# limma: Linear Models for Microarray Data User's Guide

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# 1 Introduction

Limma is a package for the analysis of gene expression microarray data, especially the use of linear models for analysing designed experiments and the assessment of differential expression. Limma provides the ability to analyse comparisons between many RNA targets simultaneously. It has features which make the analyses stable even for experiments with small number of arrays—this is achieved by borrowing information across genes. The normalization and exploratory data analysis functions are for two-colour spotted microarrays. The linear model and differential expression functions apply to all microarrays including Affymetrix and other single-channel microarray experiments.

This guide gives a tutorial-style introduction to the main limma features but does not describe every feature of the package. A full description of the package is given by the individual function help documents available from the R online help system. To access the online help, type help(package=limma) at the R prompt or else start the html help system using help.start() or the Windows drop-down help menu.

The Bioconductor package marray provides alternative functions for reading and normalizing spotted microarray data. The marray package provides flexible location and scale normalization routines for log-ratios from two-color arrays. The limma package overlaps with marray in functionality but is based on a more general separation between within-array and between-array normalization. If you are using limma in conjunction with the marray package, see Section 10. The Bioconductor package affy provides functions for reading and normalizing Affymetrix microarray data. If you are using the affy package, see Section 7.2 and the relevant case studies.

This guide describes limma as a command-driven package. Packages limmaGUI and affylmGUI are also available which provides graphical user interfaces to the most commonly used functions in limma (Wettenhall and Smyth, 2004). Both packages are available from Bioconductor or from http://bioinf.wehi.edu.au/limmaGUI. The package limmaGUI is for use with two-color data while afflmGUI is for Affymetrix data.

This tutorial was prepared using R Version 2.0 for Windows and limma version 1.8.6.

Help with limma is available by sending questions or problems to the Bioconductor mailing list bioconductor@stat.math.ethz.ch.

## 2 Installation

Limma is a package for the R computing environment and it is assumed that you have already installed R. See the R project at http://www.r-project.org.

**Installing from CRAN**. Limma is available as a contributed package from the R Project CRAN site. This is the recommended repository from which to obtain limma. If you are using R on a system with a suitable internet connection and with installation privileges on your computer, you should be able to install it via

```
> install.packages("limma")
```

at the R prompt from an internet-connected computer. If you are using Windows, use the drop-down menu [Packages > Install package(s) from CRAN ...].

Installing from WEHI. The limma home page is http://bioinf.wehi.edu.au/limma. The latest version of the package is always available from this page, sometimes a few days ahead of the CRAN site. Unlike CRAN, this page supports only the latest release of R (not the developmental version) and does not provide a Mac package build. You should be able to install limma from this page using

```
> install.packages("limma",contriburl="http://bioinf.wehi.edu.au/limma")
```

at the R prompt.

Installing from Bioconductor. Limma is available as part of the Bioconductor project at http://www.bioconductor.org. Bioconductor works on a 6-monthly official release cycle, lagging each major R release by a few weeks. This means that Bioconductor software is updated only once every six months, unless you are using the developmental version R. Updates

of limma between the Bioconductor official releases should be obtained from one of the above two sites.

Change-log. Limma is updated frequently, often a couple of times a week. The change-log can be viewed at http://bioinf.wehi.edu.au/limma/changelog.txt. It can also be viewed from the R prompt. To see the most recent 20 lines type:

> changeLog(n=20)

## 3 A Few Preliminaries on R

R is a program for statistical computing. It is a command-driven language meaning that you have to type commands into it rather than pointing and clicking using a mouse. A good way to get started is to type

```
> help.start()
```

at the R prompt or, if you're using Windows, to follow the drop-down menu [Help > Html help]. Following the links [Packages > limma] from the html help page will lead you to the contents page of help topics for commands in limma.

Before you can use any limma commands you have to load the package by typing

```
> library(limma)
```

at the R prompt. You can get help on any function in any loaded package by typing? and the function name at the R prompt, for example

```
> ?read.maimages
```

for detailed help on the read.maimages function. Anything that you create in R is an "object". Objects might include data sets, variables, functions, anything at all. For example

```
> x <- 2
```

will create a variable x and will assign it the value 2. At any stage of your R session you can type

```
> objects()
```

to get a list of all the objects you have created. You see show the contents of any object by typing the name of the object at the prompt, for example either of the following commands will print out the contents of x:

```
> show(x)
> x
```

We hope that you can use limma without having to spend a lot of time learning about the R language itself but a little knowledge in this direction will be very helpful, especially when you want to do something not explicitly provided for in limma or in the other Bioconductor packages. For more details about the R language see An Introduction to R which is available from the online help. For more background on using R for statistical analyses see Dalgaard (2002).

# 4 Quick Start

For those who want to see very quickly what a limma analysis might look like for cDNA data, here is a quick analysis of four replicate arrays (including two dye-swaps). The data has been scanned using an Axon scanner, producing a GenePix Array List (GAL) file, and then the intensities have been captured from the images using SPOT software. The GAL file and the image analysis files are in the current working directory of R. For more detail about the data see the Swirl Data example below.

```
# Read file containing info about the hybridizations,
          # including names of files containing the intensity data
> targets <- readTargets("SwirlSample.txt")</pre>
          # Read in the data
> RG <- read.maimages(targets$FileName, source="spot")</pre>
          # Read in GAL file containing gene names, only needed if using SPOT!
> RG$genes <- readGAL()
          # Set printer layout information
> RG$printer <- getLayout(RG$genes)
          # Print-tip group loess normalization
> MA <- normalizeWithinArrays(RG)
          # Scale normalization between arrays, optional
> MA <- normalizeBetweenArrays(MA)
          # Estimate all the fold changes by fitting a linear model.
          # The design matrix indicates which arrays are dye-swaps
> fit <- lmFit(MA, design=c(-1,1,-1,1))
          # Apply Bayesian smoothing to the standard errors (very important!)
> fit <- eBayes(fit)
> options(digits=3)
          # Show the top 30 genes, control false discovery rate
> topTable(fit, n=30, adjust="fdr")
    Block Row Column
                           ID
                               Name
                                         М
                                              Α
                                                    t P.Value
3721
        8
            2
                               BMP2 -2.21 12.1 -21.1 0.000357 7.96
                   1 control
            2
                               BMP2 -2.30 13.1 -20.3 0.000357 7.78
1609
        4
                   1 control
3723
                   3 control
                               Dlx3 -2.18 13.3 -20.0 0.000357 7.71
1611
        4
            2
                               Dlx3 -2.18 13.5 -19.6 0.000357 7.62
                   3 control
8295
       16
          16
                  15 fb94h06 20-L12 1.27 12.0
                                                 14.1 0.002067 5.78
7036
       14
                                     1.35 13.8 13.5 0.002067 5.54
           8
                   4 fb40h07 7-D14
        1 22
                  11 fc22a09 27-E17
                                     1.27 13.2 13.4 0.002067 5.48
515
                                                 13.4 0.002067 5.48
5075
       10 14
                  11 fb85f09 18-G18
                                     1.28 14.4
7307
       14 19
                  11 fc10h09 24-H18 1.20 13.4
                                                13.2 0.002067 5.40
319
        1 14
                   7 fb85a01
                             18-E1 -1.29 12.5 -13.1 0.002067 5.32
                   9 fb85d05 18-F10 -2.69 10.3 -13.0 0.002067 5.29
2961
          14
4032
        8
           14
                  24 fb87d12 18-N24
                                     1.27 14.2 12.8 0.002067 5.22
                                 Vox -1.26 13.4 -12.8 0.002067 5.20
6903
       14
           2
                  15 control
4546
        9 14
                  10 fb85e07 18-G13 1.23 14.2 12.8 0.002067 5.18
        2
            7
                  11 fb37b09 6-E18 1.31 13.3 12.4 0.002182 5.02
683
        4
            5
                  17 fb26b10 3-I20 1.09 13.3
                                                 12.4 0.002182 4.97
1697
       15
          5
                   3 fb24g06 3-D11 1.33 13.6 12.3 0.002182 4.96
7491
        8 21
4188
                  12 fc18d12 26-F24 -1.25 12.1 -12.2 0.002209 4.89
4380
                  12 fb37e11 6-G21 1.23 14.0 12.0 0.002216 4.80
```

```
3726
        8
             2
                    6 control fli-1 -1.32 10.3 -11.9 0.002216 4.76
2679
         6
             2
                                 Vox -1.25 13.4 -11.9 0.002216 4.71
                   15 control
5931
        12
             6
                    3 fb32f06 5-C12 -1.10 13.0 -11.7 0.002216 4.63
             9
                   18 fb50g12 9-L23 1.16 14.0 11.7 0.002216 4.63
7602
        15
        5
             2
                                vent -1.40 12.7 -11.7 0.002216 4.62
2151
                   15 control
             4
                   22 fb23d08
                               2-N16 1.16 12.5 11.6 0.002221 4.58
3790
        8
7542
        15
             7
                    6 fb36g12
                               6-D23 1.12 13.5 11.0 0.003000 4.27
                                vent -1.41 12.7 -10.8 0.003326 4.13
4263
        9
             2
                   15 control
6375
        13
             2
                   15 control
                                vent -1.37 12.5 -10.5 0.004026 3.91
        3
             4
                   18 fb22a12
                               2-I23 1.05 13.7 10.2 0.004242 3.76
1146
                                6-I1 -1.82 10.8 -10.2 0.004242 3.75
157
                   13 fb38a01
```

# 5 Reading Data into Limma

This chapter is for two-color arrays. If you are using Affymetrix arrays, you should use the affy or affyPLM packages to read and normalize the data. If you have single channel arrays others than Affymetrix, you will need to the read the intensity data into your R session yourself using the basic R read functions such as read.table. You will need to create a matrix containing the log-intensities with rows for probes and columns are arrays.

### 5.1 Recommended Files

We assume that an experiment has been conducted with one or more microarrays, all printed with the same library of probes. Each array has been scanned to produce a TIFF image. The TIFF images have then been processed using an image analysis program such a ArrayVision, ImaGene, GenePix, QuantArray or SPOT to acquire the red and green foreground and background intensities for each spot. The spot intensities have then been exported from the image analysis program into a series of text files. There should be one file for each array or, in the case of Imagene, two files for each array.

You will need to have the image analysis output files. In most cases these files will include the IDs and names of the probes and possibly other annotation information. A few image analysis programs, for example SPOT, do not write the probe IDs into the output files. In this case you will also need a genelist file which describes the probes. It most cases it is also desirable to have a *targets file* which describes which RNA sample was hybridized to each channel of each array. A further optional file is the *spot types* file which identifies special probes such as control spots.

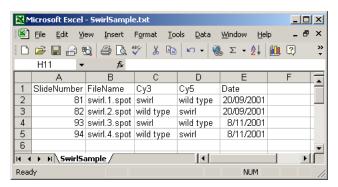
# 5.2 The Targets Frame

The first step in preparing data for input into limma is usually to create a targets file which lists the RNA target hybridized to each channel of each array. It is normally in tab-delimited text format and should contain a row for each microarray in the experiment. The file can have any name but the default is Targets.txt. If it has the default name, it can be read into the R session using

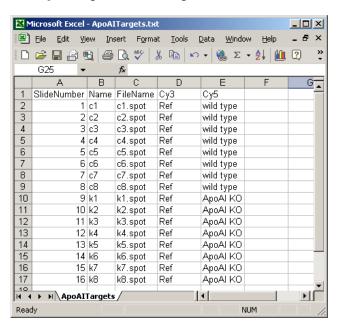
### > targets <- readTargets()</pre>

Once read into R, it becomes the targets frame.

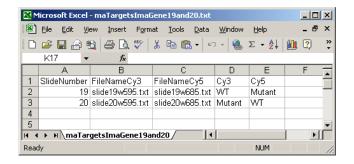
The targets frame normally contains a FileName column, giving the name of the imageanalysis output file, a Cy3 column giving the RNA type labelled with Cy3 dye for that slide and a Cy5 column giving the RNA type labelled with Cy5 dye for that slide. Other columns are optional. The targets file can be prepared using any text editor, but spreadsheet programs such as Microsoft Excel are convenient. The targets file for the Swirl case study includes optional SideNumber and Date columns:



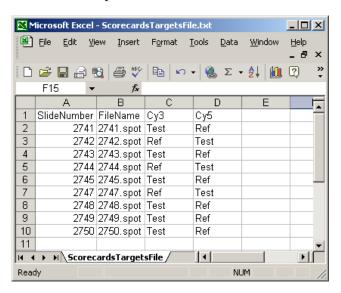
The targets fril the ApoAI case study includes a Name column which can be used to associate labels with the different arrays for plots and output:



For ImaGene files, the FileName column is split into a FileNameCy3 column and a FileNameCy5 because ImaGene stores red and green intensities in separate files. This is a short example:



The targets file below was used to analyse the Scorecard spike-in controls for a particular experiment. Spike-in controls often need to be analyzed separately from other probes because there are only two different spike-in RNA samples, "Reference" and "Test", whereas other probes may respond to any arbitrary number of RNA targets depending on the experiment. This means that, in a multi-array experiment, the spike-in control spots may not respond to the same design matrix as the other probes.



## 5.3 Reading in Intensity Data

Let files be a character vector containing the names of the image analysis output files. The foreground and background intensities can be read into an RGList object using a command of the form

```
RG <- read.maimages(files, source="<imageanalysisprogram>", path="<directory>")
```

where <imageanalysisprogram> is the name of the image analysis program and <directory> is the full path of the directory containing the files. If the files are in the current R working directory then the argument path can be omitted; see the help entry for setwd for how to set the current working directory. The file names are usually read from the Targets File. For example, the Targets File Targets.txt is in the current working directory together with the SPOT output files, then one might use

```
> targets <- readTargets()
> RG <- read.maimages(targets$FileName, source="spot")</pre>
```

If the files are GenePix output files then they might be read using

```
> RG <- read.maimages(targets$FileName, source="genepix")
```

given an appropriate Targets File. Consult the help entry for read.maimages to see which other image analysis programs are supported. Files are assumed by default to be tab-delimited. If the files use a different separator this may be specified using the sep= argument. For example if the Genepix files were comma-separated (csv) then the read command would be

```
RG <- read.maimages(files, source="genepix", sep=",")
```

Reading data from ImaGene software is a little different to that of other image analysis programs because the red and green intensities are stored in separate files. This means that the targets frame should include two filename columns called, say, FileNameCy3 and FileNameCy5, giving the names of the files containing the green and red intensities respectively. An example is given in Section 5.2. Typical code with ImaGene data might be

```
> targets <- readTargets()
> files <- targets[,c("FileNameCy3","FileNameCy5")]
> RG <- read.maimages(files, source="imagene")</pre>
```

For ImaGene data, the files argument to read.maimages() is expected to be a 2-column matrix of filenames rather than a vector.

What should you do if your image analysis program is not currently supported by limma? If your output files are of a standard format, you can supply the column names corresponding to the intensities yourself. For example,

is exactly equivalent to the earlier command with source="genepix". "Standard format" means here that there is a unique column name identifying each column of interest and that there are no lines in the file following the last line of data. Header information at the start of the file is ok.

It is a good idea to look at your data to check that it has been read in correctly. Type

> show(RG)

to see a print out the first few lines of data. Also try

> summary(RG\$R)

to see a five-number summary of the red intensities for each array, and so on.

It is possible to read the data in several steps. If RG1 and RG2 are two data sets corresponding to different sets of arrays then

```
> RG <- cbind(RG1, RG2)
```

will combine them into one large data set. Data sets can also be subsetted. For example RG[,1] is the data for the first array while RG[1:100,] is the data on the first 100 genes.

## 5.4 Spot Quality Weights

It is desirable to use the image analysis to compute a weight for each spot between 0 and 1 which indicates the reliability of the acquired intensities at that spot. For example, if the SPOT image analysis program is used and the size of an ideal perfectly circular spot is known to be 100 pixels, then one might use

```
> RG <- read.maimages(files, source="spot", wt.fun=wtarea(100))
```

The function wtarea(100) gives full weight to spots with area 100 pixels and down-weights smaller and larger spots. Spots which have zero area or are more than twice the ideal size are given zero weight. This will create a component called weights in the RG list. The weights will be used automatically by functions such as normalizeWithinArrays which operate on the RG-list. With GenePix data

```
> RG <- read.maimages(files, source="genepix", wt.fun=wtflags(0.1))
```

will give weight 0.1 to any spot which receives a negative flag from the GenePix program.

The appropriate way to computing spot quality weights depends on the image analysis program that you are using. Consult the help entry QualityWeights to see what quality weight functions are available. The wt.fun argument is very flexible and allows you to construct your own weights. The wt.fun argument can be any function which takes a data set as argument and computes the desired weights. For example, if you wish to give zero weight to all Genepix flags less than -50 you could use

```
> myfun <- function(x) as.numeric(x$Flags > -50.5)
> RG <- read.maimages(files, source="genepix", wt.fun=myfun)</pre>
```

The wt.fun facility can be used to compute weights based on any number of columns in the image analysis files. For example, some researchers like to filter out spots if the foreground mean and median from GenePix for a given spot differ by more than a certain threshold, say 50. This could be achieved by

```
> myfun <- function(x, threshold=50) {
+    okred <- abs(x[,"F635 Median"]-x[,"F635 Mean"]) < threshold
+    okgreen <- abs(x[,"F532 Median"]-x[,"F532 Mean"]) < threshold
+    as.numeric(okgreen & okred)
+}
> RG <- read.maimages(files, source="genepix", wt.fun=myfun)</pre>
```

Then all the "bad" spots will get weight zero which, in limma, is equivalent to flagging them out. The definition of myfun here could be replaced with any other code to compute weights using the columns in the GenePix output files.

## 5.5 Reading the Gene List

In most cases the RGList read by read.maimages() will contain a component RG\$genes containing the probe IDs and other probe-specific annotation. In some cases the genes component

will not be set because there is no probe information in the image analysis output files. An example is output from the SPOT program. In such cases, the probe information needs to be read separately.

If the arrays have been scanned with an Axon scanner, then the gene names will be available in a GenePix Array List (GAL) file. If the GAL file has extension "gal" and is in the current working directory, then it may be read into a data frame by

### > RG\$genes <- readGAL()

Non-Genepix gene lists can be read into R using the function read.table from R base.

Once the gene array list is available, the print layout of the arrays can be extracted from it by

### > RG\$printer <- getLayout(RG\$genes)

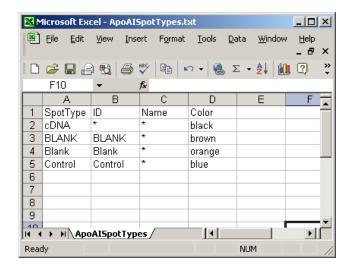
This will set the number of pins, or print-tips, using during the printing of the arrays. This determines the number of what are often called grids or meta rows and columns on the arrays. For ImaGene data, the print layout is already set automatically by read.maimages because this information, called "field dimensions" by ImaGene, is stored as part of the ImaGene output files.

## 5.6 The Spot Types File

The Spot Types file (STF) is another optional tab-delimited text file which allows you to identify different types of spots from the gene list. The STF is used to set the control status of each spot on the arrays so that plots may highlight different types of spots in an appropriate way. It is typically used to distinguish control spots from those corresponding to genes of interest and to distinguish positive from negative controls, ratio from calibration controls and so on. The STF should have a SpotType column giving the names of the different spot-types. One or more other columns should have the same names as columns in the gene list and should contain patterns or regular expressions sufficient to identify the spot-type. Any other columns are assumed to contain plotting attributes, such as colors or symbols, to be associated with the spot-types. This is one row for each spot-type to be distinguished.

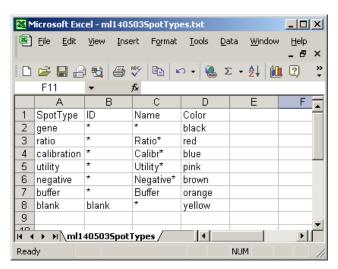
The STF uses simplified regular expressions to match patterns. For example, AA\* means any string starting with AA, \*AA means any code ending with AA, AA means exactly these two letters, \*AA\* means any string containing AA, AA. means AA followed by exactly one other character and AA\. means exactly AA followed by a period and no other characters. For those familiar with regular expressions, any other regular expressions are allowed but the codes for beginning of string and \$ for end of string should be excluded. Note that the patterns are matched sequentially from first to last, so more general patterns should be included first. The first row should specify the default spot-type and should have pattern \* for all the pattern-matching columns.

Here is a short STF appropriate for the ApoAI data:



In this example, the columns ID and Name are found in the gene-list and contain patterns to match. The asterisks are wildcards which can represent anything. Be careful to use upper or lower case as appropriate and don't insert any extra spaces. The remaining column gives colors to be associated with the different types of points.

Here is a STF below appropriate for arrays with Lucidea Universal ScoreCard control spots.



If the STF has default name SpotTypes.txt then it can be read using

### > spottypes <- readSpotTypes()</pre>

It is typically used as an argument to the controlStatus() function to set the status of each spot on the array, for example

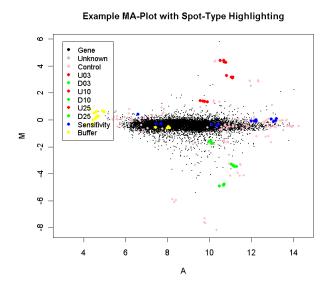
> RG\$genes\$Status <- controlStatus(spottypes, RG)

# 6 Data Exploration

It is advisable to display your data in various ways as a quality check and to check for unexpected effects. We recommend an imageplot of the raw log-ratios and an MA-plot of the raw data for each array as a minimum routine displays. See the Swirl case study for some examples. The functions <code>imageplot3by2</code> and <code>plotMA3by2</code> can be used to automate the production of plots for all arrays in an experiment.

The following is an example MA-Plot for an Incyte array with various spike-in and other controls. (Data courtesy of Rebecca McCracken and Steve Gerondakis, Walter and Eliza Hall Institute of Medical Research.) The plot was produced using

> spottypes <- readSpotTypes()
> RG\$genes\$Status <- controlStatus(spottypes, RG)
> plotMA(RG)



The array includes spike-in ratio controls which are 3-fold, 10-fold and 25-fold up and down regulated, as well an non-differentially expressed sensitivity controls and negative controls.

# 7 Normalization

Limma implements a range of normalization methods for spotted microarrays. Smyth and Speed (2003) describe some of the mostly commonly used methods. The methods may be broadly classified into methods which normalize the M-values for each array separately (within-array normalization) and methods which normalize intensities or log-ratios to be comparable across arrays (between-array normalization). This section discusses mainly within-array normalization. Between-array normalization is discussed further in Section 15.

Print-tip loess normalization (Yang et al, 2001) is the default normalization method and can be performed by

### > MA <- normalizeWithinArrays(RG)

There are some notable cases in which this is not appropriate. For example, Agilent arrays do not have print-tip groups, so one should use global loess normalization instead:

### > MA <- normalizeWithinArrays(RG, method="loess")

Print-tip loess is also unreliable for small arrays with less than, say, 150 spots per print-tip group. Arrays with are larger than this may behave as small arrays if the number of spots with non-missing M-values is small for one or more of the print-tip groups. In these cases one should either use global "loess" normalization or else use robust spline normalization

### > MA <- normalizeWithinArrays(RG, method="robustspline")

which is an empirical Bayes compromise between print-tip and global loess normalization, with 5-parameter regression splines used in place of the loess curves.

Loess normalization assumes that the bulk of the probes on the array are not differentially expressed. It not assumed that that differential expression is symmetric about zero, provided that the loess fit is implemented in a robust fashion, but it is necessary that there be a substantial body of probes which do not change expression levels. This assumption can be suspect for boutique arrays where the total number of unique genes on the array is small, say less than 150, particularly if these genes have been selected for being specifically expressed in one of the RNA sources. In such a situation, the best strategy is to include on the arrays a series of non-differentially expressed control spots, such as a titration series of whole-library-pool spots, and to use the up-weighting method discussed belwo. In the absence of the such control spots, normalization of boutique arrays requires specialist advice.

Any spot quality weights found in RG will be used in the normalization by default. This means for example that spots with zero weight (flagged out) will not influence the normalization of other spots. The use of spot quality weights will not however result in any spots being removed from the data object. Even spots with zero weight will be normalized and will appear in the output object, such spots will simply not have any influence on the other spots. If you do not wish the spot quality weights to be used in the normalization, their use can be over-ridden using

### > MA <- normalizeWithinArrays(RG, weights=NULL)

The output object MA will still contain any spot quality weights found in RG, but these weights will not be used in the normalization step.

It is often useful to make use of control spots to assist the normalization process. For example, if the arrays contain a series of spots which are known in advance to be non-differentially expressed, these spots can be given more weight in the normalization process. Spots which are known in advance to be differentially expressed can be down-weighted. Suppose for example that the controlStatus() has been used to identify spike-in spots which are differentially expressed and a titration series of whole-library-pool spots which should not be differentially expressed. Then one might use

```
> w <- modifyWeights(RG$weights, RG$genes$Status, c("spikein","titration"), c(0,2)) > MA <- normalizeWithinArrays(RG, weights=w)
```

to give zero weight to the spike-in spots and double weight to the titration spots. The idea of up-weighting the titration spots is in the same spirit as the composite normalization method proposed by Yang et al (2002) but is more flexible and generally applicable. The above code assumes that RG already contains spot quality weights. If not, one could use

```
> w <- modifyWeights(array(1,dim(RG)), RG$genes$Status, c("spikein","titration"), c(0,2))
> MA <- normalizeWithinArrays(RG, weights=w)
instead.
```

Limma contains some more sophisticated normalization methods. In particular, some between-array normalization methods are discussed in Section 15 of this guide.

# 8 Background Correction

The default background correction action is to subtract the background intensity from the foreground intensity for each spot. If the RGList object has not already been background corrected, then normalizeWithinArrays will do this by default. Hence

```
> MA <- normalizeWithinArrays(RG)
is equivalent to
> RGb <- backgroundCorrect(RG, method="subtract")
> MA <- normalizeWithinArrays(RGb)</pre>
```

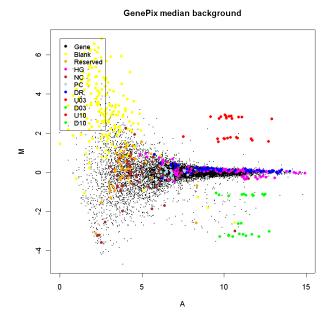
However there are many other background correction options which may be preferable in certain situations.

For the purpose of assessing differential expression, we often find

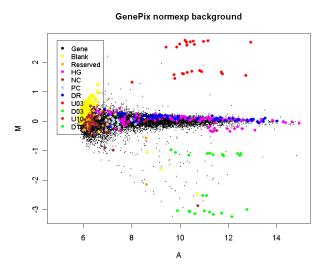
```
> RG <- backgroundCorrect(RG, method="normexp", offset=50)
```

to be preferable to the simple background subtraction with most image analysis programs. This method adjusts the foreground adaptively for the background intensities and results in strictly positive adjusted intensities, i.e., negative or zero corrected intensities are avoided. The use of an offset damps the variation of the log-ratios for very low intensities spots towards zero.

To illustrate some differences between the different background correction methods we consider one cDNA array which was self-self hybridized, i.e., the same RNA source was hybridized to both channels. For this array there is no actual differential expression. The array was printed with a human 10.5k library and hybridized with Jurkatt RNA on both channels. (Data courtesy Andrew Holloway and Dileepa Diyagama, Peter MacCallum Cancer Centre, Melbourne.) The array included a selection of control spots which are highlighted on the plots. Of particular interest are the spike-in ratio controls which should show up and down fold changes of 3 and 10. The first plot displays data acquired with GenePix software and background corrected by subtracting the median local background, which is the default with GenePix data. The plot shows the typical wedge shape with fanning of the M-values at low intensities. The range of observed M-values dominates the spike-in ratio controls. The are also 1148 spots not shown on the plot because the background corrected intensities were zero or negative.



The second plot shows the same array background corrected with method="normexp" and offset=50. The spike-in ratio controls now standout clearly from the range of the M-values. All spots on the array are shown on the plot because there are now no missing M-values.



The third plot shows the same array quantified with SPOT software and with "morph" background subtracted. This background estimator produces a similar effect to that with normexp.

# SPOT morph background SPOT morph background SPOT morph background SPOT morph background SPOT morph background

The effect of using "morph" background or using method="normexp" with an offset is to stabilize the variability of the M-values as a function of intensity. The empirical Bayes methods implemented in the limma package for assessing differential expression will yield most benefit when the variabilities are as homogenous as possible between genes. This can best be achieved by reducing the dependence of variability on intensity as far as possible.

10

Α

12

14

# 9 Linear Models

### 9.1 Introduction

The package limma uses an approach called *linear models* to analyse designed microarray experiments. This approach allows very general experiments to be analysed just as easily as a simple replicated experiment. The approach is outlined in Smyth (2004) and Yang and Speed (2002). The approach requires one or two matrices to be specified. The first is the *design matrix* which indicates in effect which RNA samples have been applied to each array. The second is the *contrast matrix* which specifies which comparisons you would like to make between the RNA samples. For very simple experiments, you may not need to specify the contrast matrix.

The philosophy of the approach is as follows. You have to start by fitting a linear model to your data which fully models the systematic part of your data. The model is specified by the design matrix. Each row of the design matrix corresponds to an array in your experiment and each column corresponds to a coefficient which is used to describe the RNA sources in your experiment. With Affymetrix or single-channel data, or with two-color with a common reference, you will need as many coefficients as you have distinct RNA sources, no more and no less. With direct-design two-color data you will need one fewer coefficient than you have distinct RNA sources, unless you wish to estimate a dye-effect for each gene, in which case the number of RNA sources and the number of coefficients will be the same. Any set of independent coefficients will do, providing they describe all your treatments. The main

purpose of this step is to estimate the variability in the data, hence the systematic part needs to modelled so it can be distinguished from random variation.

In practice the requirement to have exactly as many coefficients as RNA sources is too restrictive in terms of questions you might want to answer. You might be interested in more or fewer comparisons between the RNA source. Hence the contrasts step is provided so that you can take the initial coefficients and compare them in as many ways as you want to answer any questions you might have, regardless of how many or how few these might be.

If you have data from Affymetrix experiments, from single-channel spotted microarrays or from spotted microarrays using a common reference, then linear modeling is the same as ordinary analysis of variance or multiple regression except that a model is fitted for every gene. With data of this type you can create design matrices as one would do for ordinary modeling with univariate data. If you have data from spotted microarrays using a direct design, i.e., a connected design with no common reference, then the linear modeling approach is very powerful but the creation of the design matrix may require more statistical knowledge.

For statistical analysis and assessing differential expression, limma uses an empirical Bayes method to moderate the standard errors of the estimated log-fold changes. This results in more stable inference and improved power, especially for experiments with small numbers of arrays (Smyth, 2004). For arrays with within-array replicate spots, limma uses a pooled correlation method to make full use of the duplicate spots (Smyth et al, 2003).

## 9.2 Affymetrix and Other Single-Channel Designs

Affymetrix data will usually be normalized using the affy package. We will assume here that the data is available as an exprSet object called eset. Such an object will have an slot containing the log-expression values for each gene on each array which can be extracted using exprs(eset). Affymetrix and other single-channel microarray data may be analysed very much like ordinary linear models or anova models. The difference with microarray data is that it is almost always necessary to extract particular contrasts of interest and so the standard parametrizations provided for factors in R are not usually adequate.

There are many ways to approach the analysis of a complex experiment in limma. A straightforward strategy is to set up the simplest possible design matrix and then to extract from the fit the contrasts of interest.

Suppose that there are three RNA sources to be compared. Suppose that the first three arrays are hybridized with RNA1, the next two with RNA2 and the next three with RNA3. Suppose that all pair-wise comparisons between the RNA sources are of interest. We assume that the data has been normalized and stored in an exprSet object, for example by

```
> data <- ReadAffy()
> eset <- rma(data)</pre>
```

An appropriate design matrix can be created and a linear model fitted using

```
> design <- model.matrix(~ -1+factor(c(1,1,1,2,2,3,3,3)))
> colnames(design) <- c("group1", "group2", "group3")
> fit <- lmFit(eset, design)</pre>
```

To make all pair-wise comparisons between the three groups the appropriate contrast matrix can be created by

```
> contrast.matrix <- makeContrasts(group2-group1, group3-group2, group3-group1, levels=design)
> fit2 <- contrasts.fit(fit, contrast.matrix)
> fit2 <- eBayes(fit2)</pre>
```

A list of top genes differential expressed in group2 versus group1 can be obtained from

```
> topTable(fit2, coef=1, adjust="fdr")
```

The outcome of each hypothesis test can be assigned using

```
> results <- decideTests(fit2)</pre>
```

A Venn diagram showing numbers of genes significant in each comparison can be obtained from

> vennDiagram(results)

## 9.3 Common Reference Designs

Now consider two-color microarray experiments in which a common reference has been used on all the arrays. Such experiments can be analysed very similarly to Affymetrix experiments except that allowance must be made for dye-swaps. The simplest method is to setup the design matrix using the modelMatrix() function and the targets file. As an example, we consider part of an experiment conducted by Joëlle Michaud, Catherine Carmichael and Dr Hamish Scott at the Walter and Eliza Hall Institute to compare the effects of transcription factors in a human cell line. The targets file is as follows:

```
> targets <- readTargets("runxtargets.txt")</pre>
> targets
   SlideNumber
                       Cy3
                                  Cy5
                      EGFP
1
          2144
                                 AML1
2
           2145
                     EGFP
                                 AML1
3
           2146
                     AML1
                                 EGFP
4
           2147
                     EGFP AML1.CBFb
5
           2148
                     EGFP AML1.CBFb
6
           2149 AML1.CBFb
                                 EGFP
7
           2158
                     EGFP
                                 CBFb
8
           2159
                      CBFb
                                 EGFP
9
          2160
                     EGFP AML1.CBFb
10
           2161 AML1.CBFb
                                 EGFP
11
          2162
                     EGFP AML1.CBFb
12
          2163 AML1.CBFb
                                 EGFP
13
           2166
                     EGFP
                                 CBFb
14
           2167
                      CBFb
                                 EGFP
```

In the experiment, green fluorescent protein (EGFP) has been used as a common reference. An adenovirus system was used to transport various transcription factors into the nuclei of HeLa cells. Here we consider the transcription factors AML1, CBFbeta or both. A simple design matrix was formed and a linear model fit:

```
> design <- modelMatrix(targets,ref="EGFP")</pre>
> design
   AML1 AML1.CBFb CBFb
       1
                  0
                        0
1
2
      1
                  0
3
                  0
                        0
     -1
4
       0
                  1
5
       0
                  1
                        0
6
       0
                 -1
                        0
7
       0
                        1
                  0
8
       0
                  0
                       -1
9
       0
                  1
                        0
10
       0
                 -1
11
       0
                        0
12
       0
                        0
                 -1
13
       0
                  0
                        1
14
       0
                  0
                       -1
> fit <- lmFit(RG, design)</pre>
```

It is of interest to compare each of the transcription factors to EGFP and also to compare the combination transcription factor with AML1 and CBFb individually. An appropriate contrast matrix was formed as follows:

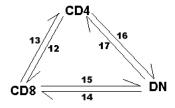
```
> contrast.matrix <- makeContrasts(AML1,CBFb,AML1.CBFb,AML1.CBFb-AML1,AML1.CBFb-CBFb,
       levels=design)
> contrast.matrix
          AML1 CBFb AML1.CBFb AML1.CBFb - AML1 AML1.CBFb - CBFb
                                             -1
AML1
             1
                  0
                            0
                                                                0
AML1.CBFb
             0
                            1
                                              1
                                                                1
CBFb
             0
                  1
                             0
                                              0
                                                               -1
```

The linear model fit can now be expanded and empirical Bayes statistics computed:

```
> fit2 <- contrasts.fit(fit, contrasts.matrix)
> fit2 <- eBayes(fit2)</pre>
```

## 9.4 Direct Two-Color Designs

Two-colour designs without a common reference require the most statistical knowledge to choose the appropriate design matrix. A direct design is one in which there is no single RNA source which is hybridized to every array. As an example, we consider an experiment conducted by Dr Mireille Lahoud at the Walter and Eliza Hall Institute to compare gene expression in three different populations of dendritric cells (DC).



Arrow heads represent Cy5, i.e. arrows point in the Cy3 to Cy5 direction

This experiment involved six cDNA microarrays in three dye-swap pairs, with each pair used to compare two DC types. The design is shown diagrammatically above. The targets file was as follows:

#### 

There are many valid choices for a design matrix for such an experiment and no single correct choice. We chose to setup the design matrix as follows:

```
> design <- cbind("CD8-CD4"=c(1,-1,1,-1,0,0),"DN-CD4"=c(0,0,-1,1,1,-1))
> rownames(design) <- removeExt(targets$FileName)
> design
```

	CD8-CD4	DN-CD4
ml12med	1	0
ml13med	-1	0
${\tt ml14med}$	1	-1
ml15med	-1	1
ml16med	0	1
ml17med	0	-1

In this design matrix, the CD8 and DN populations have been compared back to the CD4 population. The coefficients estimated by the linear model will correspond to the log-ratios of CD8 vs CD4 (first column) and DN vs CD4 (second column). After appropriate normalization of the expression data, a linear model was fit using

```
> fit <- lmFit(MA, design, ndups=2)</pre>
```

The use of ndups is to specify that the arrays contained duplicates of each gene, see Section ??.

The linear model can now be interrogated to answer any questions of interest. For this experiment it was of interest to make all pairwise comparisons between the three DC populations. This was accomplished using the contrast matrix

The contrast matrix can be used to expand the linear model fit and then to compute empirical Bayes statistics:

```
> fit2 <- constrast.fit(fit, contrast.matrix)
> fit2 <- eBayes(fit2)</pre>
```

# 10 Special Designs

## 10.1 Simple Comparisons

The simplest possible microarray experiment is one with a series of replicate two-color arrays all comparing the same two RNA sources. For a three-array experiment comparing wild type (wt) and mutant (mu) RNA, the targets file might contain the following entries:

FileName	СуЗ	Cy5
File1	wt	mu
File2	wt	mu
File3	wt	mu

A list of differentially expressed genes might be found for this experiment by

```
> fit <- lmFit(MA)
> fit <- eBayes(fit)
> topTable(fit, adjust="fdr")
```

where MA holds the normalized data. The default design matrix used here is just a single column of ones. The experiment here measures the fold change of mutant over wild type. Genes which have positive M-values are more highly expressed in the mutant RNA while genes with negative M-values are more highly expressed in the wild type. The analysis is analogous to the classical single-sample t-test except that we have used empirical Bayes methods to borrow information between genes.

# 10.2 Dye Swaps

A simple modification of the above experiment would be to swap the dyes for one of the arrays. The targets file might now be

FileName	СуЗ	Cy5
File1	wt	mu
File2	mu	wt
File3	wt	mu

Now the analysis would be

```
> design <- c(1,-1,1)
> fit <- lmFit(MA, design)
> fit <- eBayes(fit)
> topTable(fit, adjust="fdr")
```

Alternatively the design matrix could be set, replacing the first of the above code lines, by

```
> design <- modelMatrix(targets, ref="wt")</pre>
```

where targets is the data frame holding the targets file information.

If there are at least two arrays with each dye-orientation, it may be useful to estimate and the probe-specific dye effects. The dye-effect is estimated by an intercept term. If the experiment was

FileName	СуЗ	Cy5
File1	wt	mu
File2	mu	wt
File3	wt	mu
File4	mu	wt

then we could set

```
> design <- cbind(DyeEffect=1,MUvsWT=c(1,-1,1,-1))
> fit <- lmFit(MA, design)
> fit <- eBayes(fit)</pre>
```

Now a list of differentially expressed genes would be obtained by

```
> topTable(fit, coef="MUvsWT", adjust="fdr")
```

The genes which show dye effects could be seen by

```
> topTable(fit, coef="DyeEffect", adjust="fdr")
```

Including the dye-effect in the model in this way uses up one degree of freedom which might otherwise be used to estimate the residual variability, but may be valuable if many genes show non-negligible dye-effects.

## 10.3 Technical Replication I

In the previous sections we have assumed that all arrays are biological replicates. Now consider an experiment in which two wild type and two mutant mice are compared using two arrays for each pair of mice. The targets might be

FileName	СуЗ	Cy5
File1	wt1	mu1
File2	wt1	mu1
File3	wt2	mu2
File4	wt2	mu2

The first and second and third and fourth arrays are *technical replicates*. It would not be correct to treat these as four replicate arrays because the technical replicate pairs are not independent. If there are any differences between two wild type or two mutant mice then the technical replicate pairs are likely to be positively correlated.

One way to analyze these data is the following:

```
> corfit <- duplicateCorrelation(MA, ndups=1, block=c(1,1,2,2))
> fit <- lmFit(MA, block=c(1,1,2,2), correlation=corfit$consensus)
> fit <- eBayes(fit)
> topTable(fit, adjust="fdr")
```

The argument block indicates the two blocks corresponding to biological replicates. The value corfit\$consensus measures the average correlation within the blocks and should be positive. (If corfit\$consensus is negative, then the above method should not be used. In that case the technical replicate structure can be ignored, meaning that the data can be analyzed as if all arrays were biological replicates.) This analysis is analogous to mixed model analysis of variance (Milliken and Johnson, 1992, Chapter 18) except that information has been borrowed between genes. Information is borrowed (i) by constraining the within-block correlations to be equal between genes and (ii) by using empirical Bayes methods to moderate the standard deviations between genes.

If the technical replicates were in dye-swap pairs as

FileName	СуЗ	Cy5
File1	wt1	mu1
File2	mu1	wt1
File3	wt2	mu2
File4	mu2	wt2

then one might use

```
> design <- c(1,-1,1,-1)
> corfit <- duplicateCorrelation(MA, design, ndups=1, block=c(1,1,2,2))
> fit <- lmFit(MA, design, block=c(1,1,2,2), correlation=corfit$consensus)
> fit <- eBayes(fit)
> topTable(fit, adjust="fdr")
```

In this case the correlation corfit\$consensus should be negative, because the technical replicates are dye-swaps and should vary in opposite directions.

This method of handling technical replication using duplicateCorrelation() is somewhat limited. If for example one technical replicate was dye-swapped and other not,

FileName	СуЗ	Cy5
File1	wt1	mu1
File2	mu1	wt1
File3	wt2	mu2
File4	wt2	mu2

then there is no way to use duplicateCorrelation() because the technical replicate correlation will be negative for the first pair but positive for the second.

## 10.4 Technical Replication II

In the last example of the previous section, it was noted that duplicateCorrelation() could not be used. An alternative is to include a coefficient for mouse in the linear model, i.e., to fit a separate effect for each mouse. This could be accomplished by defining

```
> design <- designMatrix(targets, ref="wt1")
> fit <- lmFit(MA, design)
This will fit a linear model with three coefficients,
> colnames(fit)
[1] "mu1" "mu2" "wt2"
```

which measure differences between the other mice and wt1. The coefficient mu1 measures the difference between mu2 mu3 muse mu1 and mouse wt1. Coefficient mu2 measures the difference between mu2 and wt1. Coefficient wt2 measures the difference between wt2 and wt1. What we want is the average difference between the mutant and wild type mice, and this is extracted by the contrast (mu1+mu2-wt2)/2:

```
> cont.matrix <- makeContrasts(MUvsWT=(mu1+mu2-wt2)/2, levels=design)
> fit2 <- contrasts.fit(fit, cont.matrix)
> fit2 <- eBayes(fit2)
> topTable(fit2, adjust="fdr")
```

This technique of including an effect for each biological replicate, in this case each mouse, is well suited to situations with a lot of technical replication. Here is a larger example from a real experiment. Three mutant mice are to be compared with three wild type mice. Eighteen two-color arrays were used with each mouse appearing on six different arrays:

### > targets

```
FileName Cy3 Cy5
1391 1391.spot wt1 mu1
1392 1392.spot mu1 wt1
1340 1340.spot wt2 mu1
1341 1341.spot mu1 wt2
1395 1395.spot wt3 mu1
1396 1396.spot mu1 wt3
1393 1393.spot wt1 mu2
1394 1394.spot mu2 wt1
1371 1371.spot wt2 mu2
1372 1372.spot mu2 wt2
1338 1338.spot wt3 mu2
1339 1339.spot mu2 wt3
1387 1387.spot wt1 mu3
1388 1388.spot mu3 wt1
1399 1399.spot wt2 mu3
1390 1390.spot mu3 wt2
1397 1397.spot wt3 mu3
1398 1398.spot mu3 wt3
```

The comparison of interest is the average difference between the mutant and wild type mice. duplicateCorrelation() could not be used here because the arrays do not group neatly into biological replicate groups. In any case, with six arrays on each mouse it is much safer and more conservative to fit an effect for each mouse. We could proceed as

```
> design <- modelMatrix(targets, ref="wt1")
> design <- cbind(Dye=1,design)
> colnames(design)

[1] "Dye" "mu1" "mu2" "mu3" "wt2" "wt3"
```

The above code treats the first wild-type mouse as a baseline reference so that columns of the design matrix represent the difference between each of the other mice and wt1. The design matrix also includes an intercept term which represents the dye effect of cy5 over cy3 for each gene. If you don't wish to allow for a dye effect, the second line of code can be omitted.

```
> fit <- lmFit(MA, design)
> cont.matrix <- makeContrasts(muvswt=(mu1+mu2+mu3-wt2-wt3)/3, levels=design)
> fit2 <- contrasts.fit(fit, cont.matrix)
> fit2 <- eBayes(fit2)
> topTable(fit2, adjust="fdr")
```

The contrast defined by the function makeContrasts represents the average difference between the mutant and wild-type mice, which is the comparison of interest.

This general approach is applicable to many studies involving biological replicates. Here is another example based on a real example conducted by the WEHI Scott Lab. RNA is collected from four human subjects from the same family, two affected by a leukemia-inducing mutation and two unaffected. Each of the two affected subjects (A1 and A2) is compared with each of the two unaffected subjects (U1 and U2):

FileName	СуЗ	Cy5
File1	U1	A1
File2	A1	U2
File3	U2	A2
File4	A2	U1

Our interest is to find genes which are differentially expressed between the affected and unaffected subjects. Although all four arrays compare an affected with an unaffected subject, the four arrays are not independent. We need to take account of the fact that RNA from each subject appears on two different arrays. We do this by fitting a model with a coefficient for each subject and then extracting the contrast between the affected and unaffected subjects:

```
> design <- modelMatrix(targets, ref="U1")
> fit <- lmFit(MA, design)
> cont.matrix <- makeContrasts(AvsU=(A1+A2-U2)/2, levels=design)
> fit2 <- contrasts.fit(fit, cont.matrix)
> fit2 <- eBayes(fit2)
> topTable(fit2, adjust="fdr")
```

## 10.5 Two Groups

Suppose now that we wish to compare two wild type (Wt) mice with three mutant (Mu) mice using arrays hybridized with a common reference RNA (Ref):

FileName	СуЗ	Cy5
File1	Ref	WT
File2	Ref	WT
File3	Ref	Mu
File4	Ref	Mu
File5	Ref	Mu

The interest here is in the comparison between the mutant and wild type mice. There are two major ways in which this comparison can be made. We can

- 1. create a design matrix which includes a coefficient for the mutant vs wild type difference, or
- 2. create a design matrix which includes separate coefficients for wild type and mutant mice and then extract the difference as a contrast.

For the first approach, the design matrix should be as follows

### > design

	WTvsREF	MUvsWT
Array1	1	0
Array2	1	0
Array3	1	1
Array4	1	1
Array5	1	1

Here the first coefficient estimates the difference between wild type and the reference for each probe while the second coefficient estimates the difference between mutant and wild type. For those not familiar with model matrices in linear regression, it can be understood in the following way. The matrix indicates which coefficients apply to each array. For the first two arrays the fitted values will be just the WTvsREF coefficient, which is correct. For the remaining arrays the fitted values will be WTvsREF + MUvsWT, which is equivalent to mutant vs reference, also correct. For reasons that will be apparent later, this is sometimes called the treatment-contrasts parametrization. Differentially expressed genes can be found by

```
> fit <- lmFit(MA, design)
> fit <- eBayes(fit)
> topTable(fit, coef="MUvsWT", adjust="fdr")
```

There is no need here to use contrasts.fit() because the comparison of interest is already built into the fitted model. This analysis is analogous to the classical *pooled two-sample t-test* except that information has been borrowed between genes.

For the second approach, the design matrix should be

```
WT MU
Array1 1 0
Array2 1 0
Array3 0 1
Array4 0 1
Array5 0 1
```

The first coefficient now represents wild-type vs the reference and the second represents mutant vs the reference. Our comparison of interest is the difference between these two coefficients. We will call this the *group-means* parametrization. Differentially expressed genes can be found by

```
> fit <- lmFit(MA, design)
> cont.matrix <- makeContrasts(MUvsWT=WT-MU, levels=design)
> fit2 <- contrasts.fit(fit, cont.matrix)
> fit2 <- eBayes(fit2)
> topTable(fit2, adjust="fdr")
```

The results will be exactly the same as for the first approach.

The design matrix can be constructed

- 1. manually,
- 2. using the limma function modelMatrix(), or
- 3. using the built-in R function model.matrix().

Let Group be the factor defined by

```
> Group <- factor(c("WT","WT","Mu","Mu","Mu"), levels=c("WT","Mu"))</pre>
```

For the first approach, the treatment-contrasts parametrization, the design matrix can be computed by

```
> design <- cbind(WTvsRef=1,MUvsWT=c(0,0,1,1,1))
or by
> param <- cbind(WTvsRef=c(-1,1,0),MUvsWT=c(0,-1,1))
> rownames(param) <- c("Ref","WT","Mu")
> design <- modelMatrix(targets, parameters=param)
or by
> design <- model.matrix(~Group)
> colnames(design) <- c("WTvsRef","MUvsWT")</pre>
```

all of which produce the same result. For the second approach, the group-means parametrization, the design matrix can be computed by

```
> design <- cbind(WT=c(1,1,0,0,0,MU=c(0,0,1,1,1)) or by
```

```
> param <- cbind(WT=c(-1,1,0),MU=c(-1,0,1))
> rownames(param) <- c("Ref","WT","Mu")
> design <- modelMatrix(targets, parameters=param)
or by
> design <- model.matrix(~O+Group)
> colnames(design) <- c("WT","Mu")</pre>
```

all of which again produce the same result.

## 10.6 Two Groups: Affymetrix

Suppose now that we wish to compare two wild type (Wt) mice with three mutant (Mu) mice using Affymetrix arrays or any other single-channel array technology:

FileName	Target
File1	WT
File2	WT
File3	Mu
File4	Mu
File5	Mu

Everything is exactly as in the previous section, except that the function modelMatrix() would not be used. We can either

- 1. create a design matrix which includes a coefficient for the mutant vs wild type difference, or
- 2. create a design matrix which includes separate coefficients for wild type and mutant mice and then extract the difference as a contrast.

For the first approach, the treatment-contrasts parametrization, the design matrix should be as follows:

### > design

```
WT MUvsWT
Array1 1 0
Array2 1 0
Array3 1 1
Array4 1 1
Array5 1 1
```

Here the first coefficient estimates the mean log-expression for wild type mice and plays the role of an intercept. The second coefficient estimates the difference between mutant and wild type. Differentially expressed genes can be found by

```
> fit <- lmFit(eset, design)
> fit <- eBayes(fit)
> topTable(fit, coef="MUvsWT", adjust="fdr")
```

where eset is an exprSet or matrix object containing the log-expression values. For the second approach, the design matrix should be

```
WT MU
Array1 1 0
Array2 1 0
Array3 0 1
Array4 0 1
Array5 0 1
```

Differentially expressed genes can be found by

```
> fit <- lmFit(eset, design)
> cont.matrix <- makeContrasts(MUvsWT=WT-MU, levels=design)
> fit2 <- contrasts.fit(fit, cont.matrix)
> fit2 <- eBayes(fit2)
> topTable(fit2, adjust="fdr")
```

For the first approach, the treatment-contrasts parametrization, the design matrix can be computed by

```
> design <- cbind(WT=1,MUvsWT=c(0,0,1,1,1))
or by
> design <- model.matrix(~Group)
> colnames(design) <- c("WT","MUvsWT")</pre>
```

For the second approach, the group-means parametrization, the design matrix can be computed by

```
> design <- cbind(WT=c(1,1,0,0,0,MU=c(0,0,1,1,1))
or by
> design <- model.matrix(~0+Group)
> colnames(design) <- c("WT","MU")</pre>
```

# 10.7 Factorial Designs

Factorial designs are those where more than one experimental dimension is being varied and each combination of treatment conditions is observed. Suppose that cells are extracted from wild type and mutant mice and these cells are either stimulated (S) or unstimulated (U). RNA from the treated cells is then extracted and hybridized to a microarray. We will assume for simplicity that the arrays are single-color arrays such as Affymetrix. Consider the following targets frame:

FileName	Strain	Treatment
File1	WT	U
File2	WT	S
File3	Mu	U
File4	Mu	S
File5	Mu	S

The two experimental dimensions or *factors* here are Strain and Treatment. Strain specifies the genotype of the mouse from which the cells are extracted and Treatment specifies whether the cells are stimulated or not. All four combinations of Strain and Treatment are observed, so this is a factorial design. It will be convenient for us to collect the Strain/Treatment combinations into one vector as follows:

```
> TS <- paste(targets$Strain, targets$Treatment, sep=".")
> TS

[1] "WT.U" "WT.S" "Mu.U" "Mu.S" "Mu.S"
```

It is especially important with a factorial design to decide what are the comparisons of interest. We will assume here that the experimenter is interested in

- 1. which genes respond to stimulation in wild-type cells,
- 2. which genes respond to stimulation in mutant cells, and
- 3. which genes respond differently in mutant compared to wild-type cells.

as these are the questions which are most usually relevant in a molecular biology context. The first of these questions relates to the WT.S vs WT.U comparison and the second to Mu.S vs Mu.U. The third relates to the difference of differences, i.e., (Mu.S-Mu.U)-(WT.S-WT.U), which is called the *interaction* term.

We describe first a simple way to analyse this experiment using limma commands in a similar way to that in which two-sample designs were analyzed. Then we will go on to describe the more classical statistical approaches using factorial model formulas. All the approaches considered are equivalent and yield identical bottom-line results. The most basic approach is to fit a model with a coefficient for each of the four factor combinations and then to extract the comparisons of interest as contrasts:

```
> TS <- factor(TS, levels=c("WT.U","WT.S","Mu.U","Mu.S"))
> design <- model.matrix(~0+TS)
> colnames(design) <- levels(TS)
> fit <- lmFit(eset, design)</pre>
```

This fits a model with four coefficients corresponding to WT.U, WT.S, Mu.U and Mu.S respectively. Our three contrasts of interest can be extracted by

```
> cont.matrix <- makeContrasts(
+ WT.SvsU=WT.S-WT.U,
+ Mu.SvsU=Mu.S-Mu.U,
+ Diff=(Mu.S-Mu.U)-(WT.S-WT.U),
+ levels=design)
> fit2 <- contrasts.fit(fit, cont.matrix)
> fit2 <- eBayes(fit2)</pre>
```

We can use topTable() to look at lists of differentially expressed genes for each of three contrasts, or else

```
> results <- decideTests(fit2)</pre>
```

to look at all three contrasts simultaneously.

The analysis of factorial designs has a long history in statistics and a system of factorial *model formulas* has been developed to facilitate the analysis of complex designs. It is important to understand though that the above three molecular biology questions do not correspond to any of the usual parametrizations used in statistics for factorial designs. Suppose for example that we proceed in the usual statistical way,

```
> Strain <- factor(targets$Strain, levels=c("WT","Mu"))
> Treatment <- factor(targets$Treatment, levels=c("U","S"))
> design <- model.matrix(~Strain*Treatment)</pre>
```

This creates a design matrix which defines four coefficients with the following interpretations:

Coefficient	Comparison	Interpretation
Intercept	WT.U	Baseline level of unstimulated WT
StrainMu	Mu.U-WT.U	Difference between unstimulated strains
TreatmentS	WT.S-WT.U	Stimulation effect for WT
StrainMu: TreatmentS	(Mu.S-Mu.U)-(WT.S-WT.U)	Interaction

This is called the *treatment-contrast* parametrization. Notice that one of our comparisons of interest, Mu.S-Mu.U, is not represented and instead the comparison Mu.U-WT.U, which might not be of direct interest, is included. We need to use contrasts to extract all the comparisons of interest:

```
> fit <- lmFit(eset, design)
> cont.matrix <- cbind(WT.SvsU=c(0,0,1,0),Mu.SvsU=c(0,0,1,1),Diff=c(0,0,0,1))
> fit2 <- contrasts.fit(fit, cont.matrix)
> fit2 <- eBayes(fit2)</pre>
```

This extracts the WT stimulation effect as the third coefficient and the interaction as the fourth coefficient. The mutant stimulation effect is extracted as the sum of the third and fourth coefficients of the original model. This analysis yields exactly the same results as the previous analysis.

An even more classical statistical approach to the factorial experiment would be to use the *sum to zero* parametrization. In R this is achieved by

```
> contrasts(Strain) <- contr.sum(2)
> contrasts(Treatment) <- contr.sum(2)
> design <- model.matrix(~Strain*Treatment)</pre>
```

This defines four coefficients with the following interpretations:

Coefficient	Comparison	Interpretation
Intercept	(WT.U+WT.S+Mu.U+Mu.S)/4	Grand mean
Strain1	(WT.U+WT.S-Mu.U-Mu.S)/4	Strain main effect
Treatment1	(WT.U-WT.S+Mu.U-Mu.S)/4	Treatment main effect
Strain1:Treatment1	(WT.U-WT.S-Mu.U+Mu.S)/4	Interaction

<sup>&</sup>gt; vennDiagram(results)

This parametrization has many appealing mathematical properties and is the classical parametrization used for factorial designs in much experimental design theory. However it defines only one coefficient which is directly of interest to us, namely the interaction. Our three contrasts of interest could be extracted using

```
> fit <- lmFit(eset, design)
> cont.matrix <- cbind(WT.SvsU=c(0,0,-2,-2),Mu.SvsU=c(0,0,-2,2),Diff=c(0,0,0,4))
> fit2 <- contrasts.fit(fit, cont.matrix)
> fit2 <- eBayes(fit2)</pre>
```

The results will be identical to those for the previous two approaches.

The three approaches described here for the  $2 \times 2$  factorial problem are equivalent and differ only in the parametrization chosen for the linear model. The three fitted model objects fit will differ only in the coefficients and associated components. The residual standard deviations fitsigma, residual degrees of freedom fitdresidual and all components of fit2 will be identical for the three approaches. Since the three approaches are equivalent, users are free to choose whichever one is most convenient or intuitive.

# 11 Statistics for Differential Expression

A number of summary statistics are computed by the eBayes() function for each gene and each contrast. The M-value (M) is the log2-fold change, or sometimes the log2-expression level, for that gene. The A-value (A) is the the average expression level for that gene across all the arrays and channels. The moderated t-statistic (t) is the ratio of the M-value to its standard error. This has the same interpretation as an ordinary t-statistic except that the standard errors have been moderated across genes, effectively borrowing information from the ensemble of genes to aid with inference about each individual gene. The ordinary t-statistics are not usually required or recommended, but they can be recovered by

```
> tstat.ord <- fit$coef / fit$stdev.unscaled / fit$sigma
```

after fitting a linear model. The ordinary t-statistic is on fit\$df.residual degrees of freedom while the moderated t-statistic is on fit\$df.residual+fit\$df.prior degrees of freedom.

The p-value (p-value) is obtained from the moderated t-statistic, usually after some form of adjustment for multiple testing. The most popular form of adjustment is "fdr" which is Benjamini and Hochberg's method to control the false discovery rate. The meaning of the adjusted p-value is as follows. If you select all genes with p-value below a given value, say 0.05, as differentially expression, then the expected proportion of false discoveries in the selected group should be less than that value, in this case less than 5%.

The B-statistic (lods or B) is the log-odds that that gene is differentially expressed. Suppose for example that B=1.5. The odds of differential expression is  $\exp(1.5)=4.48$ , i.e, about four and a half to one. The probability that the gene is differentially expressed is 4.48/(1+4.48)=0.82, i.e., the probability is about 82% that this gene is differentially expressed. A B-statistic of zero corresponds to a 50-50 chance that the gene is differentially expressed. The B-statistic is automatically adjusted for multiple testing by assuming that 1%

of the genes, or some other percentage specified by the user, are expected to be differentially expressed. If there are no missing values in your data, then the moderated t and B statistics will rank the genes in exactly the same order. Even you do have spot weights or missing data, the p-values and B-statistics will usually provide a very similar ranking of the genes.

Please keep in mind that the moderated t-statistic p-values and the B-statistic probabilities depend on various sorts of mathematical assumptions which are never exactly true for microarray data. The B-statistics also depend on a prior guess for the proportion of differentially expressed genes. Therefore they are intended to be taken as a guide rather than as a strict measure of the probability of differential expression. Of the three statistics, the moderated-t, the associated p-value and the B-statistics, we usually base our gene selections on the p-value. All three measures are closely related, but the moderated-t and its p-value do not require a prior guess for the number of differentially expressed genes.

The above mentioned statistics are computed for every contrast for each gene. The eBayes() function computes one more useful statistic. The moderated F-statistic (F) combines the t-statistics for all the contrasts into an overall test of significance for that gene. The moderated F-statistic tests whether any of the contrasts are non-zero for that gene, i.e., whether that gene is differentially expressed on any contrast. The moderated-F has numerator degrees of freedom equal to the number of contrasts and denominator degrees of freedom the same as the moderated-t. Its p-value is stored as fit\$F.p.value. It is similar to the ordinary F-statistic from analysis of variance except that the denominator mean squares are moderated across genes.

In a complex experiment with many contrasts, it may be desirable to select genes firstly on the basis of their moderated F-statistics, and subsequently to decide which of the individual contrasts are significant for the selected genes. This cuts down on the number of tests which need to be conducted and therefore on the amount of adjustment for multiple testing. The function decideTests() with method="nestedF" is able to conduct such tests.

A warning on distributional assumptions. In the microarray context it is difficult to verify distributional assumptions, such as normality of the M-values, that the p-values are based on. This is a limitation of all model-based methods for micoarray data. This means that the p-values given are intended as a guide only. Also beware that the Benjamini and Hochberg method used to control the false discovery rate does assume that the t-statistics for different probes are independent, whereas the t-statistics for different probes are actually somewhat dependent as a result of being based on observations made on the same set of arrays. Reiner et al (2003) have argued that the Benjamini and Hochberg approach is actually quite stable with respect to dependence between the probes, but there remains no theoretical results to support this.

# 12 Data Objects in Limma

There are four main types of data objects created and used in limma:

RGList. Red-Green list. A class used to store raw intensities as they are read in from an image analysis output file, usually by read.maimages().

- MAList. Intensities converted to M-values and A-values, i.e., to with-spot and whole-spot contrasts on the log-scale. Usually created from an RGList using MA.RG() or normal-izeWithinArrays(). Objects of this class contain one row for each spot. There may be more than one spot and therefore more than one row for each probe.
- MArrayLM. Store the result of fitting gene-wise linear models to the normalized intensities or log-ratios. Usually created by lmFit. Objects of this class normally contain one row for each unique probe.
- TestResults. Store the results of testing a set of contrasts equal to zero for each probe. Usually created by decideTests. Objects of this class normally contain one row for each unique probe.

For those who are familiar with matrices in R, all these objects are designed to obey many analogies with matrices. In the case of RGList and MAList, rows correspond to spots and columns to arrays. In the case of MarrayLM, rows correspond to unique probes and columns to parameters or contrasts. The functions summary, dim, length, ncol, nrow, dimnames, rownames, colnames have methods for these classes. For example

```
> dim(RG)
```

[1] 11088 4

shows that the RGList object RG contains data for 11088 spots and 4 arrays.

> colnames(RG)

will give the names of the filenames or arrays in the object, while if fit is an MArrayLM object then

> colnames(fit)

would give the names of the coefficients in the linear model fit.

Objects of any of these classes may be subsetted, so that RG[,j] means the data for array j and RG[i,] means the data for probes indicated by the index i. Multiple data objects may be combined using cbind, rbind or merge. Hence

```
> RG1 <- read.maimages(files[1:2], source="genepix")
> RG2 <- read.maimages(files[3:5], source="genepix")
> RG <- cbind(RG1, RG2)
is equivalent to
> RG <- read.maimages(files[1:5], source="genepix")</pre>
```

Alternatively, if control status has been set in the an MAList object then

```
> i <- MA$genes$Status=="Gene"
> MA[i,]
```

might be used to eliminate control spots from the data object prior to fitting a linear model.

### 13 Case Studies

## 13.1 Swirl Zebrafish: A Single-Sample Experiment

In this section we consider a case study in which two RNA sources are compared directly on a set of replicate or dye-swap arrays. The case study includes reading in the data, data display and exploration, as well as normalization and differential expression analysis. The analysis of differential expression is analogous to a classical one-sample test of location for each gene.

In this example we assume that the data is provided as a GAL file called fish.gal and raw SPOT output files and that these files are in the current working directory.

```
> dir()
[1] "fish.gal"          "swirl.1.spot"          "swirl.2.spot"          "swirl.3.spot"          "swirl.4.spot"
[6] "SwirlSample.txt"
```

**Background**. The experiment was carried out using zebrafish as a model organism to study the early development in vertebrates. Swirl is a point mutant in the BMP2 gene that affects the dorsal/ventral body axis. The main goal of the Swirl experiment is to identify genes with altered expression in the Swirl mutant compared to wild-type zebrafish.

The hybridizations. Two sets of dye-swap experiments were performed making a total of four replicate hybridizations. Each of the arrays compares RNA from swirl fish with RNA from normal ("wild type") fish. The experimenters have prepared a tab-delimited targets file called SwirlSamples.txt which describes the four hybridizations:

```
> library(limma)
> targets <- readTargets("SwirlSample.txt")</pre>
> targets
SlideNumber
                FileName
                                СуЗ
                                           Cy5
                                                    Date
           81 swirl.1.spot
                                swirl wild type 2001/9/20
2
           82 swirl.2.spot wild type
                                           swirl 2001/9/20
3
           93 swirl.3.spot
                                swirl wild type 2001/11/8
           94 swirl.4.spot wild type
                                           swirl 2001/11/8
```

We see that slide numbers 81, 82, 93 and 94 were used to make the arrays. On slides 81 and 93, swirl RNA was labelled with green (Cy3) dye and wild type RNA was labelled with red (Cy5) dye. On slides 82 and 94, the labelling was the other way around.

Each of the four hybridized arrays was scanned on an Axon scanner to produce a TIFF image, which was then processed using the image analysis software SPOT. The data from the arrays are stored in the four output files listed under FileName. Now we read the intensity data into an RGList object in R. The default for SPOT output is that Rmean and Gmean are used as foreground intensities and morphR and morphG are used as background intensities:

```
> RG <- read.maimages(targets$FileName, source="spot")
Read swirl.1.spot
Read swirl.2.spot
Read swirl.3.spot</pre>
```

```
Read swirl.4.spot
> RG
An object of class "RGList"
$R
       swirl.1
                 swirl.2
                            swirl.3
                                        swirl.4
[1,] 19538.470 16138.720 2895.1600 14054.5400
[2,] 23619.820 17247.670 2976.6230 20112.2600
[3,] 21579.950 17317.150 2735.6190 12945.8500
                6794.381
      8905.143
                           318.9524
                                       524.0476
[5,]
      8676.095
                6043.542 780.6667
                                       304.6190
8443 more rows ...
\$G
       swirl.1
                  swirl.2
                            swirl.3
                                        swirl.4
[1,] 22028.260 19278.770 2727.5600 19930.6500
[2,] 25613.200 21438.960 2787.0330 25426.5800
[3,] 22652.390 20386.470 2419.8810 16225.9500
     8929.286
                6677.619
                           383.2381
                                       786.9048
[5,]
                6576.292 901.0000
     8746.476
                                       468.0476
8443 more rows ...
$Rb
     swirl.1 swirl.2 swirl.3 swirl.4
         174
                  136
                           82
[1,]
                                    48
[2,]
                           82
         174
                  133
                                    48
[3,]
         174
                  133
                           76
                                    48
[4,]
         163
                  105
                           61
                                    48
                  105
                                    49
[5,]
         140
                           61
8443 more rows ...
$Gb
     swirl.1 swirl.2 swirl.3 swirl.4
[1,]
         182
                  175
                           86
                                    97
[2,]
         171
                  183
                           86
                                    85
[3,]
         153
                  183
                           86
                                    85
[4,]
         153
                  142
                           71
                                    87
[5,]
         153
                  142
                           71
                                    87
8443 more rows ...
```

The arrays. The microarrays used in this experiment were printed with 8448 probes (spots), including 768 control spots. The array printer uses a print head with a 4x4 arrangement of print-tips and so the microarrays are partitioned into a 4x4 grid of tip groups. Each grid consists of 22x24 spots that were printed with a single print-tip. The gene name associated with each spot is recorded in a GenePix array list (GAL) file:

```
geno3
      1
         1
                 3 control
4
      1
         1
                              3XSSC
                 4 control
5
         1
                 5 control
                              3XSSC
6
      1
          1
                 6 control
                              EST1
7
      1
          1
                 7 control
                              geno1
8
      1
          1
                 8 control
                              geno2
9
      1
         1
                 9 control
                              geno3
10
      1
         1
                10 control
                              3XSSC
11
      1
          1
                11 control
                              3XSSC
12
      1
         1
                12 control
                              3XSSC
         1
                              EST2
13
      1
                13 control
14
      1
         1
                14 control
                               EST3
15
      1
         1
                15 control
                               EST4
16
      1
         1
                16 control
                              3XSSC
17
      1
         1
                17 control
                              Actin
18
      1
          1
                18 control
                              Actin
19
      1
         1
                19 control
                              3XSSC
20
      1
         1
                20 control
                              3XSSC
21
         1
                21 control
                              3XSSC
      1
22
      1
          1
                22 control
                              3XSSC
23
      1
         1
                23 control
                              Actin
24
      1 1
               24 control
                             Actin
      1 2
25
                 1 control
                              ath1
26
      1 2
                 2 control
                              Cad-1
      1 2
27
                 3 control
                             DeltaB
28
      1 2
                 4 control
                               Dlx4
29
          2
      1
                 5 control ephrinA4
30
                 6 control
                               FGF8
```

The 4x4x22x24 print layout also needs to be set. The easiest way to do this is to infer it from the GAL file:

```
> RG$printer <- getLayout(RG$genes)
```

**Image plots**. It is interesting to look at the variation of background values over the array. Consider image plots of the red and green background for the first array:

```
> imageplot(log2(RG$Rb[,1]), RG$printer, low="white", high="red")
> imageplot(log2(RG$Gb[,1]), RG$printer, low="white", high="green")
```

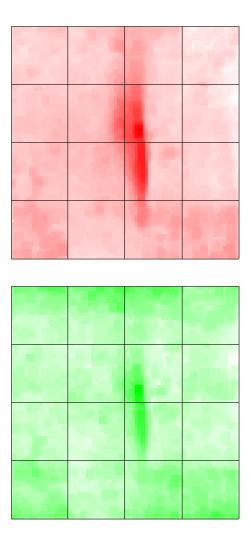


Image plot of the un-normalized log-ratios or M-values for the first array:

<sup>&</sup>gt; MA <- normalizeWithinArrays(RG, method="none")</pre>

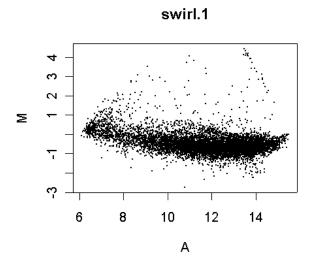
<sup>&</sup>gt; imageplot(MA\$M[,1], RG\$printer, zlim=c(-3,3))



The imageplot function lies the slide on its side, so the first print-tip group is bottom left in this plot. We can see a red streak across the middle two grids of the 3rd row caused by a scratch or dust on the array. Spots which are affected by this artefact will have suspect M-values. The streak also shows up as darker regions in the background plots.

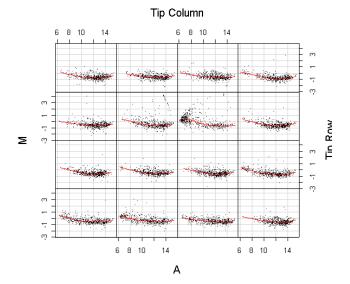
**MA-plots**. An MA-plot plots the log-ratio of R vs G against the overall intensity of each spot. The log-ratio is represented by the M-value,  $M = \log_2(R) - \log_2(G)$ , and the overall intensity by the A-value,  $A = (\log_2(R) + \log_2(G))/2$ . Here is the MA-plot of the un-normalized values for the first array:

> plotMA(MA)



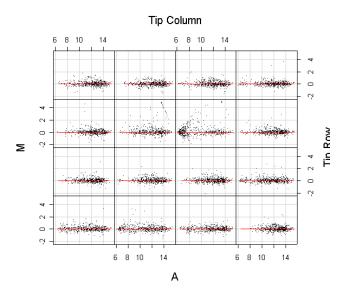
The red streak seen on the image plot can be seen as a line of spots in the upper right of this plot. Now we plot the individual MA-plots for each of the print-tip groups on this array, together with the loess curves which will be used for normalization:

#### > plotPrintTipLoess(MA)



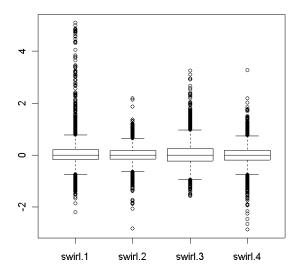
## **Normalization**. Print-tip loess normalization:

- > MA <- normalizeWithinArrays(RG)
- > plotPrintTipLoess(MA)



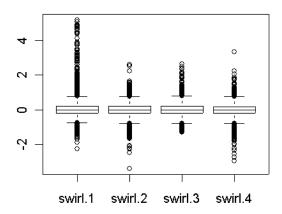
We have normalized the M-values with each array. A further question is whether normalization is required between the arrays. The following plot shows overall boxplots of the M-values for the four arrays.

> boxplot(MA\$M~col(MA\$M),names=colnames(MA\$M))



There is some evidence that the different arrays have different spreads of M-values, so we will scale normalize between the arrays.

- > MA <- normalizeBetweenArrays(MA)</pre>
- > boxplot(MA\$M~col(MA\$M),names=colnames(MA\$M))



**Linear model**. Now estimate the average M-value for each gene. We do this by fitting a simple linear model for each gene. The negative numbers in the design matrix indicate the dye-swaps.

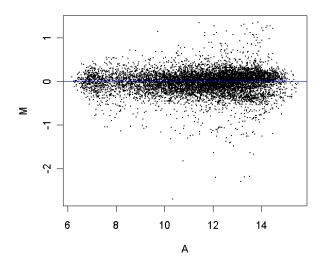
```
> design <- c(-1,1,-1,1)
> fit <- lmFit(MA,design)</pre>
An object of class "MArrayLM"
$coefficients
[1] -0.3943421 -0.3656843 -0.3912506 -0.2505729 -0.3432590
8443 more elements ...
$stdev.unscaled
[1] 0.5 0.5 0.5 0.5 0.5
8443 more elements ...
$sigma
[1] 0.3805154 0.4047829 0.4672451 0.3206071 0.2838043
8443 more elements ...
$df.residual
[1] 3 3 3 3 3
8443 more elements ...
$method
[1] "ls"
$design
     [,1]
[1,] -1
[2,]
[3,] -1
[4,]
$genes
 Block Row Column
                       ID Name
    1 1 1 control geno1
     1 1
              2 control geno2
     1 1
              3 control geno3
     1 1
              4 control 3XSSC
     1 1
                5 control 3XSSC
8443 more rows ...
$Amean
[1] 13.46481 13.67631 13.42665 10.77730 10.88446
8443 more elements ...
```

In the above fit object, coefficients is the average M-value for each gene and sigma is the sample standard deviations for each gene. Ordinary t-statistics for comparing mutant to wt could be computed by

```
> ordinary.t <- fit$coef / fit$stdev.unscaled / fit$sigma</pre>
```

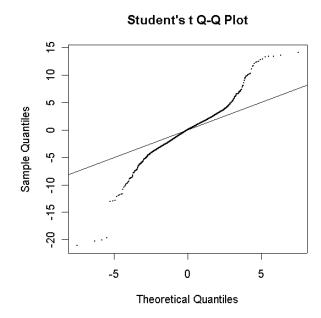
We prefer though to use empirical Bayes moderated t-statistics which are computed below. Now create an MA-plot of the average M and A-values for each gene.

```
> plotMA(fit)
> abline(0,0,col="blue")
```



**Empirical Bayes analysis**. We will now go on and compute empirical Bayes statistics for differential expression. The moderated t-statistics use sample standard deviations which have been shrunk towards a pooled standard deviation value.

```
> fit <- eBayes(fit)
> qqt(fit$t,df=fit$df.prior+fit$df.residual,pch=16,cex=0.2)
> abline(0,1)
```



Visually there seems to be plenty of genes which are differentially expressed. We will obtain a summary table of some key statistics for the top genes.

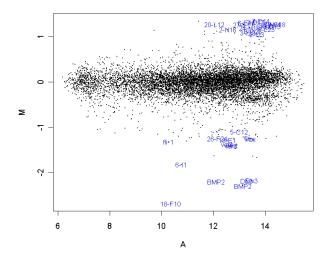
- > options(digits=3)
- > topTable(fit,number=30,adjust="fdr")

```
Block Row Column
                                            Α
                          TD
                                       М
                                                  t P.Value
3721
        8
            2
                               BMP2 -2.21 12.1 -21.1 0.000357 7.96
                   1 control
            2
        4
                               BMP2 -2.30 13.1 -20.3 0.000357 7.78
1609
                   1 control
3723
            2
                   3 control
                               Dlx3 -2.18 13.3 -20.0 0.000357 7.71
            2
                              Dlx3 -2.18 13.5 -19.6 0.000357 7.62
1611
        4
                   3 control
8295
       16 16
                  15 fb94h06 20-L12 1.27 12.0
                                               14.1 0.002067 5.78
7036
       14
           8
                   4 fb40h07
                             7-D14
                                    1.35 13.8
                                               13.5 0.002067 5.54
          22
                  11 fc22a09 27-E17
                                     1.27 13.2
                                               13.4 0.002067 5.48
515
        1
5075
       10
           14
                  11 fb85f09 18-G18
                                     1.28 14.4
                                               13.4 0.002067 5.48
7307
       14 19
                  11 fc10h09 24-H18
                                    1.20 13.4
                                               13.2 0.002067 5.40
319
                   7 fb85a01 18-E1 -1.29 12.5 -13.1 0.002067 5.32
2961
        6
           14
                   9 fb85d05 18-F10 -2.69 10.3 -13.0 0.002067 5.29
           14
                  24 fb87d12 18-N24
                                    1.27 14.2
                                               12.8 0.002067 5.22
4032
        8
       14
           2
                  15 control
                                Vox -1.26 13.4 -12.8 0.002067 5.20
6903
4546
          14
                  10 fb85e07 18-G13
                                    1.23 14.2
                                               12.8 0.002067 5.18
        2
                  11 fb37b09 6-E18
683
                                    1.31 13.3
                                               12.4 0.002182 5.02
        4
                  17 fb26b10 3-I20
                                    1.09 13.3
1697
            5
                                               12.4 0.002182 4.97
7491
       15
            5
                   3 fb24g06 3-D11 1.33 13.6
                                              12.3 0.002182 4.96
4188
        8
           21
                  12 fc18d12 26-F24 -1.25 12.1 -12.2 0.002209 4.89
4380
        9
            7
                  12 fb37e11 6-G21 1.23 14.0 12.0 0.002216 4.80
3726
        8
            2
                   6 control fli-1 -1.32 10.3 -11.9 0.002216 4.76
                                Vox -1.25 13.4 -11.9 0.002216 4.71
2679
        6
                  15 control
5931
       12
                   3 fb32f06 5-C12 -1.10 13.0 -11.7 0.002216 4.63
7602
       15
            9
                  18 fb50g12 9-L23
                                    1.16 14.0 11.7 0.002216 4.63
        5
            2
                  15 control
                               vent -1.40 12.7 -11.7 0.002216 4.62
2151
3790
                  7
                   6 fb36g12 6-D23 1.12 13.5 11.0 0.003000 4.27
7542
       15
4263
        9
            2
                  15 control
                               vent -1.41 12.7 -10.8 0.003326 4.13
                               vent -1.37 12.5 -10.5 0.004026 3.91
6375
       13
            2
                  15 control
1146
        3
                  18 fb22a12 2-I23 1.05 13.7 10.2 0.004242 3.76
                               6-I1 -1.82 10.8 -10.2 0.004242 3.75
157
        1
                  13 fb38a01
```

The top gene is BMP2 which is significantly down-regulated in the Swirl zebrafish, as it should be because the Swirl fish are mutant in this gene. Other positive controls also appear in the top 30 genes in terms.

In the table, t is the empirical Bayes moderated t-statistic, the corresponding P-values have been adjusted to control the false discovery rate and B is the empirical Bayes log odds of differential expression.

```
> plotMA(fit)
> ord <- order(fit$lods,decreasing=TRUE)
> top30 <- ord[1:30]
> text(fit$Amean[top30],fit$coef[top30],labels=fit$genes[top30,"Name"],cex=0.8,col="blue")
```



## 13.2 ApoAI Knockout Data: A Two-Sample Experiment

In this section we consider a case study where two RNA sources are compared through a common reference RNA. The analysis of the log-ratios involves a two-sample comparison of means for each gene.

In this example we assume that the data is available as an RGList in the data file ApoAI.RData.

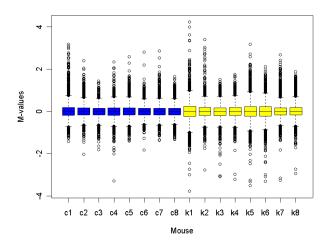
Background. The data is from a study of lipid metabolism by Callow et al (2000). The apolipoprotein AI (ApoAI) gene is known to play a pivotal role in high density lipoprotein (HDL) metabolism. Mice which have the ApoAI gene knocked out have very low HDL cholesterol levels. The purpose of this experiment is to determine how ApoAI deficiency affects the action of other genes in the liver, with the idea that this will help determine the molecular pathways through which ApoAI operates.

**Hybridizations**. The experiment compared 8 ApoAI knockout mice with 8 normal C57BL/6 ("black six") mice, the control mice. For each of these 16 mice, target mRNA was obtained from liver tissue and labelled using a Cy5 dye. The RNA from each mouse was hybridized to a separate microarray. Common reference RNA was labelled with Cy3 dye and used for all the arrays. The reference RNA was obtained by pooling RNA extracted from the 8 control mice.

Number of arrays	Red	Green	
8	Normal "black six" mice	Pooled reference	
8	ApoAI knockout	Pooled reference	

This is an example of a single comparison experiment using a common reference. The fact that the comparison is made by way of a common reference rather than directly as for the swirl experiment makes this, for each gene, a two-sample rather than a single-sample setup.

```
> library(limma)
> load("ApoAI.RData")
> objects()
[1] "RG"
> names(RG)
[1] "R" "G" "Rb" "Gb" "printer" "genes" "targets"
> RG$targets
      FileName Cy3
                        Cy5
c1 a1koc1.spot Pool C57BL/6
c2 a1koc2.spot Pool C57BL/6
c3 a1koc3.spot Pool C57BL/6
c4 a1koc4.spot Pool C57BL/6
c5 a1koc5.spot Pool C57BL/6
c6 a1koc6.spot Pool C57BL/6
c7 a1koc7.spot Pool C57BL/6
c8 a1koc8.spot Pool C57BL/6
k1 a1kok1.spot Pool ApoAI-/-
k2 a1kok2.spot Pool ApoAI-/-
k3 a1kok3.spot Pool ApoAI-/-
k4 a1kok4.spot Pool ApoAI-/-
k5 a1kok5.spot Pool ApoAI-/-
k6 a1kok6.spot Pool ApoAI-/-
k7 a1kok7.spot Pool ApoAI-/-
k8 a1kok8.spot Pool ApoAI-/-
> MA <- normalizeWithinArrays(RG)
> cols <- MA$targets$Cy5</pre>
> cols[cols=="C57BL/6"] <- "blue"
> cols[cols=="ApoAI-/-"] <- "yellow"
> boxplot(MA$M~col(MA$M),names=rownames(MA$targets),col=cols,xlab="Mouse",ylab="M-values")
```



Since the common reference here is a pool of the control mice, we expect to see more differences from the pool for the knock-out mice than for the control mice. In terms of the above plot, this should translate into a wider range of M-values for the knock-out mice arrays than for

the control arrays, and we do see this. Since the different arrays are not expected to have the same range of M-values, between-array scale normalization of the M-values is not appropriate here.

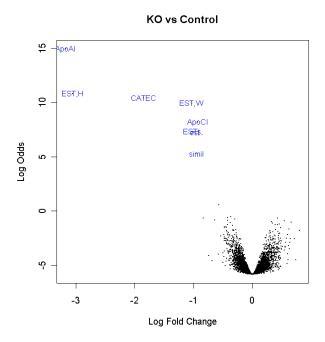
Now we can go on to estimate the fold change between the two groups. In this case the design matrix has two columns. The coefficient for the second column estimates the parameter of interest, the log-ratio between knockout and control mice.

```
> design <- cbind("Control-Ref"=1,"KO-Control"=MA$targets$Cy5=="ApoAI-/-")
> design
      Control-Ref KO-Control
 [1,]
                1
 [2,]
                1
                           0
 [3,]
                1
                           0
 [4,]
                           0
                1
 [5,]
                1
                           0
 [6,]
                1
                           0
 [7,]
                           0
                1
 [8,]
                1
                           0
 [9,]
                1
                           1
[10,]
[11,]
                1
                           1
[12,]
                           1
[13,]
                1
                           1
[14,]
                1
                           1
[15,]
                1
                           1
[16,]
                1
> fit <- lmFit(MA, design)</pre>
> fit$coef[1:5,]
     Control-Ref KO-Control
[1,]
         -0.6595
                     0.6393
[2,]
          0.2294
                     0.6552
[3,]
         -0.2518
                     0.3342
[4,]
         -0.0517
                     0.0405
[5,]
         -0.2501
                     0.2230
> fit <- eBayes(fit)
> options(digits=3)
> topTable(fit,coef=2,number=15,adjust="fdr")
     GridROW GridCOL ROW COL
                                              NAME TYPE
                                                             Μ
                                                                     t P. Value
2149
           2
                   2
                       8
                                   ApoAI, lipid-Img cDNA -3.166 -23.98 3.05e-11 14.927
540
           1
                   2
                          15 EST, HighlysimilartoA cDNA -3.049 -12.96 5.02e-07 10.813
5356
                           1 CATECHOLO-METHYLTRAN cDNA -1.848 -12.44 6.51e-07 10.448
           3
                       8
                           2 EST, WeaklysimilartoC cDNA -1.027 -11.76 1.21e-06 9.929
4139
                   3
           2
                       7
                                 ApoCIII, lipid-Img cDNA -0.933 -9.84 1.56e-05
1739
                   1
                          17
2537
           2
                   3
                       7
                          17 ESTs, Highlysimilar to cDNA -1.010 -9.02 4.22e-05
                                                                                7.305
1496
           1
                      15
                                               est cDNA -0.977 -9.00 4.22e-05
                                                                                7.290
4941
           4
                   1
                       8
                           6 similartoyeaststerol cDNA -0.955
                                                                -7.44 5.62e-04 5.311
947
           1
                   3
                       8
                           2 EST, WeaklysimilartoF cDNA -0.571
                                                                -4.55 1.77e-01 0.563
           4
                   3
                      1 18
                                                   cDNA -0.366 -3.96 5.29e-01 -0.553
5604
4140
           3
                   3 8
                           3
                                      APXL2,5q-Img cDNA -0.420 -3.93 5.29e-01 -0.619
6073
           4
                   4
                       5
                           4
                                       estrogenrec cDNA
                                                        0.421
                                                                 3.91 5.29e-01 -0.652
1337
           1
                          14 psoriasis-associated cDNA -0.838 -3.89 5.29e-01 -0.687
```

```
954 1 3 8 9 Caspase7, heart-Img cDNA -0.302 -3.86 5.30e-01 -0.757
563 1 2 8 17 FATTYACID-BINDINGPRO cDNA -0.637 -3.81 5.30e-01 -0.839
```

Notice that the top gene is ApoAI itself which is heavily down-regulated. Theoretically the M-value should be minus infinity for ApoAI because it is the knockout gene. Several of the other genes are closely related. The top eight genes here were confirmed by independent assay subsequent to the microarray experiment to be differentially expressed in the knockout versus the control line.

> volcanoplot(fit,coef=2,highlight=8,names=fit\$genes\$NAME,main="KO vs Control")



# 13.3 Ecoli Lrp Data: Affymetrix Data with Two Targets

The data are from experiments reported in Hung et al (2002) and are available from the www site http://visitor.ics.uci.edu/genex/cybert/tutorial/index.html. The data is also available from the ecoliLeucine data package available from the Bioconductor www site under "Experimental Data". Hung et al (2002) state that

The purpose of the work presented here is to identify the network of genes that are differentially regulated by the global  $E.\ coli$  regulatory protein, leucine-responsive regulatory protein (Lrp), during steady state growth in a glucose supplemented minimal salts medium. Lrp is a DNA-binding protein that has been reported to affect the expression of approximately 55 genes.

Gene expression in two E. coli bacteria strains, labelled lrp+ and lrp-, were compared using eight Affymetrix ecoli chips, four chips each for lrp+ and lrp-.

The following code assumes that the data files for the eight chips are in your current working directory.

The data is read and normalized using the affy package. The package ecolicdf must also be installed, otherwise the rma() function will attempt to download and install it for you—without giving you to opportunity to veto the download.

```
> library(limma)
> library(affy)
Welcome to Bioconductor
         Vignettes contain introductory material. To view,
         simply type: openVignette()
         For details on reading vignettes, see
         the openVignette help page.
> Data <- ReadAffy()</pre>
> eset <- rma(Data)
Background correcting
Normalizing
Calculating Expression
> pData(eset)
            sample
nolrp_1.CEL
                 1
nolrp_2.CEL
nolrp_3.CEL
                 3
nolrp_4.CEL
                 5
wt_1.CEL
wt_2.CEL
                 6
wt_3.CEL
                 7
wt_4.CEL
```

Now we consider differential expression between the lrp+ and lrp- strains.

```
> strain <- c("lrp-","lrp-","lrp-","lrp+","lrp+","lrp+","lrp+")
> design <- model.matrix(~factor(strain))</pre>
> colnames(design) <- c("lrp-","lrp+vs-")</pre>
> design
  1rp-1rp+vs-
1
    1
             0
2
     1
             0
3
    1
             0
4
             0
5
             1
    1
6
             1
7
    1
             1
    1
attr(,"assign")
[1] 0 1
attr(,"contrasts")
attr(,"contrasts")$"factor(strain)"
[1] "contr.treatment"
```

The first coefficient measures  $\log_2$ -expression of each gene in the lrp- strain. The second coefficient measures the  $\log_2$ -fold change of lrp+ over lrp-, i.e., the log-fold change induced by lrp.

```
> fit <- eBayes(fit)
> options(digits=2)
> topTable(fit, coef=2, n=40, adjust="fdr")
                         ProbeSetID
                                        М
                                              Α
                                                    t P. Value
                                                                   В
4282
      IG_821_1300838_1300922_fwd_st -3.32 12.4 -23.1 5.3e-05
                                                               8.017
5365
                      serA_b2913_st 2.78 12.2
                                                15.8 6.0e-04
1389
                      gltD_b3213_st
                                     3.03 10.9
                                                 13.3 1.6e-03
4625
                       lrp_b0889_st 2.30
                                          9.3
                                                11.4 4.0e-03
                                                 11.1 4.0e-03
1388
                      gltB_b3212_st
                                    3.24 10.1
4609
                      livK_b3458_st 2.35
                                          9.9
                                                 10.8 4.0e-03
                                                               4.593
4901
                      oppB_b1244_st -2.91 10.7 -10.6 4.0e-03
                                                               4.504
4903
                      oppD_b1246_st -1.94 10.4 -10.5 4.0e-03
                                                               4.434
5413
                      sodA_b3908_st 1.50 10.3
                                                  9.7 6.5e-03
                      oppA_b1243_st -2.98 13.0
4900
                                                -9.1 9.2e-03
                                                               3.601
5217
                       rmf_b0953_st -2.71 13.6
                                                -9.0 9.3e-03
                                                               3.474
7300
                      ytfK_b4217_st -2.64 11.1
                                                -8.9 9.3e-03
                                                               3.437
                      pntA_b1603_st 1.58 10.1
5007
                                                  8.3 1.4e-02
                                                               3.019
      IG_820_1298469_1299205_fwd_st -2.45 10.7
4281
                                                -8.1 1.6e-02
                                                               2.843
4491
                      ilvI_b0077_st 0.95 10.0
                                                  7.4 2.9e-02
                                                               2,226
5448
                      stpA_b2669_st 1.79 10.0
                                                  7.4 2.9e-02
                                                               2.210
611
                           b2343_st -2.12 10.8
                                                -7.1 3.4e-02
                                                               2.028
5930
                      ybfA_b0699_st -0.91 10.5
                                                 -7.0 3.5e-02
                                                               1.932
1435
                      grxB_b1064_st -0.91
                                           9.8
                                                -6.9 3.8e-02
                                                               1.810
4634
                      lysU_b4129_st -3.30
                                           9.3
                                                -6.9 3.9e-02
4829
                       ndk_b2518_st 1.07 11.1
                                                  6.7 4.3e-02
                                                               1.616
2309 IG_1643_2642304_2642452_rev_st 0.83
                                           9.6
                                                  6.7 4.3e-02
                                                               1.570
4902
                      oppC_b1245_st -2.15 10.7
                                                -6.3 5.9e-02
                                                               1.238
4490
                      ilvH_b0078_st 1.11
                                           9.9
                                                  5.9 8.8e-02
                                                               0.820
1178
                      fimA_b4314_st 3.40 11.7
                                                  5.9 8.8e-02
                                                               0.743
6224
                      ydgR_b1634_st -2.35
                                           9.8
                                                -5.8 8.8e-02
4904
                      oppF_b1247_st -1.46
                                           9.9
                                                -5.8 8.8e-02
                                                               0.720
792
                           b3914_st -0.77
                                           9.5
                                                -5.7 1.0e-01
5008
                      pntB_b1602_st
                                    1.47 12.8
                                                  5.6 1.0e-01
                                                               0.496
4610
                      livM_b3456_st
                                    1.04 8.5
                                                  5.5 1.1e-01
                                                               0.376
                      ptsG_b1101_st
                                     1.16 12.2
5097
                                                  5.5 1.1e-01
                                                               0.352
4886
                      nupC_b2393_st 0.79
                                           9.6
                                                  5.5 1.1e-01
                                                               0.333
                      ompT_b0565_st
4898
                                    2.67 10.5
                                                  5.4 1.2e-01
                                                               0.218
5482
                       tdh_b3616_st -1.61 10.5
                                                -5.3 1.3e-01
                                                               0.092
           IG_13_14080_14167_fwd_st -0.55
1927
                                           8.4
                                                -5.3 1.3e-01
                                                               0.076
6320
                      yeeF_b2014_st 0.88 9.9
                                                  5.3 1.3e-01
196
                      atpG_b3733_st
                                    0.60 12.5
                                                  5.2 1.4e-01 -0.033
954
                      cydB_b0734_st -0.76 11.0
                                                -5.0 1.8e-01 -0.272
1186
                      fimI_b4315_st 1.15 8.3
                                                  5.0 1.8e-01 -0.298
4013
         IG_58_107475_107629_fwd_st -0.49 10.4 -4.9 2.0e-01 -0.407
```

> fit <- lmFit(eset, design)</pre>

The column M gives the log<sub>2</sub>-fold change while the column A gives the average log<sub>2</sub>-intensity for the probe-set. Positive M-values mean that the gene is up-regulated in lrp+, negative

values mean that it is repressed.

It is interesting to compare this table with Tables III and IV in Hung et al (2002). Note that the top-ranked gene is an intergenic region (IG) tRNA gene. The knock-out gene itself is in position four. Many of the genes in the above table, including the ser, glt, liv, opp, lys, ilv and fim families, are known targets of lrp.

# 13.4 Estrogen Data: A 2x2 Factorial Experiment with Affymetrix Arrays

This data is from the estrogen package on Bioconductor. A subset of the data is also analysed in the factDesign package vignette. To repeat this case study you will need to have the R packages affy, estrogen and hgu95av2cdf installed.

The data gives results from a 2x2 factorial experiment on MCF7 breast cancer cells using Affymetrix HGU95av2 arrays. The factors in this experiment were estrogen (present or absent) and length of exposure (10 or 48 hours). The aim of the study is the identify genes which respond to estrogen and to classify these into early and late responders. Genes which respond early are putative direct-target genes while those which respond late are probably downstream targets in the molecular pathway.

First load the required packages:

The data files are contained in the extdata directory of the estrogen package:

The targets file is called phenoData.txt. We see there are two arrays for each experimental condition, giving a total of 8 arrays.

```
> targets <- readTargets("phenoData.txt",path=datadir,sep="",row.names="filename")
> targets
            filename estrogen time.h
low10-1
         low10-1.cel absent
                                  10
low10-2 low10-2.cel absent
                                  10
high10-1 high10-1.cel present
                                  10
high10-2 high10-2.cel present
                                  10
low48-1 low48-1.cel
                                  48
                      absent
low48-2
         low48-2.cel
                       absent
                                  48
```

```
high48-1 high48-1.cel present 48
high48-2 high48-2.cel present 48
```

Now read the cel files into an AffyBatch object and normalize using the rma() function from the affy package:

```
> ab <- ReadAffy(filenames=targets$filename, celfile.path=datadir)
> eset <- rma(ab)
Background correcting
Normalizing
Calculating Expression</pre>
```

There are many ways to construct a design matrix for this experiment. Given that we are interested in the early and late estrogen responders, we can choose a parametrization which includes these two contrasts.

```
> treatments <- factor(c(1,1,2,2,3,3,4,4),labels=c("e10","E10","e48","E48")) > contrasts(treatments) <- cbind(Time=c(0,0,1,1),E10=c(0,1,0,0),E48=c(0,0,0,1)) > design <- model.matrix(~treatments) > colnames(design) <- c("Intercept","Time","E10","E48")
```

The second coefficient picks up the effect of time in the absence of estrogen. The third and fourth coefficients estimate the  $\log_2$ -fold change for estrogen at 10 hours and 48 hours respectively.

```
> fit <- lmFit(eset,design)</pre>
```

We are only interested in the estrogen effects, so we choose a contrast matrix which picks these two coefficients out:

```
> cont.matrix <- cbind(E10=c(0,0,1,0),E48=c(0,0,0,1))
> fit2 <- contrasts.fit(fit, cont.matrix)
> fit2 <- eBayes(fit2)</pre>
```

We can examine which genes respond to estrogen at either time using the moderated F-statistics on 2 degrees of freedom. The moderated F p-value is stored in the component fit2\$F.p.value.

What p-value cutoff should be used? One way to decide which changes are significant for each gene would be to use Benjamini and Hochberg's method to control the false discovery rate across all the genes and both tests:

```
> results <- decideTests(fit2, method="global")
```

Another method would be to adjust the F-test p-values rather than the t-test p-values:

```
> results <- decideTests(fit2, method="nestedF")</pre>
```

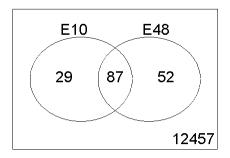
Here we use a more conservative method which depends far less on distributional assumptions, which is to make use of control and spike-in probe-sets which theoretically should not be differentially-expressed. The smallest p-value amongst these contols turns out to be about 0.00014:

```
> i <- grep("AFFX",geneNames(eset))
> summary(fit2$F.p.value[i])
    Min. 1st Qu. Median Mean 3rd Qu. Max.
0.0001391 0.1727000 0.3562000 0.4206000 0.6825000 0.9925000
```

So a cutoff p-value of 0.0001, say, would conservatively avoid selecting any of the control probe-sets as differentially expressed:

```
> results <- classifyTestsF(fit2, p.value=0.0001)</pre>
> summary(results)
   E10
        E48
-1
     40
            76
0 12469 12410
     116
          139
> table(E10=results[,1],E48=results[,2])
    E48
E10 -1
          0
        29
              11
                     0
  -1
  0
        47 12370
                    52
  1
              29
                    87
         0
```

> vennDiagram(results,include="up")



> vennDiagram(results,include="down")



We see that 87 genes were up regulated at both 10 and 48 hours, 29 only at 10 hours and 52 only at 48 hours. Also, 29 genes were down-regulated throughout, 11 only at 10 hours and 47 only at 48 hours. No genes were up at one time and down at the other.

topTable gives a detailed look at individual genes. The leading genes are clearly significant, even using the default p-value adjustment method, which is the highly conservative Holm's method.

- > options(digits=3)
- > topTable(fit2,coef="E10",n=20)

```
Α
                     М
                                 t P. Value
                                                В
9735
                              23.7 5.99e-05 9.97
       39642_at
                 2.94
                        7.88
12472
         910_at
                 3.11
                        9.66
                              23.6 6.26e-05 9.94
1814
       31798_at
                 2.80 12.12
                              16.4 1.29e-03 7.98
11509
       41400_at
                 2.38 10.04
                              16.2 1.41e-03 7.92
                 2.56
10214
       40117_at
                        9.68
                              15.7 1.86e-03 7.70
953
        1854_at
                 2.51
                       8.53
                              15.2 2.46e-03 7.49
                              15.1 2.59e-03 7.45
9848
       39755_at
                 1.68 12.13
922
      1824_s_at
                 1.91
                        9.24
                              14.9 2.86e-03 7.37
140
      1126_s_at
                 1.78
                        6.88
                              13.8 5.20e-03 6.89
580
        1536_at
                 2.66
                        5.94
                              13.3 7.30e-03 6.61
12542
         981_at
                 1.82
                        7.78
                              13.1 8.14e-03 6.52
3283
       33252_at
                 1.74
                        8.00
                              12.6 1.12e-02 6.25
546
        1505_at
                 2.40
                        8.76
                              12.5 1.20e-02 6.19
                        5.55 -12.2 1.44e-02 6.03
4405
       34363_at -1.75
985
      1884_s_at
                 2.80
                        9.03
                              12.1 1.59e-02 5.95
       36134_at
                 2.49
                        8.28
                              11.8 1.90e-02 5.79
6194
7557
       37485_at
                 1.61
                        6.67
                              11.4 2.50e-02 5.55
                 1.57 11.25
1244
         239_at
                              10.4 5.14e-02 4.90
8195
       38116_at
                 2.32
                        9.51
                              10.4 5.16e-02 4.90
10634
       40533_at
                 1.26
                       8.47
                              10.4 5.31e-02 4.87
```

<sup>&</sup>gt; topTable(fit2,coef="E48",n=20)

```
ID
                     М
                           Α
                                 t P.Value
                                                 В
         910_at
                 3.86
                       9.66
                              29.2 1.04e-05 11.61
12472
1814
       31798_at
                 3.60 12.12
                              21.1 1.62e-04
                              20.2 2.29e-04
953
                 3.34
                        8.53
                                              9.64
        1854_at
8195
       38116_at
                 3.76
                        9.51
                              16.9 1.02e-03
                                              8.48
       38065_at
                       9.10
                              16.2 1.42e-03
                                              8.21
8143
                 2.99
9848
       39755 at
                 1.77 12.13
                              15.8 1.72e-03
                                              8.05
642
        1592_at
                 2.30
                       8.31
                              15.8 1.76e-03
                                              8.03
11509
       41400 at
                 2.24 10.04
                              15.3 2.29e-03
                                              7.81
       33730_at -2.04
                       8.57 -15.1 2.48e-03
                                              7.74
3766
732
        1651_at
                 2.97 10.50
                              14.8 3.02e-03
                                              7.57
8495
       38414_at
                 2.02
                        9.46
                              14.6 3.36e-03
                                              7.48
1049
        1943_at
                 2.19
                        7.60
                              14.0 4.69e-03
                                              7.18
10214
       40117_at
                 2.28
                        9.68
                              14.0 4.79e-03
                                              7.16
10634
       40533_at
                 1.64
                        8.47
                              13.5 6.24e-03
                                              6.93
9735
       39642_at
                 1.61
                        7.88
                              13.0 8.46e-03
                                              6.65
4898
                 1.96
                        9.96
                              12.8 9.47e-03
       34851_at
                                              6.55
922
      1824_s_at
                 1.64
                        9.24
                              12.8 1.00e-02
                                              6.50
       35995_at
                 2.76
                        8.87
                              12.7 1.05e-02
                                              6.46
6053
12455
         893_at
                 1.54 10.95
                              12.7 1.06e-02
                                              6.45
10175
       40079_at -2.41 8.23 -12.6 1.09e-02
```

## 13.5 Weaver Mutant Data: A 2x2 Factorial Experiment with Two-Color Data

This case study considers a more involved analysis in which the sources of RNA have a factorial structure.

Background. This is a case study examining the development of certain neurons in wild-type and weaver mutant mice from Diaz et al (2002). The weaver mutant affects cerebellar granule neurons, the most numerous cell-type in the central nervous system. Weaver mutant mice are characterized by a weaving gait. Granule cells are generated in the first postnatal week in the external granule layer of the cerebellum. In normal mice, the terminally differentiated granule cells migrate to the internal granule layer but in mutant mice the cells die before doing so, meaning that the mutant mice have strongly reduced numbers of cells in the internal granule layer. The expression level of any gene which is specific to mature granule cells, or is expressed in response to granule cell derived signals, is greatly reduced in the mutant mice.

Tissue dissection and RNA preparation. At each time point (P11 = 11 days postnatal and P21 = 21 days postnatal) cerebella were isolated from two wild-type and two mutant littermates and pooled for RNA isolation. RNA was then divided into aliquots and labelled before hybridizing to the arrays. (This means that different hybridizations are biologically related through using RNA from the same mice, although we will ignore this here. See Yang and Speed (2002) for a detailed discussion of this issue in the context of this experiment.)

**Hybridizations**. There are four different treatment combinations, P11wt, P11mt, P21wt and P21mt, which might think of as a 2x2 factorial structure. We consider ten arrays in total. There are six arrays comparing the four different RNA sources to a common reference,

which was a pool of RNA from all the time points, and four arrays making direct comparisons between the four treatment combinations.

First read in the data. We assume that the data is an directory called c:/Weaver. We first read in the targets frame, and then read the intensity data using file names recorded in the targets file. The data was produced using SPOT image analysis software and is stored in the subdirectory /spot. Notice that a spot quality weight function as been set. For these arrays the median spot area is just over 50 pixels. The spot quality function has been set so that any spot with an area less than 50 pixels will get reduced weight, so that a hypothetical spot of zero area would get zero weight.

```
> library(limma)
> setwd("C:/Weaver")
> targets <- readTargets("targets.txt")</pre>
> targets
              FileName
                           Tissue Mouse
                                            Cy5
                                                  Cy3
cbmut.3
          cbmut.3.spot Cerebellum Weaver P11wt
          cbmut.4.spot Cerebellum Weaver P11mt Pool
cbmut.4
cbmut.5
          cbmut.5.spot Cerebellum Weaver P21mt Pool
cbmut.6
          cbmut.6.spot Cerebellum Weaver P21wt Pool
cbmut.15 cbmut.15.spot Cerebellum Weaver P21wt Pool
cbmut.16 cbmut.16.spot Cerebellum Weaver P21mt Pool
             cb.1.spot Cerebellum Weaver P11wt P11mt
cb.1
cb.2
             cb.2.spot Cerebellum Weaver P11mt P21mt
             cb.3.spot Cerebellum Weaver P21mt P21wt
cb.3
cb.4
             cb.4.spot Cerebellum Weaver P21wt P11wt
> wtfun <- function(x) pmax(x$area/50, 1)</pre>
> RG <- read.maimages(targets$FileName, source = "spot", path = "spot", wt.fun = wtfun)
Read spot/cbmut.3.spot
Read spot/cbmut.4.spot
Read spot/cbmut.5.spot
Read spot/cbmut.6.spot
Read spot/cbmut.15.spot
Read spot/cbmut.16.spot
Read spot/cb.1.spot
Read spot/cb.2.spot
Read spot/cb.3.spot
Read spot/cb.4.spot
```

The SPOT software does not store probe IDs in the output files, so we need to read in the ID and annotation information separately. We also read in a spottypes file and set a range of control spots.

```
> RG$genes <- read.delim("genelist.txt", header = TRUE, as.is = TRUE)
> RG$printer <- list(ngrid.r = 8, ngrid.c = 4, nspot.r = 25, nspot.c = 24)
> spottypes <- readSpotTypes("spottypes.txt")
> spottypes
```

```
SpotType
                          ID
                                                   Name
                                                                col cex
              Riken
                                                             black 0.2
1
2
            Custom Control
                                                             black 1.0
3
            Buffer Control
                                                 3x SSC
                                                             yellow 1.0
4
   CerEstTitration Control
                                          cer est \\(*
                                                         lightblue 1.0
5
      LysTitration Control
                                              Lys \\(*
                                                             orange 1.0
                                                             orange 1.0
6
      PheTitration Control
                                              Phe \\(*
7
    RikenTitration Control
                                        Riken est \\(*
                                                               blue 1.0
8
      ThrTitration Control
                                              Thr \\(*
                                                             orange 1.0
9
                18S Control
                                   18S \\(0.15ug/ul\\)
                                                               pink 1.0
10
              GAPDH Control
                               GAPDH \\(0.15 ug/ul\\)
                                                                red 1.0
11
            Lysine Control
                               Lysine \setminus (0.2 \text{ ug/ul} \setminus)
                                                           magenta 1.0
12
         Threonine Control Threonine \\(0.2ug/ul\\) lightgreen 1.0
13
            Tubulin Control Tubulin \\(0.15 ug/ul\\)
                                                             green 1.0
```

#### > RG\$genes\$Status <- controlStatus(spottypes, RG)

Matching patterns for: ID Name

Found 19200 Riken

Found 2304 Custom

Found 710 Buffer

Found 192 CerEstTitration

Found 224 LysTitration

Found 260 PheTitration

Found 160 RikenTitration

Found 224 ThrTitration

Found 64 18S

Found 64 GAPDH

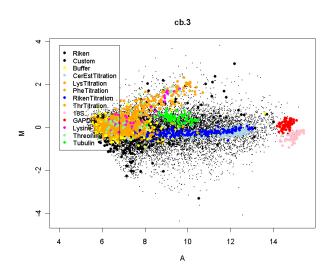
Found 32 Lysine

Found 32 Threonine

Found 64 Tubulin

Setting attributes: values col cex

#### > plotMA(RG,array=9,xlim=c(4,15.5))



Here Buffer is an obvious negative control while 18S, GAPDH, Lysine, Threonine and Tubulin are single-gene positive controls, sometime called house-keeping genes. RikenTitration is a titration series of a pool of the entire Riken library, and can be reasonably expected to be non-differentially expressed. CerEstTitration is a titration of a pool of a cerebellum EST library. This will show higher expression in later mutant tissues. The Lys, Phe and Thr series are single-gene titration series which were not spike-in in this case and can be treated as negative controls.

Now normalize the data. Because the Riken titration library, being based on a pool of a large number of non-specific genes, should not be differentially expressed, we up-weight these spots in the print-tip normalization step:

```
> w <- modifyWeights(RG$weights, RG$genes$Status, "RikenTitration", 2)
> MA <- normalizeWithinArrays(RG, weights = w)</pre>
```

Now fit a linear model to the data. Because of the composite design, with some common reference arrays and some direct comparison arrays, the simplest method is to use a group-mean parametrization with all RNA samples compared back to the Pool.

```
> design <- modelMatrix(targets, ref = "Pool")
Found unique target names:
P11mt P11wt P21mt P21wt Pool</pre>
```

#### > design

	P11mt	P11wt	P21mt	P21wt
cbmut.3	0	1	0	0
cbmut.4	1	0	0	0
cbmut.5	0	0	1	0
cbmut.6	0	0	0	1
${\tt cbmut.15}$	0	0	0	1
cbmut.16	0	0	1	0
cb.1	-1	1	0	0
cb.2	1	0	-1	0
cb.3	0	0	1	-1
cb.4	0	-1	0	1

All the control spots are removed before fitting the linear model:

```
> isGene <- MA$genes$Status == "Riken"
> fit <- lmFit(MA[isGene, ], design)</pre>
```

We now extract all possible comparisons of interest as contrasts. We look for the mutant vs wt comparisons at 11 and 21 days, the time effects for mutant and wt, and the interaction terms:

```
> cont.matrix <- makeContrasts(
+ WT11.MT11=P11mt-P11wt,
+ WT21.MT21=P21mt-P21wt,
+ WT11.WT21=P21wt-P11wt,</pre>
```

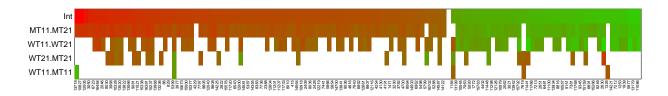
```
+ MT11.MT21=P21mt-P11mt,
+ Int=(P21mt-P11mt)-(P11mt-P11wt),
+ levels=design)
> fit2 <- contrasts.fit(fit, cont.matrix)
> fit2 <- eBayes(fit2)</pre>
```

Adjustment for multiple testing, with Benjamini and Hochberg's method applied to the F-test p-values across genes with 5% false discovery rate, and nesting F-testing used within contrasts, leads to the following:

```
> results <- decideTests(fit2, method = "nestedF")
> summary(results)
   WT11.MT11 WT21.MT21 WT11.WT21 MT11.MT21
                                               Int
-1
                     30
                              135
                                         136
                                                 43
0
       16886
                  16786
                            16648
                                       16573 16769
                              113
                                         187
```

There are 187 genes up and 136 genes down in mutant at 21 days vs 11 days. There are 84 genes which respond more up in the mutant than the wt, and 43 genes which respond more down in the mutant than the wt. A heatdiagram shows that the genes are mostly responding in the same direction in the mutant and wt, but to different degrees:

> heatDiagram(results, fit2\$coef, primary = "Int")



# 14 Within-Array Replicate Spots

In this section we consider a case study in which all genes (ESTs and controls) are printed more than once on the array. This means that there is both within-array and between-array replication for each gene. The structure of the experiment is therefore essentially a randomized block experiment for each gene. The approach taken here is to estimate a common correlation for all the genes for between within-array duplicates. The theory behind the approach is explained in Smyth, Michaud and Scott (2003). This approach assumes that all genes are replicated the same number of times on the array and that the spacing between the replicates is entirely regular.

#### 14.1 Example. Bob Mutant Data

In this example we assume that the data is available as an RG list.

Background. This data is from a study of transcription factors critical to B cell maturation by Lynn Corcoran and Wendy Dietrich at the WEHI. Mice which have a targeted mutation in the Bob (OBF-1) transcription factor display a number of abnormalities in the B lymphocyte compartment of the immune system. Immature B cells that have emigrated from the bone marrow fail to differentiate into full fledged B cells, resulting in a notable deficit of mature B cells.

Arrays. Arrays were printed with expressed sequence tags (ESTs) from the National Institute of Aging 15k mouse clone library, plus a range of positive, negative and calibration controls. The arrays were printed using a 48 tip print head and 26x26 spots in each tip group. Data from 24 of the tip groups are given here. Every gene (ESTs and controls) was printed twice on each array.

Hybridizations. A retrovirus was used to add Bob back to a Bob deficient cell line. Two RNA sources were compared using 2 dye-swap pairs of microarrays. One RNA source was obtained from the Bob deficient cell line after the retrovirus was used to add GFP ("green fluorescent protein", a neutral protein). The other RNA source was obtained after adding both GFP and Bob protein. RNA from Bob+GFP was labelled with Cy5 in arrays 2 and 4, and with Cy3 in arrays 1 and 4.

```
> objects()
[1] "design" "gal"
                      "layout" "RG"
> design
[1] -1 1 -1 1
> gal[1:40,]
  Library
                      Name
1 Control
                 cDNA1.500
2 Control
                 cDNA1.500
3 Control Printing.buffer
4 Control Printing.buffer
5 Control Printing.buffer
6 Control Printing.buffer
  Control Printing.buffer
8 Control Printing.buffer
9 Control
                 cDNA1.500
                 cDNA1.500
10 Control
11 Control Printing.buffer
12 Control Printing.buffer
13 Control Printing.buffer
14 Control Printing.buffer
15 Control Printing.buffer
16 Control Printing.buffer
17 Control
                 cDNA1.500
18 Control
                 cDNA1.500
19 Control Printing.buffer
20 Control Printing.buffer
```

```
21 Control Printing.buffer
22 Control Printing.buffer
23 Control Printing.buffer
24 Control Printing.buffer
25 Control
                 cDNA1.500
26 Control
                cDNA1.500
27 NIA15k
                      H31
                      H31
28 NIA15k
29
   NIA15k
                      H32
30 NIA15k
                      H32
31 NIA15k
                      H33
32 NIA15k
                      H33
33 NIA15k
                      H34
34 NIA15k
                      H34
35 NIA15k
                      H35
                      H35
36 NIA15k
37 NIA15k
                      Н36
38 NIA15k
                      Н36
39 NIA15k
                      H37
40 NIA15k
                      Н37
```

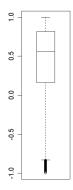
Although there are only four arrays, we have a total of eight spots for each gene, and more for the controls. Naturally the two M-values obtained from duplicate spots on the same array are highly correlated. The problem is how to make use of the duplicate spots in the best way. The approach taken here is to estimate the spatial correlation between the adjacent spots using REML and then to conduct the usual analysis of the arrays using generalized least squares.

First normalize the data using print-tip loess regression.

#### > MA <- normalizeWithinArrays(RG,layout)

Now estimate the spatial correlation. We estimate a correlation term by REML for each gene, and then take a trimmed mean on the atanh scale to estimate the overall correlation. This command takes a lot of time, perhaps as much as an hour for a series of arrays.

```
> cor <- duplicateCorrelation(MA,design,ndups=2) # A slow computation!
> cor$consensus.correlation
[1] 0.571377
> boxplot(cor$all.correlations)
```

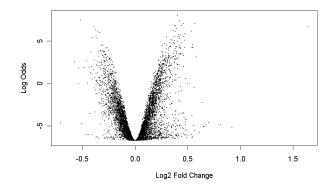


```
> fit <- lmFit(MA,design,ndups=2,correlation=0.571377)
> fit <- eBayes(fit)</pre>
```

> topTable(fit,n=30,adjust="fdr")

```
М
                                     P. Value
                                                    В
     Name
                              t
  H34599
          0.4035865
                     13.053838 0.0004860773 7.995550
  H31324 -0.5196599 -12.302094 0.0004860773 7.499712
          0.4203320
                      12.089742 0.0004860773 7.352862
  H33309
   H3440
          0.5678168
                      11.664229 0.0004860773 7.049065
5
  H36795
          0.4600335
                      11.608550 0.0004860773 7.008343
6
   H3121
          0.4408640
                      11.362917 0.0004860773 6.825927
7
  H36999
          0.3806754
                      11.276571 0.0004860773 6.760715
8
   H3132
          0.3699805
                      11.270201 0.0004860773 6.755881
  H32838
          1.6404839
                     11.213454 0.0004860773 6.712681
10 H36207 -0.3930972 -11.139510 0.0004860773 6.656013
11 H37168 0.3909476
                     10.839880 0.0005405097 6.421932
12 H31831 -0.3738452 -10.706775 0.0005405097 6.315602
13 H32014 0.3630416
                     10.574797 0.0005405097 6.208714
14 H34471 -0.3532587 -10.496483 0.0005405097 6.144590
15 H37558 0.5319192
                     10.493157 0.0005405097 6.141856
   H3126 0.3849980
                      10.467091 0.0005405097 6.120389
17 H34360 -0.3409371 -10.308779 0.0005852911 5.988745
18 H36794
          0.4716704
                      10.145670 0.0006399135 5.850807
19 H3329
          0.4125222 10.009042 0.0006660758 5.733424
20 H35017
          0.4337911
                       9.935639 0.0006660758 5.669656
21 H32367
          0.4092668
                       9.765338 0.0006660758 5.519781
22 H32678
          0.4608290
                       9.763809 0.0006660758 5.518423
23 H31232 -0.3717084
                      -9.758581 0.0006660758 5.513778
24 H3111
          0.3693533
                       9.745794 0.0006660758 5.502407
25 H34258
          0.2991668
                       9.722656 0.0006660758 5.481790
26 H32159
          0.4183633
                       9.702614 0.0006660758 5.463892
27 H33192 -0.4095032
                      -9.590227 0.0007130533 5.362809
28 H35961 -0.3624470
                      -9.508868 0.0007205823 5.288871
29 H36025
          0.4265827
                       9.503974 0.0007205823 5.284403
                       9.316136 0.0008096722 5.111117
   H3416 0.3401763
```

> volcanoplot(fit)



# 15 Using Objects from the marray Package

The package marray is a well known R package for pre-processing of two-color microarray data. Marray provides functions for reading, normalization and graphical display of data. Marray and limma are both descendants of the earlier and path-breaking SMA package available from http://www.stat.berkeley.edu/users/terry/zarray/Software/smacode.html but limma has maintained and built upon the original data structures whereas marray has converted to a fully formal data class representation. For this reason, Limma is backwardly compatible with SMA while marray is not.

Normalization functions in marray focus on a flexible approach to location and scale normalization of M-values, rather than the within and between-array approach of limma. Marray provides some normalization methods which are not in limma including 2-D loess normalization and print-tip-scale normalization. Although there is some overlap between the normalization functions in the two packages, both providing print-tip loess normalization, the two approaches are largely complementary. Marray also provides highly developed functions for graphical display of two-color microarray data.

Read functions in marray produce objects of class marrayRaw while normalization produces objects of class marrayNorm. Objects of these classes may be converted to and from limma data objects using the convert package. marrayRaw objects may be converted to RGList objects and marrayNorm objects to MAList objects using the as function. For example, if Data is an marrayNorm object then

```
> library(convert)
> MA <- as(Data, "MAList")</pre>
```

converts to an MAList object.

marrayNorm objects can also be used directly in limma without conversion, and this is generally recommended. If Data is an marrayNorm object, then

```
> fit <- lmFit(Data, design)</pre>
```

fits a linear model to Data as it would to an MAList object. One difference however is that the marray read functions tend to populate the maW slot of the marrayNorm object with qualitative

spot quality flags rather than with quantitative non-negative weights, as expected by limma. If this is so then one may need

> fit <- lmFit(Data, design, weights=NULL)</pre>

to turn off use of the spot quality weights.

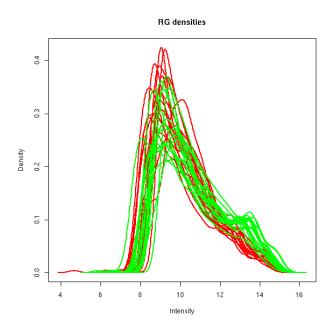
# 16 Between-Array Normalization of Two-Color Arrays

This section explores some of the methods available for between-array normalization of two-color arrays. A feature which distinguishes most of these methods from within-array normalization is the focus on the individual red and green intensity values rather than merely on the log-ratios. These methods might therefore be called *individual channel* or *separate channel* normalization methods. Individual channel normalization is typically a prerequisite to individual channel analysis methods such as that provided by <code>lmscFit()</code>. Further discussion of the issues involved is given by Yang and Thorne (2003). The ApoAI data set from Section 13.2 will be used to illustrate these methods. We assume that the ApoAI data has been loaded and background corrected as follows:

> load("ApoAI.RData")
> RG.b <-backgroundCorrect(RG,method="minimum")</pre>

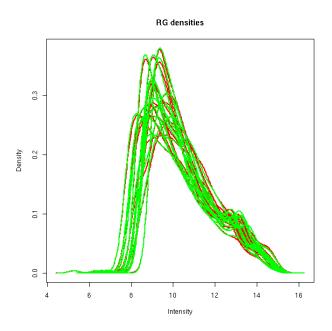
This section shows how to reproduce some of the results given in Yang and Thorne (2003). plotDensities displays smoothed empirical densities for the individual green and red channels on all the arrays. Without any normalization there is considerable variation between both channels and between arrays:

> plotDensities(RG.b, log.transform=TRUE)



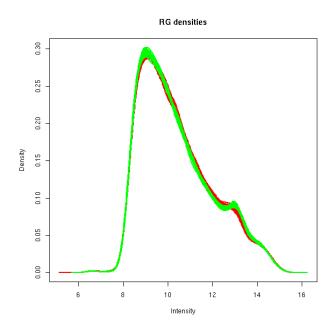
After loess normalization of the M-values for each array the red and green distributions become essentially the same for each array, although there is still considerable variation between arrays:

- > MA.p <-normalizeWithinArrays(RG.b)</pre>
- > plotDensities(MA.p)



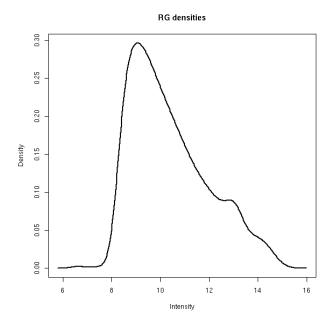
Loess normalization doesn't affect the A-values. Applying quantile normalization to the A-values makes the distributions essentially the same across arrays as well as channels:

- > MA.pAq <- normalizeBetweenArrays(MA.p, method="Aquantile")
- > plotDensities(MA.pAq)



Applying quantile normalization directly to the individual red and green intensities produces a similar result but is somewhat noisier:

```
> MA.n <- normalizeWithinArrays(RG.b, method="none")
> MA.q <- normalizeWithinArrays(RG.b, method="quantile")
> plotDensities(MA.pq, col="black")
```



There are other between-array normalization methods not explored here. For example normalizeBetweenArrays with method="vsn" gives an interface to the variance-stabilizing normalization methods of the vsn package.

## Conventions

Where possible, limma tries to use the convention that class names are in upper CamelCase, i.e., the first letter of each word is capitalized, while function names are in lower camelCase, i.e., first word is lowercase. When periods appear in function names, the first word should be an action while the second word is the name of a type of object on which the function acts.

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# Published Articles Using limma

The following articles are not cited in the User's Guide but are examples of biologically orientated publications which use the limma package.

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