Outline
Aims of modeling the EURACE labor market
Labor market overview
Sequence of action: Matching algorithm
Additional features

Labor Market in EURACE

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Aims of modeling the EURACE labor market

Labor market overview

Sequence of action: Matching algorithm

- Step 1: Vacancies and Dismissals
- Step 2: Households read vacancies and send applications
- Step 3: Firms read applications and send job offers
- Step 4: Households read job offers and send acceptance
- Step 5: Firms adjust their work force and their vacancies
- Step 6: Wage offer and reservation wage adjustment

Additional features



Aims for the labor market: Wage

- Aims for the labor market regarding wages:
 - 1. Wage dispersion across workers with different general skill levels.
 - ⇒ High skilled workers should generally receive higher wages than low skilled.
 - 2. Wage dispersion within a group of equally qualified workers.
 - \Rightarrow It should be possible that a high (low) skilled worker receives a higher or lower wage than another equally high (low) skilled worker.
 - 3. Wage competition between firms.
 - \Rightarrow Firms should increase the wage offers to attract more (high skilled) workers.
 - The development of wages should be connected to the development of the productivity of workers.
 - ⇒ Increasing productivity of workers should lead to increasing wages.



Aims for the labor market: Employment

- ▶ Aims for the labor market regarding employment:
 - 1. Reasonable unemployment rate.
 - \Rightarrow The unemployment rate should be in the range of real European unemployment rates.
 - 2. Different unemployment rates across households with different education levels.
 - \Rightarrow The unemployment rate for high skilled workers should be lower than for low skilled.
 - The unemployment rate should be connected to the production development in the economy.
 - ⇒ An increasing production level should lead to a decreasing (stable) unemployment rate.
 - 4. Voluntary unemployment.
 - \Rightarrow It should be possible that workers do not apply for jobs although they are unemployed.



Other aims for the labor market

- ▶ Other aims for the labor market:
 - 1. Frictions on the labor market.
 - ⇒ Vacancies and unemployed should exist contemporaneously.
 - 2. Spatial frictions on the labor market.
 - \Rightarrow In a multiple region setting different flows of commuters should be generated.

Important modeling features of workers to reach these aims

- Workers have a differentiated skill structure.
 - 1. General skills Education:
 - 5 exogenously given general skill groups.
 - Proxy for individual education.
 - Heterogenous within and across regions.
 - 2. Specific skills Productivity:
 - Capabilities and experiences attained on the job.
 - Associated with technology used by the employer.
- Workers increase specific skills over time.
 - ▶ Speed depends on the general skill level $b_{\mathbf{w}}^{\mathbf{gen}}$ and quality of technology used by employer $A_{i,t}$

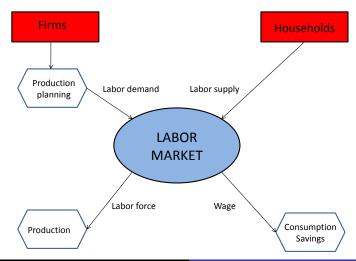
$$b_{w,t+1} = b_{w,t} + \chi(b_w^{gen})(A_{i,t} - b_{w,t})$$



Important features of firms to reach these aims

- Firms invest in new capital goods to increase the used technology $A_{i,t}$.
 - \Rightarrow Employees can improve their specific skills.
- Firms post wage offers for each skill group.
 - \Rightarrow Differentiated wage structure.

Embedment of the labor market in the EURACE model



Labor Demand and Labor supply

- Labor demand:
 - ▶ The labor demand is generated on the consumption goods market.
 - If the demand for consumption goods of one firm increases (decreases) the labor demand for production increases (decreases).
 - Firms enter the labor market once a month. This day is heterogenous across firms.
- Labor supply:
 - Unemployed generate the labor supply.
 - Labor supply is differentiated due to general and specific skills.
 - Unemployed enter the labor market every day as long as they are unemployed.

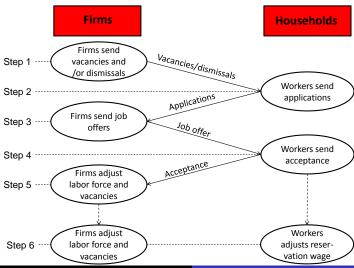
Step 1: Vacancies and Dismissals

Step 2: Households read vacancies and send applications

Step 3: Firms read applications and send job offers Step 4: Households read job offers and send acceptance

Step 5: Firms adjust their work force and their vacancies Step 6: Wage offer and reservation wage adjustment

Sequence of action: Matching algorithm



Step 2: Households read vacancies and send applications
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Sequence of action: Matching algorithm

- Step 1: Firms send dismissals and /or firms post vacancies including wage offers for each general skill level.
- ▶ Step 2: Workers/job seekers extract from the list of vacancies those postings to which they fit in terms of their reservation wage and send applications.
- Step 3: Firms read the incoming applications and send as many job offers as they have vacancies to fill.
- Step 4: Workers rank the incoming job offers according to the wages net of commuting costs and accept the highest ranked job offer.
- Step 5: Firms adjust their work force and their vacancies.
- Step 6: If the number of vacancies not filled exceeds some threshold firms raise the base wage offer. If an unemployed job seeker did not find a job he reduces his reservation wage.
- The labor market loop is repeated one time if one or more firms did not fill their vacancies during the first loop.



Step 3: Firms read applications and send job offers

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Step 1: Labor demand driven dismissals

▶ If firms want to decrease the production quantity they have to dismiss employees.

⇒ Connection between production level and unemployment rate.

- Three different rules:
 - 1. Random firing: Firms randomly choose which employees will be dismissed.
 - 2. Lowest general skills first: Firms dismiss employees with low general skill.
 - 3. Lowest specific skills first: Firms dismiss employees with low specific skills.

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Step 1: Random dismissals

- ightharpoonup Firms dismiss a randomly determined fraction γ_t of the employees in each period.
 - $ightharpoonup \gamma_{\mathbf{t}} \in [\mathit{lowerbound}, \mathit{upperbound}], \, \mathsf{for} \, \mathsf{example} \, \gamma_{\mathbf{t}} \in [0, 10]$
 - ► The boundaries are exogenously given.
- The idea: We combine several reasons for a job separation.
 - 1. Employees quit because they found a better job (on-the-job-search).
 - 2. Employees quit because they moved or were not satisfied with their actual job.
 - 3. Firms dismiss workers because they were not satisfied with the performance.



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Step 1: Vacancies

- If firms want to raise the production they have to increase the number of employees and to post vacancies.
 - ⇒ Connection between production level and unemployment rate.
- ► Two important characteristics of vacancies:
 - 1. Wage offers for each general skill group.
 - The region_id of the firm: Job seekers who want to work in a foreign region have to bear commuting costs (optional).

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Step 1: Vacancies Determination of the wage offer

Firm i determines the wage offer $w_{i,t,g}^O$ in period t for each general skill level g where $g \in [1,5]$

$$\Rightarrow w_{i,t,g}^O = w_{i,t}^b \times \bar{B}_{i,t,g}.$$

- ▶ The offered wage $w_{i,t,g}^{O}$ consists of two parts:
 - 1. Base wage offer $w_{i,t}^b$ which is paid for one unit of specific skills.
 - w_{i,t}^b will be increased in the second loop if the number of unfilled vacancies exceeded an exogenously given threshold ν.
 - The base wage offer is market driven and an increase is not price neutral.
 - 2. Average specific skill level $\bar{B}_{i,t,g}$ of employees with general skill level g in firm i.
 - The wage offer will be increased (decreased) if the productivity of workers increased (decreased).
 - This increase is price neutral.



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Step 1: Wage offer

- Via this wage offer determination the model produces different wage offers for different general skills.
 - ⇒ Connection of wage offers to the productivity of workers.
 - ⇒ Wage dispersion across and within skill groups.

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Step 2: Applications

 Workers/job seekers extract from the list of vacancies those postings to which they fit in terms of their reservation wage.

$$w_{i,t,g}^O \geq w_{w,t}^R$$

- ▶ If the wage offer $w_{i,t,g}^O$ is lower than the reservation wage $w_{w,t}^R$ of job seeker w in period t then the job seeker will ignore this posted vacancy.
- If the vacancy is posted by firm j from a foreign region the job seeker has to take commuting costs comm (optional) into account.

$$w_{j,t,g}^{O}-comm \geq w_{w,t}^{R}$$

⇒ Voluntary unemployment.



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Step 2: Applications

- ▶ The job seeker sends applications to z randomly chosen firms.
 - The exogenously given parameter z is the number of applications a job seeker can send where $z \in [0, NumberFirms]$.
 - The iob seeker chooses the firms randomly because we want to avoid that all iob seekers apply to the same firm, i.e. the firm with the highest wage offer.
 - → Imperfect Information

Step 3: Firms read applications and send job offers

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Step 3: Job offers

- Two possible cases:
 - 1. Case: The number of applicants is \leq than the number of vacancies.
 - Firms send job offers to all applicants.
 - 2. Case: The number of applicants is > than the number of vacancies.
 - Logit model: General skills of applicants are translated into an employment probability.
 - Higher general skills lead to higher employment probabilities.

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Step 3: Job offers - More applicants than vacancies

- Firms store the incoming applications in a list.
- We use a logit model to translate the general skills of an applicant a into an employment probability proba,t.

$$prob_{a,t} = rac{\exp^{\lambda b_a^{gen}}}{\sum\limits_{a=1}^{A} \exp^{\lambda b_a^{gen}}}$$

- The exogenously given parameter λ measures the sensitivity of employment probabilities with respect to the general skill levels and A is the number of applicants on the list.
- Firms randomly choose as many applicants as they have vacancies to fill and send job offers.



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Step 3: Job offers - Employment probabilities

- ▶ The influence of λ on the employment probabilities.
 - λ = 0: Applicants are chosen equally likely.
 - $ightharpoonup \lambda > 0$: As λ increases, applicants with higher general skills are chosen more likely.
 - $\lambda \to -\infty$: Employment probability for applicants with the highest general skill level (g=5) converges to 1.
 - ▶ Higher general skills lead to higher employment probabilities.
 - \Rightarrow Basis for different unemployment rates across the general skill groups.

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Step 4: Job acceptance and refusal

- If households receive one or more job offers they rank the incoming job offers.
 - 1. The job offer with the highest wage net of commuting costs is ranked first.
 - 2. If the offered wages of two job offers are equal they are ranked randomly.
- Households accept the highest ranked job offer.
- ▶ Households adjust the reservation wage to the new wage net commuting costs that is

$$w_{w,t}^R = w_{i,t,g}^O$$
 or $w_{w,t}^R = w_{j,t,g}^O - comm$.

- The other job offers are refused.
 - ⇒ Frictions: Vacancies remain unfilled.
 - ⇒ Frictions: Some unemployed do not get a job offer.



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Step 5: Work force and vacancies adjustment

- ▶ If firms receive one or more job acceptances:
 - The applicant is added to the work force and his ID, wage, general skill level and specific skills are stored.
 - 2. The number of vacancies is decreased by the number of job acceptances.

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Step 6: Wage offer adjustment

If the number of vacancies not filled exceeds an exogenously given threshold ν firms raise the base wage offer $w_{i,t}^{b}$ by an exogenously determined fraction φ .

$$\begin{aligned} w^b_{i,t+\tau} &= (1+\varphi)w^b_{i,t} \\ \Rightarrow w^O_{i,t+\tau,g} &= w^b_{i,t+\tau} \times \bar{B}_{i,t,g} \end{aligned}$$

- ► The market driven wage increase should attract more (high skilled) workers to fill the unfilled vacancies.
- ► The base wage offer is increased only after the first loop on the labor market and not after the second loop.



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Step 6: Wage offer adjustment

- Base wage offer adjustments lead to:
 - ⇒ Wage competition between firms.
 - ⇒ Connection between consumption goods demand and wages.
 - ⇒ Different wages across firms for the same general skill group.
 - ⇒ Wage dispersion within the general skill groups and across firms.

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Step 6: Reservation wage adjustment

▶ If a job seeker did not find a job he reduces his reservation wage by a fraction ϕ .

$$w_{w,t+\tau}^R = (1-\phi)w_{w,t}^R$$

- ▶ In the next round or period the job offer will also extract posted vacancies with a lower wage offer.
- ▶ There exists a lower bound for the reservation wage w_{min}^R .
 - ▶ The lower bound is determined by the unemployment benefit.



Wage increase due to productivity increase

▶ The wage of employee i in period t+1 will be increased if the productivity increased.

$$w_{i,t+1} = w_{i,t}(1 + P_{r,t})$$

- \triangleright $P_{r,t}$ is the average productivity increase in region r in period t.
- ▶ Interpretation: Simplified version of a wage bargaining agreement.
 - ⇒ Connection between wages and productivity progress.

Unemployment benefit

- Unemployed receive unemployment benefits UB.
- Unemployment benefits are based on an exogenously given regional unemployment benefit rate u_r of their last net wage.

$$UB_{i,t+1} = u_r(w_{i,t}(1 - taxrate))$$

The lower bound of unemployment benefits is 50% of the average net wage in the economy.

Spatial structure

- The EURACE model allows to have more than one region which can be calibrated differently, e.g. Germany and Poland.
- Implications for the labor market:
 - 1. Regional labor market with different properties.
 - 2. Commuting of workers between the regions.

Spatial structure - Different properties

- Regions can be calibrated differently regarding the labor market (and other markets).
 - 1. Different general skill distributions.
 - 2. Different specific skills.
 - 3. Different unemployment benefit rates.
 - 4. Different (base) wage offers.

Spatial structure - Different properties

► Calibration: Germany vs. Poland

| General skill level | Germany | Poland |
|---------------------|---------|--------|
| 1 | 10% | 42% |
| 2 | 30% | 33% |
| 3 | 40% | 20% |
| 4 | 15% | 4% |
| 5 | 5% | 1% |

| Variable | Germany | Poland |
|---------------------------|---------|--------|
| Specific skills | 1.5 | 1.0 |
| Base wage offer | 1.5 | 1.0 |
| Wage offer | 2.25 | 1.0 |
| Unemployment benefit rate | 0.7 | 0.6 |

Spatial structure - Commuting of workers

- ▶ The parameter commuting costs *comm* steers the flow of commuters.
- ▶ Job seekers only apply for a job in a foreign region if

$$w_{j,t,g}^{O} - comm \ge w_{w,t}^{R}.$$

If commuting costs are high

$$\lim_{comm \rightarrow \infty} (w_{j,t,g}^{O} - comm) = -\infty. \ \Rightarrow w_{j,t,g}^{O} - comm < w_{w,t}^{R}$$

- No commuting between regions.
- Interpretation: Labor markets are closed.
 - \Rightarrow Two or more separated labor markets.



Spatial structure - Commuting of workers

▶ If commuting costs are low

$$\lim_{comm \rightarrow 0} (w_{j,t,g}^{O} - comm) = w_{j,t,g}^{O} \Rightarrow w_{j,t,g}^{O} - comm \stackrel{\leq}{>} w_{w,t}^{R}.$$

- Commuting between regions.
- Interpretation: Labor markets are completely open.
 - ⇒ One completely integrated labor market.

Spatial structure - Commuting of workers

▶ There is a range of commuting costs $comm \in [\underline{comm}, \overline{comm}]$ where

$$w_{j,t,g}^{O} - comm < w_{w,t}^{R}$$
 for some job seekers and

$$w_{j,t,g}^{O} - comm \ge w_{w,t}^{R}$$
 for others.

▶ If additionally the wage offer by a firm *j* from a foreign region is higher than the wage offer by firm *i* from the domestic region some workers might commute and some not.

$$\Rightarrow w_{j,t,g}^{O} - comm > w_{i,t,g}^{O}$$

Interpretation: Two or more open labor markets with spatial frictions.



Spatial structure - Commuting costs

- ► Interpretation of commuting costs:
 - 1. Monetary costs for traveling.
 - 2. Opportunity costs: forgone leisure.
 - 3. Regulations by law: employment permit.