

Slow (kinematic) model discretization

$$\frac{\partial \dot{X}_1}{\partial X_4} = \cos(X_5 + X_7) \quad \frac{\partial \dot{X}_1}{\partial X_5} = -X_4 \cdot \sin(X_5 + X_7) \quad \frac{\partial \dot{X}_1}{\partial X_7} = -X_4 \sin(X_5 + X_7)$$

$$\frac{\partial \dot{X}_2}{\partial X_4} = \sin(X_5 + X_7) \quad \frac{\partial \dot{X}_2}{\partial X_5} = X_4 \cdot \cos(X_5 + X_7) \quad \frac{\partial \dot{X}_2}{\partial X_7} = X_4 \cos(X_5 + X_7)$$

$$\frac{\partial \dot{X}_3}{\partial u_2} = 1 \quad \frac{\partial \dot{X}_4}{\partial u_2} = 1 \quad \frac{\partial \dot{X}_5}{\partial X_3} = \frac{X_4 \cdot \cos(X_7)}{l_{wb}} \cdot \frac{1}{\cos^2(X_3)}$$

$$\frac{\partial \dot{X}_5}{\partial X_4} = \frac{\cos(X_7)}{l_{wb}} \cdot \tan(X_3) \quad \frac{\partial \dot{X}_5}{\partial X_7} = -\frac{X_4 \tan(X_3)}{l_{wb}} \cdot \sin(X_7)$$

$$\frac{\partial \dot{X}_6}{\partial X_3} = \frac{1}{l_{wb}} \cdot \left(u_2 \cdot \cos(X_7) \cdot \frac{1}{\cos^2(X_3)} - X_4 \cdot \sin(X_7) \cdot \left(\frac{1}{\cos^2(X_3)} \cdot \dot{X}_7 + \tan(X_3) \cdot \frac{\partial \dot{X}_7}{\partial X_3} \right) + X_4 \cdot \cos(X_7) \cdot u_1 \cdot 2 \cdot \frac{\sin(X_3)}{\cos^3(X_3)} \right)$$

$$\frac{\partial \dot{X}_6}{\partial X_4} = \frac{1}{l_{wb}} \cdot \left(-\sin(X_7) \cdot \tan(X_3) \cdot \dot{X}_7 + \frac{\cos(X_7)}{\cos^2(X_3)} \cdot u_1 \right)$$

$$\frac{\partial \dot{X}_6}{\partial X_7} = \frac{1}{l_{wb}} \cdot \left(-u_2 \tan(X_3) \cdot \sin(X_7) - X_4 \tan(X_3) \cdot \dot{X}_7 \cdot \cos(X_7) - \frac{X_4 \cdot u_1}{\cos^2(X_3)} \cdot \sin(X_7) \right)$$

$$\frac{\partial \dot{X}_6}{\partial u_2} = \frac{1}{l_{wb}} \cdot \left(\frac{X_4 \cdot (\cos(X_7))}{\cos^2(X_3)} \right) \quad \frac{\partial \dot{X}_6}{\partial u_1} = \frac{1}{l_{wb}} \cdot (\cos(X_7) \cdot \tan(X_3))$$

$$\frac{\partial \dot{X}_7}{\partial X_3} = -\frac{2 \cdot \left(\tan(X_3) \cdot \frac{l_r}{l_{wb}} \right) \cdot \frac{l_r}{l_{wb}} \cdot \frac{1}{\cos^2(X_3)}}{\left(1 + \left(\tan(X_3) \cdot \frac{l_r}{l_{wb}} \right)^2 \right)^2} \cdot \frac{l_r}{l_{wb}} \cdot \frac{u_1}{\cos^2(X_3)} + \frac{u_2}{1 + \left(\tan(X_3) \cdot \frac{l_r}{l_{wb}} \right)^2} \cdot \frac{l_r}{l_{wb}} \cdot 2 \cdot \frac{\sin(X_3)}{\cos^3(X_3)}$$

$$\frac{\partial \dot{x}_7}{\partial u_1} = \frac{1}{1 + \left(\tan(x_3) \cdot \frac{L_r}{L_{wb}} \right)^2} \cdot \frac{L_r}{L_{wb}} \cdot \frac{1}{\cos^2(x_3)}$$