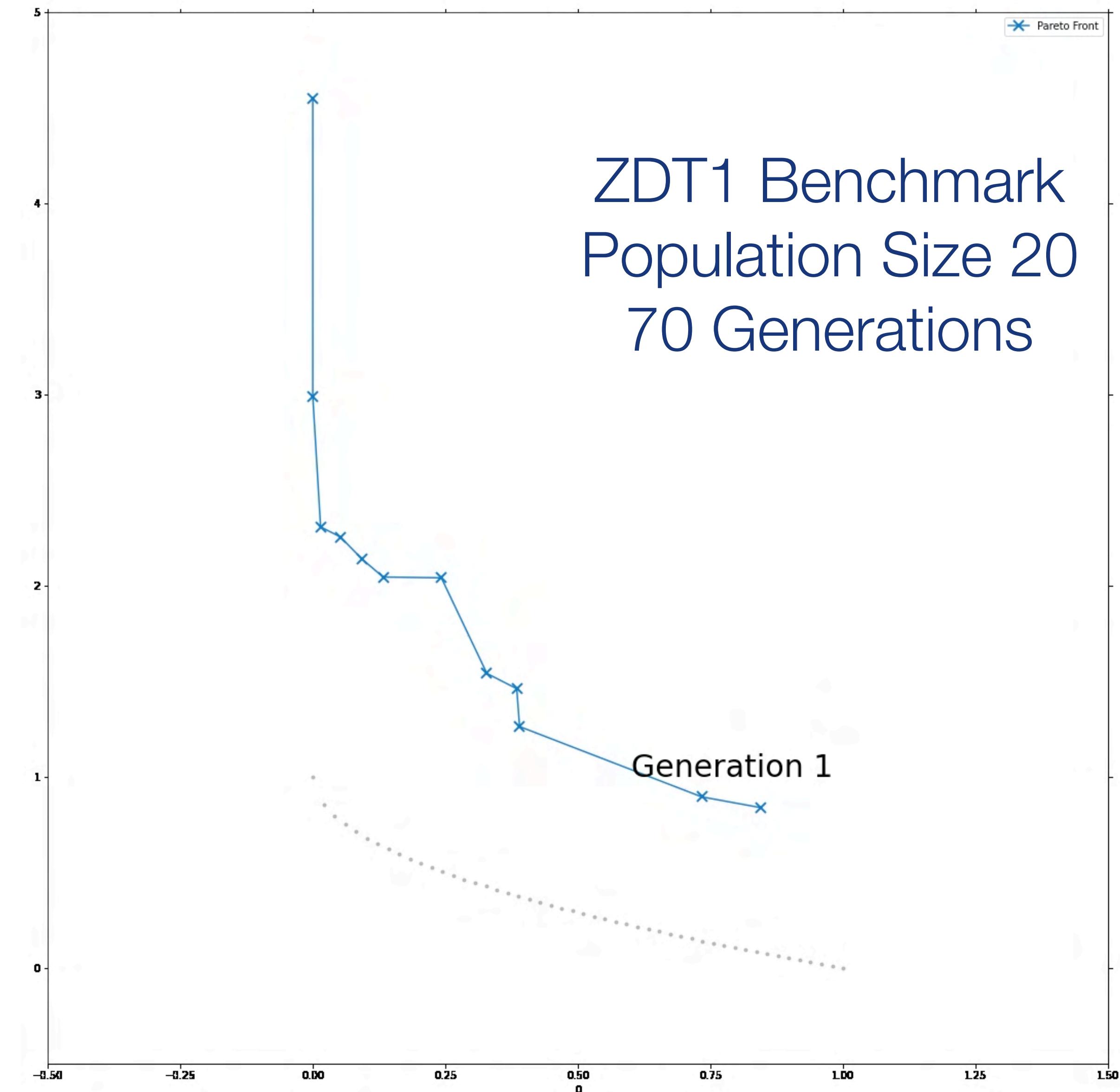
Search-Based Testing (SBT)



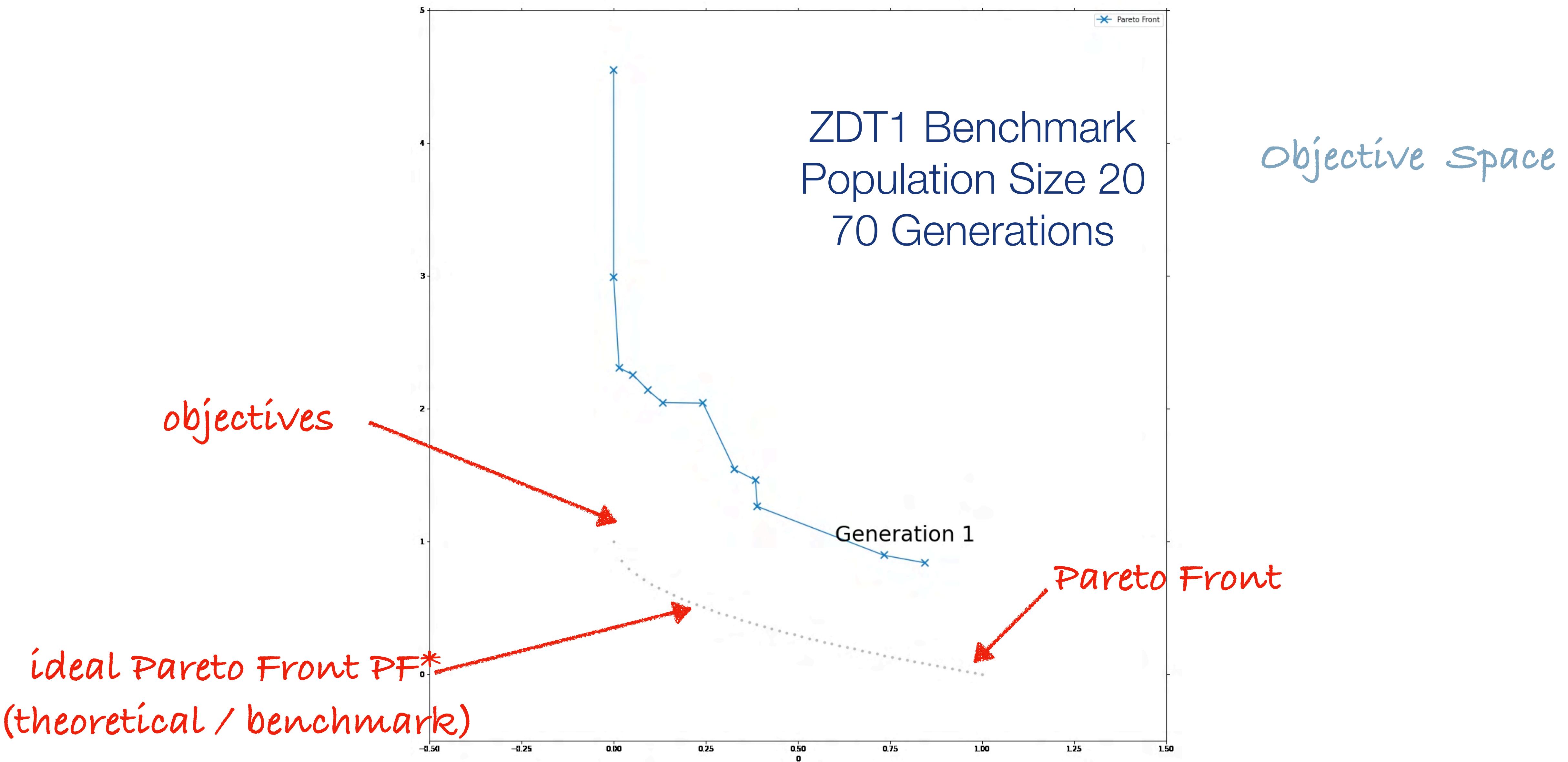
Search-Based Testing (SBT)



Search-Based Testing (SBT)

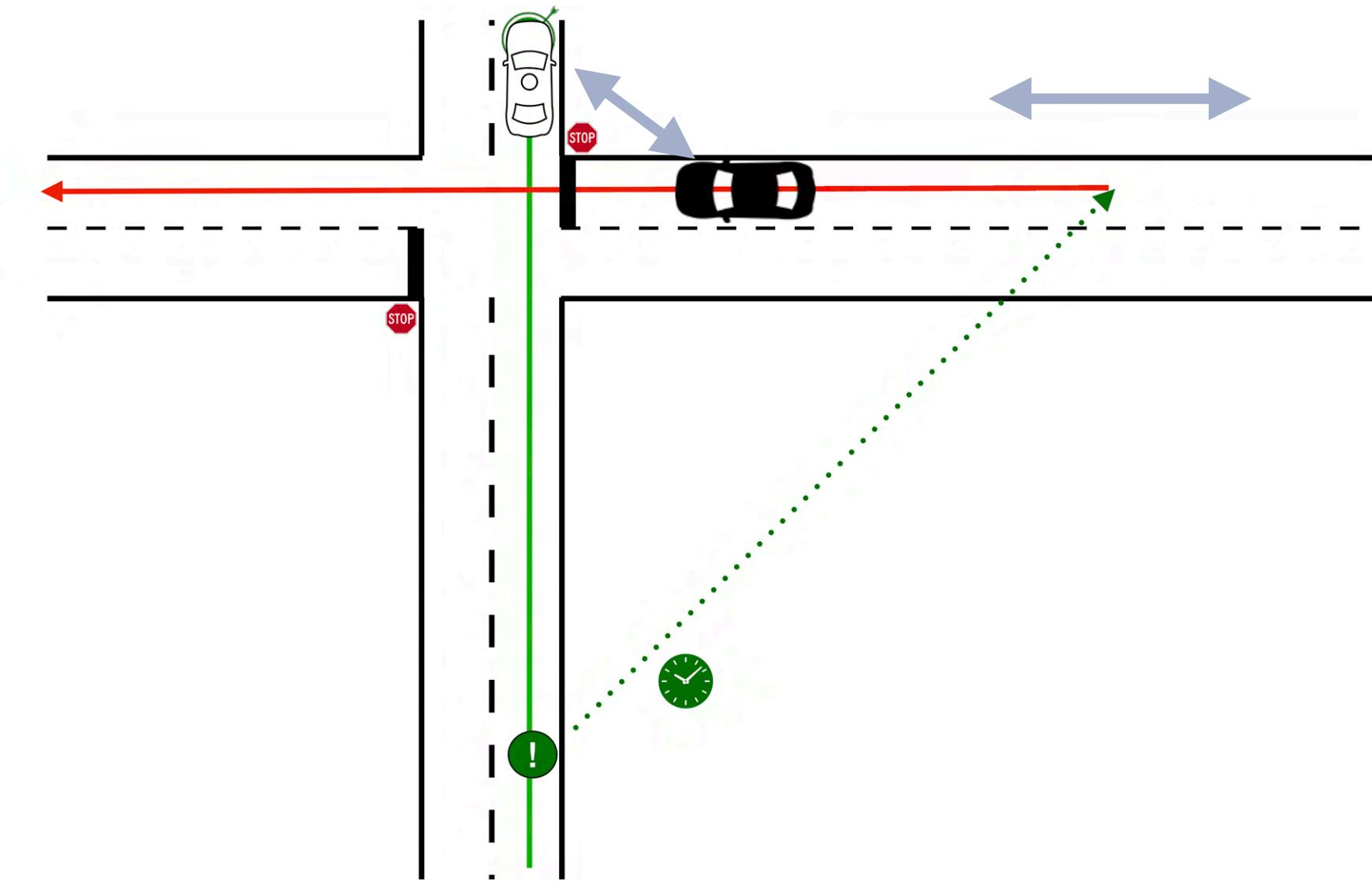


Search-Based Testing (SBT)

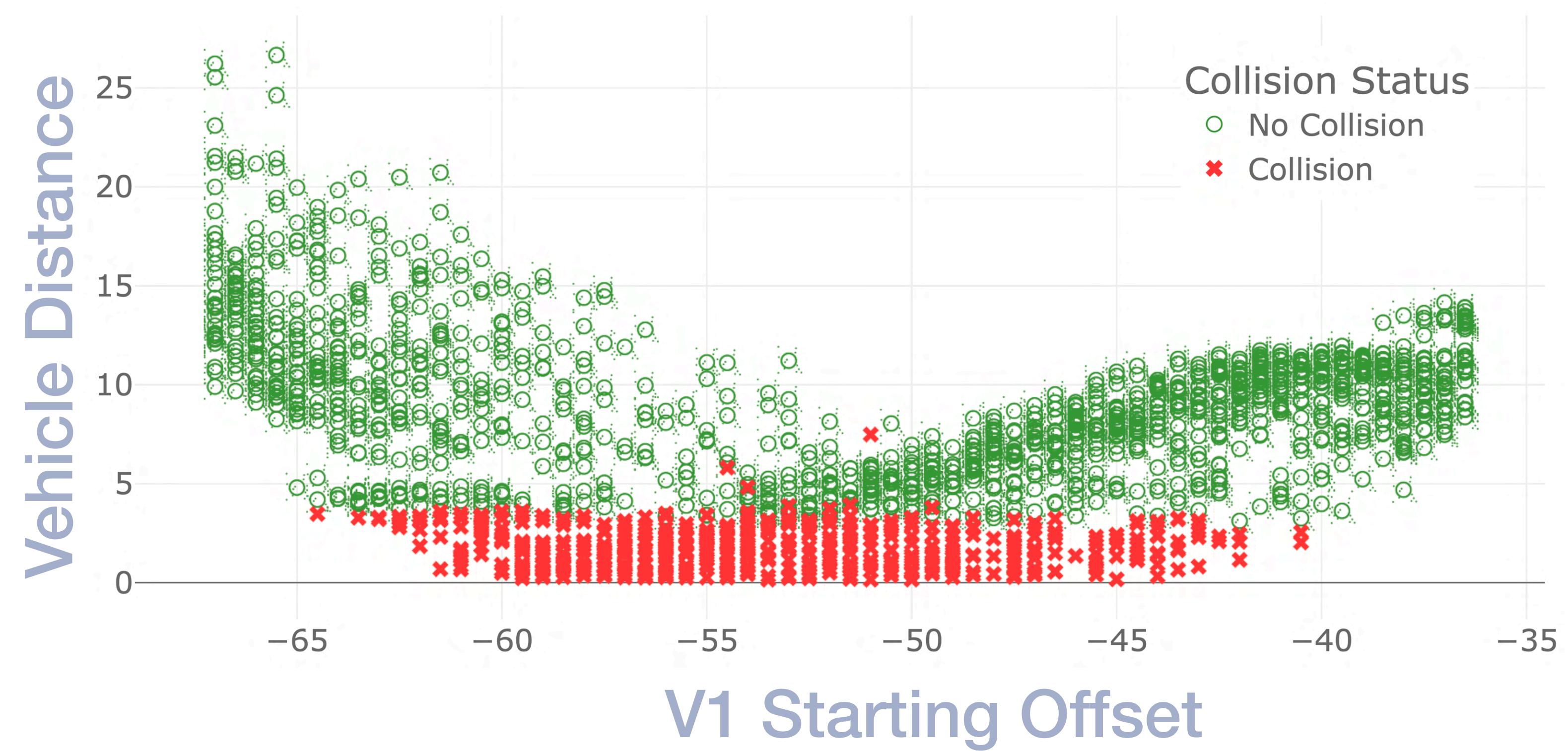


The Problem

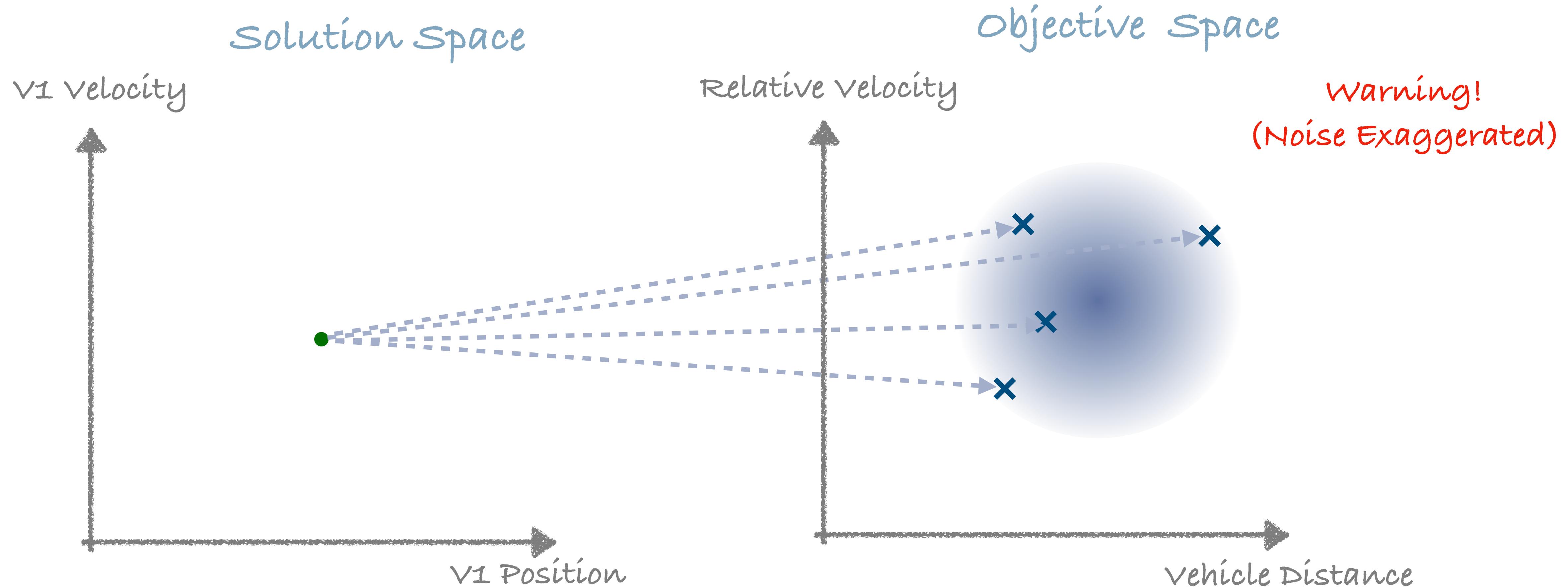
Autonomoose
is noisy
(non-deterministic)



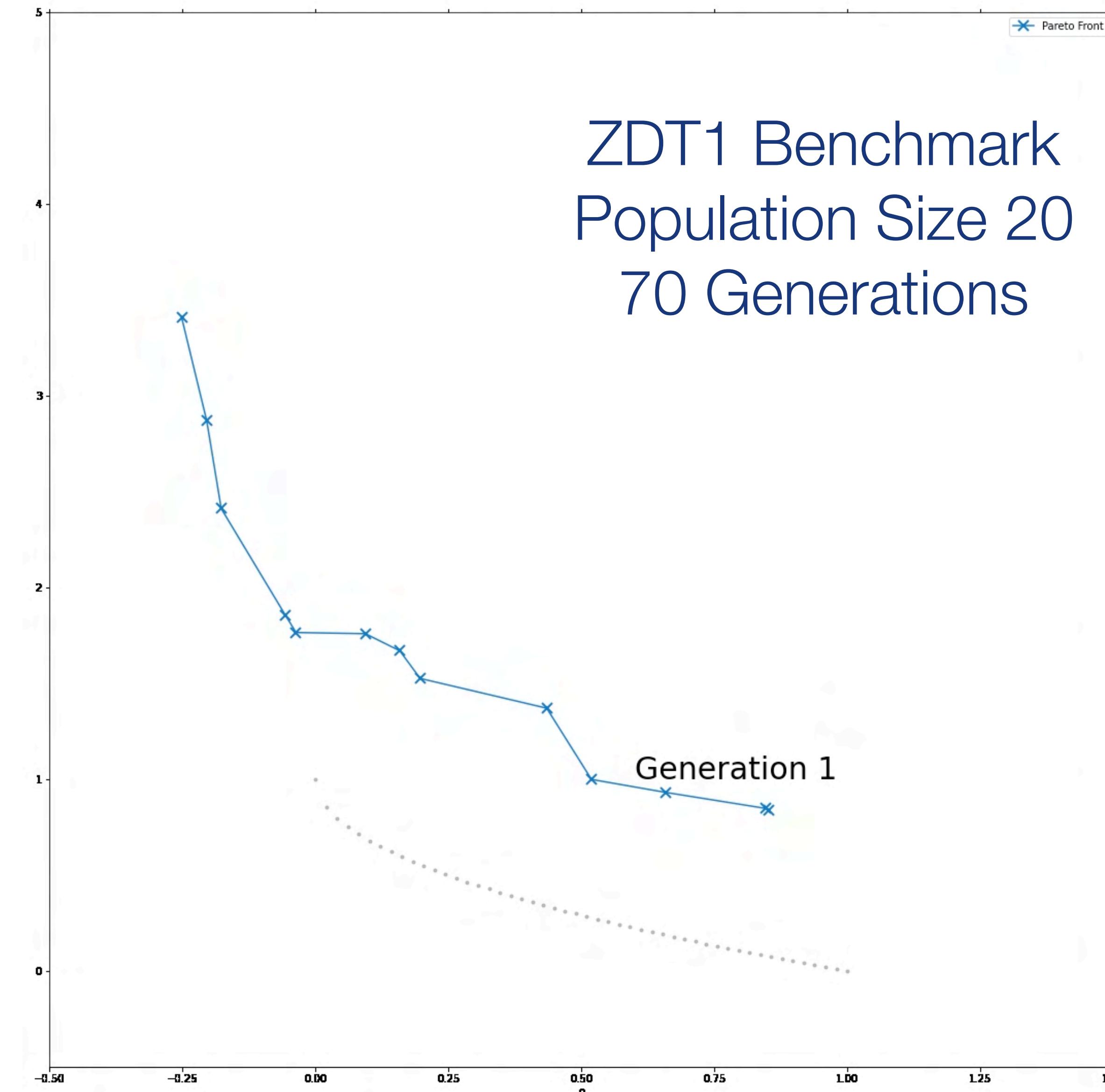
Noise Evaluation



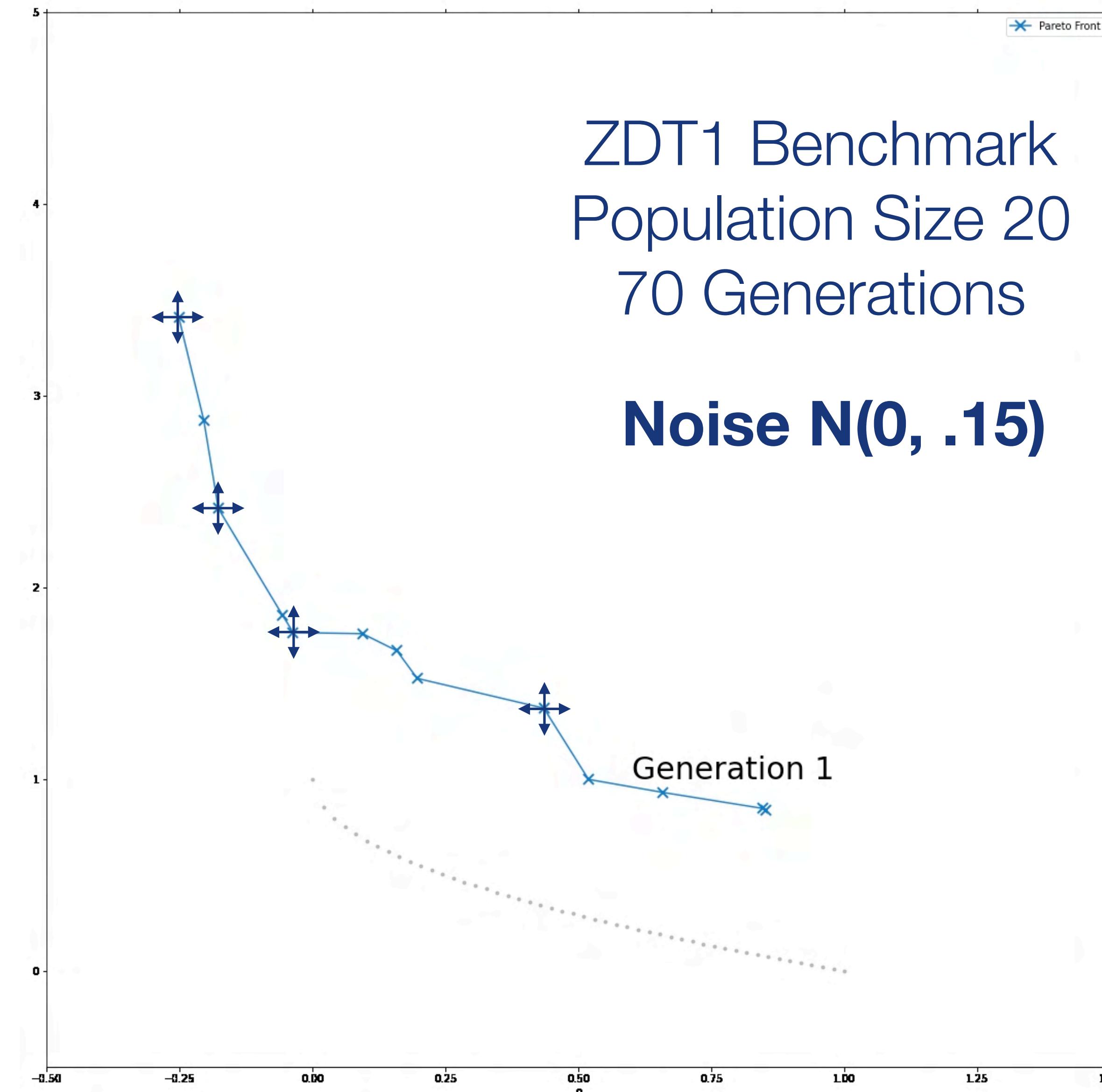
Noisy Search-Based Testing (SBT)



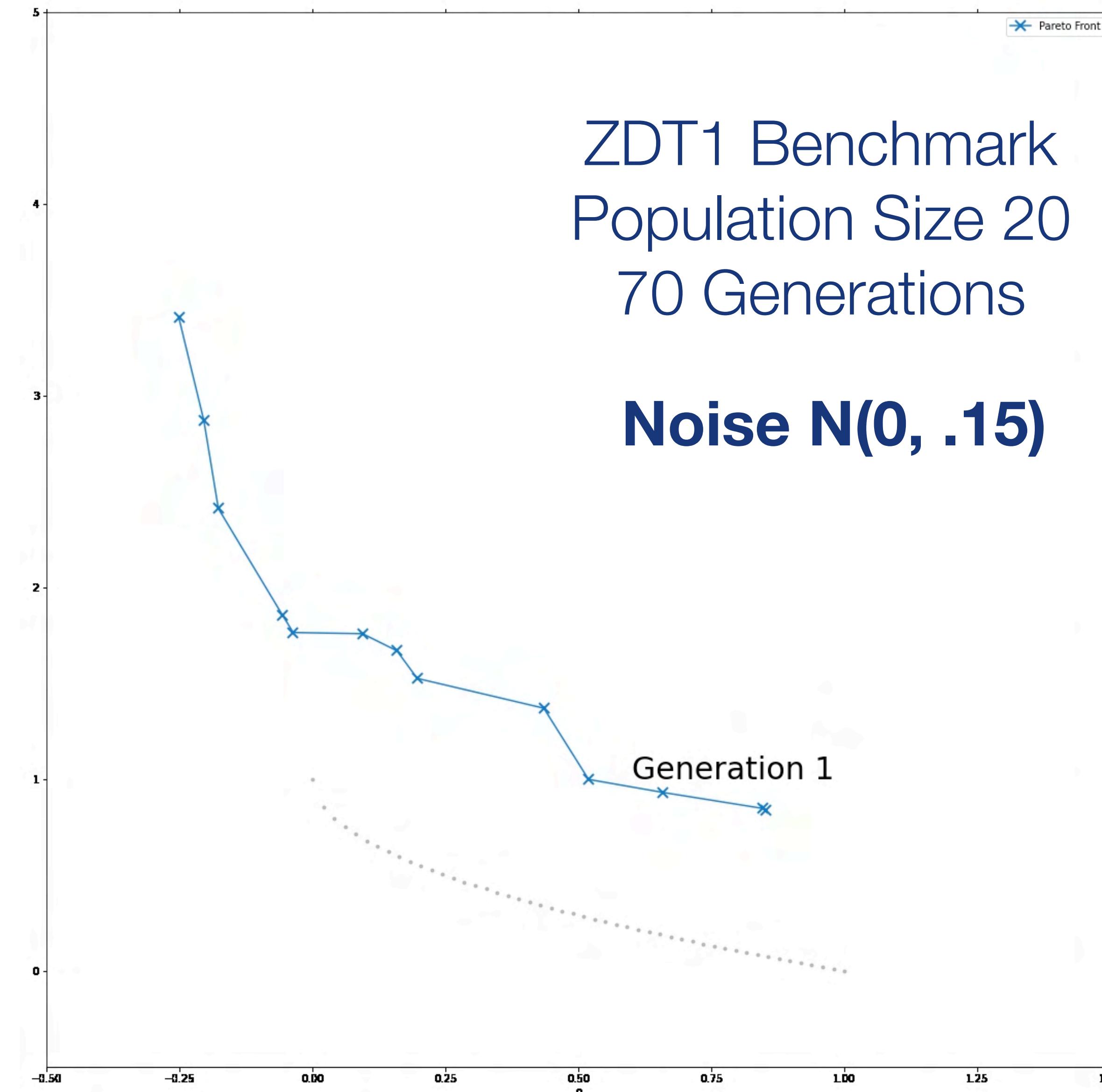
Noisy Search-Based Testing (SBT)



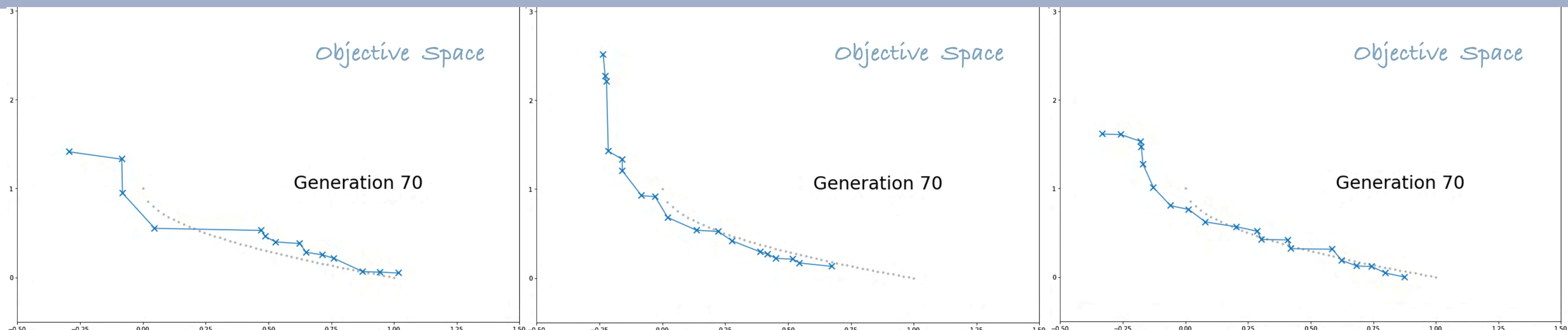
Noisy Search-Based Testing (SBT)



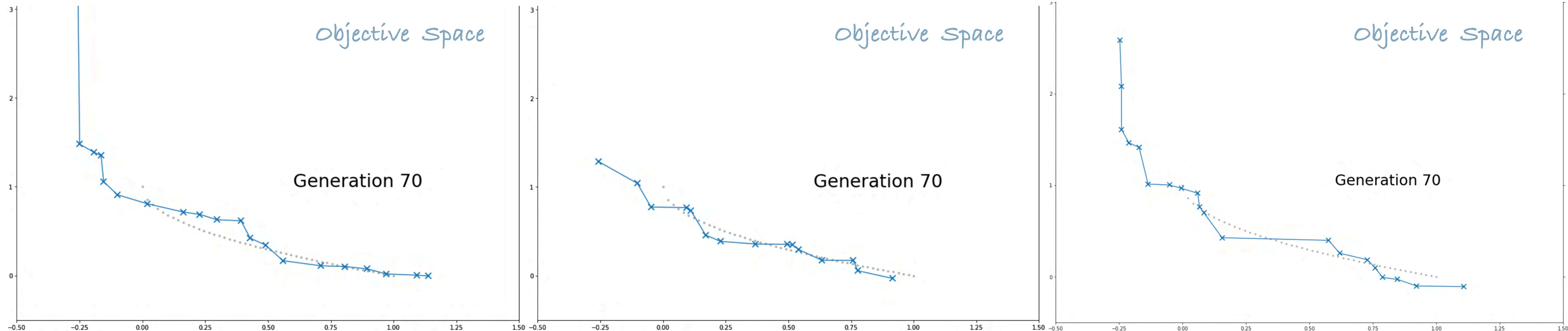
Noisy Search-Based Testing (SBT)



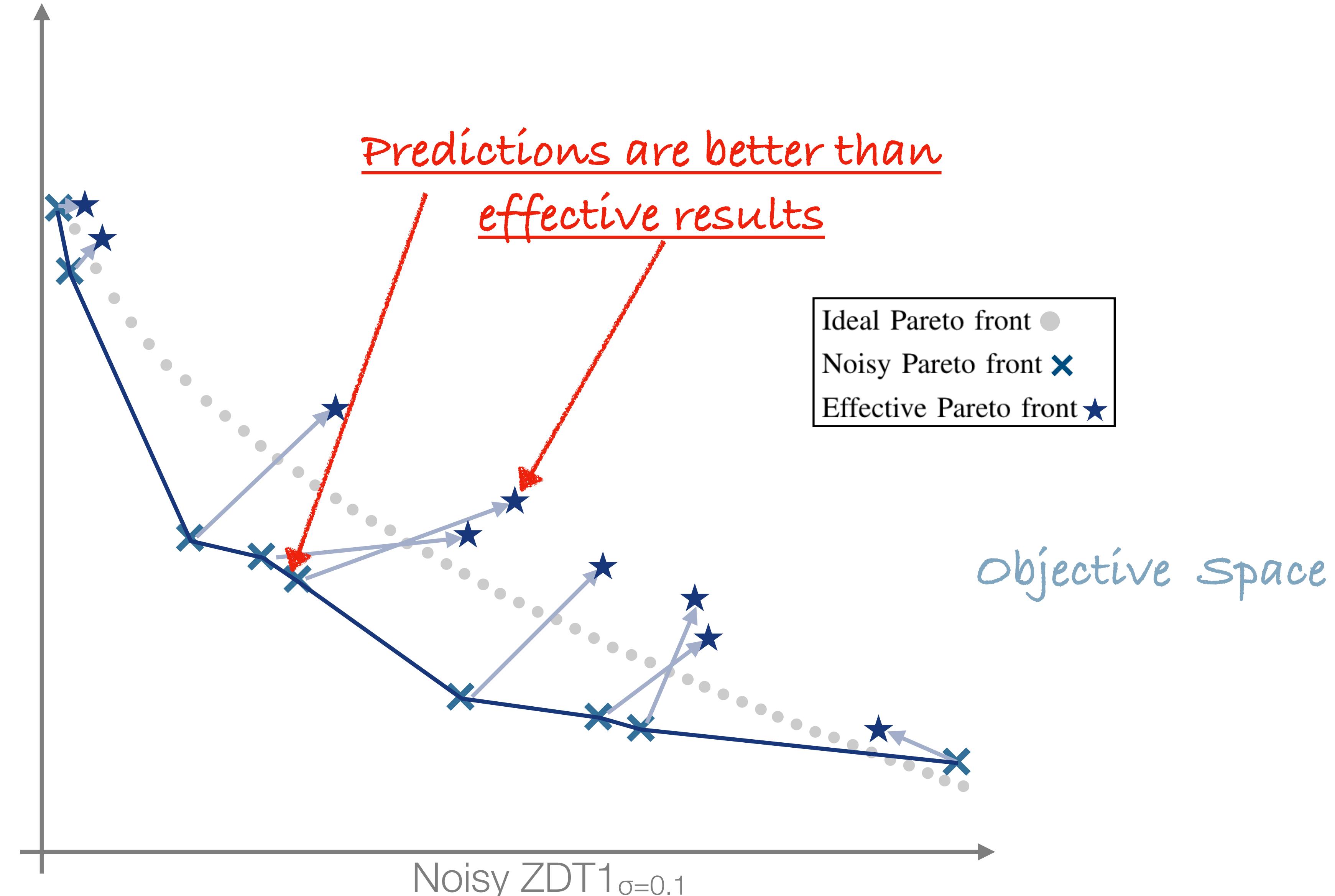
Noisy Search-Based Testing (SBT)



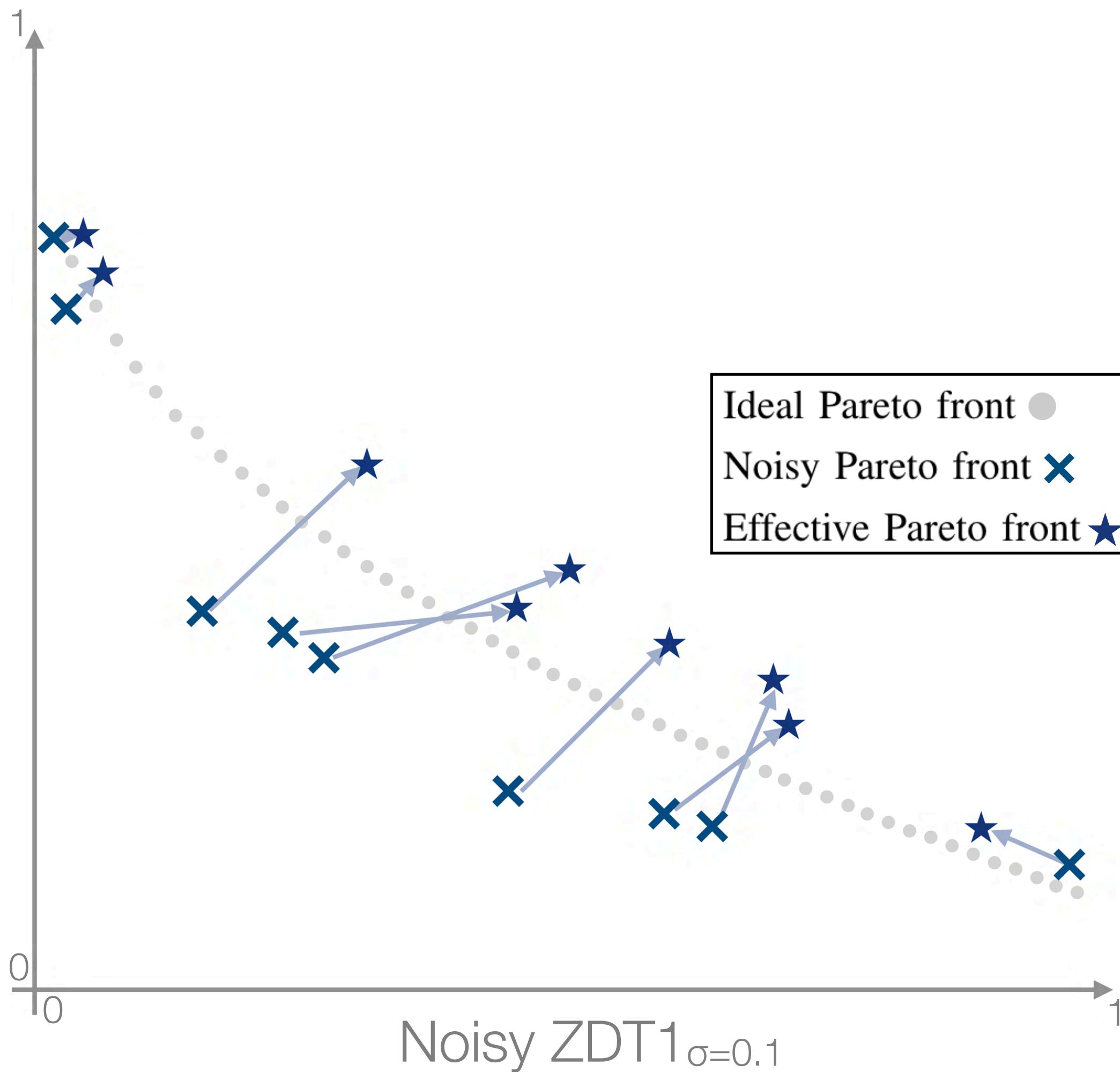
Repeat Experiments



Noisy Search-Based Testing



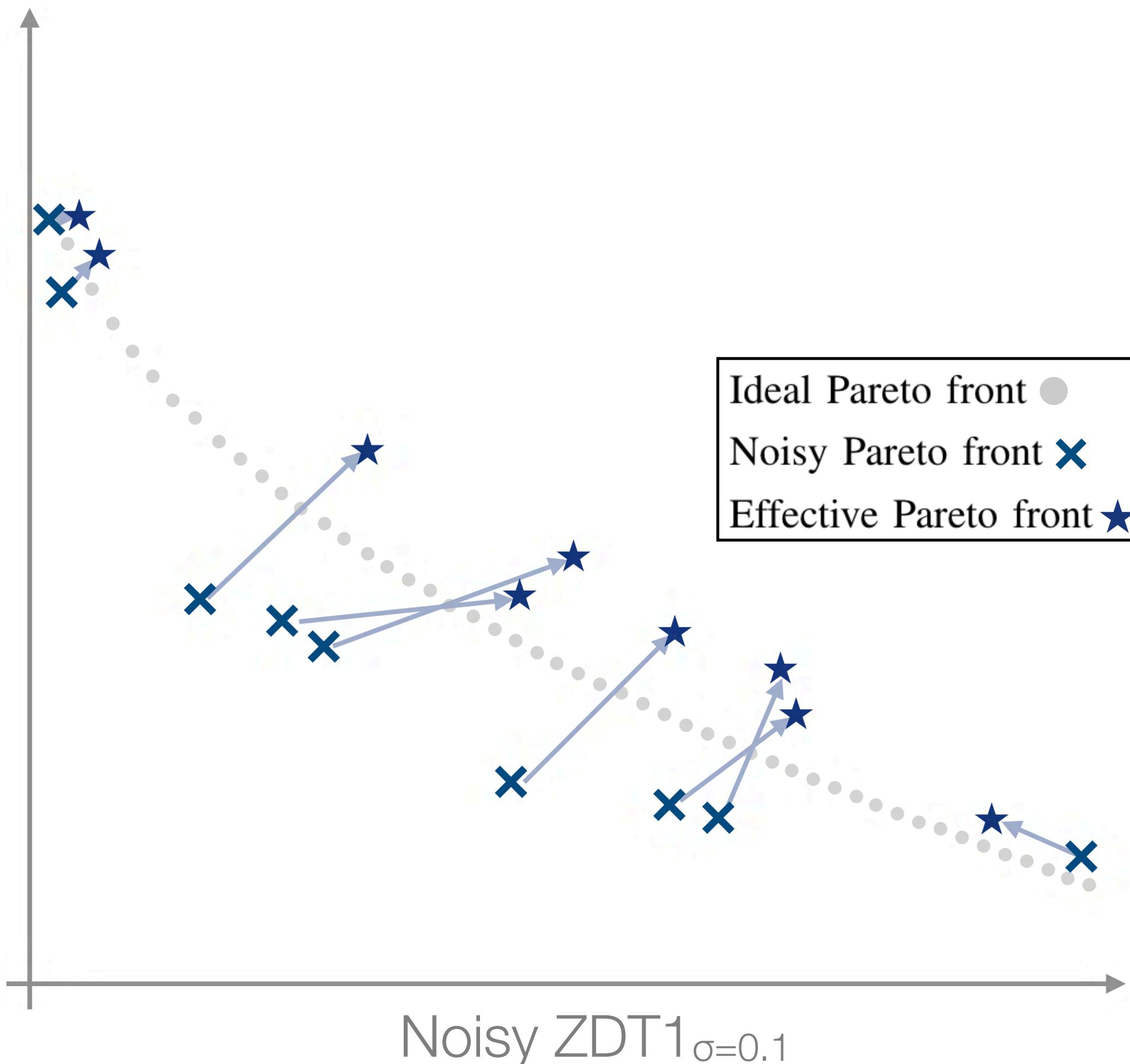
Noisy Search-Based Testing



Observations

1. (Noisy) PF surpasses Ideal PF
2. Repetition yields Effective PF
3. Some Effective PF values are dominated
4. PF (mostly) positively impacted by noise
5. PF values are extreme outliers (exceeding σ)
6. Noise hinders further improvement

Noisy Search-Based Testing



Problems

- Selection of non-representative outliers
- Yielded objectives not reproducible
(not reliable/trustworthy)

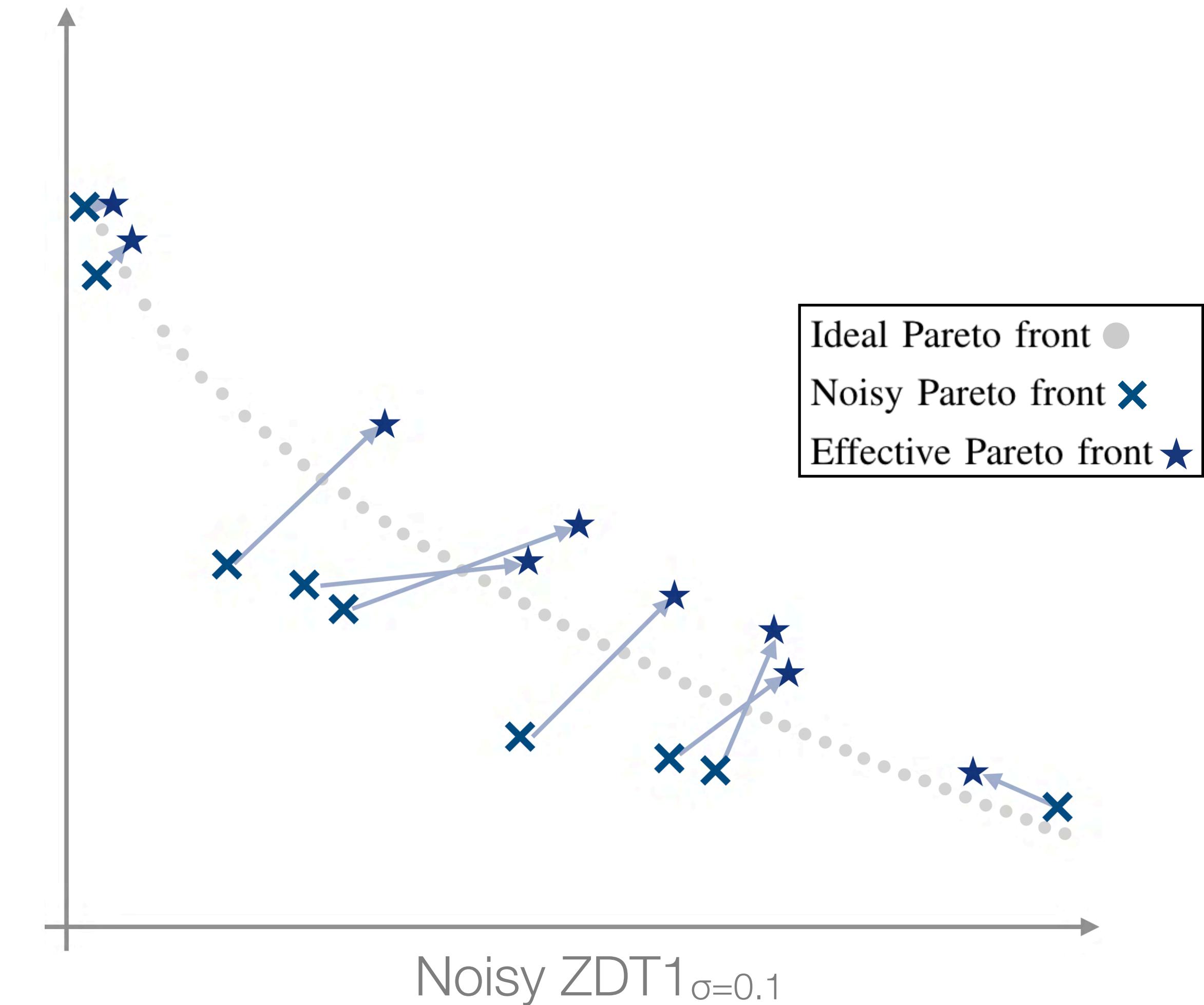
Research Goal

Our **goal** is to

push the **Pareto Front** closer
towards the **Effective Pareto Front**,

but

keep the **Effective Pareto Front** close
to the **Ideal Pareto front**.



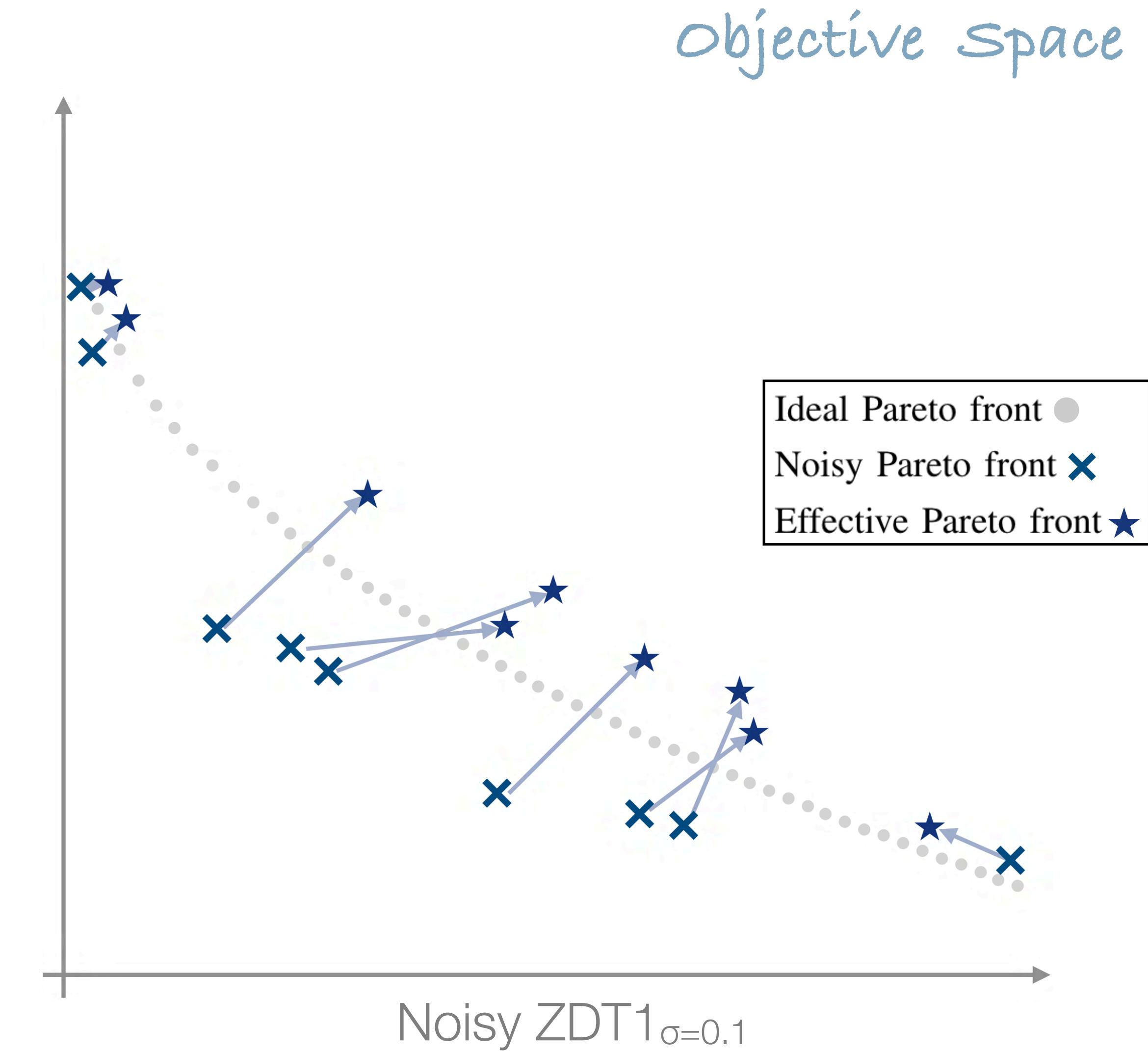
Research Goal

Our **goal** is to

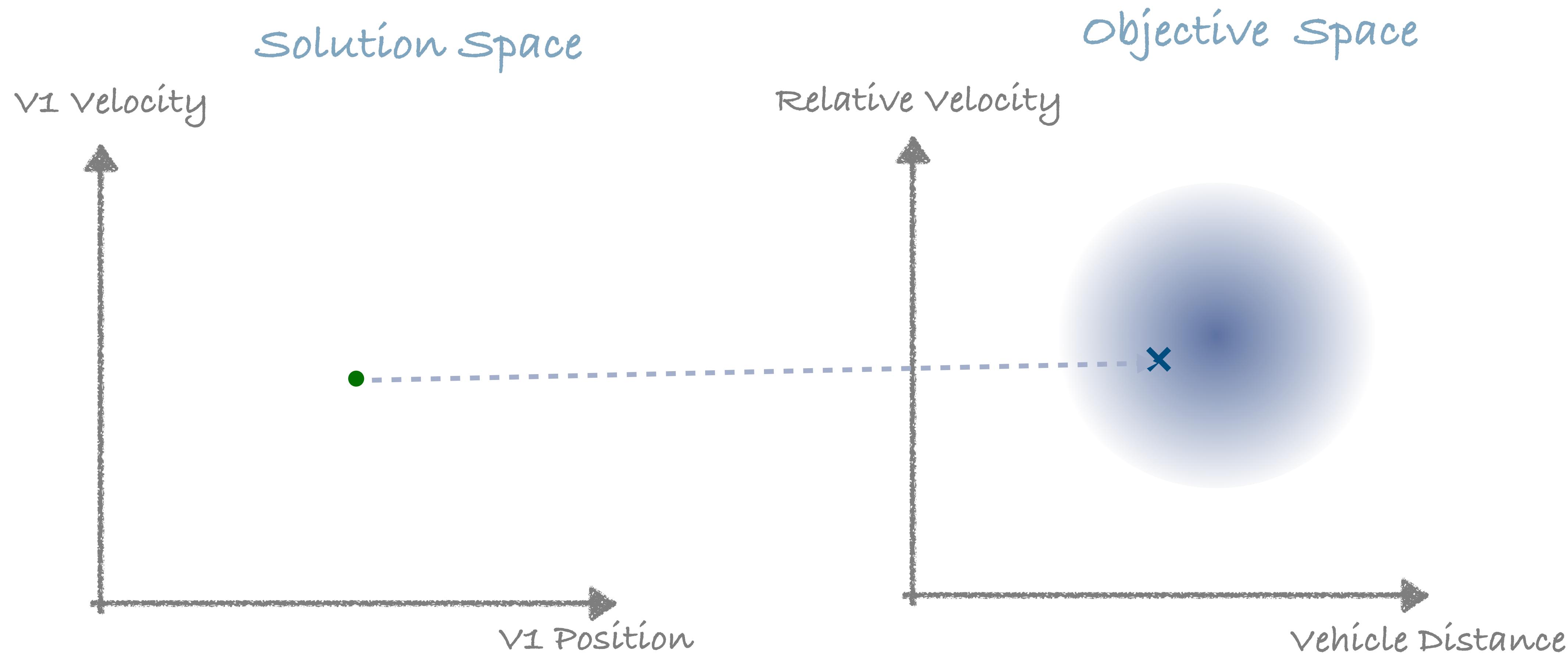
push the X closer towards the ★,

but

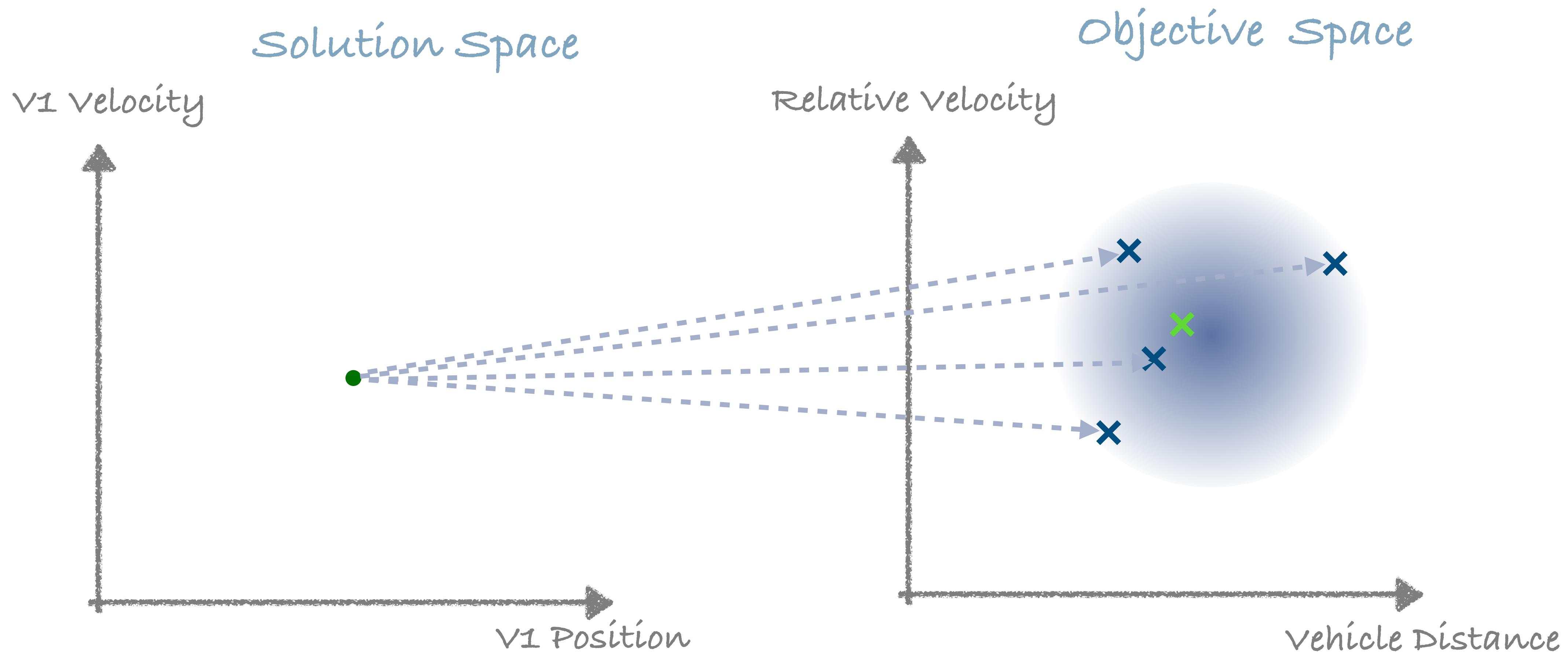
keep the ★ close to the ●.



Repetition to the Rescue



Repetition to the Rescue



But it is expensive...

$$\begin{array}{c} \text{System} \\ \left(\begin{array}{l} 1 \text{ GPU} \\ + \\ 60\text{-}120 \text{ sec} \end{array} \right) \times \left(\begin{array}{l} 10 \text{ pop size} \\ \times \\ 100 \text{ generations} \end{array} \right) = \text{15 - 30 hours} \\ \text{per scenario optimisation} \\ \\ \times 10 \text{ repetitions} = \end{array}$$



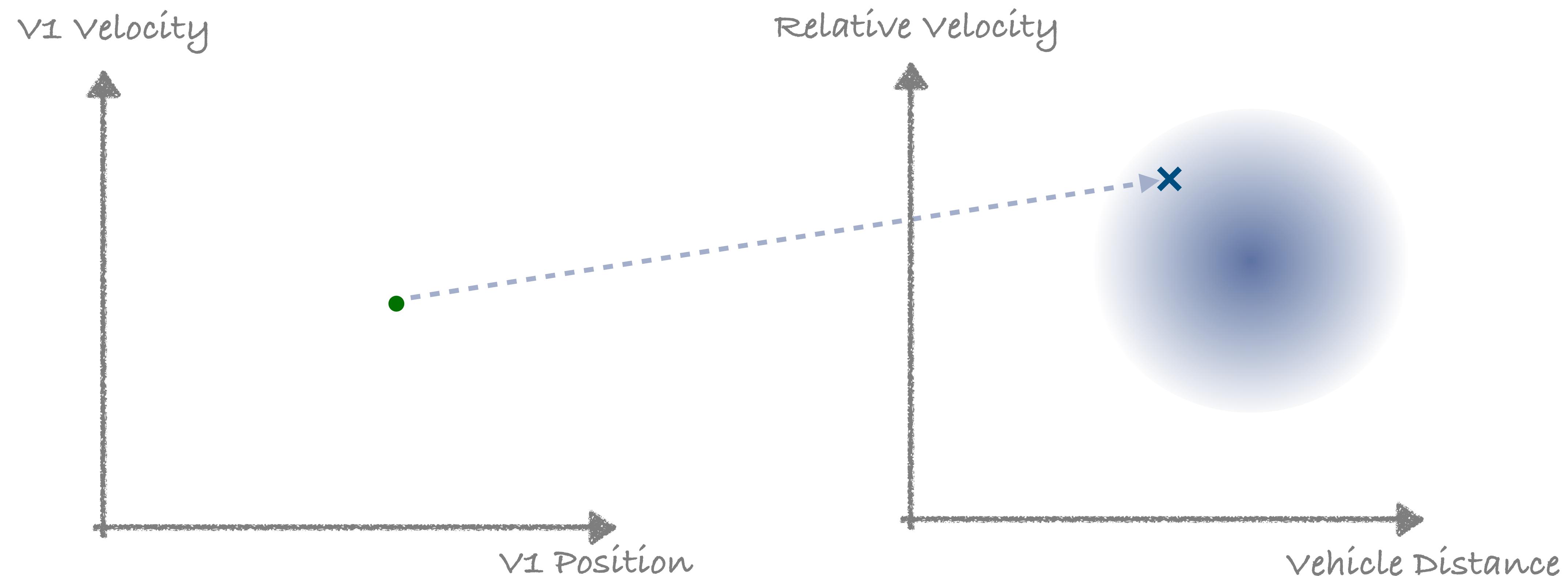
kNN-Averaging

a.k.a. *Let's repeat without repeating?*



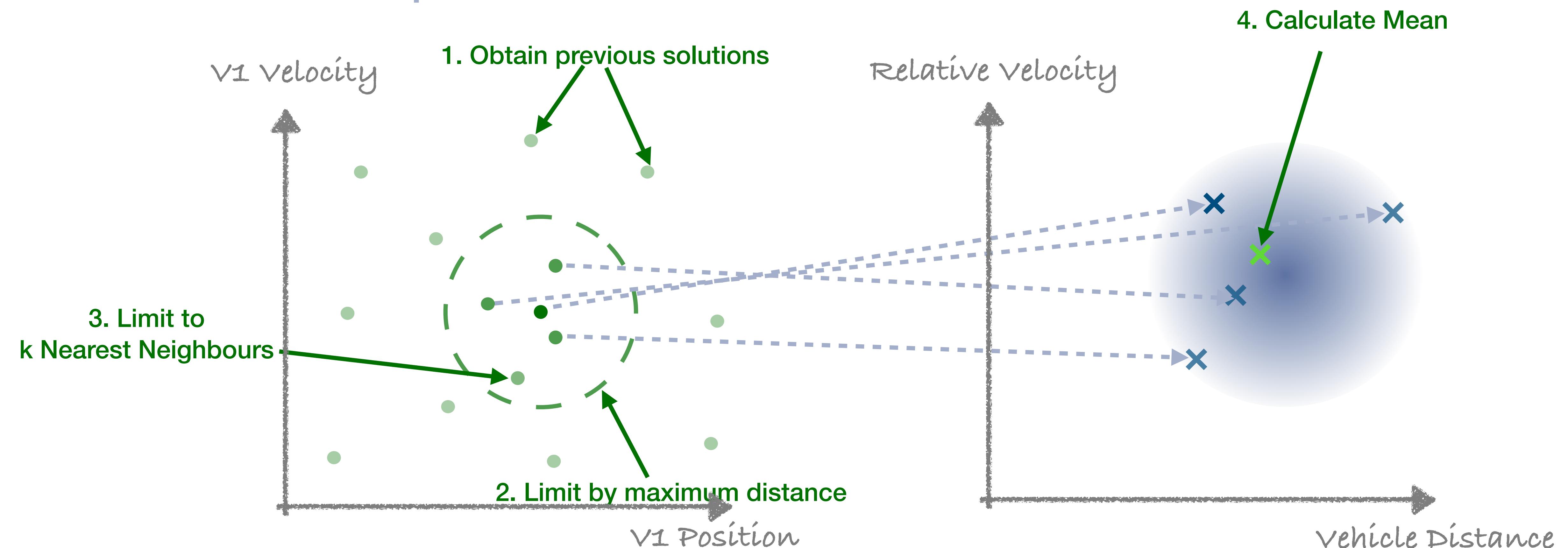
kNN-Averaging

Idea: Use Historical Values
to Simulate Repetition



kNN-Averaging

Idea: Use Historical Values
to Simulate Repetition



Open Questions (Hyper-Parameters)

How many neighbours do we need?

Intuition: Looking at more neighbours, we get a more representative value.

What's the size of the neighbourhood?

Intuition: In sparse spaces, do not use too distant neighbours.

Should close neighbours weigh more?

Intuition: Close neighbours are similar, similarity drops with distance.

Research Questions

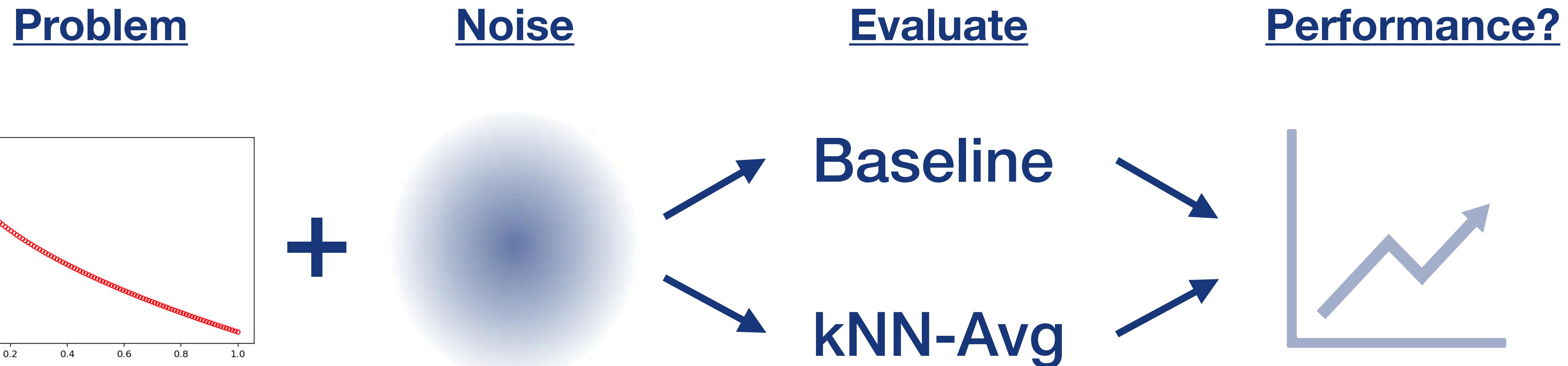
RQ1: Can kNN-Avg reduce outlier-effect?

RQ2: Are solutions by kNN-Avg better/worse?

RQ3: Relation noise-level and kNN-Avg's efficiency

RQ4: Influence of hyper-parameters

Experimental Setup



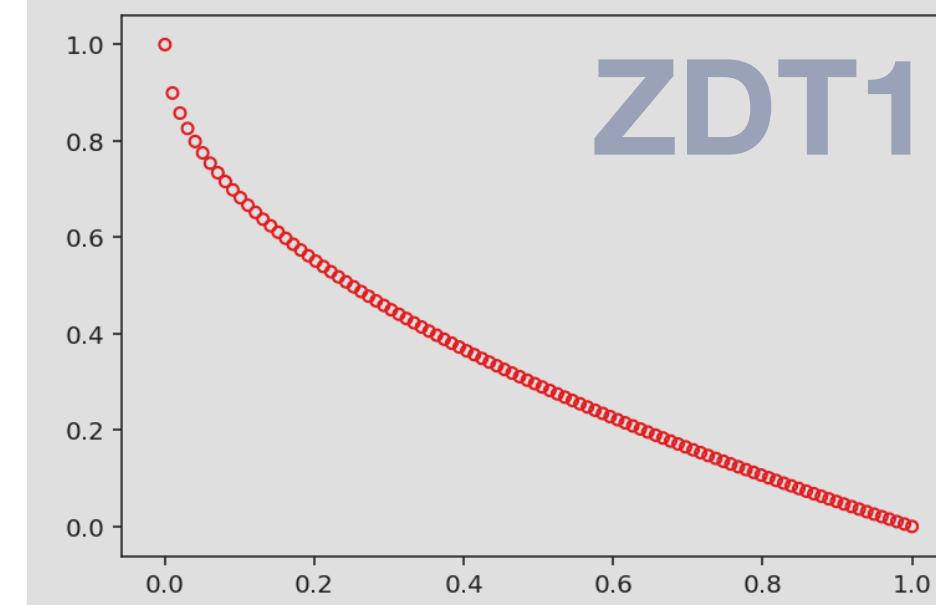
Implementation based on www.pymoo.org // NSGA-II

Experimental Setup

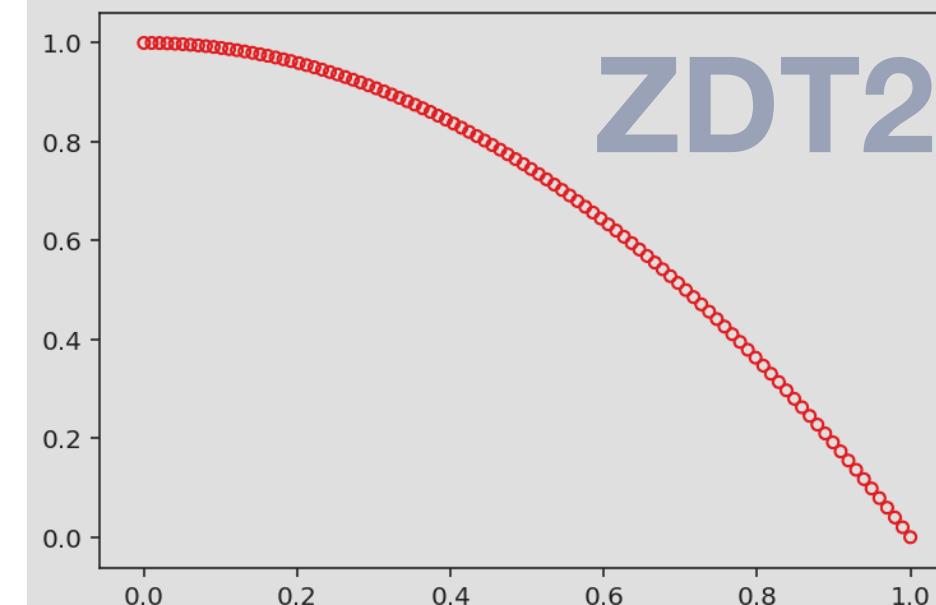
Problem

$n_{\text{var}} \in [2, 4, 10]$

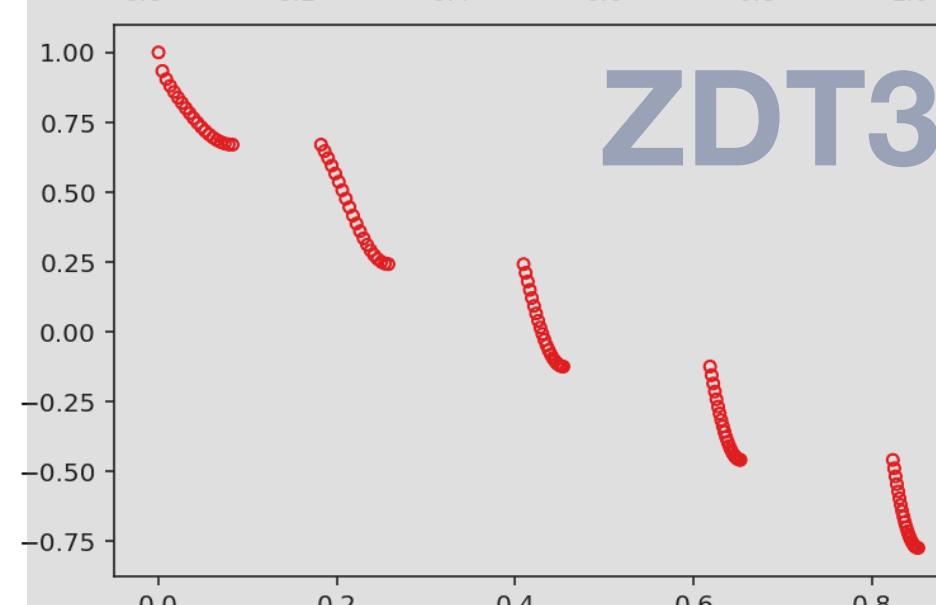
ZDT1



ZDT2

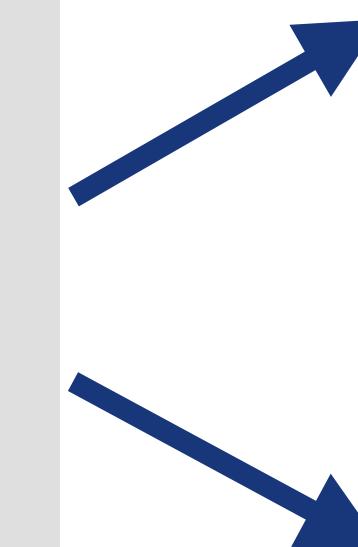
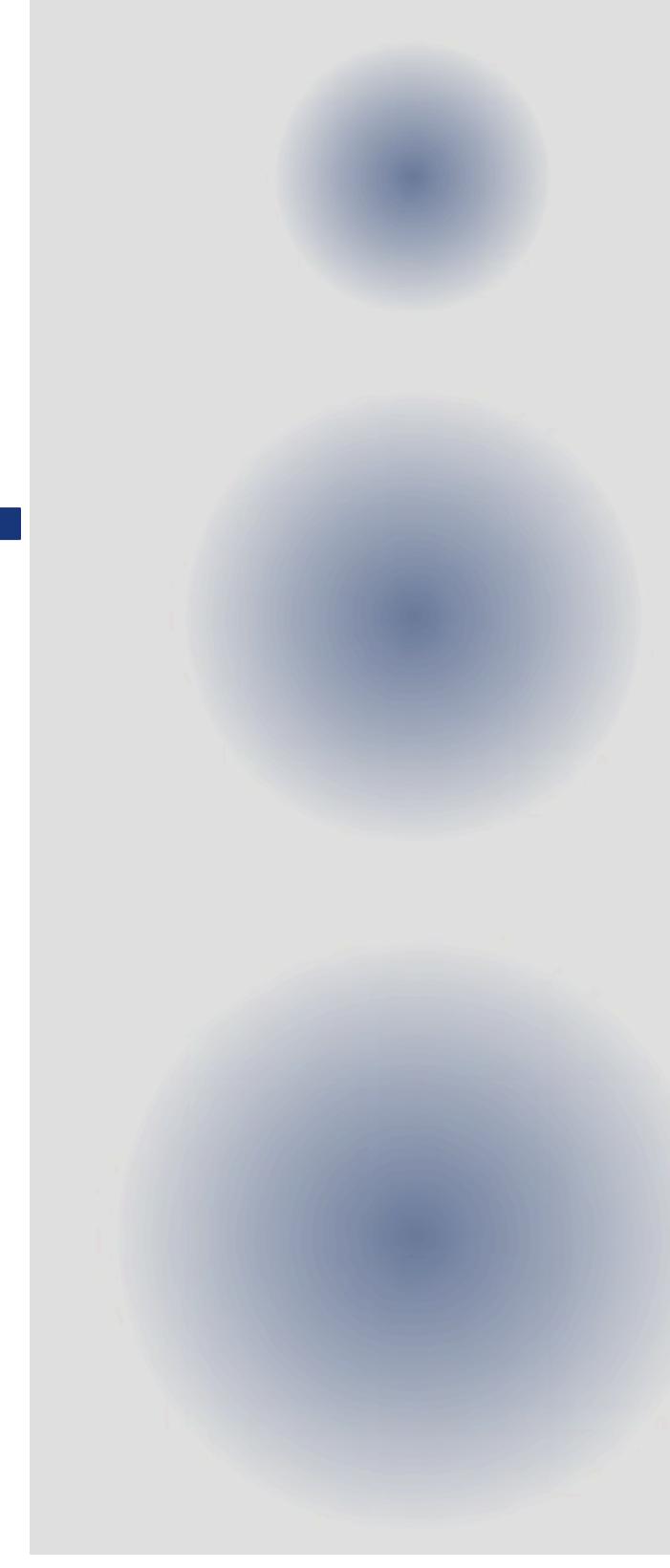


ZDT3



Noise

$\sigma \in [0, .05, .1, .25, .5]$



Evaluate

Configurations:

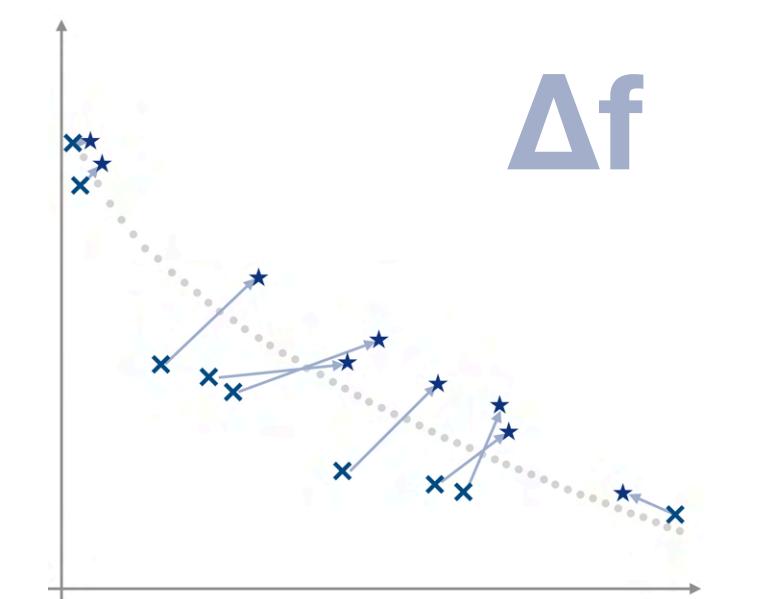
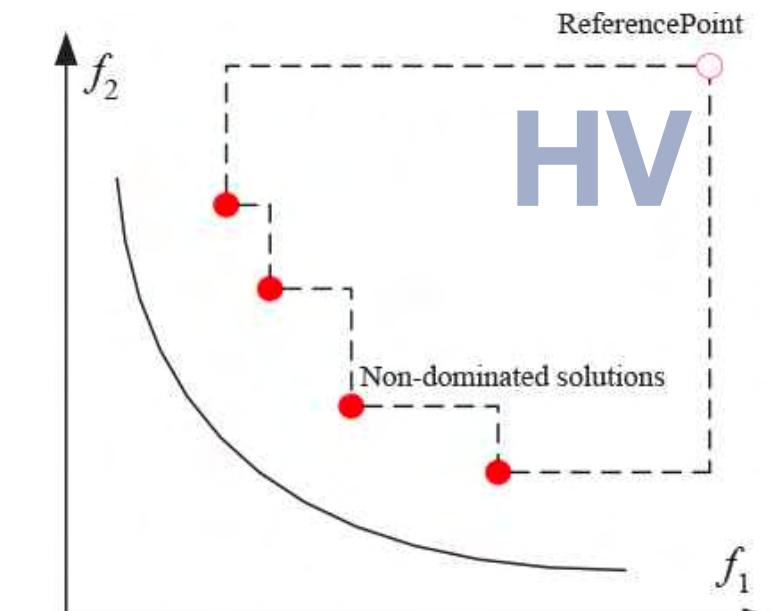
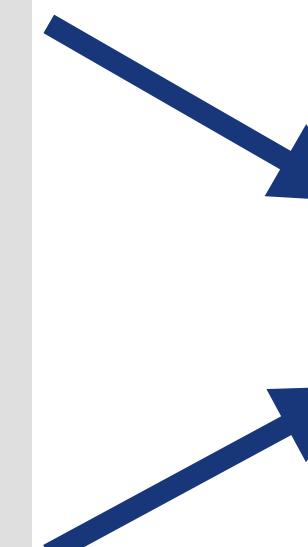
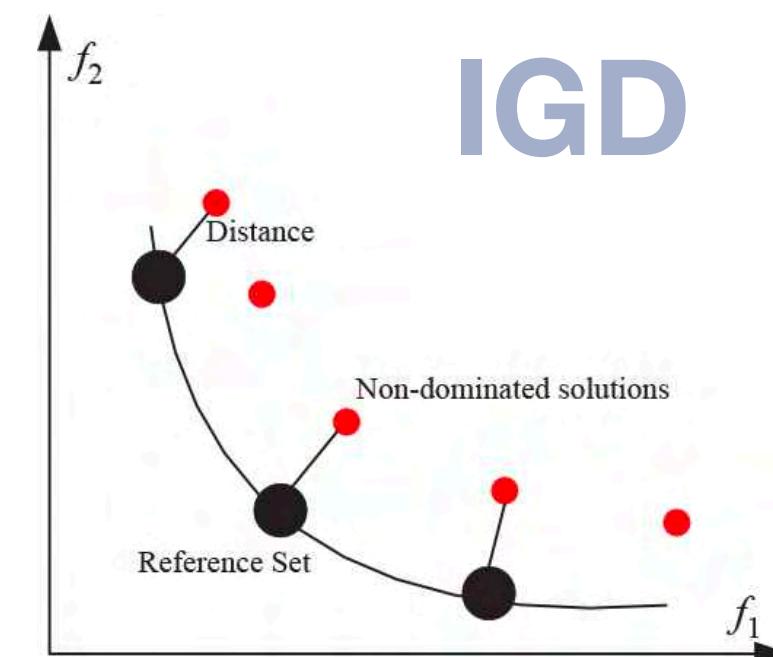
$k \in [1, 10, 25, 50, 100, 1000]$

$MD \in [.25, .5, 1, 2, 4]$

$\text{pop size} \in [10, 20]$

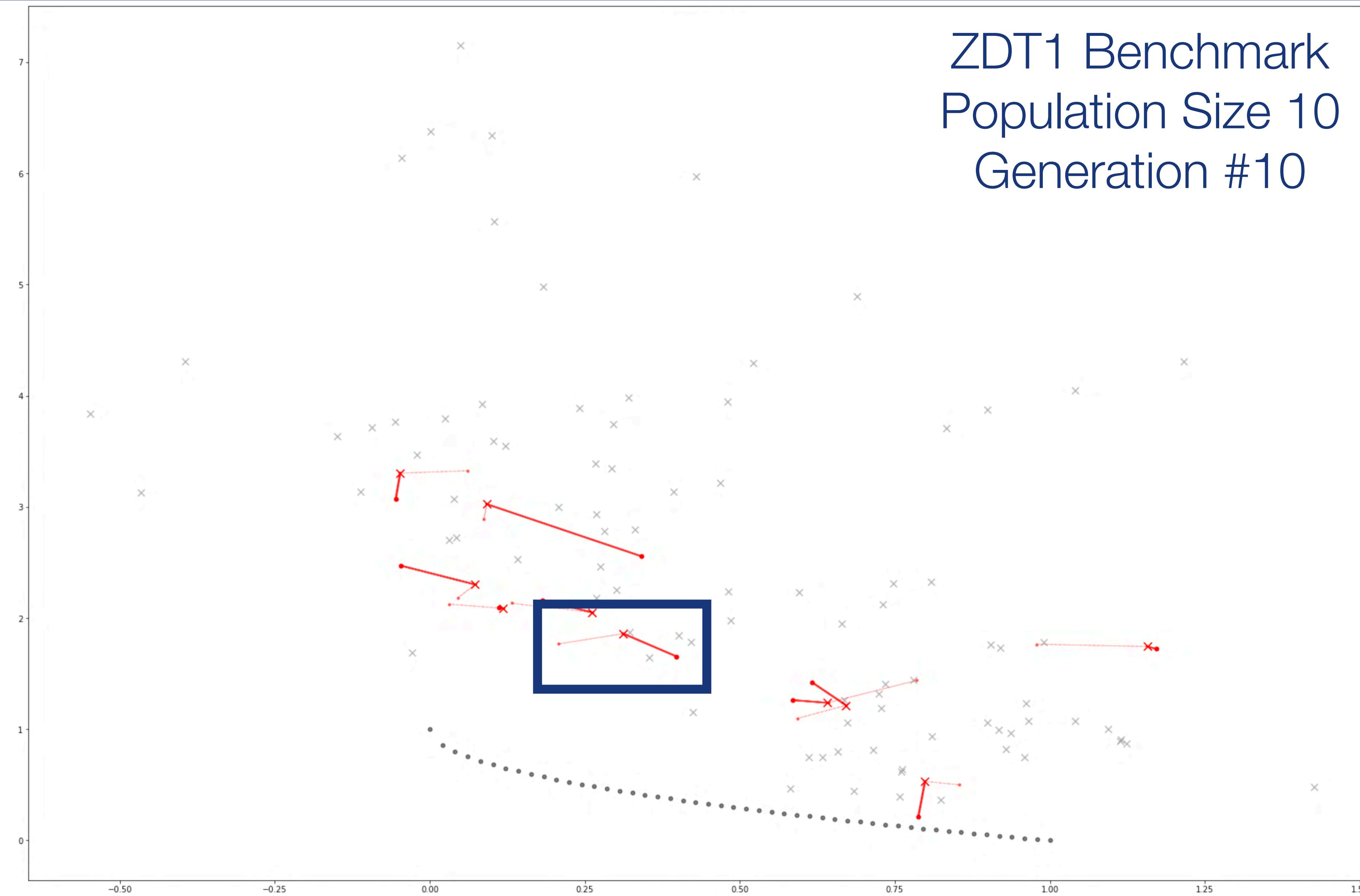
100 generations

Performance?

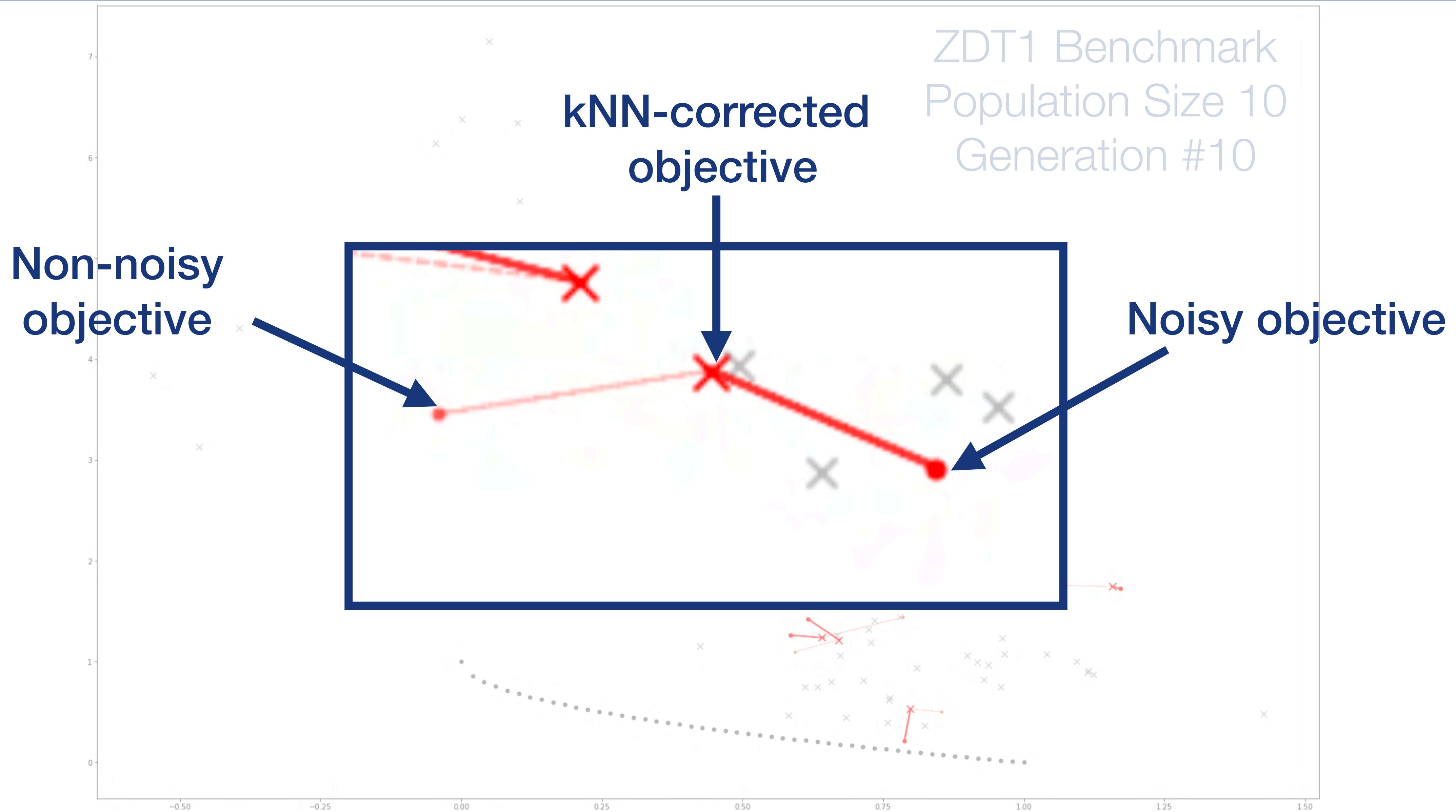


kNN-Avg Effect

ZDT1 Benchmark
Population Size 10
Generation #10

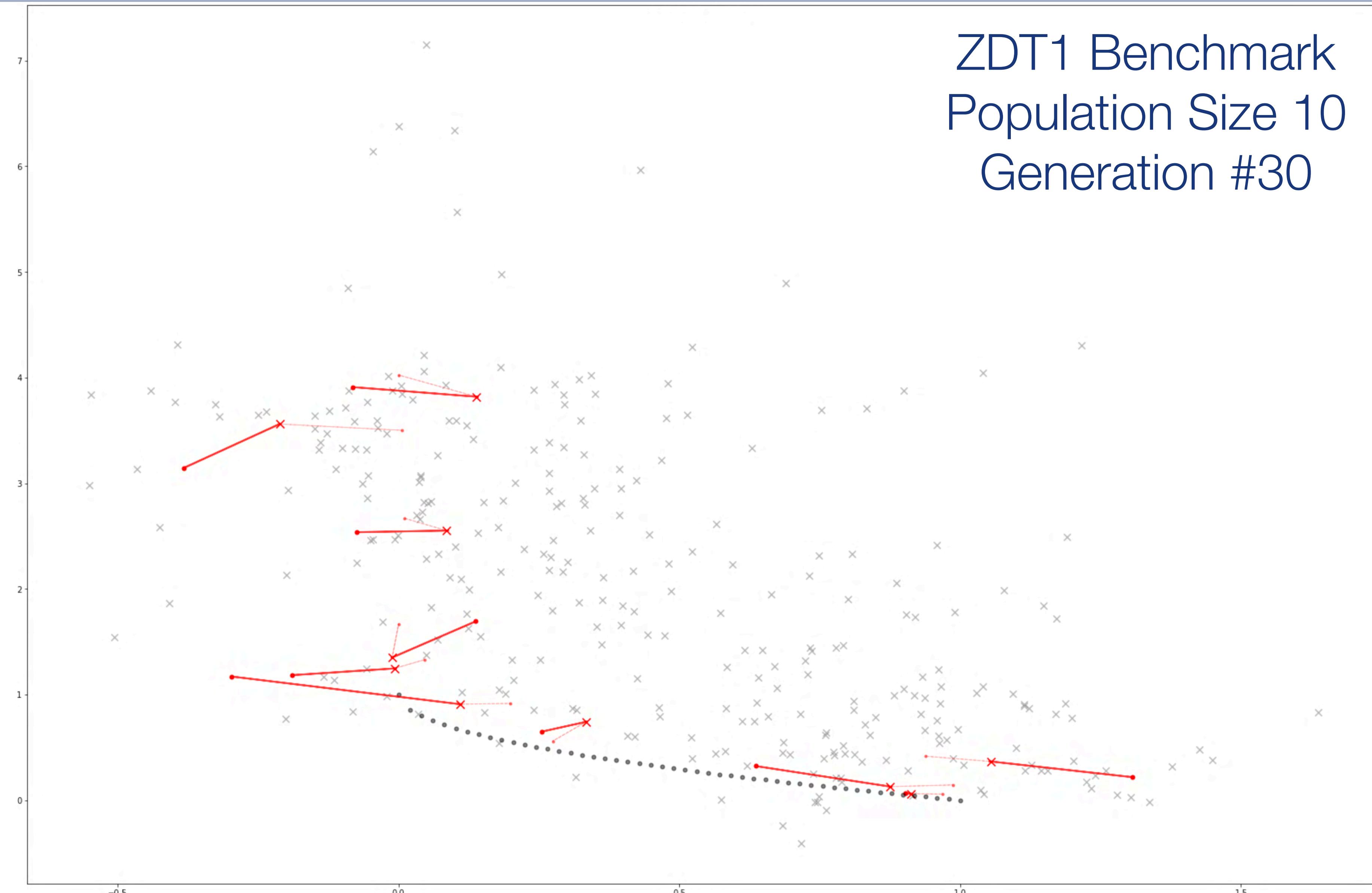


ZDT1 Benchmark
Population Size 10
Generation #10



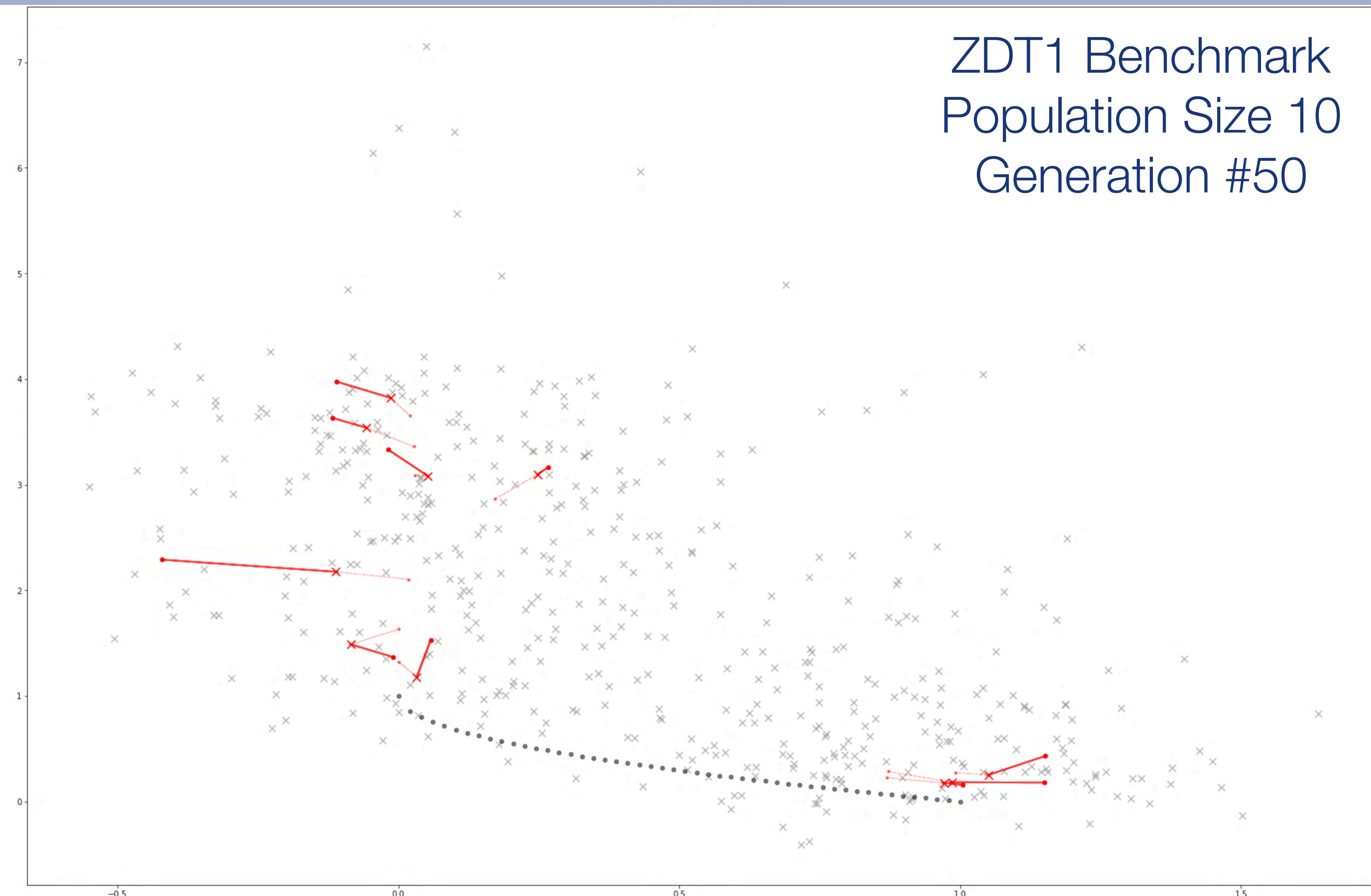
kNN-Avg Effect

ZDT1 Benchmark
Population Size 10
Generation #30



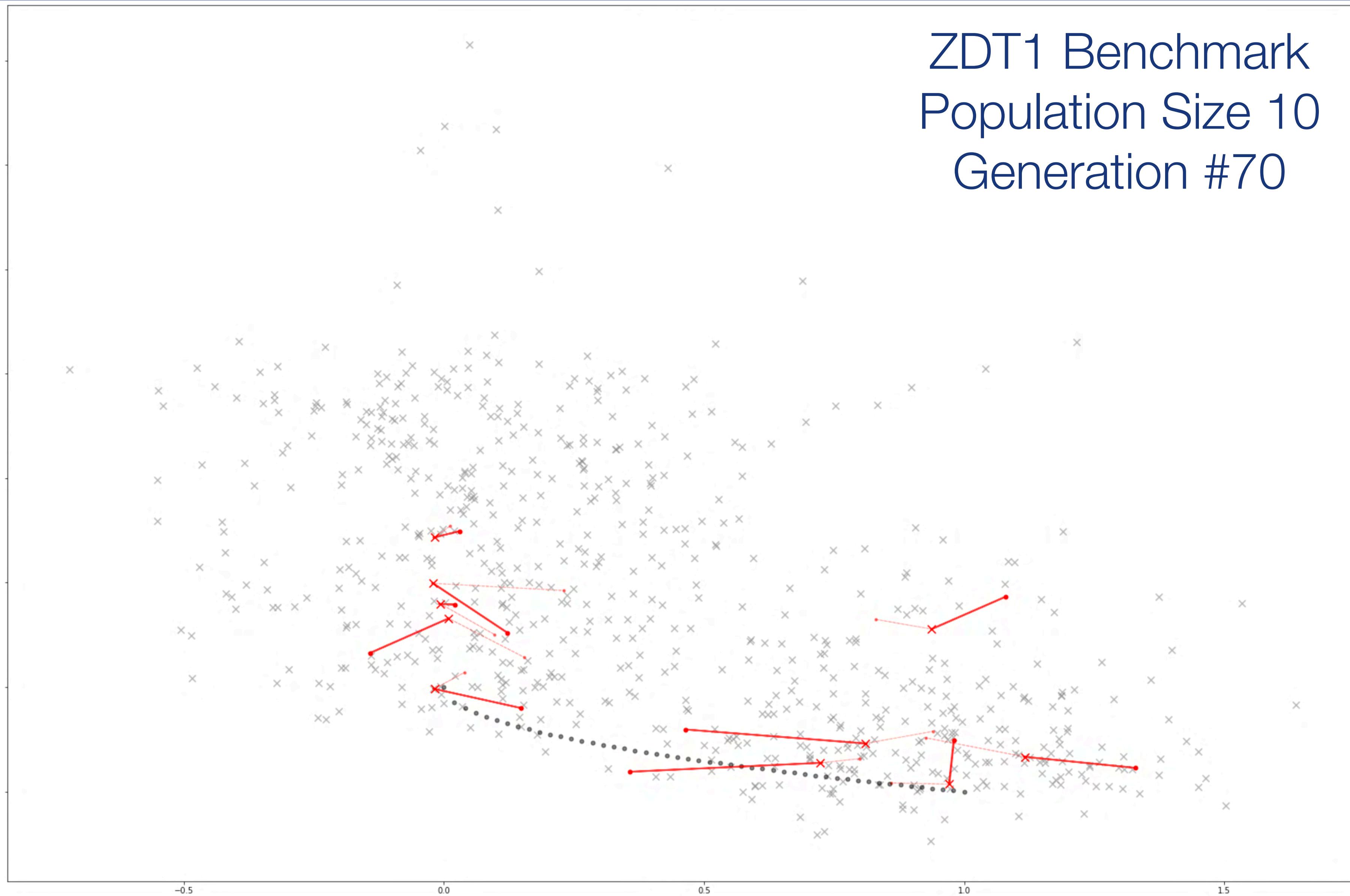
kNN-Avg Effect

ZDT1 Benchmark
Population Size 10
Generation #50



kNN-Avg Effect

ZDT1 Benchmark
Population Size 10
Generation #70



Results

KNN^{MD}_k

(a) No noise (b) $\sigma = 0.05$ (c) $\sigma = 0.1$ (d) $\sigma = 0.25$ (e) $\sigma = 0.5$

App.	HV	IGD	Δf	App.	HV	IGD	Δf	App.	HV	IGD	Δf	App.	HV	IGD	Δf	App.	HV	IGD	Δf	
KNN ₁₀ ^{0.25}	≡	X	X	KNN ₁₀ ^{0.25}	X	≡	✓	KNN ₁₀ ^{0.25}	≡	✓	✓	KNN ₁₀ ^{0.25}	≡	≡	✓	KNN ₁₀ ^{0.25}	≡	≡	✓	
KNN ₁₀ ^{0.5}	X	X	X		KNN ₁₀ ^{0.5}	≡	≡	✓	KNN ₁₀ ^{0.5}	≡	≡	✓	KNN ₁₀ ^{0.5}	≡	≡	✓	KNN ₁₀ ^{0.5}	≡	≡	✓
KNN ₁₀ ^{1.0}	X	X	X		KNN ₁₀ ^{1.0}	X	X	✓	KNN ₁₀ ^{1.0}	≡	≡	✓	KNN ₁₀ ^{1.0}	≡	≡	✓	KNN ₁₀ ^{1.0}	≡	≡	✓
KNN ₁₀ ^{2.0}	X	X	X		KNN ₁₀ ^{2.0}	X	X	✓	KNN ₁₀ ^{2.0}	X	X	✓	KNN ₁₀ ^{2.0}	≡	✓	✓	KNN ₁₀ ^{2.0}	≡	≡	✓
KNN ₁₀ ^{4.0}	X	X	X		KNN ₁₀ ^{4.0}	X	X	✓	KNN ₁₀ ^{4.0}	X	X	✓	KNN ₁₀ ^{4.0}	X	≡	✓	KNN ₁₀ ^{4.0}	≡	≡	✓
KNN ₂₅ ^{0.25}	X	X	X		KNN ₂₅ ^{0.25}	≡	≡	✓	KNN ₂₅ ^{0.25}	≡	✓	✓	KNN ₂₅ ^{0.25}	≡	≡	✓	KNN ₂₅ ^{0.25}	≡	≡	✓
KNN ₂₅ ^{0.5}	X	X	X		KNN ₂₅ ^{0.5}	X	X	✓	KNN ₂₅ ^{0.5}	≡	≡	✓	KNN ₂₅ ^{0.5}	≡	≡	✓	KNN ₂₅ ^{0.5}	≡	≡	✓
KNN ₂₅ ^{1.0}	X	X	X		KNN ₂₅ ^{1.0}	X	X	✓	KNN ₂₅ ^{1.0}	X	≡	✓	KNN ₂₅ ^{1.0}	≡	≡	✓	KNN ₂₅ ^{1.0}	≡	≡	✓
KNN ₂₅ ^{2.0}	X	X	X		KNN ₂₅ ^{2.0}	X	X	✓	KNN ₂₅ ^{2.0}	X	X	✓	KNN ₂₅ ^{2.0}	X	≡	✓	KNN ₂₅ ^{2.0}	≡	≡	✓
KNN ₂₅ ^{4.0}	X	X	X		KNN ₂₅ ^{4.0}	X	X	≡	KNN ₂₅ ^{4.0}	X	X	✓	KNN ₂₅ ^{4.0}	X	≡	✓	KNN ₂₅ ^{4.0}	≡	≡	✓
KNN ₅₀ ^{0.25}	X	X	X	KNN ₅₀ ^{0.25}	KNN ₅₀ ^{0.25}	≡	≡	KNN ₅₀ ^{0.25}	≡	≡	✓	KNN ₅₀ ^{0.25}	✓	✓	✓	KNN ₅₀ ^{0.25}	≡	≡	✓	
KNN ₅₀ ^{0.5}	X	X	X		KNN ₅₀ ^{0.5}	≡	≡	✓	KNN ₅₀ ^{0.5}	≡	≡	✓	KNN ₅₀ ^{0.5}	≡	≡	✓	KNN ₅₀ ^{0.5}	≡	≡	✓
KNN ₅₀ ^{1.0}	X	X	X		KNN ₅₀ ^{1.0}	X	X	✓	KNN ₅₀ ^{1.0}	≡	≡	✓	KNN ₅₀ ^{1.0}	≡	✓	✓	KNN ₅₀ ^{1.0}	≡	≡	✓
KNN ₅₀ ^{2.0}	X	X	X		KNN ₅₀ ^{2.0}	X	X	≡	KNN ₅₀ ^{2.0}	X	X	✓	KNN ₅₀ ^{2.0}	X	≡	✓	KNN ₅₀ ^{2.0}	≡	≡	✓
KNN ₅₀ ^{4.0}	X	X	X		KNN ₅₀ ^{4.0}	X	X	≡	KNN ₅₀ ^{4.0}	X	X	✓	KNN ₅₀ ^{4.0}	X	≡	✓	KNN ₅₀ ^{4.0}	≡	≡	✓
KNN ₁₀₀ ^{0.25}	X	X	X		KNN ₁₀₀ ^{0.25}	≡	≡	✓	KNN ₁₀₀ ^{0.25}	≡	≡	✓	KNN ₁₀₀ ^{0.25}	≡	✓	✓	KNN ₁₀₀ ^{0.25}	≡	≡	✓
KNN ₁₀₀ ^{0.5}	X	X	X		KNN ₁₀₀ ^{0.5}	X	X	✓	KNN ₁₀₀ ^{0.5}	≡	≡	✓	KNN ₁₀₀ ^{0.5}	≡	✓	✓	KNN ₁₀₀ ^{0.5}	≡	≡	✓
KNN ₁₀₀ ^{1.0}	X	X	X		KNN ₁₀₀ ^{1.0}	X	X	≡	KNN ₁₀₀ ^{1.0}	≡	≡	✓	KNN ₁₀₀ ^{1.0}	≡	✓	✓	KNN ₁₀₀ ^{1.0}	≡	≡	✓
KNN ₁₀₀ ^{2.0}	X	X	X		KNN ₁₀₀ ^{2.0}	X	X	≡	KNN ₁₀₀ ^{2.0}	X	X	✓	KNN ₁₀₀ ^{2.0}	≡	✓	✓	KNN ₁₀₀ ^{2.0}	≡	≡	✓
KNN ₁₀₀ ^{4.0}	X	X	X		KNN ₁₀₀ ^{4.0}	X	X	≡	KNN ₁₀₀ ^{4.0}	X	X	✓	KNN ₁₀₀ ^{4.0}	X	≡	✓	KNN ₁₀₀ ^{4.0}	≡	≡	✓
KNN ₁₀₀₀ ^{0.25}	X	X	X	KNN ₁₀₀₀ ^{0.25}	KNN ₁₀₀₀ ^{0.25}	≡	≡	KNN ₁₀₀₀ ^{0.25}	≡	✓	✓	KNN ₁₀₀₀ ^{0.25}	≡	✓	✓	KNN ₁₀₀₀ ^{0.25}	≡	≡	✓	
KNN ₁₀₀₀ ^{0.5}	X	X	X		KNN ₁₀₀₀ ^{0.5}	X	X	✓	KNN ₁₀₀₀ ^{0.5}	≡	≡	✓	KNN ₁₀₀₀ ^{0.5}	≡	✓	✓	KNN ₁₀₀₀ ^{0.5}	≡	≡	✓
KNN ₁₀₀₀ ^{1.0}	X	X	X		KNN ₁₀₀₀ ^{1.0}	X	X	≡	KNN ₁₀₀₀ ^{1.0}	≡	≡	✓	KNN ₁₀₀₀ ^{1.0}	≡	✓	✓	KNN ₁₀₀₀ ^{1.0}	≡	≡	✓
KNN ₁₀₀₀ ^{2.0}	X	X	X		KNN ₁₀₀₀ ^{2.0}	X	X	≡	KNN ₁₀₀₀ ^{2.0}	X	X	≡	KNN ₁₀₀₀ ^{2.0}	≡	✓	✓	KNN ₁₀₀₀ ^{2.0}	≡	≡	✓
KNN ₁₀₀₀ ^{4.0}	X	X	X		KNN ₁₀₀₀ ^{4.0}	X	X	≡	KNN ₁₀₀₀ ^{4.0}	X	X	≡	KNN ₁₀₀₀ ^{4.0}	≡	✓	✓	KNN ₁₀₀₀ ^{4.0}	≡	≡	✓

Hyper-Parameters

KNN^{MD}_k

	(a) No noise	(b) $\sigma = 0.05$	(c) $\sigma = 0.1$	(d) $\sigma = 0.25$	(e) $\sigma = 0.5$
	App. HV IGD Δf				
K=10	KNN ₁₀ ^{0.25} ≡ X X	KNN ₁₀ ^{0.25} X ≡ ✓	KNN ₁₀ ^{0.25} ≡ ✓ ✓	KNN ₁₀ ^{0.25} ≡ ≡ ✓	KNN ₁₀ ^{0.25} ≡ ≡ ✓
	KNN ₁₀ ^{0.5} X X X	KNN ₁₀ ^{0.5} ≡ ≡ ✓			
	KNN ₁₀ ^{1.0} X X X	KNN ₁₀ ^{1.0} X X ✓	KNN ₁₀ ^{1.0} ≡ ≡ ✓	KNN ₁₀ ^{1.0} ≡ ≡ ✓	KNN ₁₀ ^{1.0} ≡ ≡ ✓
	KNN ₁₀ ^{2.0} X X X	KNN ₁₀ ^{2.0} X X ✓	KNN ₁₀ ^{2.0} X X ✓	KNN ₁₀ ^{2.0} ≡ ≡ ✓	KNN ₁₀ ^{2.0} ≡ ≡ ✓
	KNN ₁₀ ^{4.0} X X X	KNN ₁₀ ^{4.0} X X ✓	KNN ₁₀ ^{4.0} X X ✓	KNN ₁₀ ^{4.0} X ≡ ✓	KNN ₁₀ ^{4.0} ≡ ≡ ✓
	KNN ₂₅ ^{0.25} X X X	KNN ₂₅ ^{0.25} ≡ ≡ ✓	KNN ₂₅ ^{0.25} ≡ ✓ ✓	KNN ₂₅ ^{0.25} ≡ ≡ ✓	KNN ₂₅ ^{0.25} ≡ ≡ ✓
	KNN ₂₅ ^{0.5} X X X	KNN ₂₅ ^{0.5} X X ✓	KNN ₂₅ ^{0.5} ≡ ≡ ✓	KNN ₂₅ ^{0.5} ≡ ≡ ✓	KNN ₂₅ ^{0.5} ≡ ≡ ✓
	KNN ₂₅ ^{1.0} X X X	KNN ₂₅ ^{1.0} X X ✓	KNN ₂₅ ^{1.0} X ≡ ✓	KNN ₂₅ ^{1.0} ≡ ≡ ✓	KNN ₂₅ ^{1.0} ≡ ≡ ✓
	KNN ₂₅ ^{2.0} X X X	KNN ₂₅ ^{2.0} X X ✓	KNN ₂₅ ^{2.0} X X ✓	KNN ₂₅ ^{2.0} X ≡ ✓	KNN ₂₅ ^{2.0} ≡ ≡ ✓
	KNN ₂₅ ^{4.0} X X X	KNN ₂₅ ^{4.0} X X ≡	KNN ₂₅ ^{4.0} X X ✓	KNN ₂₅ ^{4.0} X ≡ ✓	KNN ₂₅ ^{4.0} ≡ ≡ ✓
K=25	KNN ₅₀ ^{0.25} X X X	KNN ₅₀ ^{0.25} ≡ ≡ ✓	KNN ₅₀ ^{0.25} ≡ ≡ ✓	KNN ₅₀ ^{0.25} ✓ ✓ ✓	KNN ₅₀ ^{0.25} ≡ ≡ ✓
	KNN ₅₀ ^{0.5} X X X	KNN ₅₀ ^{0.5} ≡ ≡ ✓			
	KNN ₅₀ ^{1.0} X X X	KNN ₅₀ ^{1.0} X X ✓	KNN ₅₀ ^{1.0} ≡ ≡ ✓	KNN ₅₀ ^{1.0} ≡ ≡ ✓	KNN ₅₀ ^{1.0} ≡ ≡ ✓
	KNN ₅₀ ^{2.0} X X X	KNN ₅₀ ^{2.0} X X ≡	KNN ₅₀ ^{2.0} X X ✓	KNN ₅₀ ^{2.0} X ≡ ✓	KNN ₅₀ ^{2.0} ≡ ≡ ✓
	KNN ₅₀ ^{4.0} X X X	KNN ₅₀ ^{4.0} X X ≡	KNN ₅₀ ^{4.0} X X ✓	KNN ₅₀ ^{4.0} X ≡ ✓	KNN ₅₀ ^{4.0} ≡ ≡ ✓
	KNN ₁₀₀ ^{0.25} X X X	KNN ₁₀₀ ^{0.25} ≡ ≡ ✓			
	KNN ₁₀₀ ^{0.5} X X X	KNN ₁₀₀ ^{0.5} X X ✓	KNN ₁₀₀ ^{0.5} ≡ ≡ ✓	KNN ₁₀₀ ^{0.5} ≡ ≡ ✓	KNN ₁₀₀ ^{0.5} ≡ ≡ ✓
	KNN ₁₀₀ ^{1.0} X X X	KNN ₁₀₀ ^{1.0} X X ≡	KNN ₁₀₀ ^{1.0} ≡ ≡ ✓	KNN ₁₀₀ ^{1.0} ≡ ≡ ✓	KNN ₁₀₀ ^{1.0} ≡ ≡ ✓
	KNN ₁₀₀ ^{2.0} X X X	KNN ₁₀₀ ^{2.0} X X ≡	KNN ₁₀₀ ^{2.0} X X ✓	KNN ₁₀₀ ^{2.0} ≡ ≡ ✓	KNN ₁₀₀ ^{2.0} ≡ ≡ ✓
	KNN ₁₀₀ ^{4.0} X X X	KNN ₁₀₀ ^{4.0} X X ≡	KNN ₁₀₀ ^{4.0} X X ✓	KNN ₁₀₀ ^{4.0} X ≡ ✓	KNN ₁₀₀ ^{4.0} ≡ ≡ ✓
K=50	KNN ₁₀₀₀ ^{0.25} X X X	KNN ₁₀₀₀ ^{0.25} ≡ ≡ ✓			
	KNN ₁₀₀₀ ^{0.5} X X X	KNN ₁₀₀₀ ^{0.5} X X ✓	KNN ₁₀₀₀ ^{0.5} ≡ ≡ ✓	KNN ₁₀₀₀ ^{0.5} ≡ ≡ ✓	KNN ₁₀₀₀ ^{0.5} ≡ ≡ ✓
	KNN ₁₀₀₀ ^{1.0} X X X	KNN ₁₀₀₀ ^{1.0} X X ≡	KNN ₁₀₀₀ ^{1.0} ≡ ≡ ✓	KNN ₁₀₀₀ ^{1.0} ≡ ≡ ✓	KNN ₁₀₀₀ ^{1.0} ≡ ≡ ✓
	KNN ₁₀₀₀ ^{2.0} X X X	KNN ₁₀₀₀ ^{2.0} X X ≡	KNN ₁₀₀₀ ^{2.0} X X ✓	KNN ₁₀₀₀ ^{2.0} ≡ ≡ ✓	KNN ₁₀₀₀ ^{2.0} ≡ ≡ ✓
	KNN ₁₀₀₀ ^{4.0} X X X	KNN ₁₀₀₀ ^{4.0} X X ≡	KNN ₁₀₀₀ ^{4.0} X X ✓	KNN ₁₀₀₀ ^{4.0} X ≡ ✓	KNN ₁₀₀₀ ^{4.0} ≡ ≡ ✓
	KNN ₁₀₀₀ ^{0.25} X X X	KNN ₁₀₀₀ ^{0.25} ≡ ≡ ✓			
	KNN ₁₀₀₀ ^{0.5} X X X	KNN ₁₀₀₀ ^{0.5} X X ✓	KNN ₁₀₀₀ ^{0.5} ≡ ≡ ✓	KNN ₁₀₀₀ ^{0.5} ≡ ≡ ✓	KNN ₁₀₀₀ ^{0.5} ≡ ≡ ✓
	KNN ₁₀₀₀ ^{1.0} X X X	KNN ₁₀₀₀ ^{1.0} X X ≡	KNN ₁₀₀₀ ^{1.0} ≡ ≡ ✓	KNN ₁₀₀₀ ^{1.0} ≡ ≡ ✓	KNN ₁₀₀₀ ^{1.0} ≡ ≡ ✓
	KNN ₁₀₀₀ ^{2.0} X X X	KNN ₁₀₀₀ ^{2.0} X X ≡	KNN ₁₀₀₀ ^{2.0} X X ✓	KNN ₁₀₀₀ ^{2.0} ≡ ≡ ✓	KNN ₁₀₀₀ ^{2.0} ≡ ≡ ✓
	KNN ₁₀₀₀ ^{4.0} X X X	KNN ₁₀₀₀ ^{4.0} X X ≡	KNN ₁₀₀₀ ^{4.0} X X ✓	KNN ₁₀₀₀ ^{4.0} X ≡ ✓	KNN ₁₀₀₀ ^{4.0} ≡ ≡ ✓

Discussion

RQ1: Can kNN-Avg reduce outlier-effect?

kNN-Avg reduces the outlier effect

RQ2: Are solutions by kNN-Avg better/worse?

kNN-Avg tends to be slightly worse or equal generally

RQ3: Relation noise-level and kNN-Avg's efficiency

kNN-Avg performs better with higher noise, equal / worse on low noise

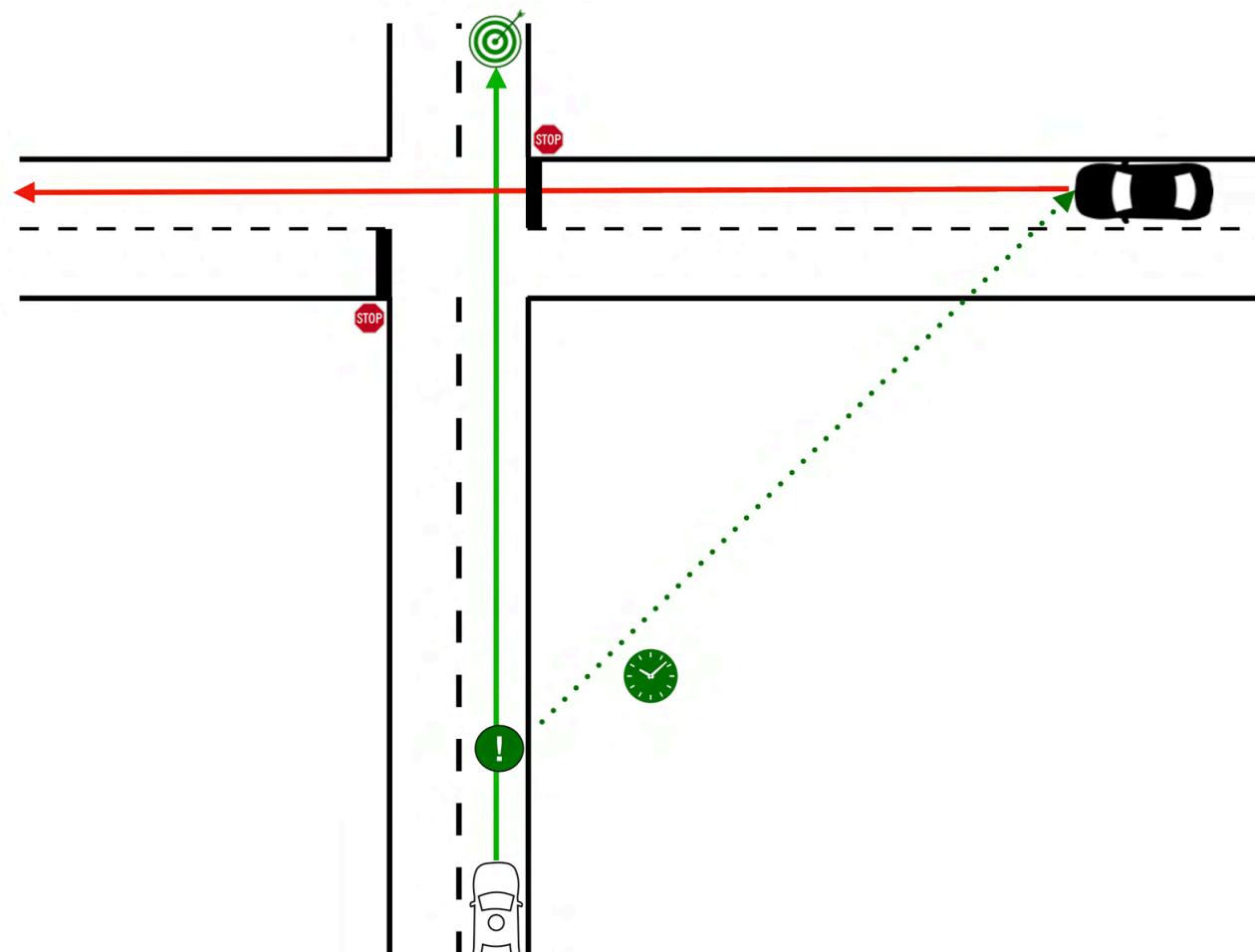
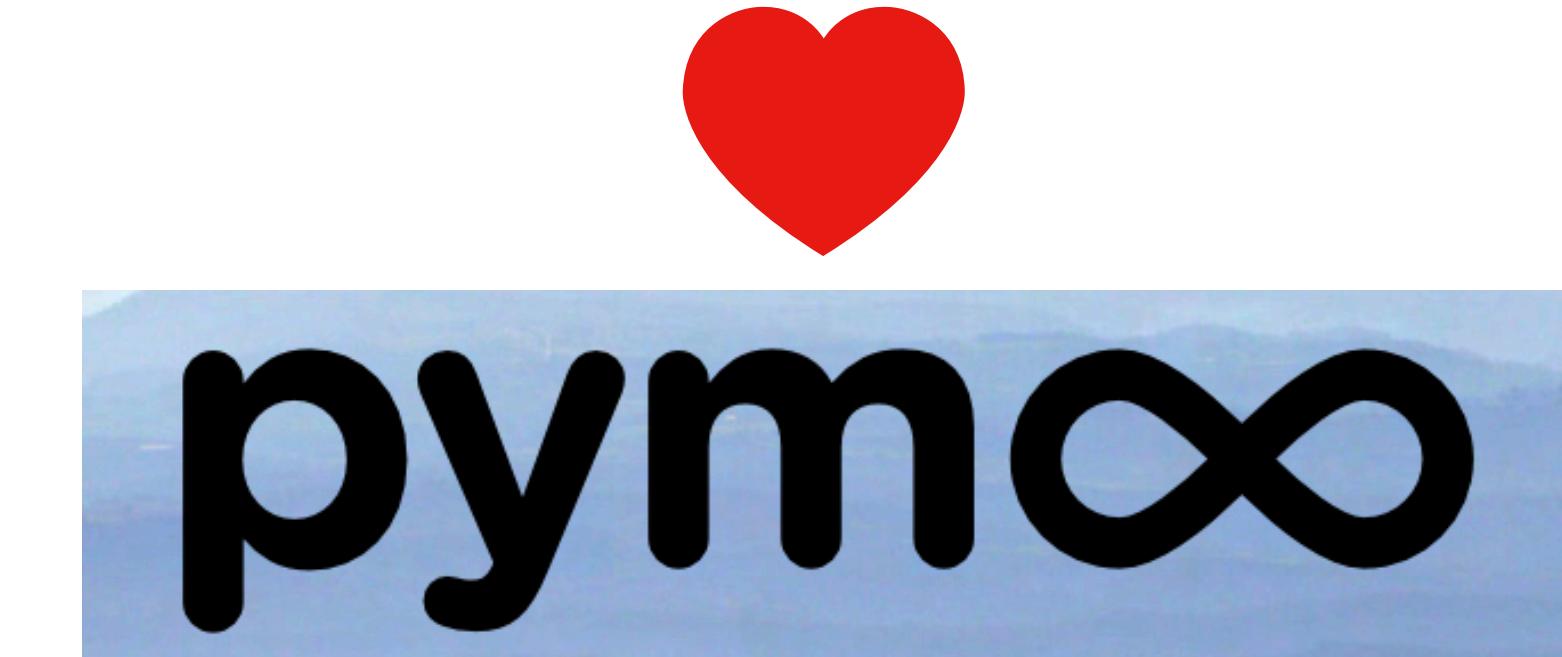
RQ4: Influence of hyper-parameters

k seems not very significant, smaller MD yields better results

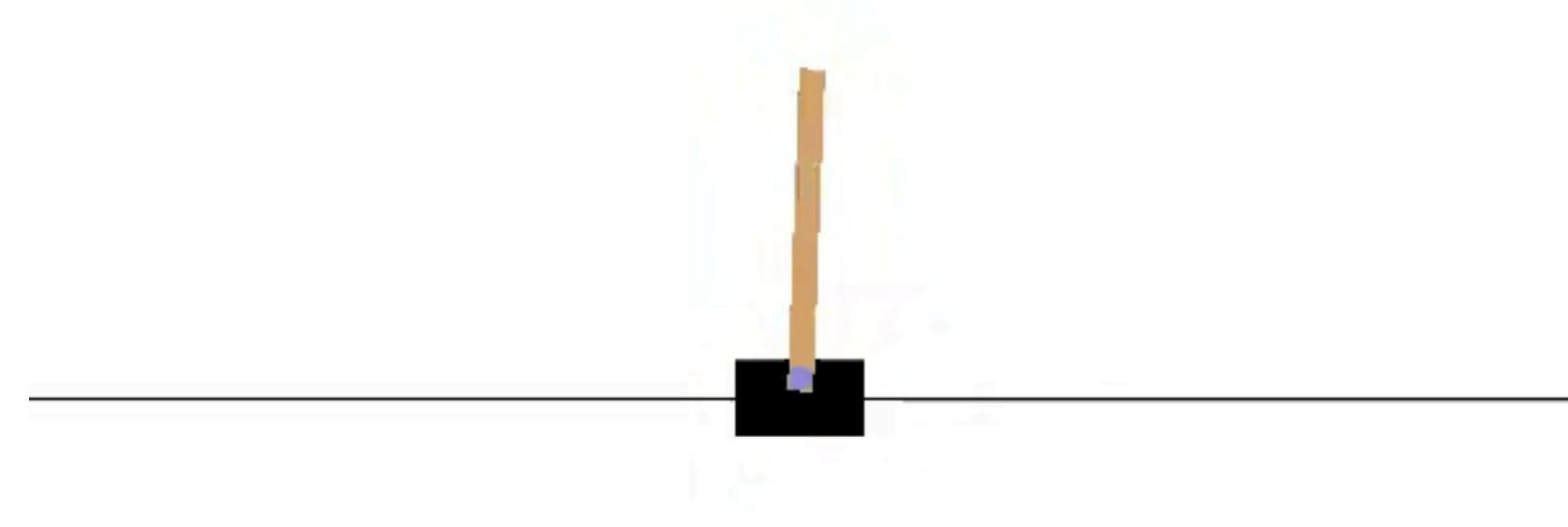
Future

XinSheYang02	2		"go-xinsheyang02"
XinSheYang03	2		"go-xinsheyang03"
XinSheYang04	2		"go-xinsheyang04"
Xor	9		"go-xor"
YaoLiu04	2		"go-yaoliu04"
YaoLiu09	2		"go-yaoliu09"
Zacharov	2		"go-zacharov"
ZeroSum	2		"go-zeroSum"
Zettl	2		"go-zettl"
Zimmerman	2		"go-zimmerman"
Zirilli	2		"go-zirilli"

kNN-Averaging



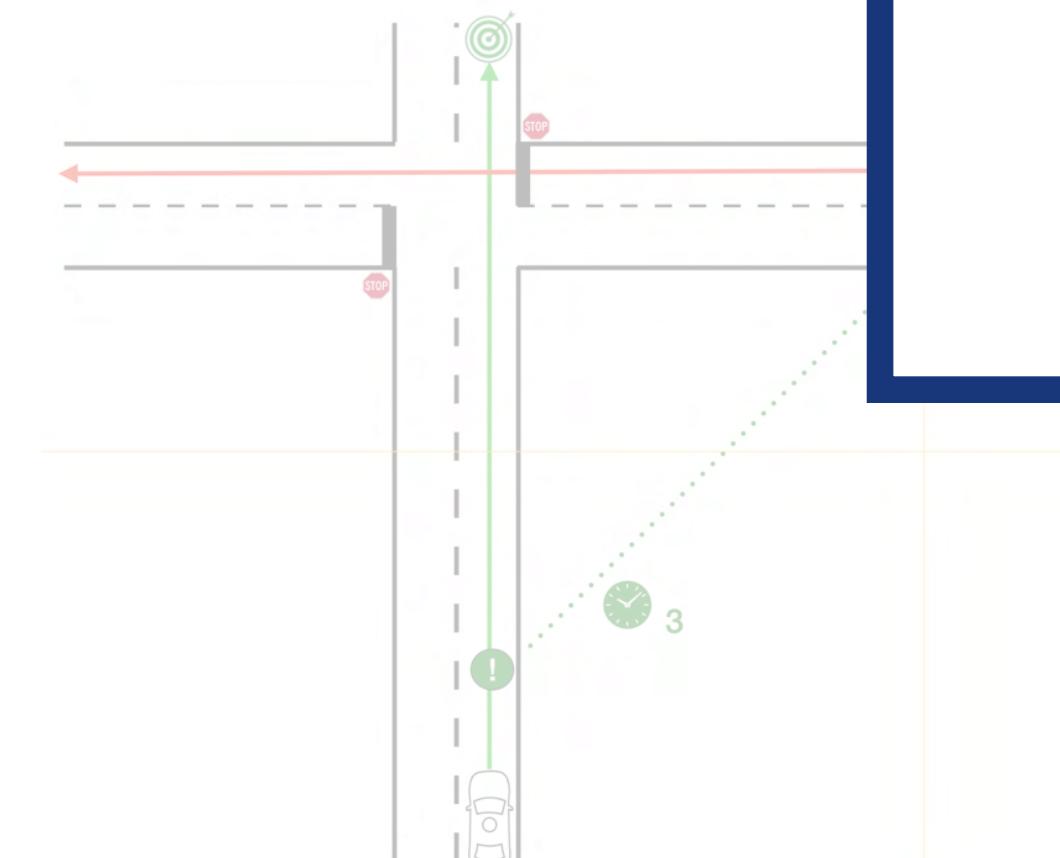
Noisy Controls



[Klikovits, Arcaini, PRDC'21]

Future

XinSheYang02	2		"go-xinsheyang02"
XinSheYang03	2		"go-xinsheyang03"
XinSheYang04	2		"go-xinsheyang04"
Xor	9		"go-xor"
YaoLiu04	2		"go-yao.liu04"
YaoLiu09	2		"go-yao.liu09"
Zacharov	2		
ZeroSum	2		
Zettl	2		
Zimmerman	2		
Zirilli	2		

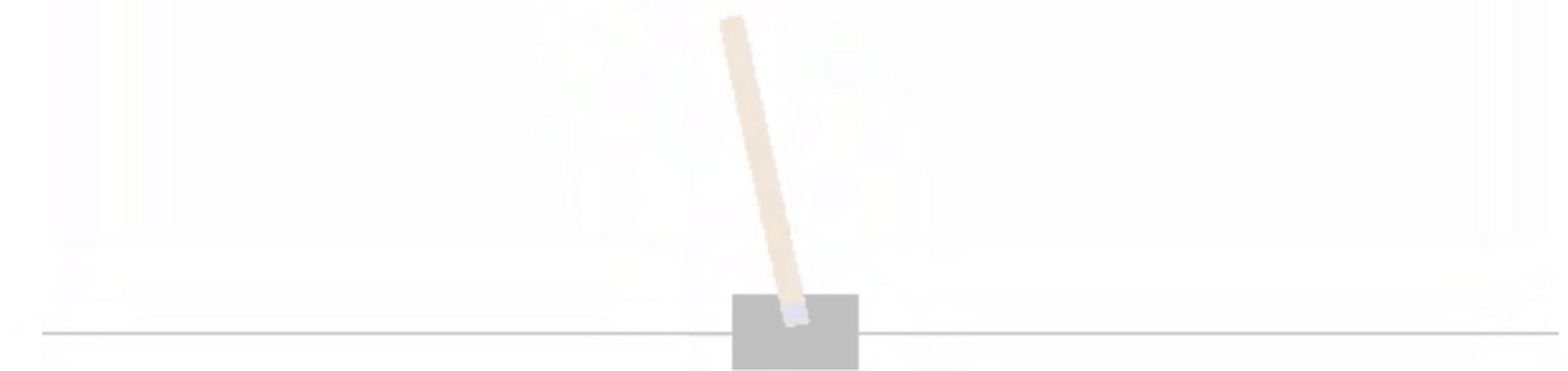


Let's try your
Noisy System

kNN-Averaging

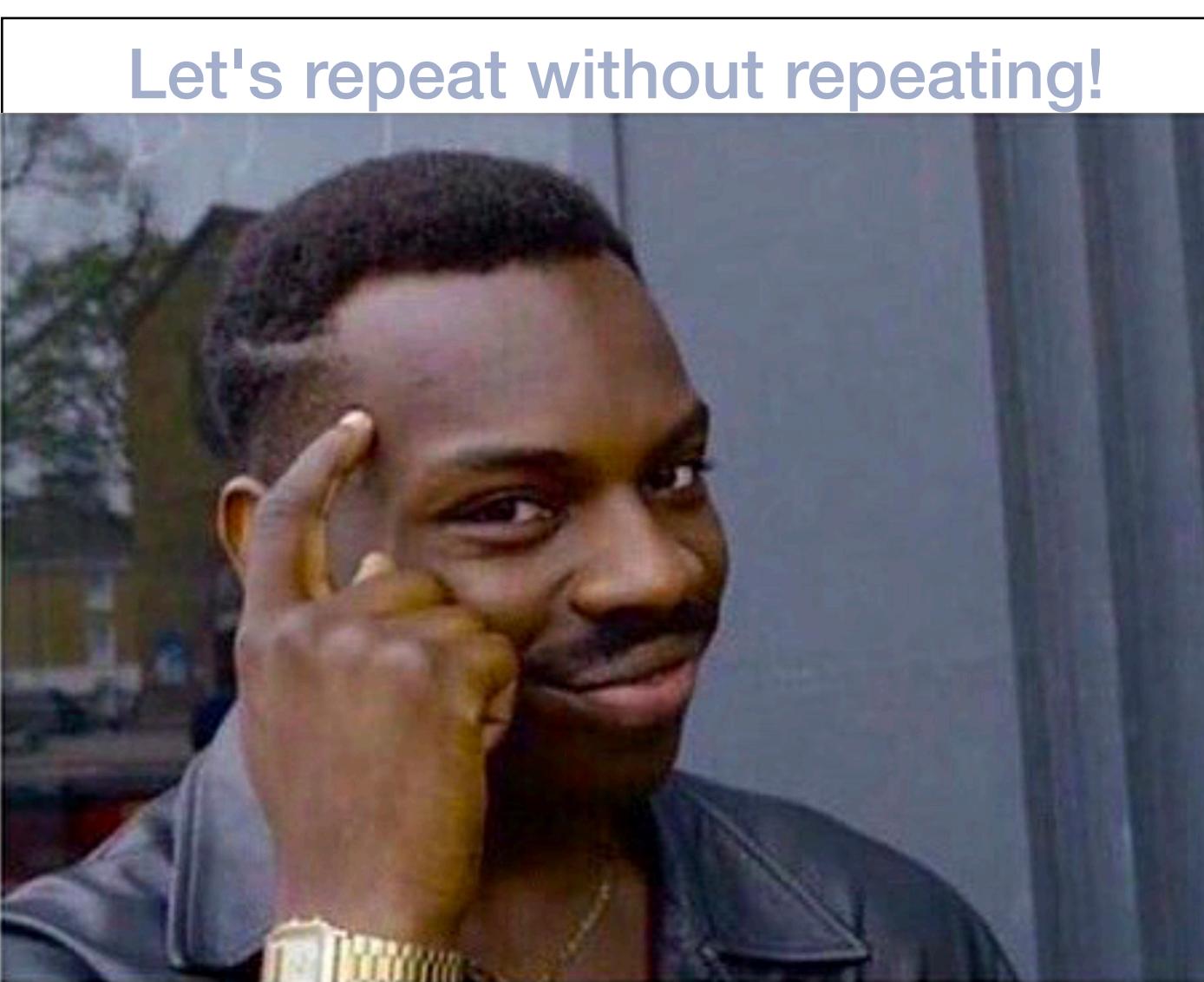
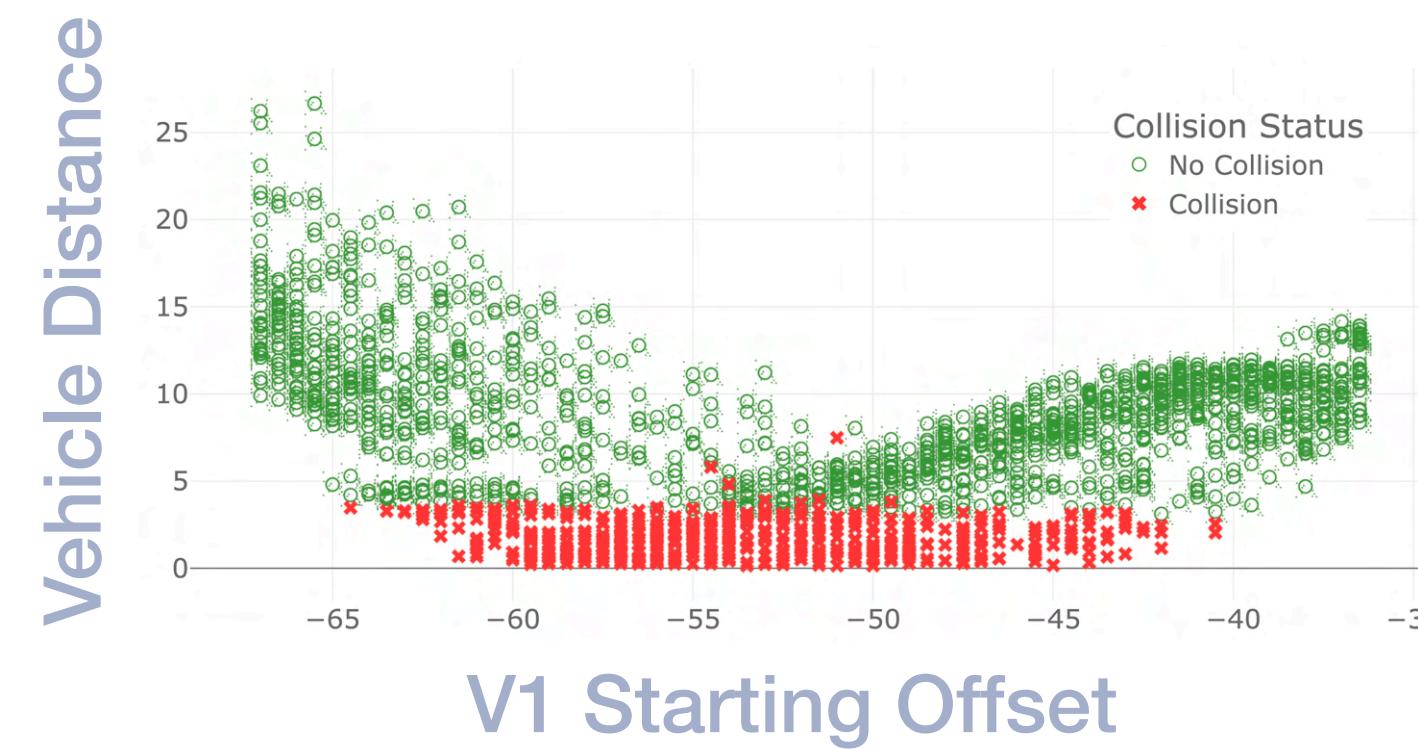
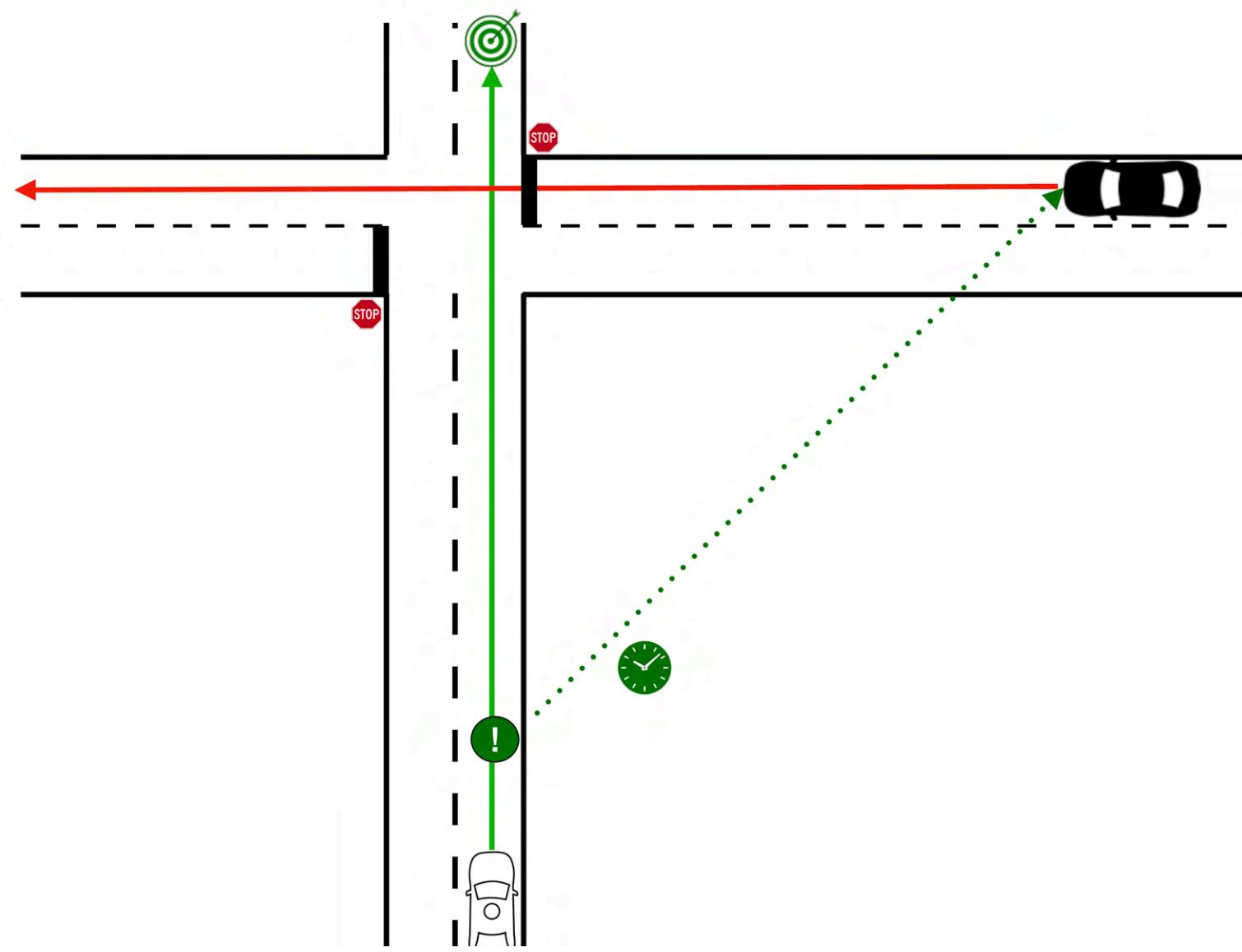


ontrols

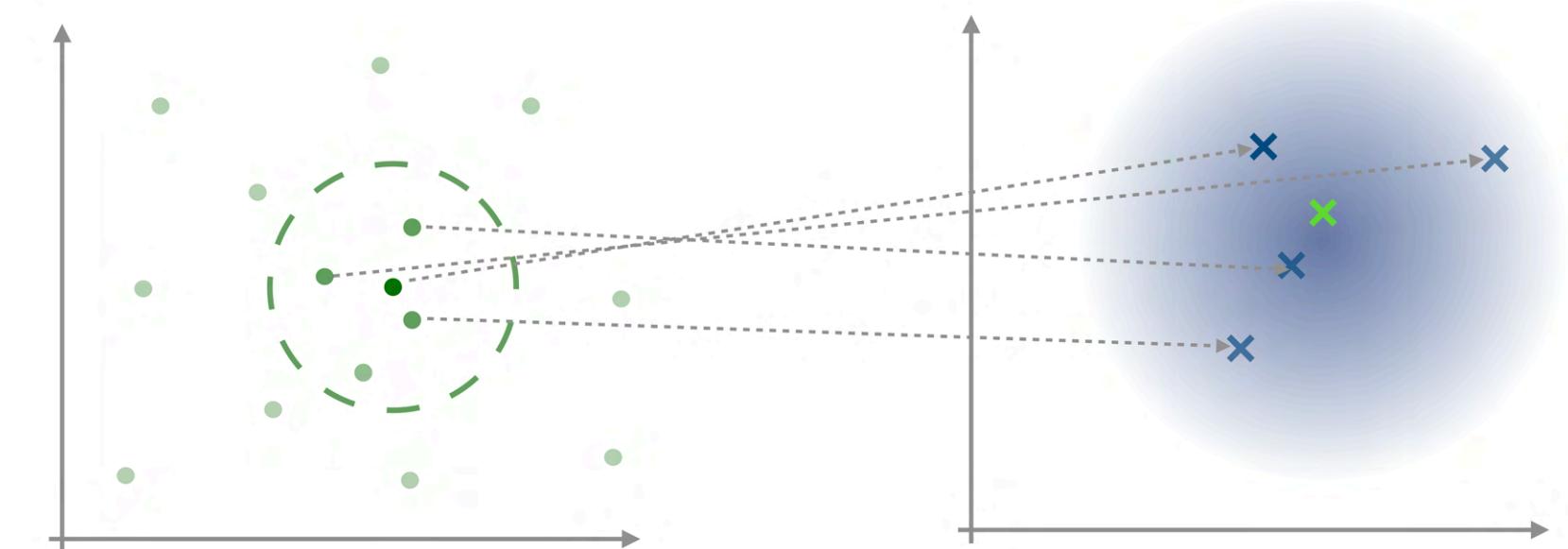


[Klikovits, Arcaini, PRDC'21]

Conclusion



kNN-Averaging



KNN-Averaging for Noisy Multi-Objective Optimisation

Stefan Klikovits^{*}, Paolo Arcaini



ERATO MMSD Hasuo Project
National Institute of Informatics, Tokyo

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