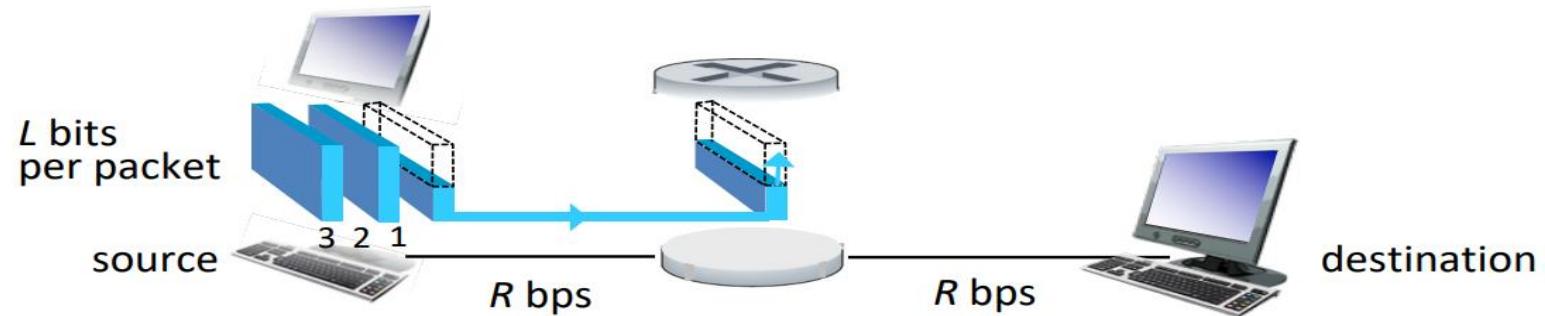




Networks Issues

Packet-switching: store-and-forward



- **packet transmission delay:** takes L/R seconds to transmit (push out) L -bit packet into link at R bps
- **store and forward:** entire packet must arrive at router before it can be transmitted on next link

One-hop numerical example:

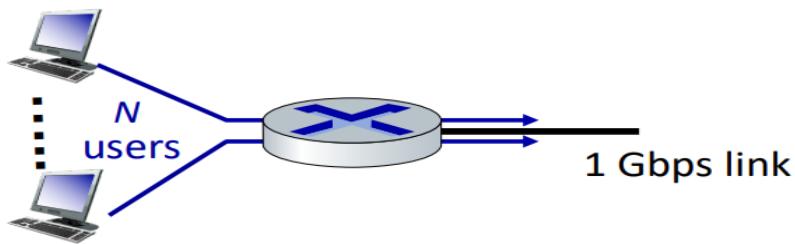
- $L = 10 \text{ Kbits}$
- $R = 100 \text{ Mbps}$
- one-hop transmission delay
 $= 0.1 \text{ msec}$

Transmission delay = $L/R = 10*10^3 / 100 * 10^6 = 10^{-4} \text{ sec} = 10^{-4} / 10^{-3} = 0.1 \text{ msec}$

Packet switching versus circuit switching

example:

- 1 Gb/s link
- each user:
 - 100 Mb/s when "active"
 - active 10% of time



Q: how many users can use this network under circuit-switching and packet switching?

- **circuit-switching:** 10 users
- **packet switching:** with 35 users, probability > 10 active at same time is less than .0004 *

Q: how did we get value 0.0004?

A: HW problem (for those with course in probability only)

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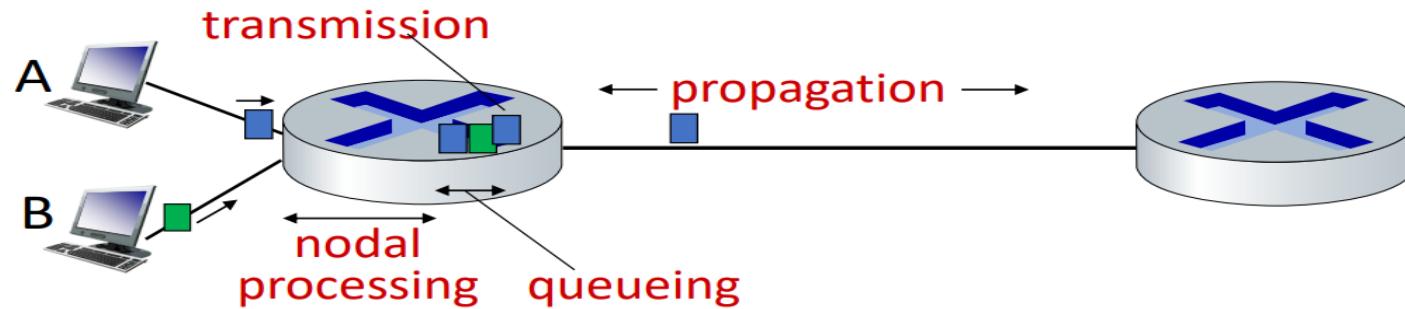
Circuit switched: each user needs $1/10$ of link, so can reserve only 10 channels on the link, whether they are using it 10% or 100%.

Packet switched: Each user is using the channel 10% of the time, so probability of a given user being active is $p = 0.1$, and inactive $q = 0.9$.

It's a binomial distribution $X \sim B(35, 0.1)$, so probability $Pr(X=k) = C(35, k) p^k q^{35-k}$. You need $Pr(X>10)$ which is $1 - Pr(X\leq 10)$ which is $1 - (Pr(X=0) + Pr(X=1) + \dots + Pr(X=10))$.

I actually get 0.000424, not "less than 0.0004"

Packet delay: four sources



$$d_{\text{nodal}} = d_{\text{proc}} + d_{\text{queue}} + d_{\text{trans}} + d_{\text{prop}}$$

d_{trans} : transmission delay:

- L : packet length (bits)
- R : link transmission rate (bps)
- $d_{\text{trans}} = L/R$

d_{trans} and d_{prop}
very different

d_{prop} : propagation delay:

- d : length of physical link
- s : propagation speed ($\sim 2 \times 10^8$ m/sec)
- $d_{\text{prop}} = d/s$

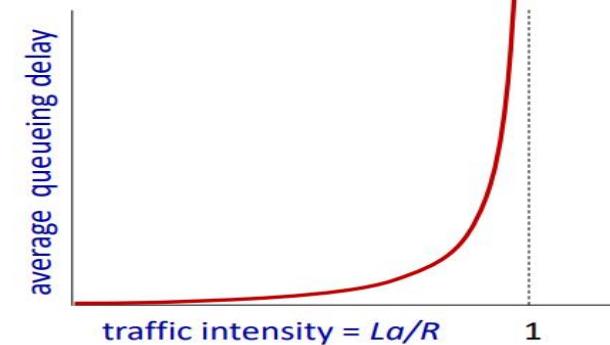
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Packet queueing delay (revisited)

- a : average packet arrival rate
- L : packet length (bits)
- R : link bandwidth (bit transmission rate)

$$\frac{L \cdot a}{R} : \frac{\text{arrival rate of bits}}{\text{service rate of bits}} \quad \text{"traffic intensity"}$$

- $La/R \sim 0$: avg. queueing delay small
- $La/R \rightarrow 1$: avg. queueing delay large
- $La/R > 1$: more “work” arriving is more than can be serviced - average delay infinite!



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Q) A user can directly connect to a server through either long-range wireless or a twisted-pair cable for transmitting a 1500-bytes file. The transmission rates of the wireless and wired media are 2 and 100 Mbps, respectively. Assume that the propagation speed in air is 3×10^8 m/s, while the speed in the twisted pair is 2×10^8 m/s. If the user is located 1 km away from the server, what is the nodal delay when using each of the two technologies.

File size = $1500 * 8$ bits

Transmission rate of wireless = 2Mbps

Propagation speed of wireless = 3×10^8 m/s

Transmission rate of wired = 100Mbps

Propagation speed of wired = 2×10^8 m/s

1. Wireless

- Transmission Delay = $L(\text{bits}) / R(\text{bps})$**
 $= 1500 * 8(\text{bits}) / 2 * 10^6(\text{bps}) = 0.006(\text{s}) = 6(\text{ms})$

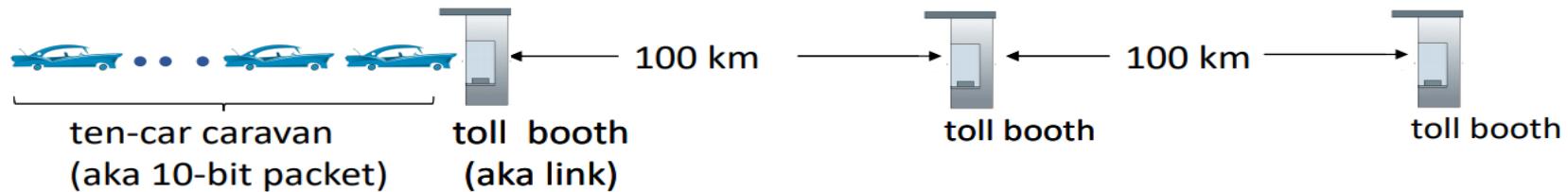
- Propagation Delay = $d(\text{m}) / s(\text{m/s})$**
 $= 1 * 10^3(\text{m}) / 3 * 10^8(\text{m/s}) = 0.00000333333(\text{s}) = 0.003(\text{ms})$

- Nodal Delay = Transmission Delay + Propagation Delay = 6ms
+ 0.003ms = 6.003ms**

2. Wired

- **Transmission Delay** = $L(\text{bits}) / R(\text{bps})$
 $= 1500 * 8(\text{bits}) / 100 * 10^6(\text{bps}) = 0.00012(\text{s}) = 0.12(\text{ms})$
- **Propagation Delay** =
 $d(\text{m})s(\text{m/s}) = 1000(\text{m}) * 2 * 108(\text{m/s}) = 0.000005(\text{s}) = 0.005(\text{ms})$
- **Nodal Delay** = Transmission Delay + Propagation Delay =
 $0.12\text{ms} + 0.005\text{ms} = 0.125\text{ms}$

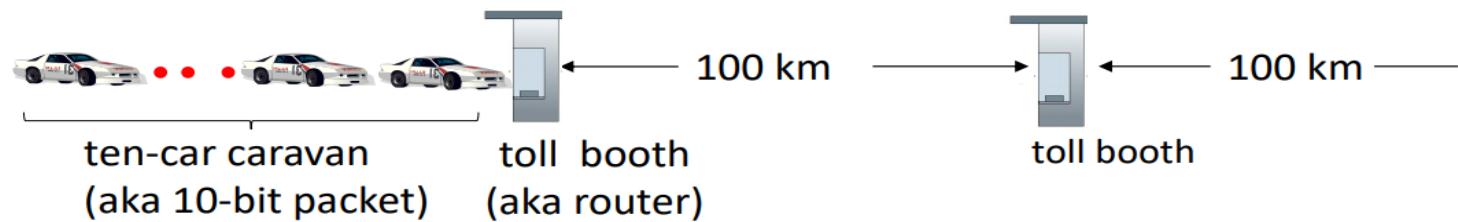
Caravan analogy



- car ~ bit; caravan ~ packet; toll service ~ link transmission
- toll booth takes 12 sec to service car (bit transmission time)
- “propagate” at 100 km/hr
- **Q: How long until caravan is lined up before 2nd toll booth?**
- time to “push” entire caravan through toll booth onto highway = $12 * 10 = 120$ sec
- time for last car to propagate from 1st to 2nd toll both: $100\text{km}/(100\text{km/hr}) = 1$ hr
- **A: 62 minutes**

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Caravan analogy



- suppose cars now “propagate” at 1000 km/hr
- and suppose toll booth now takes one min to service a car
- **Q: Will cars arrive to 2nd booth before all cars serviced at first booth?**
- **A: Yes!** after 7 min, first car arrives at second booth; three cars still at first booth

Q) Review the car-caravan analogy in Section 1.4. Assume a propagation speed of 100 km/hour. Tollbooths are 75 km apart, and the cars propagate at 100km/hr. A tollbooth services a car at a rate of one car every 12 seconds. There are 10 cars.

(a.) Suppose the caravan travels 150 km, beginning in front of one tollbooth, passing through a second tollbooth, and finishing just after a third tollbooth. What is the end-to-end delay?

Propagation speed = 100 (km/hr), Distance between tollbooth = 75 (km)

Propogation Delay = Distance / Propagation Speed = 75(km) / 100(km/hr) = 0.75 hr = 45 (min)

Time for taken by each tollbooth to reach 10 cars = 12(s) x 10 = 2 (min)

End-to-end Delay (3 Toolbooths and 2 Hops in between) = 45 x 2 + 2 x 3 = 96 (min)

(b.) Repeat (a.), now assuming that there are eight cars in the caravan instead of ten.

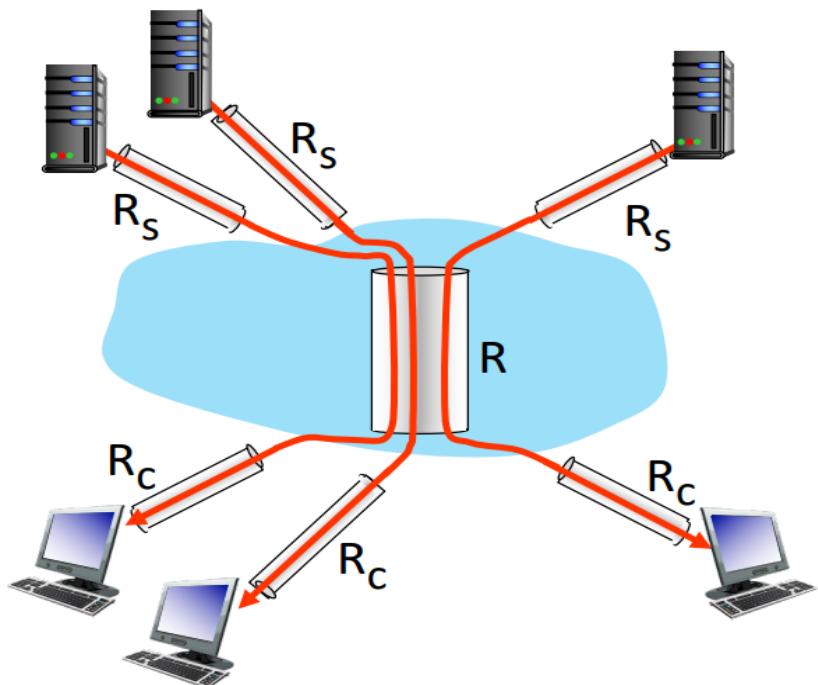
Propagation speed = 100 (km/hr), Distance between tollbooth = 75 (km)

Propogation Delay = Distance / Propagation Speed = 75(km) / 100(km/hr) = 45 (min)

Time for taken by each tollbooth to reach 8 cars = 12(s) x 8 = 96 (s) = 1.6 (min)

End-to-end Delay (3 Toolbooths and 2 Hops in between) = 45 x 2 + 1.6 x 3 = 94.8 (min)

Throughput: network scenario



10 connections (fairly) share
backbone bottleneck link R bits/sec

- per-connection end-end throughput: $\min(R_c, R_s, R/10)$
- in practice: R_c or R_s is often bottleneck

* Check out the online interactive exercises for more examples: http://gaia.cs.umass.edu/kurose_ross/

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Suppose Host A wants to send a large file to Host B. The path from Host A to Host B has three links, of rate $R_1 = 500$ kbps, $R_2 = 2$ Mbps, and $R_3 = 1$ Mbps.

(a.) Assuming no other traffic in the network, what is the throughput for the file transfer?

Given: $R_1 = 500$ kbps, $R_2 = 2$ Mbps, $R_3 = 1$ Mbps

The throughput for the file transfer = $\min(R_1, R_2, R_3) = 500$ kbps

(b.) Suppose the file is 4 million bytes. Dividing the file size by the throughput, roughly how long will it take to transfer the file to Host B?

$$L(\text{bits}) / R(\text{bps}) = 4 * 10^6 \text{ (bytes)} / 500 \text{ (kbps)}$$

$$= 32*10^6 / 500 * 10^3 = 64 \text{ sec}$$

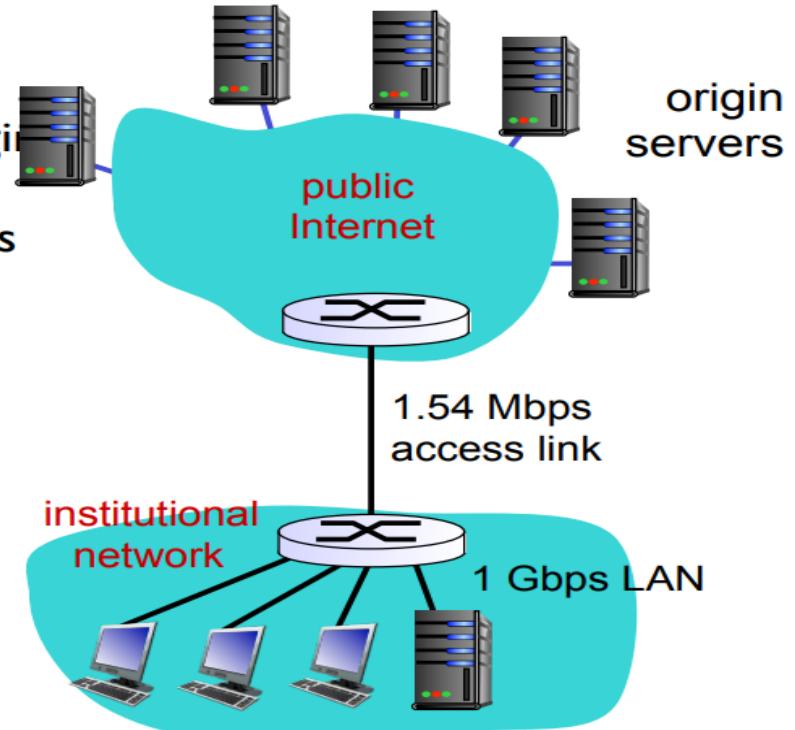
(c.) Repeat (a.) and (b.), but now with R2 reduced to 100 kbps.
Throughput = 100 kbps

$$L(\text{bits}) / R(\text{bps}) = 32*10^6 / 100 * 10^3 = 320 \text{ sec}$$

Caching example:

assumptions:

- ❖ avg object size: $S=100K$ bits
- ❖ avg request rate from browsers to origin servers: $A=15/\text{sec}$
- ❖ avg data rate to browsers: $R=1.50 \text{ Mbps}$
- ❖ access link rate: $C=1.54 \text{ Mbps}$
- ❖ RTT from institutional router to any origin server: $T=200 \text{ ms}$



consequences:

- ❖ LAN utilization: 0.15%
- ❖ access link utilization $\approx 99\%$ *problem!*
- ❖ total delay = Internet delay + access delay + LAN delay
 $= 200 \text{ ms} + \approx \text{minutes} + \mu\text{secs}$

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Average data rate to browsers = $100k \text{ bits} * 15 = 1.5 \text{ Mbps}$

Access link rate = 1.54 Mbps

RTT from client to server = 200 msec

LAN Link rate = 1 Gbps

LAN utilization = $\text{Avg data rate to browsers} / \text{LAN link rate} = 1.5 \text{ Mbps} / 1 \text{ Gbps} = 0.0015 = 0.15\%$

Access Link utilization = $\text{Avg data rate to browsers} / \text{access link rate} = 1.5 \text{ Mbps} / 1.54 \text{ Mbps} = 99\% \text{ (problem in queuing delay)}$

Total delay = internet delay (RTT) + Access delay + LAN delay

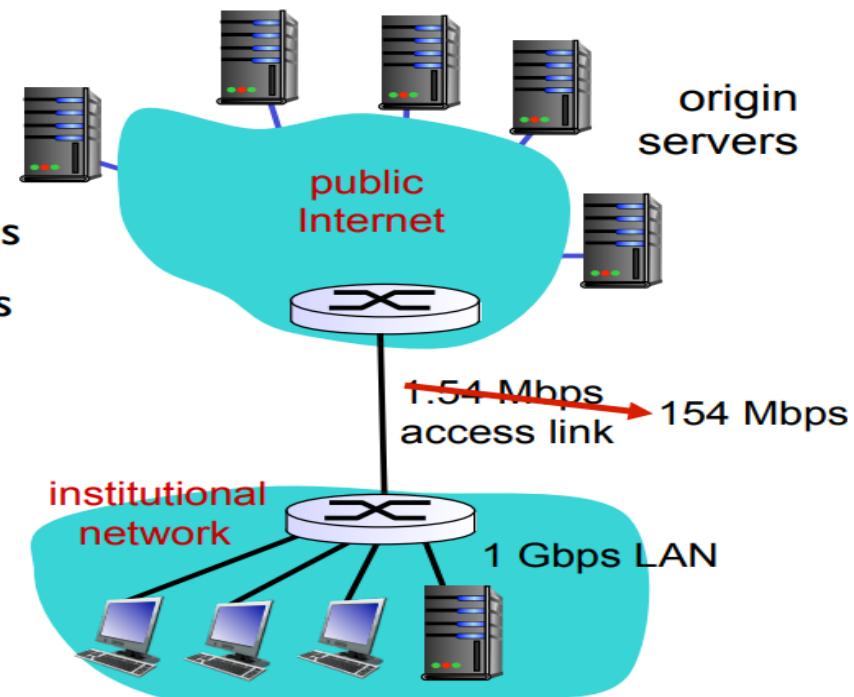
Caching example: fatter access link

assumptions:

- ❖ avg object size: $S=100K$ bits
- ❖ avg request rate from browsers to origin servers: $A=15/\text{sec}$
- ❖ avg data rate to browsers: $R=1.50 \text{ Mbps}$
- ❖ access link rate: $C=1.54 \text{ Mbps}$
- ❖ RTT from institutional router to any origin server: $T=200 \text{ ms}$

consequences:

- ❖ LAN utilization: 0.15% (as before)
- ❖ access link utilization = ~~99%~~ $\rightarrow 9.9\%$
- ❖ total delay = Internet delay + access delay + LAN delay
 $= 200 \text{ ms} + \cancel{\sim \text{minutes}} + \cancel{\text{usecs}} \approx \text{ms}$



Cost: increased access link speed (not cheap!)

Caching example: install local cache

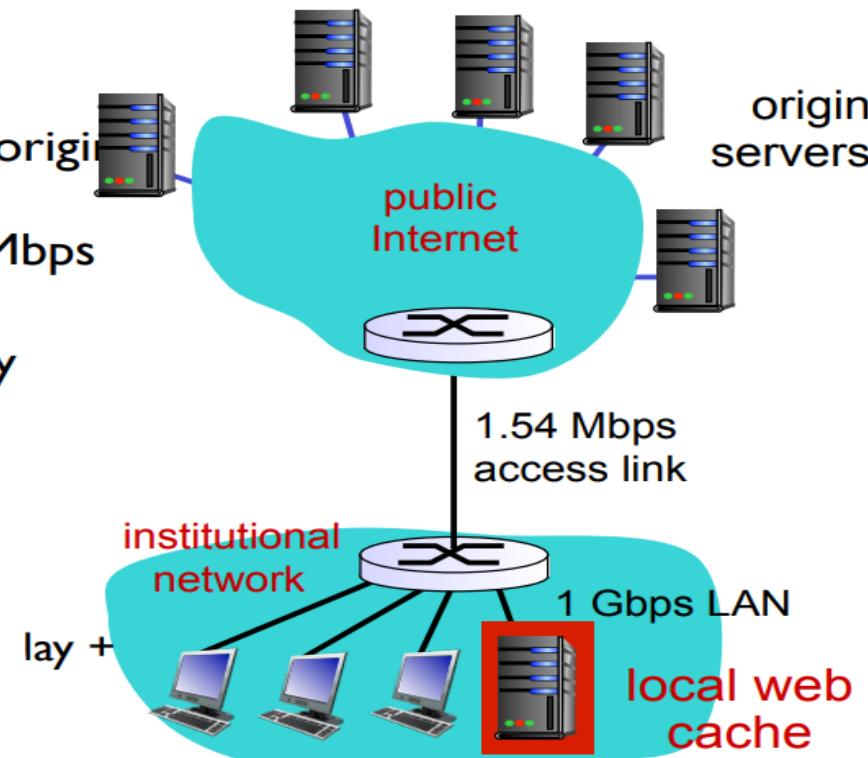
assumptions:

- ❖ avg object size: $S=100K$ bits
- ❖ avg request rate from browsers to origin servers: $A=15/\text{sec}$
- ❖ avg data rate to browsers: $R=1.50 \text{ Mbps}$
- ❖ access link rate: $C=1.54 \text{ Mbps}$
- ❖ RTT from institutional router to any origin server: $T=200 \text{ ms}$

consequences:

- ❖ LAN utilization: 0.15% (as before)
- ❖ access link utilization = ?
- ❖ total delay = ?

How to compute link utilization, delay?

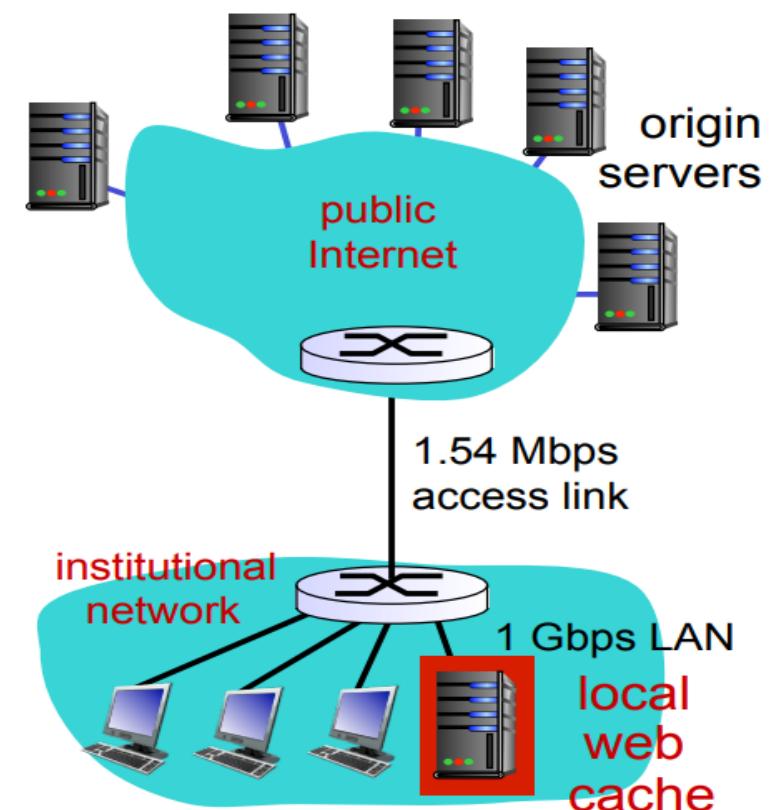


Cost: web cache (cheap!)

assumptions:

- ❖ avg object size: $S=100K$ bits
- ❖ avg request rate from browsers to origin servers: $A=15/\text{sec}$
- ❖ avg data rate to browsers: $R=1.50 \text{ Mbps}$
- ❖ access link rate: $C=1.54 \text{ Mbps}$
- ❖ RTT from institutional router to any origin server: $T=200 \text{ ms}$

install local cache



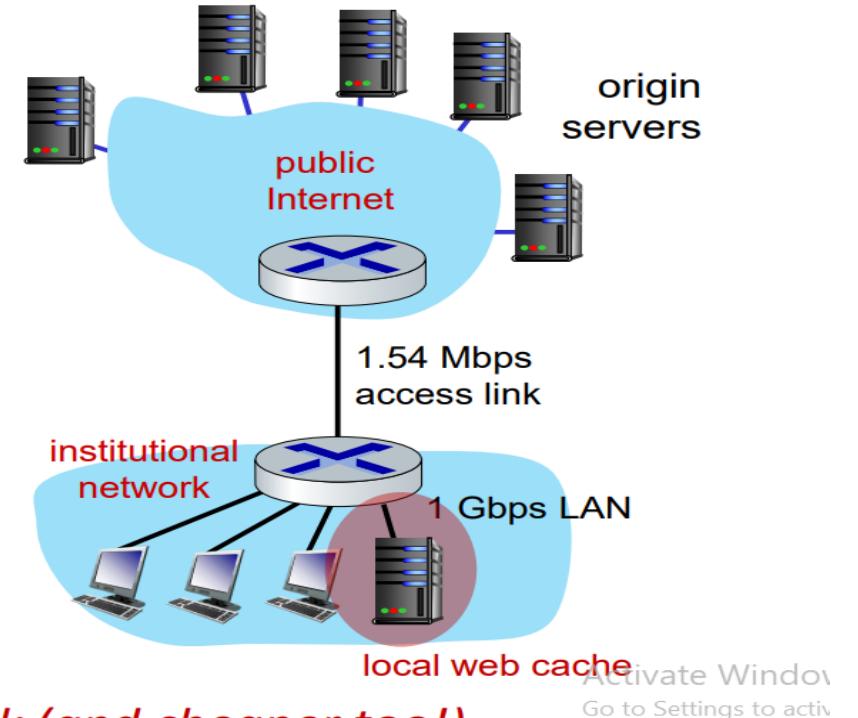
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Calculating access link utilization, end-end delay with cache:

suppose cache hit rate is 0.4:

- 40% requests served by cache, with low (msec) delay
- 60% requests satisfied at origin
 - rate to browsers over access link
 $= 0.6 * 1.50 \text{ Mbps} = .9 \text{ Mbps}$
 - access link utilization = $0.9/1.54 = .58$ means low (msec) queueing delay at access link
- average end-end delay:
 $= 0.6 * (\text{delay from origin servers}) + 0.4 * (\text{delay when satisfied at cache})$
 $= 0.6 (2.01) + 0.4 (\sim\text{msecs}) = \sim 1.2 \text{ secs}$

lower average end-end delay than with 154 Mbps link (and cheaper too!)



Internet checksum: example

example: add two 16-bit integers

	1	1	1	0	0	1	1	0	0	1	1	0	0	1	1	0
	1	1	0	1	0	1	0	1	0	1	0	1	0	1	0	1
<hr/>																
wraparound	1	1	0	1	1	1	0	1	1	1	0	1	1	1	0	1
sum	1	0	1	1	1	0	1	1	1	0	1	1	1	0	0	0
checksum	0	1	0	0	0	1	0	0	0	1	0	0	0	1	1	1

Note: when adding numbers, a carryout from the most significant bit needs to be added to the result

Internet checksum: weak protection!

example: add two 16-bit integers

TCP sequence numbers, ACKs

Sequence numbers:

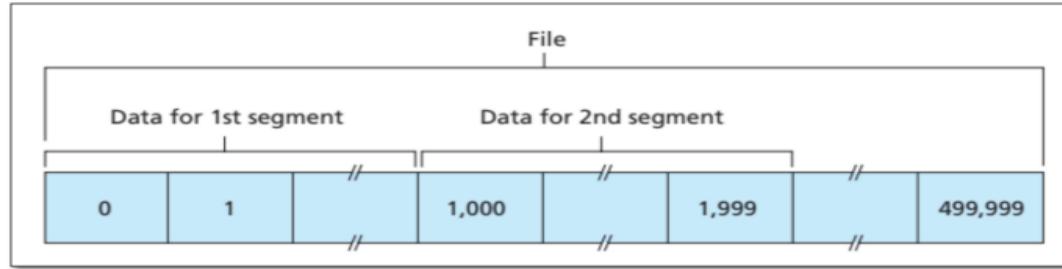
- byte stream “number” of first byte in segment’s data

Acknowledgements:

- seq # of next byte expected from other side
- cumulative ACK

Q: how receiver handles out-of-order segments

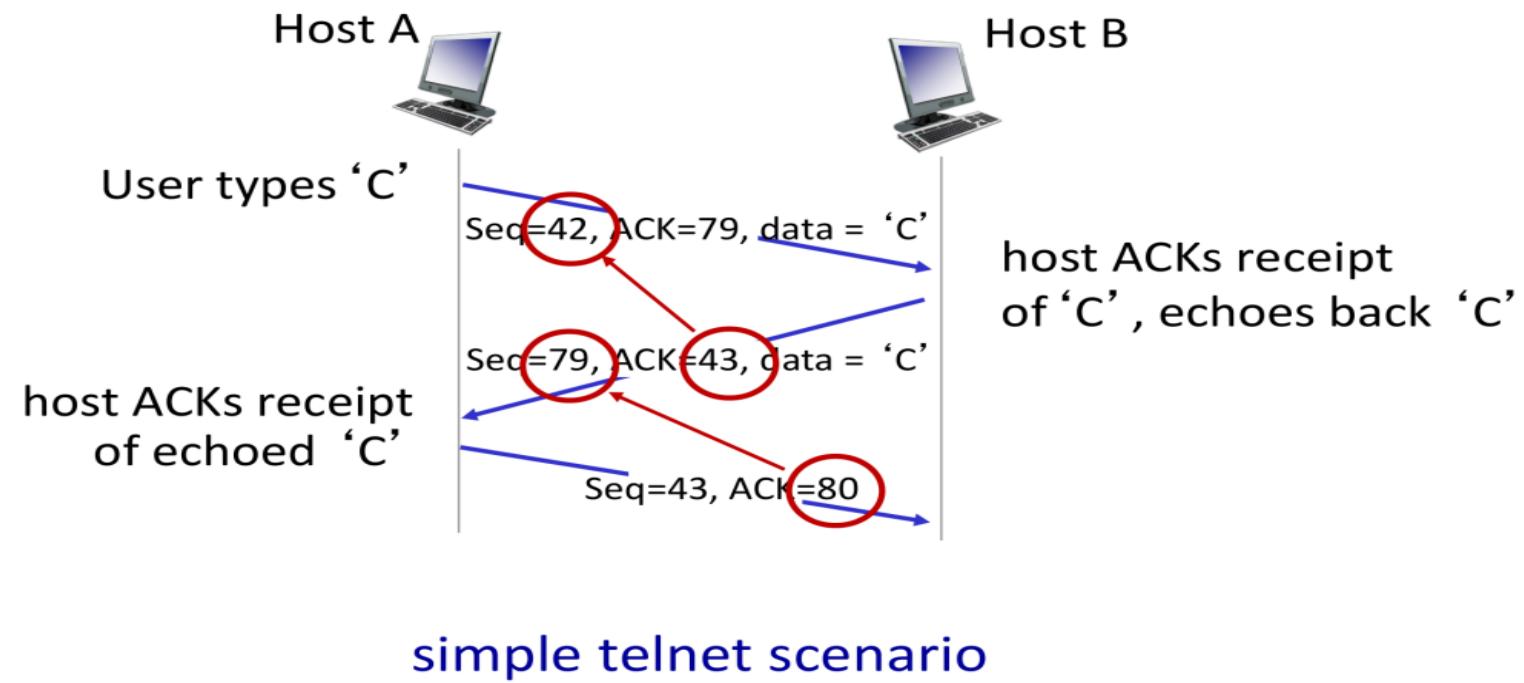
- A: TCP spec doesn’t say, - up to implementor



- **File size:** 500,000 bytes.
- **MSS:** 1,000 bytes
- TCP constructs 500 segments
- The **first segment** sequence number 0
- The **second segment** sequence number 1,000
- The **third segment** sequence number 2,000, and so on.

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TCP sequence numbers, ACKs

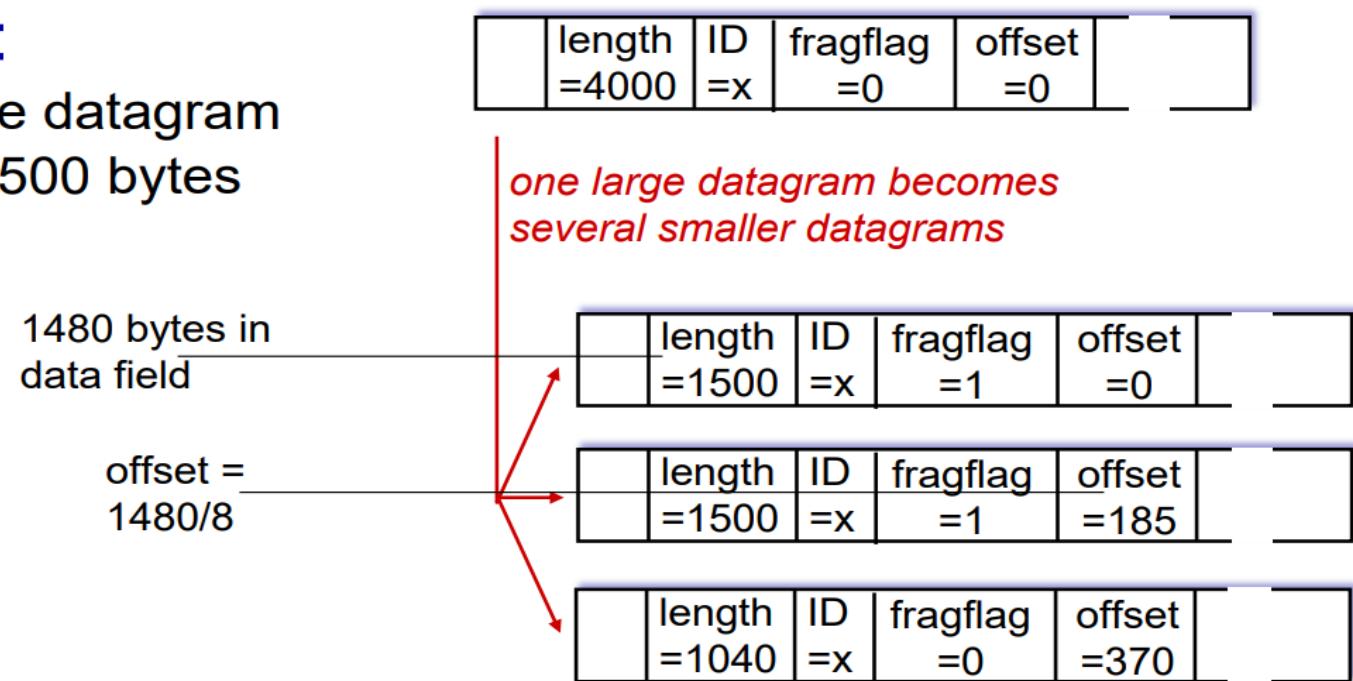


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IP Datagram: fragmentation/reassembly

example:

- 4000 byte datagram
- MTU = 1500 bytes

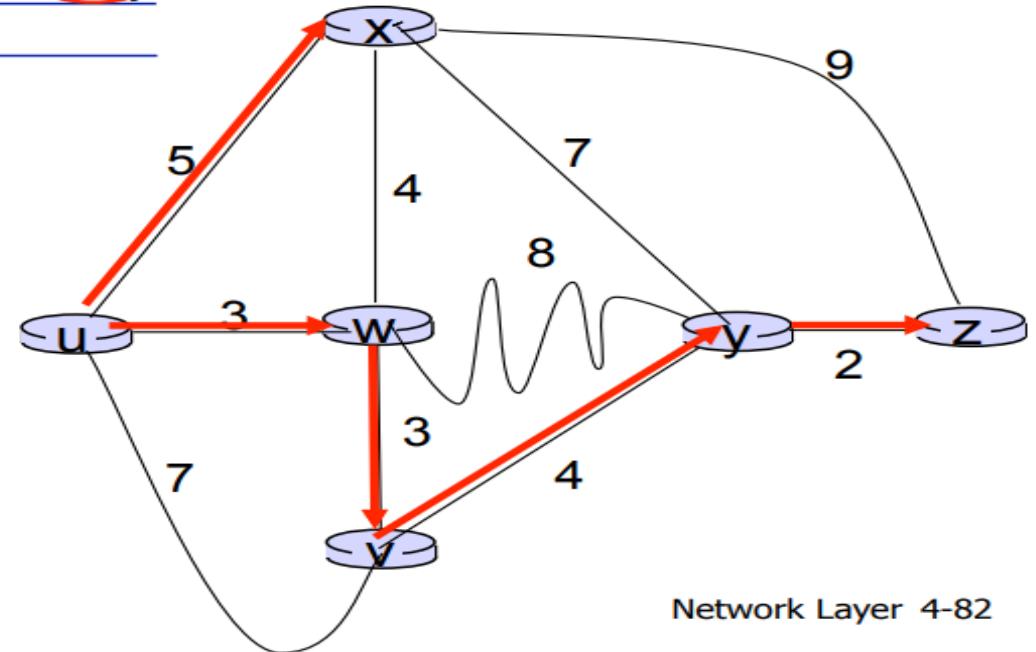


Dijkstra's algorithm: example

Step	N'	D(v)	D(w)	D(x)	D(y)	D(z)
		p(v)	p(w)	p(x)	p(y)	p(z)
0	u	7,u	3,u	5,u	∞	∞
1	uw	6,w		5,u	11,w	∞
2	uwx	6,w		11,w	14,x	
3	uwxv			10,y	14,x	
4	uwxvy				12,y	
5	uwxvzy					

notes:

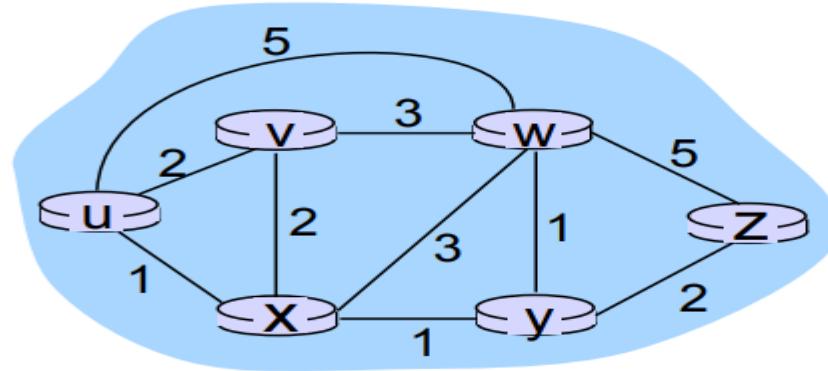
- ❖ construct shortest path tree by tracing predecessor nodes
- ❖ ties can exist (can be broken arbitrarily)



Network Layer 4-82

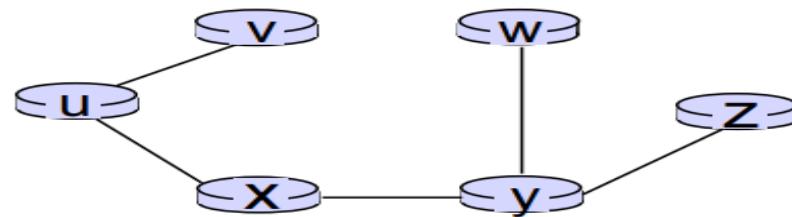
Dijkstra's algorithm: another example

Step	N'	D(v),p(v)	D(w),p(w)	D(x),p(x)	D(y),p(y)	D(z),p(z)
0	u	2,u	5,u	1,u	∞	∞
1	ux	2,u	4,x		2,x	∞
2	uxy	2,u	3,y		4,y	
3	uxyv		3,y		4,y	
4	uxyvw					4,y
5	uxyvwz					



Dijkstra's algorithm: example (2)

resulting shortest-path tree from u:



resulting forwarding table in u:

destination	link
v	(u,v)
x	(u,x)
y	(u,x)
w	(u,x)
z	(u,x)

Distance vector algorithm

Bellman-Ford equation (dynamic programming)

let

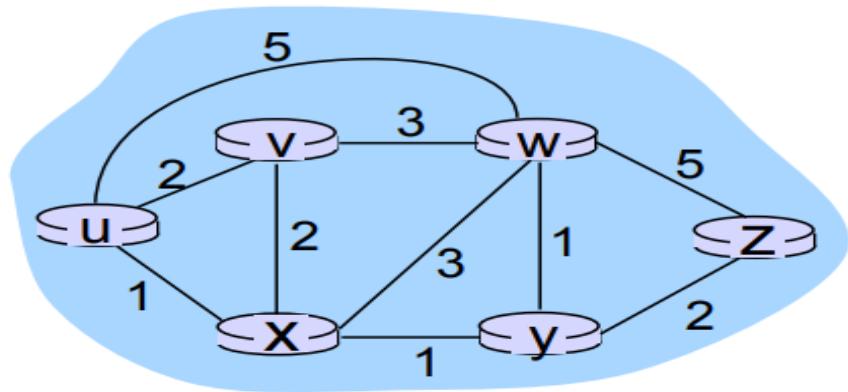
$d_x(y) :=$ cost of least-cost path from x to y

then

$$d_x(y) = \min_v \{ c(x, v) + d_v(y) \}$$

| | |
| | |
cost to neighbor v cost from neighbor v to destination y
 \min taken over all neighbors v of x

Bellman-Ford example



clearly, $d_v(z) = 5$, $d_x(z) = 3$, $d_w(z) = 3$

B-F equation says:

$$\begin{aligned}d_u(z) &= \min \{ c(u,v) + d_v(z), \\&\quad c(u,x) + d_x(z), \\&\quad c(u,w) + d_w(z) \} \\&= \min \{ 2 + 5, \\&\quad 1 + 3, \\&\quad 5 + 3 \} = 4\end{aligned}$$

node achieving minimum is next
hop in shortest path, used in forwarding table