Pedotransfer functions (PTFs) developed for Ksat using Multivariate polynomial regeression (MPR) and Random forest (RF)

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Abstract:

We prepared a comprehensive global compilation of measured Ksat training point data (N= 13,267) called "SoilKsatDB" by importing, quality controlling and standardizing tabular data from existing soil profile databases and legacy reports. The SoilKsatDB was used to develop the pedotransfer functions (PTFs) for temperate climate region and lab-based measured soil samples. These PTFs were applied to tropical climate region and field-based measurements, respectively to evaluate the suitability for other regions. Here, the objective of this report to show the methods used to develop the PTFs with R code and stepwise description.

```
#Loading Libraries
library(Metrics)
library(raster)

## Loading required package: sp

library(sp)
library(rgdal)
```

```
## rgdal: version: 1.4-8, (SVN revision 845)
## Geospatial Data Abstraction Library extensions to R successfully loaded
## Loaded GDAL runtime: GDAL 2.2.3, released 2017/11/20
## Path to GDAL shared files: C:/Users/guptasu.D/Documents/R/R-3.6.3/library/rgdal/gd
al
## GDAL binary built with GEOS: TRUE
## Loaded PROJ.4 runtime: Rel. 4.9.3, 15 August 2016, [PJ_VERSION: 493]
## Path to PROJ.4 shared files: C:/Users/guptasu.D/Documents/R/R-3.6.3/library/rgdal/
proj
## Linking to sp version: 1.4-1
```

```
library(hexbin)
library(lattice)
library(RColorBrewer)
library(viridis)
## Loading required package: viridisLite
library(ranger)
library(mlr)
## Loading required package: ParamHelpers
## Attaching package: 'ParamHelpers'
## The following object is masked from 'package:raster':
##
##
       getValues
## 'mlr' is in maintenance mode since July 2019. Future development
## efforts will go into its successor 'mlr3' (<https://mlr3.mlr-org.com>).
##
## Attaching package: 'mlr'
## The following object is masked from 'package:raster':
##
##
       resample
```

#Temperate climate region Ksat values PTF

Here, we loaded the temperate climate region soil samples. The soil samples were converted into log scale and then selected points with available three soil basic properties (sand, clay and bulk density).

```
rm.hydroprops = read.csv("E:/maps_tests/All_regions_ksat/Temperate_5_04_2020.csv")
rm.hydroprops$log_ksat = signif(log10( rowMeans(rm.hydroprops[,c("ksat_lab","ksat_fiel d")], na.rm=TRUE) ), 4)
soil_temp_clay <- rm.hydroprops[!is.na(rm.hydroprops$clay_tot_p),]
soil_temp_clay_bd<- soil_temp_clay[!is.na(soil_temp_clay$db_od),]</pre>
```

The ksat values were divided into training and testing datasets. We took 80% samples for developing the PTF and 20% for testing the model. Further multivariate polynomial regression (MPR) was fitted.

```
# Randomly split the dataset into training and testing datasets
sample_size = floor(0.80*nrow(soil_temp_clay_bd))
set.seed(777)
picked = sample(seq_len(nrow(soil_temp_clay_bd)), size = sample_size)
development = soil_temp_clay_bd[picked,]
nrow(development)
```

```
## [1] 6666
```

```
holdout =soil_temp_clay_bd[-picked,]
nrow(holdout)
```

```
## [1] 1667
```

```
##Fitting MPR model with degree 2
model_temp_ksat<- lm(log_ksat ~ poly(db_od,clay_tot_p, sand_tot_p, degree=2, raw=TRU
E), data =development )
summary(model_temp_ksat)</pre>
```

```
##
## Call:
## lm(formula = log ksat ~ poly(db od, clay tot p, sand tot p, degree = 2,
       raw = TRUE), data = development)
##
##
## Residuals:
##
       Min
                1Q Median
                                3Q
                                       Max
  -4.0153 -0.3059 0.0518 0.3707 3.1768
##
## Coefficients:
##
                                                                      Estimate
## (Intercept)
                                                                     1.910e+00
## poly(db_od, clay_tot_p, sand_tot_p, degree = 2, raw = TRUE)1.0.0 1.237e+00
## poly(db od, clay tot p, sand tot p, degree = 2, raw = TRUE)2.0.0 -8.892e-01
## poly(db_od, clay_tot_p, sand_tot_p, degree = 2, raw = TRUE)0.1.0 1.011e-02
## poly(db_od, clay_tot_p, sand_tot_p, degree = 2, raw = TRUE)1.1.0 -2.195e-02
## poly(db_od, clay_tot_p, sand_tot_p, degree = 2, raw = TRUE)0.2.0
## poly(db_od, clay_tot_p, sand_tot_p, degree = 2, raw = TRUE)0.0.1
## poly(db_od, clay_tot_p, sand_tot_p, degree = 2, raw = TRUE)1.0.1 1.054e-03
## poly(db_od, clay_tot_p, sand_tot_p, degree = 2, raw = TRUE)0.1.1 -2.403e-04
## poly(db od, clay tot p, sand tot p, degree = 2, raw = TRUE)0.0.2 6.097e-05
##
                                                                    Std. Error
## (Intercept)
                                                                     3.925e-01
## poly(db_od, clay_tot_p, sand_tot_p, degree = 2, raw = TRUE)1.0.0 3.816e-01
## poly(db od, clay tot p, sand tot p, degree = 2, raw = TRUE)2.0.0 1.282e-01
## poly(db_od, clay_tot_p, sand_tot_p, degree = 2, raw = TRUE)0.1.0 8.906e-03
## poly(db_od, clay_tot_p, sand_tot_p, degree = 2, raw = TRUE)1.1.0 4.990e-03
## poly(db_od, clay_tot_p, sand_tot_p, degree = 2, raw = TRUE)0.2.0 6.654e-05
## poly(db_od, clay_tot_p, sand_tot_p, degree = 2, raw = TRUE)0.0.1
## poly(db_od, clay_tot_p, sand_tot_p, degree = 2, raw = TRUE)1.0.1 2.826e-03
## poly(db_od, clay_tot_p, sand_tot_p, degree = 2, raw = TRUE)0.1.1 7.228e-05
## poly(db_od, clay_tot_p, sand_tot_p, degree = 2, raw = TRUE)0.0.2 2.795e-05
##
                                                                    t value
## (Intercept)
                                                                      4.867
## poly(db_od, clay_tot_p, sand_tot_p, degree = 2, raw = TRUE)1.0.0
                                                                      3.241
## poly(db_od, clay_tot_p, sand_tot_p, degree = 2, raw = TRUE)2.0.0
                                                                     -6.935
## poly(db_od, clay_tot_p, sand_tot_p, degree = 2, raw = TRUE)0.1.0
                                                                      1.135
## poly(db_od, clay_tot_p, sand_tot_p, degree = 2, raw = TRUE)1.1.0
                                                                     -4.399
## poly(db_od, clay_tot_p, sand_tot_p, degree = 2, raw = TRUE)0.2.0
                                                                      0.166
## poly(db_od, clay_tot_p, sand_tot_p, degree = 2, raw = TRUE)0.0.1
                                                                      0.665
## poly(db_od, clay_tot_p, sand_tot_p, degree = 2, raw = TRUE)1.0.1
                                                                      0.373
## poly(db_od, clay_tot_p, sand_tot_p, degree = 2, raw = TRUE)0.1.1
                                                                    -3.325
## poly(db_od, clay_tot_p, sand_tot_p, degree = 2, raw = TRUE)0.0.2
                                                                      2.181
                                                                    Pr(>|t|)
## (Intercept)
                                                                    1.16e-06 ***
## poly(db_od, clay_tot_p, sand_tot_p, degree = 2, raw = TRUE)1.0.0 0.00120 **
## poly(db_od, clay_tot_p, sand_tot_p, degree = 2, raw = TRUE)2.0.0 4.43e-12 ***
## poly(db_od, clay_tot_p, sand_tot_p, degree = 2, raw = TRUE)0.1.0 0.25624
```

```
## poly(db_od, clay_tot_p, sand_tot_p, degree = 2, raw = TRUE)1.1.0 1.10e-05 ***
## poly(db_od, clay_tot_p, sand_tot_p, degree = 2, raw = TRUE)0.2.0 0.86823
## poly(db_od, clay_tot_p, sand_tot_p, degree = 2, raw = TRUE)0.0.1 0.50619
## poly(db_od, clay_tot_p, sand_tot_p, degree = 2, raw = TRUE)1.0.1 0.70914
## poly(db_od, clay_tot_p, sand_tot_p, degree = 2, raw = TRUE)0.1.1 0.00089 ***
## poly(db_od, clay_tot_p, sand_tot_p, degree = 2, raw = TRUE)0.0.2 0.02920 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.7199 on 6656 degrees of freedom
## Multiple R-squared: 0.477, Adjusted R-squared: 0.4763
## F-statistic: 674.4 on 9 and 6656 DF, p-value: < 2.2e-16</pre>
```

After fitting the MPR model, Ksat values were predicted for the testing soil samples and compared with the observed Ksat soil samples. Then, the model was evaluated using root mean square error (RMSE), Concordance correlation coefficient (CCC) and Coefficient of determination (R square).

```
##Predction for the testing dataset
holdout$predict<- predict(model_temp_ksat, holdout)

##Linear model between predictions and measurements

Lm_pre_mea<- lm(log_ksat~ predict, data = holdout)

summary(Lm_pre_mea)</pre>
```

```
##
## Call:
## lm(formula = log ksat ~ predict, data = holdout)
##
## Residuals:
       Min
                1Q Median
                                3Q
## -3.3523 -0.2950 0.0544 0.3747 2.6662
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 0.04647
                          0.05629
                                    0.826
                                             0.409
## predict
               0.97572
                          0.02567 38.004
                                            <2e-16 ***
## ---
## Signif. codes:
                  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.7227 on 1665 degrees of freedom
## Multiple R-squared: 0.4645, Adjusted R-squared: 0.4642
## F-statistic: 1444 on 1 and 1665 DF, p-value: < 2.2e-16
```

```
##RMSE
rmse(holdout$log_ksat, holdout$predict)
```

```
## [1] 0.7225068
```

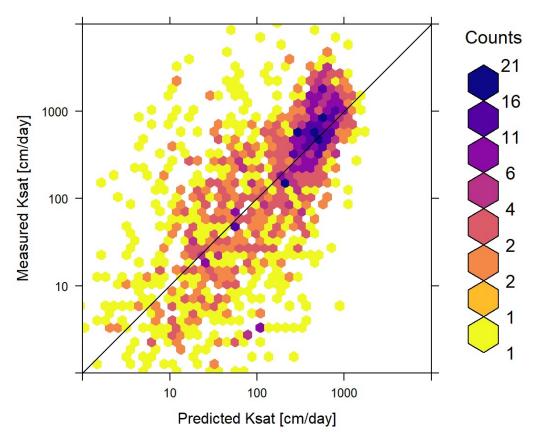
```
##CCC

ccc = DescTools::CCC(holdout$log_ksat, holdout$predict, ci = "z-transform", conf.leve
l = 0.95, na.rm=TRUE)$rho.c

ccc
```

```
## est lwr.ci upr.ci
## 1 0.6399059 0.6138452 0.6645735
```

```
##Transform log10 to normal values
holdout$log10ksat1<- 10^holdout$log_ksat
holdout$response1<- 10^holdout$predict
##Hexbin Plot
hexbinplot(log10ksat1~response1,
           panel = function(x, y, ...){
             panel.hexbinplot(x, y, ...)
                     panel.abline(c(0, 1))
           },
           data = holdout,xlab = "Predicted Ksat [cm/day]", ylab = "Measured Ksat [cm/
day]",cex.axis = 4, aspect="1", xbins=40, colramp = function(n) {viridis (8, alpha =
1, begin = 0, end = 1, direction = -1, option = "C")}, x \lim c(1,10000), y \lim c(1,10000),
           scales=list(
             x = list(log = 10, equispaced.log = FALSE),
             y = list(log = 10, equispaced.log = FALSE)
           ),
           font.lab= 6, cex.labels = 1.2,font.axis = 2,colorcut=c(0,0.01,0.03,0.07,0.1
5,0.25,0.5,0.75,1))
```



#Temperate climate region PTF tested on Tropical dataset

The temperate climate region ksat model was tested on tropical soil samples.

```
##model_tetsed_on_tropical soil samples

Trop = read.csv("E:/maps_tests/All_regions_ksat/Tropical_5_04_2020.csv")

Trop$log_ksat = signif(log10( rowMeans(Trop[,c("ksat_lab","ksat_field")], na.rm=TRUE)
), 4)

soil_temp_clay_trop <- Trop[!is.na(Trop$clay_tot_p),]

soil_temp_clay_bd_trop<- soil_temp_clay_trop[!is.na(soil_temp_clay_trop$db_od),]

##Predction for the testing dataset

soil_temp_clay_bd_trop$ predict<- predict(model_temp_ksat, soil_temp_clay_bd_trop)

##Linear model between predictions and measurements

hh_trop<- lm(log_ksat~ predict, data = soil_temp_clay_bd_trop)

summary(hh_trop)</pre>
```

```
##
## Call:
## lm(formula = log_ksat ~ predict, data = soil_temp_clay_bd_trop)
## Residuals:
      Min
             1Q Median 3Q
##
                                    Max
## -3.7416 -0.3273 0.1847 0.4658 1.7606
## Coefficients:
##
             Estimate Std. Error t value Pr(>|t|)
## (Intercept) 0.96066 0.05921 16.22 <2e-16 ***
## predict 0.60684
                        0.02816 21.55 <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.7498 on 1120 degrees of freedom
## Multiple R-squared: 0.2931, Adjusted R-squared: 0.2924
## F-statistic: 464.3 on 1 and 1120 DF, p-value: < 2.2e-16
```

```
##RMSE

rmse(soil_temp_clay_bd_trop$log_ksat, soil_temp_clay_bd_trop$predict)
```

```
## [1] 0.8348444
```

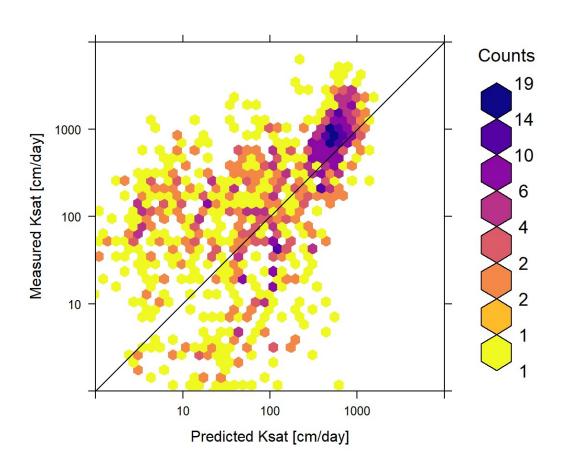
```
##CCC

ccc = DescTools::CCC(soil_temp_clay_bd_trop$log_ksat, soil_temp_clay_bd_trop$predict,
ci = "z-transform", conf.level = 0.95, na.rm=TRUE)$rho.c

ccc
```

```
## est lwr.ci upr.ci
## 1 0.5238328 0.4814777 0.563747
```

```
##Transform log10 to normal values
soil_temp_clay_bd_trop$log10ksat1<- 10^soil_temp_clay_bd_trop$log_ksat</pre>
soil_temp_clay_bd_trop$response1<- 10^soil_temp_clay_bd_trop$predict</pre>
hexbinplot(log10ksat1~response1,
           panel = function(x, y, ...){
             panel.hexbinplot(x, y, ...)
                     panel.abline(c(0, 1))
           },
           data = soil_temp_clay_bd_trop,xlab = "Predicted Ksat [cm/day]", ylab = "Mea
sured Ksat [cm/day]",cex.axis = 4, aspect="1", xbins=40, colramp = function(n) {viridi
s (8, alpha = 1, begin = 0, end = 1, direction = -1,option = "C")},xlim=c(1,10000), y
lim=c(1,10000),
           scales=list(
             x = list(log = 10, equispaced.log = FALSE),
             y = list(log = 10, equispaced.log = FALSE)
           ),
           font.lab= 6, cex.labels = 1.2,font.axis = 2,colorcut=c(0,0.01,0.03,0.07,0.1
5,0.25,0.5,0.75,1))
```



```
##model_built_on_lab measurements

lab = read.csv("E:/maps_tests/All_regions_ksat/lab_5_04_2020.csv")

lab$log_ksat = signif(log10( rowMeans(lab[,c("ksat_lab","ksat_field")], na.rm=TRUE)
), 4)

soil_temp_clay_lab <- lab[!is.na(lab$clay_tot_psa),]

soil_temp_clay_bd_lab<- soil_temp_clay_lab[!is.na(soil_temp_clay_lab$db_od),]

# Randomly split the dataset into training and testing datasets

sample_size = floor(0.80*nrow(soil_temp_clay_bd_lab)))

set.seed(777)

picked = sample(seq_len(nrow(soil_temp_clay_bd_lab)),size = sample_size)

development =soil_temp_clay_bd_lab[picked,]

nrow(development)</pre>
```

```
## [1] 6444
```

```
holdout =soil_temp_clay_bd_lab[-picked,]
nrow(holdout)
```

```
## [1] 1612
```

```
##Fitting MPR model with degree 2
model_lab<- lm(log_ksat ~ poly(db_od,clay_tot_psa, sand_tot_psa, degree=2, raw=TRUE),
data =development )
summary(model_lab)</pre>
```

```
##
## Call:
## lm(formula = log ksat ~ poly(db od, clay tot psa, sand tot psa,
       degree = 2, raw = TRUE), data = development)
##
##
## Residuals:
##
       Min
                1Q Median
                                3Q
                                       Max
  -3.8451 -0.3015 0.0516 0.3752 3.0734
##
## Coefficients:
##
                                                                          Estimate
## (Intercept)
                                                                         1,442e+00
## poly(db_od, clay_tot_psa, sand_tot_psa, degree = 2, raw = TRUE)1.0.0 2.053e+00
## poly(db od, clay tot psa, sand tot psa, degree = 2, raw = TRUE)2.0.0 -1.256e+00
## poly(db_od, clay_tot_psa, sand_tot_psa, degree = 2, raw = TRUE)0.1.0 -5.330e-02
## poly(db_od, clay_tot_psa, sand_tot_psa, degree = 2, raw = TRUE)1.1.0 -5.163e-05
## poly(db_od, clay_tot_psa, sand_tot_psa, degree = 2, raw = TRUE)0.2.0 5.538e-04
## poly(db_od, clay_tot_psa, sand_tot_psa, degree = 2, raw = TRUE)0.0.1 7.985e-03
## poly(db_od, clay_tot_psa, sand_tot_psa, degree = 2, raw = TRUE)1.0.1 -8.052e-04
## poly(db_od, clay_tot_psa, sand_tot_psa, degree = 2, raw = TRUE)0.1.1 4.311e-05
## poly(db_od, clay_tot_psa, sand_tot_psa, degree = 2, raw = TRUE)0.0.2 5.187e-05
##
                                                                        Std. Error
## (Intercept)
                                                                         3.499e-01
## poly(db_od, clay_tot_psa, sand_tot_psa, degree = 2, raw = TRUE)1.0.0 3.719e-01
## poly(db od, clay tot psa, sand tot psa, degree = 2, raw = TRUE)2.0.0 1.416e-01
## poly(db_od, clay_tot_psa, sand_tot_psa, degree = 2, raw = TRUE)0.1.0 8.242e-03
## poly(db_od, clay_tot_psa, sand_tot_psa, degree = 2, raw = TRUE)1.1.0 4.661e-03
## poly(db_od, clay_tot_psa, sand_tot_psa, degree = 2, raw = TRUE)0.2.0 5.839e-05
## poly(db_od, clay_tot_psa, sand_tot_psa, degree = 2, raw = TRUE)0.0.1
                                                                         4.595e-03
## poly(db_od, clay_tot_psa, sand_tot_psa, degree = 2, raw = TRUE)1.0.1
                                                                         2.887e-03
## poly(db_od, clay_tot_psa, sand_tot_psa, degree = 2, raw = TRUE)0.1.1
                                                                         6.710e-05
## poly(db_od, clay_tot_psa, sand_tot_psa, degree = 2, raw = TRUE)0.0.2 3.042e-05
##
                                                                        t value
## (Intercept)
                                                                          4.122
## poly(db_od, clay_tot_psa, sand_tot_psa, degree = 2, raw = TRUE)1.0.0
                                                                          5.521
## poly(db_od, clay_tot_psa, sand_tot_psa, degree = 2, raw = TRUE)2.0.0
                                                                         -8.872
## poly(db_od, clay_tot_psa, sand_tot_psa, degree = 2, raw = TRUE)0.1.0
                                                                         -6.467
## poly(db_od, clay_tot_psa, sand_tot_psa, degree = 2, raw = TRUE)1.1.0
                                                                         -0.011
## poly(db_od, clay_tot_psa, sand_tot_psa, degree = 2, raw = TRUE)0.2.0
                                                                          9.486
## poly(db od, clay tot psa, sand tot psa, degree = 2, raw = TRUE)0.0.1
                                                                          1.738
## poly(db_od, clay_tot_psa, sand_tot_psa, degree = 2, raw = TRUE)1.0.1
                                                                         -0.279
## poly(db_od, clay_tot_psa, sand_tot_psa, degree = 2, raw = TRUE)0.1.1
                                                                          0.642
## poly(db_od, clay_tot_psa, sand_tot_psa, degree = 2, raw = TRUE)0.0.2
                                                                          1.705
                                                                        Pr(>|t|)
## (Intercept)
                                                                        3.81e-05
## poly(db_od, clay_tot_psa, sand_tot_psa, degree = 2, raw = TRUE)1.0.0 3.51e-08
## poly(db_od, clay_tot_psa, sand_tot_psa, degree = 2, raw = TRUE)2.0.0 < 2e-16</pre>
## poly(db_od, clay_tot_psa, sand_tot_psa, degree = 2, raw = TRUE)0.1.0 1.07e-10
```

```
## poly(db od, clay tot psa, sand tot psa, degree = 2, raw = TRUE)1.1.0
                                                                         0.9912
## poly(db_od, clay_tot_psa, sand_tot_psa, degree = 2, raw = TRUE)0.2.0 < 2e-16</pre>
## poly(db od, clay tot psa, sand tot psa, degree = 2, raw = TRUE)0.0.1
                                                                         0.0823
## poly(db_od, clay_tot_psa, sand_tot_psa, degree = 2, raw = TRUE)1.0.1
                                                                         0.7803
## poly(db_od, clay_tot_psa, sand_tot_psa, degree = 2, raw = TRUE)0.1.1
                                                                         0.5206
## poly(db_od, clay_tot_psa, sand_tot_psa, degree = 2, raw = TRUE)0.0.2
                                                                         0.0882
##
## (Intercept)
## poly(db_od, clay_tot_psa, sand_tot_psa, degree = 2, raw = TRUE)1.0.0 ***
## poly(db_od, clay_tot_psa, sand_tot_psa, degree = 2, raw = TRUE)2.0.0 ***
## poly(db od, clay tot psa, sand tot psa, degree = 2, raw = TRUE)0.1.0 ***
## poly(db_od, clay_tot_psa, sand_tot_psa, degree = 2, raw = TRUE)1.1.0
## poly(db_od, clay_tot_psa, sand_tot_psa, degree = 2, raw = TRUE)0.2.0 ***
## poly(db_od, clay_tot_psa, sand_tot_psa, degree = 2, raw = TRUE)0.0.1 .
## poly(db_od, clay_tot_psa, sand_tot_psa, degree = 2, raw = TRUE)1.0.1
## poly(db_od, clay_tot_psa, sand_tot_psa, degree = 2, raw = TRUE)0.1.1
## poly(db_od, clay_tot_psa, sand_tot_psa, degree = 2, raw = TRUE)0.0.2 .
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.6835 on 6433 degrees of freedom
     (1 observation deleted due to missingness)
## Multiple R-squared: 0.5322, Adjusted R-squared: 0.5316
## F-statistic: 813.3 on 9 and 6433 DF, p-value: < 2.2e-16
```

```
##Predction for the testing dataset
holdout$predict<- predict(model_lab, holdout)

##Linear model between predictions and measurements

LM_pre_mea_Lab<- lm(log_ksat~ predict, data = holdout)
summary(LM_pre_mea_Lab)</pre>
```

```
##
## Call:
## lm(formula = log_ksat ~ predict, data = holdout)
## Residuals:
##
      Min
             1Q Median 3Q
                                    Max
## -3.3039 -0.2915 0.0530 0.3711 3.0341
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -0.008271 0.052005 -0.159
## predict 0.996881 0.023202 42.966 <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.6739 on 1610 degrees of freedom
## Multiple R-squared: 0.5342, Adjusted R-squared: 0.5339
## F-statistic: 1846 on 1 and 1610 DF, p-value: < 2.2e-16
```

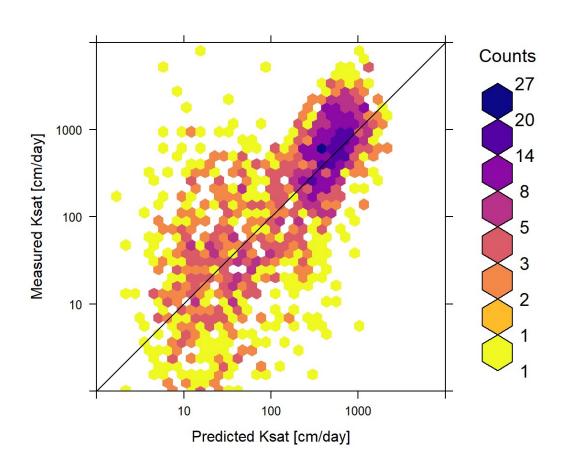
```
rmse(holdout$log_ksat, holdout$predict)
```

```
## [1] 0.673693
```

```
ccc = DescTools::CCC(holdout$log_ksat, holdout$predict, ci = "z-transform", conf.level
= 0.95, na.rm=TRUE)$rho.c
ccc
```

```
## est lwr.ci upr.ci
## 1 0.6969057 0.6733911 0.7190116
```

```
## Transform log 10 to normal values
holdout$log10ksat1<- 10^holdout$log_ksat
holdout$response1<- 10^holdout$predict
hexbinplot(log10ksat1~response1,
           panel = function(x, y, ...){
              panel.hexbinplot(x, y, ...)
                      panel.abline(c(0, 1))
           },
           data = holdout,xlab = "Predicted Ksat [cm/day]", ylab = "Measured Ksat [cm/
day]",cex.axis = 4, aspect="1", xbins=35, colramp = function(n) {viridis (8, alpha =
1, begin = 0, end = 1, direction = -1, option = "C"), x \lim_{t \to \infty} c(1,10000), y \lim_{t \to \infty} c(1,10000),
           scales=list(
             x = list(log = 10, equispaced.log = FALSE),
             y = list(log = 10, equispaced.log = FALSE)
           ),
           font.lab= 6, cex.labels = 1.2,font.axis = 2,colorcut=c(0,0.01,0.03,0.07,0.1
5,0.25,0.5,0.75,1))
```



#Lab ksat PTF tested on field dataset

Here, we applied the same method (MPR) for developing the PTF for Lab measured ksat values. We have followed the same steps as described for temperate region PTFs such as divided the dataset into training (80%) and testing soil samples (20%).

```
##model applied on field measurments
field = read.csv("E:/maps_tests/All_regions_ksat/field_5_04_2020.csv")
field$log_ksat = signif(log10( rowMeans( field[,c("ksat_lab","ksat_field")], na.rm=TR
UE) ), 4)
soil_temp_clay_field<- field[!is.na(field$clay_tot_psa),]
soil_temp_clay_bd_field<- soil_temp_clay_field[!is.na(soil_temp_clay_field$db_od),]
##Predction for the testing dataset
soil_temp_clay_bd_field$ predict<- predict(model_lab, soil_temp_clay_bd_field)
##Linear model between predictions and measurements
LM_pre_mea_field<- lm(log_ksat~ predict, data = soil_temp_clay_bd_field)
summary(LM_pre_mea_field)</pre>
```

```
##
## Call:
## lm(formula = log_ksat ~ predict, data = soil_temp_clay_bd_field)
##
## Residuals:
##
      Min
               1Q Median
                               3Q
                                     Max
## -4.0266 -0.4092 0.0809 0.5778 3.1793
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 1.26338
                          0.06120
                                   20.64
                                           <2e-16 ***
## predict
               0.38553
                          0.03668 10.51
                                           <2e-16 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.9824 on 2394 degrees of freedom
## Multiple R-squared: 0.04411,
                                  Adjusted R-squared: 0.04371
## F-statistic: 110.5 on 1 and 2394 DF, p-value: < 2.2e-16
```

```
##RMSE

rmse(soil_temp_clay_bd_field$log_ksat, soil_temp_clay_bd_field$predict)
```

[1] 1.079013

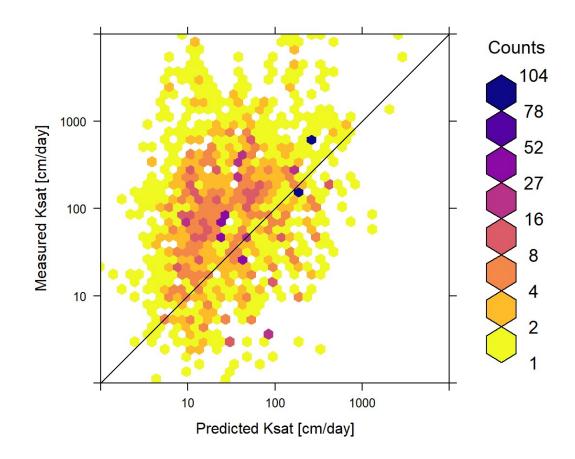
```
##CCC

ccc = DescTools::CCC(soil_temp_clay_bd_field$log_ksat, soil_temp_clay_bd_field$predic
t, ci = "z-transform", conf.level = 0.95, na.rm=TRUE)$rho.c

ccc
```

```
## est lwr.ci upr.ci
## 1 0.1654739 0.1347498 0.1958801
```

```
## Transform log 10 to normal values
soil_temp_clay_bd_field$log10ksat1<- 10^soil_temp_clay_bd_field$log_ksat</pre>
soil_temp_clay_bd_field$response1<- 10^soil_temp_clay_bd_field$predict</pre>
## hexabin plots
hexbinplot(log10ksat1~response1,
           panel = function(x, y, ...){
             panel.hexbinplot(x, y, ...)
                     panel.abline(c(0, 1))
           },
           data = soil_temp_clay_bd_field,xlab = "Predicted Ksat [cm/day]", ylab = "Me
asured Ksat [cm/day]",cex.axis = 4, aspect="1", xbins=35, colramp = function(n) {virid
is (8, alpha = 1, begin = 0, end = 1, direction = -1, option = "C")}, xlim=c(1,10000),
ylim=c(1,10000),
           scales=list(
             x = list(log = 10, equispaced.log = FALSE),
             y = list(log = 10, equispaced.log = FALSE)
           ),
           font.lab= 6, cex.labels = 1.2,font.axis = 2,colorcut=c(0,0.01,0.03,0.07,0.1
5,0.25,0.5,0.75,1))
```



Ksat PTF developed for temperate soil samples using RF

Here, we tried to fit the PTF for temperate soil samples using the random forest algorithm.

```
PTF_temp<-read.csv("E:/maps_tests/All_regions_ksat/Temperate_5_04_2020.csv")
PTF_temp$log_ksat = signif(log10( rowMeans(PTF_temp[,c("ksat_lab","ksat_field")], na.r
m=TRUE)), 4)
soil_ksat3 <- PTF_temp[!is.na(PTF_temp$clay_tot_p),]</pre>
soil_ksat4 <- soil_ksat3[!is.na(soil_ksat3$db_od),]</pre>
## Selecting the list of independent covariates used for developing a model
I.vars = make.names(unique(unlist(sapply(c( "clay_","db_od", "sand_"), function(i){nam
es(soil_ksat4)[grep(i, names(soil_ksat4))]}))))
## Dependent/Target variable
t.vars = c("log_ksat")
sel.n <- c(t.vars,I.vars)</pre>
sel.r <- complete.cases(soil_ksat4[,sel.n])</pre>
PTF_temp2 <- soil_ksat4[sel.r,sel.n]</pre>
## dividing the dataset based on testing and trainning datasets
test.set = seq(3, nrow(PTF_temp2), by = 5)
str(test.set)
```

```
## num [1:1667] 3 8 13 18 23 28 33 38 43 48 ...
```

```
training.set = which(!1:nrow(PTF_temp2) %in% test.set)
str(training.set)
```

```
## int [1:6666] 1 2 4 5 6 7 9 10 11 12 ...
```

```
##Fitting the Random forest algorithm: Ranger
learner = mlr::makeLearner("regr.ranger", mtry =3, num.trees=85)

tsk <- mlr::makeRegrTask(data = PTF_temp2, target = t.vars, blocking = NULL)

m <- mlr::train(learner, tsk,subset = training.set)

##Predction for the testing dataset

p = predict(m, newdata = PTF_temp2[test.set,])

comparison <- p$data

##Linear model between predictions and measurements

gg<- lm(comparison$truth~ comparison$response)

summary(gg)</pre>
```

```
##
## Call:
## lm(formula = comparison$truth ~ comparison$response)
##
## Residuals:
##
      Min 1Q Median
                           3Q
                                  Max
## -3.8981 -0.2560 0.0269 0.3252 2.8672
## Coefficients:
                    Estimate Std. Error t value Pr(>|t|)
##
                    ## (Intercept)
## comparison$response 0.91330 0.02081 43.878 < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.6659 on 1665 degrees of freedom
## Multiple R-squared: 0.5362, Adjusted R-squared: 0.536
## F-statistic: 1925 on 1 and 1665 DF, p-value: < 2.2e-16
```

```
##CCC

ccc = DescTools::CCC(comparison$truth, comparison$response, ci = "z-transform", conf.l
evel = 0.95, na.rm=TRUE)$rho.c

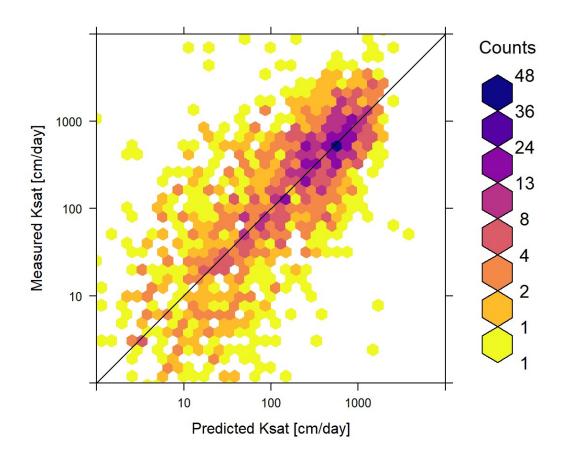
ccc
```

```
## est lwr.ci upr.ci
## 1 0.7147411 0.6916738 0.7363516
```

```
##RMSE
rmse(comparison$truth, comparison$response)
```

[1] 0.6689804

```
##Transform log10 to normal values
comparison$log10ksat1<- 10^comparison$truth</pre>
comparison$response1<- 10^comparison$response</pre>
##Hexbin Plot
hexbinplot(log10ksat1~response1,
           panel = function(x, y, ...){
             panel.hexbinplot(x, y, ...)
                     panel.abline(c(0, 1))
           },
           data =comparison ,xlab = "Predicted Ksat [cm/day]", ylab = "Measured Ksat
[cm/day]",cex.axis = 4, aspect="1", xbins=40, colramp = function(n) {viridis (8, alph
a = 1, begin = 0, end = 1, direction = -1,option = "C")},x \lim c(1,10000), y \lim c(1,10000)
00),
           scales=list(
             x = list(log = 10, equispaced.log = FALSE),
             y = list(log = 10, equispaced.log = FALSE)
           font.lab= 6, cex.labels = 1.2,font.axis = 2,colorcut=c(0,0.01,0.03,0.07,0.1
5,0.25,0.5,0.75,1))
```



Temperate Ksat PTF tested on tropical dataset

PTF developed for the temperate region using RF used to predict the ksat values for tropical soil samples.

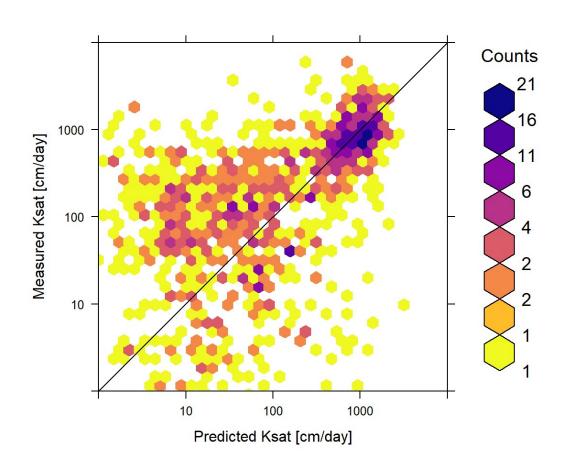
```
Trop = read.csv("E:/maps_tests/All_regions_ksat/Tropical_5_04_2020.csv")
Trop$log10ksat = signif(log10( rowMeans(Trop[,c("ksat_lab","ksat_field")], na.rm=TRU E) ), 4)
soil_temp_clay_trop <- Trop[!is.na(Trop$clay_tot_p),]
soil_temp_clay_bd_trop<- soil_temp_clay_trop[!is.na(soil_temp_clay_trop$db_od),]
##Predction for testing dataset
p = predict(m, newdata = soil_temp_clay_bd_trop)
comparison <- p$data
y<- cbind(comparison, soil_temp_clay_bd_trop)
##CCC
ccc = DescTools::CCC(y$log10ksat, y$response, ci = "z-transform", conf.level = 0.95, na.rm=TRUE)$rho.c
ccc</pre>
```

```
## est lwr.ci upr.ci
## 1 0.5076688 0.4640259 0.5488532
```

```
##RMSE
rmse(y$log10ksat, y$response)
```

```
## [1] 0.9138471
```

```
##Transform log10 to normal values
y$log10ksat1<- 10^y$log10ksat
y$response1<- 10^y$response
hexbinplot(log10ksat1~response1,
           panel = function(x, y, ...){
             panel.hexbinplot(x, y, ...)
                     panel.abline(c(0, 1))
           },
           data =y ,xlab = "Predicted Ksat [cm/day]", ylab = "Measured Ksat [cm/day]",
cex.axis = 4, aspect="1", xbins=40, colramp = function(n) {viridis (8, alpha = 1, beg
in = 0, end = 1, direction = -1, option = "C"), x \lim c(1,10000), y \lim c(1,10000),
           scales=list(
             x = list(log = 10, equispaced.log = FALSE),
             y = list(log = 10, equispaced.log = FALSE)
           ),
           font.lab= 6, cex.labels = 1.2,font.axis = 2,colorcut=c(0,0.01,0.03,0.07,0.1
5,0.25,0.5,0.75,1) )
```



Ksat PTF developed for Lab measurements soil samples using RF

```
PTF_lab<-read.csv("E:/maps_tests/All_regions_ksat/lab_5_04_2020.csv")</pre>
PTF lab$log_ksat = signif(log10( rowMeans(PTF_lab[,c("ksat_lab","ksat_field")], na.rm=
TRUE)), 4)
soil_ksat3 <- PTF_lab[!is.na(PTF_lab$clay_tot_psa),]</pre>
soil_ksat4 <- soil_ksat3[!is.na(soil_ksat3$db_od),]</pre>
## Selecting the list of independent covariates used for developing a model
I.vars = make.names(unique(unlist(sapply(c( "clay_","db_od", "sand_"), function(i){nam
es(soil_ksat4)[grep(i, names(soil_ksat4))]}))))
## Dependent/Target variable
t.vars = c("log_ksat")
sel.n <- c(t.vars,I.vars)</pre>
sel.r <- complete.cases(soil_ksat4[,sel.n])</pre>
PTF_lab2 <- soil_ksat4[sel.r,sel.n]</pre>
## dividing the dataset based on testing and training datasets
test.set = seq(3, nrow(PTF_lab2), by = 5)
str(test.set)
```

```
## num [1:1611] 3 8 13 18 23 28 33 38 43 48 ...
```

```
training.set = which(!1:nrow(PTF_lab2) %in% test.set)
str(training.set)
```

```
## int [1:6444] 1 2 4 5 6 7 9 10 11 12 ...
```

```
##Fitting the Random forest algorithm: Ranger
learner = mlr::makeLearner("regr.ranger", mtry =3, num.trees=85)

tsk <- mlr::makeRegrTask(data = PTF_lab2, target = t.vars, blocking = NULL)# weights = case.weights)

m <- mlr::train(learner, tsk,subset = training.set)

##Predction for testing dataset

p = predict(m, newdata = PTF_lab2[test.set,] )

performance(p)</pre>
```

```
## mse
## 0.4450646
```

```
comparison <- p$data
##Linear model between predictions and measurements
gg<- lm(comparison$truth~ comparison$response)
summary(gg)</pre>
```

```
##
## Call:
## lm(formula = comparison$truth ~ comparison$response)
## Residuals:
      Min
              1Q Median
                            3Q
                                  Max
## -3.3989 -0.2698 0.0459 0.3811 3.0153
##
## Coefficients:
##
                    Estimate Std. Error t value Pr(>|t|)
                     ## (Intercept)
## comparison$response 0.92434 0.02063 44.807 < 2e-16 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.6647 on 1609 degrees of freedom
## Multiple R-squared: 0.5551, Adjusted R-squared: 0.5548
## F-statistic: 2008 on 1 and 1609 DF, p-value: < 2.2e-16
```

```
##CCC

ccc = DescTools::CCC(comparison$truth, comparison$response, ci = "z-transform", conf.l
evel = 0.95, na.rm=TRUE)$rho.c

ccc
```

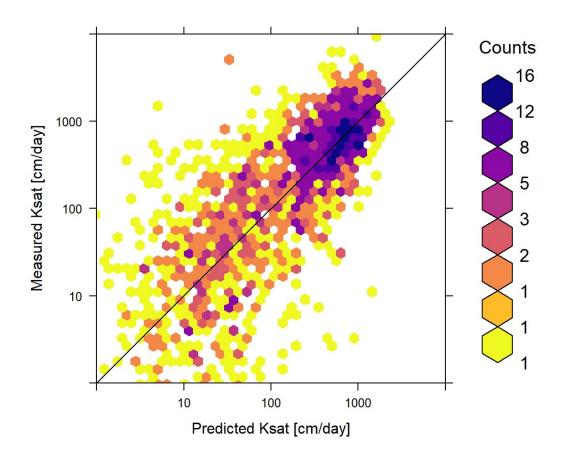
```
## est lwr.ci upr.ci
## 1 0.7280216 0.7054402 0.7491265
```

```
##RMSE

rmse(comparison$truth, comparison$response)
```

```
## [1] 0.6671316
```

```
##Transform log10 to normal values
comparison$log10ksat1<- 10^comparison$truth</pre>
comparison$response1<- 10^comparison$response</pre>
##Hexbin Plot
hexbinplot(log10ksat1~response1,
           panel = function(x, y, ...){
             panel.hexbinplot(x, y, ...)
                     panel.abline(c(0, 1))
           },
           data =comparison ,xlab = "Predicted Ksat [cm/day]", ylab = "Measured Ksat
[cm/day]",cex.axis = 4, aspect="1", xbins=40, colramp = function(n) {viridis (8, alph
a = 1, begin = 0, end = 1, direction = -1,option = "C")},x \lim c(1,10000), y \lim c(1,10000)
00),
           scales=list(
             x = list(log = 10, equispaced.log = FALSE),
             y = list(log = 10, equispaced.log = FALSE)
           ),
           font.lab= 6, cex.labels = 1.2,font.axis = 2,colorcut=c(0,0.01,0.03,0.07,0.1
5,0.25,0.5,0.75,1))
```



Lab PTF tested on field dataset

```
PTF_lab<-read.csv("E:/maps_tests/All_regions_ksat/field_5_04_2020.csv")

PTF_lab$log_ksat = signif(log10( rowMeans(PTF_lab[,c("ksat_lab","ksat_field")], na.rm=
TRUE)), 4)

soil_ksat3 <- PTF_lab[!is.na(PTF_lab$clay_tot_psa),]

soil_ksat4 <- soil_ksat3[!is.na(soil_ksat3$db_od),]

##Prediction for testing dataset

p1 = predict(m, newdata = soil_ksat4)

comparison <- p1$data

##Linear model between predictions and measurements

gg<- lm(comparison$truth~ comparison$response)

summary(gg)</pre>
```

```
##
## Call:
## lm(formula = comparison$truth ~ comparison$response)
## Residuals:
      Min
##
          1Q Median 3Q
                                   Max
## -4.0974 -0.4399 0.1435 0.5993 3.0630
## Coefficients:
                     Estimate Std. Error t value Pr(>|t|)
##
                1.47165 0.05627 26.16 < 2e-16 ***
## (Intercept)
## comparison$response 0.23983 0.03152 7.61 3.92e-14 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.9929 on 2394 degrees of freedom
## Multiple R-squared: 0.02362, Adjusted R-squared: 0.02321
## F-statistic: 57.91 on 1 and 2394 DF, p-value: 3.923e-14
##CCC
```

```
##CCC

ccc = DescTools::CCC(comparison$truth, comparison$response, ci = "z-transform", conf.l
evel = 0.95, na.rm=TRUE)$rho.c

ccc
```

```
## est lwr.ci upr.ci
## 1 0.1355882 0.1007948 0.1700505
```

```
##RMSE
```

rmse(comparison\$truth, comparison\$response)

```
## [1] 1.125453
```

```
##Transform log10 to normal values
comparison$log10ksat1<- 10^comparison$truth</pre>
comparison$response1<- 10^comparison$response</pre>
##Hexbin Plot
hexbinplot(log10ksat1~response1,
           panel = function(x, y, ...){
             panel.hexbinplot(x, y, ...)
                     panel.abline(c(0, 1))
           },
           data =comparison ,xlab = "Predicted Ksat [cm/day]", ylab = "Measured Ksat
[cm/day]",cex.axis = 4, aspect="1", xbins=40, colramp = function(n) {viridis (8, alph
a = 1, begin = 0, end = 1, direction = -1,option = "C")},x \lim c(1,10000), y \lim c(1,10000)
00),
           scales=list(
             x = list(log = 10, equispaced.log = FALSE),
             y = list(log = 10, equispaced.log = FALSE)
           ),
           font.lab= 6, cex.labels = 1.2,font.axis = 2,colorcut=c(0,0.01,0.03,0.07,0.1
5,0.25,0.5,0.75,1))
```

