Output gap estimation using the European Union's Commonly Agreed Methodology

Vade Mecum and Manual for the EUCAM software

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Executive Summary

This discussion paper provides a detailed description of a new, user-friendly, software tool aimed at simplifying the process of calculating potential output and output gap estimates, using the EU's commonly agreed, production function methodology (henceforth referred to as the EUCAM i.e. the <u>EU's Commonly Agreed Methodology</u>). It also acts as a Vade Mecum for EUCAM since in addition to providing a user manual for the software, it also includes a pedagogical summary of the key features of the methodology, as well as a comprehensive description of all the data sources and variables used in the calculations.

In terms of policy use, potential output and output gap estimates are essential for assessing the productive (supply side) capacity and the cyclical (demand side) positions of all of the EU's economies. They are estimated by DG ECFIN, using the transparent EUCAM rules as agreed by the Economic Policy Committee's Output Gap Working Group and the EPC and endorsed by the ECOFIN Council. The estimates are applied in the framework of various economic and fiscal surveillance processes. More specifically, the output gap indicator is used to cyclically adjust the budget balances of the Member States (i.e. to produce their structural budget balances) and the potential output indicator is used for assessing debt sustainability and for comparing EU economies' net government expenditures compared to their potential growth rates (which is used as part of the expenditure benchmark criterion under the preventive arm of the Stability and Growth Pact). In addition, potential output can also be relevant for evaluating the sustainability and effectiveness of different structural reform agendas, aimed at boosting the productive capacity of individual EU countries.

This paper has been written to complement the 2014 paper (Havik et al., 2014) which currently provides the most comprehensive description of the EU's official output gap methodology. To put this new EUCAM software tool and the current paper in their proper context, they are meant to be more practical and user-oriented, focusing only on the essential information needed to compute the different indicators whilst encouraging users to refer to the 2014 paper for a more exhaustive description of the method and of the underlying economic theory.

The EUCAM software is an open source program which has been developed thanks

to the collaboration of DG ECFIN and the Joint Research Centre. Its release is an important step in enhancing the user-friendliness of the EU's output gap estimation methodology. The EUCAM software is used to calculate the official EC output gap and potential output estimates since Spring 2021. It aims at streamlining the estimation of the economic indicators used in the calculations and at making the process more transparent. Regarding the first aim, it provides a common graphical user interface which allows users to control each step of the calculation process. Regarding the transparency goal, the EUCAM software relies entirely on open source technology with publicly released code, allowing outside contributions to be considered in terms of the future development of the software.

EUCAM is available on CIRCABC together with all of the data files (provided via Excel files) and models needed to fully replicate the Commission's latest output gap calculations for each of the EU's Member States, as well as for the euro area and EU aggregates (using the estimates and forecasts for a wide range of economic variables contained in either the Commission's Spring or Autumn forecasting exercises). The EUCAM software integrates the various programmes and data modules, which have steadily grown in number over the years since the inception of the method in 2002, with the result that all of the different components of the calculation process can now be executed via one single graphical user interface. This interface offers a range of user-friendly facilities including menu-driven input options; analytical tools for multicountry analyses; as well as graphical tools for comparisons across countries or vis-à-vis previous data vintages.

In terms of the structure of the paper, following a short introductory section, the paper proceeds to discuss briefly the essential elements of EUCAM by (1) describing the components of its production function approach (i.e. labour, capital and total factor productivity); (2) the way these components are forecasted for the medium-term projections (over a three to five year horizon); (3) and finally describes country specificities that are economically justified exceptions to the methodology. The third section discusses the EUCAM software, starting with the installation process, and moving to operational instructions. This section describes the step-by-step functioning of the software using both screen captures and text to guide the user through the

process. The final section includes a comprehensive overview of the various data sources used in the EUCAM calculations and of the specific data needed for the estimations.

This specific structure has been chosen since one of the main aims of this discussion paper is to demonstrate that EUCAM is not as complex as many commentators have suggested. Consequently, all the requisite elements needed to trace the final output gap results back to the initial data inputs are made available in summary form. This is achieved since, in addition to a description of the user interface and data inputs used for the calculations, the paper also includes the key equations which ultimately determine the output of the methodology and a description of the econometric methodology implemented to estimate the pivotal NAWRU and potential TFP variables. In this way, interested readers / users can discover that EUCAM is not a complex "black-box" but in fact is a relatively simple, rules-based, and 100% transparent methodology where the important data inputs, allied with the key mathematical equations underpinning the methodology, are combined to produce the final potential output and output gap estimates.

Finally, EUCAM should not be seen in static terms since there is a strong likelihood that specific details of the approach will be amended by the EU's Member States in the years to come on the basis of the practical experience garnered from using the methodology in the Commission's various surveillance exercises. As the methodology changes, updated versions of the software and of the current paper will be placed on CIRCABC. The broad structure of the current paper, however, will be retained since it tries to combine the benefits of having a Vade Mecum of the methodology itself, allied to the practicality of a "hands-on" user manual for the software which is used to replicate, in a logical step-by-step process, the potential output and output gap calculations used for EU policy surveillance purposes.

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1 Introduction

The EUCAM software enables the European Union's Commonly Agreed Methodology to estimate potential growth and output gaps. This methodology, which is described in Havik et al. (2014), has been agreed between EU Member States during discussions held at regular meetings of the Output Gap Working Group (OGWG)¹. It relies on the Cobb-Douglas production function; a brief overview is given in Section 2. A user manual to the EUCAM software is provided in Section 3. The software performs all the operations that lead to the output gap and potential growth estimates:

- it prepares all the preliminary data transformations and forecast extensions;
- it applies the Hodrick-Prescott (HP) filter to detrend the participation rate and hours worked;
- it runs Program GAP (Planas and Rossi, 2020) to get potential Total Factor Productivity (TFP) and the Non-Accelerating Wage inflation Rate of Unemployment (NAWRU);
- it puts all the intermediate results together to build the potential growth and output gap estimates;
- and, given medium-term extensions of the working age population and the investment to capital ratio, it elaborates five-year-ahead forecasts of potential growth.

Several facilities like menu-driven inputs, multi-country analysis, and graphical comparisons using another data vintage are offered. The program is open-source and can be downloaded in CIRCABC at

circabc.europa.eu/ui/welcome

following the path Browse categories - European Commission - Economic and Financial Affairs - Output Gaps - Library - PF method - EUCAM software. Users are kindly invited

¹The OGWG members are gratefully acknowledged for their suggestions and software testing.

to read the EU Licence Agreement. The program runs on 64-bit computers equipped with MS Windows 10. Installation is described in Section 3. For application to EU Member States, the official data set currently used by the European Commission is also provided via Excel files. All details about this data set are given in Section 4. Section 5 concludes.

2 Overview of the commonly agreed methodology

For the sake of completeness we give a brief overview of the EUCAM; interested readers can find a more exhaustive description in Havik et al. (2014). Given yearly observations until time T plus additional two-year-ahead forecasts for all input variables that come from the European Commission's Spring and Autumn Economic Forecasts, potential growth and output gap are first estimated until time T+2 as explained in Section 2.1. These results are then used to build medium-term forecasts from T+3 to T+5 using a simultaneous system of equations which is discussed in Section 2.2.

2.1 Potential output and output gap until T+2

The EUCAM assumes that output Y is produced by labour L, capital K, and total factor productivity TFP in a Cobb-Douglas technology as in:

$$Y = TFP L^{\alpha} K^{1-\alpha} \qquad \text{with } \alpha = 0.65$$
 (2.1)

Potential output YPOT is determined by potential total factor productivity POTTFP, potential labour LP, and capital according to:

$$YPOT = POTTFP \ LP^{\alpha} \ K^{1-\alpha} \tag{2.2}$$

The output gap YGAP relates potential to GDP as in:

$$Y = YPOT(1 + YGAP/100) (2.3)$$

where YGAP is given in percentage points. Figure 1 gives an overview of the T+2 methodology, which is reproduced from Havik et al. (2014).

MEASURING POTENTIAL **OUTPUT USING A PRODUCTION FUNCTION APPROACH** COBB-DOUGLAS PRODUCTION FUNCTION Labour Supply (Employment * Hours Worked) Total Factor Productivity (TFP) EXTRACTING THE STRUCTURAL COMPONENT Trend TFP Labour Potential Working Age Population variate Kalman Filter Model Labour Force NAWRU xploits link betwee the TFP cycle & the degree of capacity utilisation) Potential Employment Trend Hours Potential Labour Supply Capital Stock Potential Output

FIGURE 1 Overview of the production function approach

Labour, capital, and TFP are described next.

2.1.1 Labour

Labour is measured in terms of hours as the product of hours worked per employee $hpere_t$ times the number of employees $empl_t$:

$$L_t = hpere_t \times empl_t \tag{2.4}$$

Potential labour LP_t equals the product of the hours worked trend $hperehp_t$ times the employment trend $empl_{p_t}$:

$$LP_t = hperehp_t \times emplp_t \tag{2.5}$$

The trend in hours worked is calculated using the HP filter with an inverse signal to noise ratio λ set equal to 10, after extending the series from T+3 to T+8 using an autoregressive model (see Appendix C & D):

$$heperehp_t = HP(hpere_t, t = 1, \cdots, T + 8, \lambda = 10)$$
 (2.6)

To obtain the employment trend, the total number of employees is first decomposed into the working age population $popw_t$, the participation rate $part_t$, and the rate of employment, or equivalently one minus the harmonized rate of unemployment $1 - lurharm_t/100$:

$$empl_t = popw_t \times (part_t/100) \times (1 - lurharm_t/100)$$
 (2.7)

where both the participation rate and the labour unemployment rate are in %. The potential number of employees verifies:

$$emplp_t = popw_t \times (parts_t/100) \times (1 - nawru_t/100)$$
 (2.8)

where $parts_t$ denotes the trend in participation rate and $nawru_t$ the non-accelerating wage inflation rate of unemployment. The trend in participation rate is calculated using the HP filter with an inverse signal to noise ratio λ set equal to 10, after extending the series from T+3 to T+8 using an autoregressive model:

$$parts_t = HP(part_t, t = 1, \dots, T + 8, \lambda = 10)$$
 (2.9)

where the participation rate is obtained by inverting (2.7).

The trend unemployment rate is calculated as an anchored NAWRU (see Hristov et a., 2017l). In a first step the unemployment rate is decomposed in a trend (i.e. NAWRU) and

a cycle which are assumed to evolve stochastically as in:

$$lurharm_{t} = nawru_{t} + c_{t}$$

$$\Delta nawru_{t} = \eta_{t-1} + a_{nt}$$

$$\eta_{t} = \eta_{t-1} + a_{\eta t}$$

$$c_{t} = \phi_{c1}c_{t-1} + \phi_{c2}c_{t-2} + a_{ct}$$

$$(2.10)$$

where Δ denotes first-difference. The trend component $(nawru_t)$ follows a second-order integrated process without level shocks in all EU Member States, i.e. $V(a_{nt}) = 0$, except for Slovenia for which a random walk without drift is assumed, i.e. $V(a_{\eta t}) = 0$. The cyclical component of unemployment is related to a labour cost indicator w_t through the Phillips curve equation:

$$w_t = \mu_w + \phi_{w1}w_{t-1} + \beta_0 c_t + \beta_1 c_{t-1} + \gamma_w' \Delta^2 z_t + a_{wt}$$
 (2.11)

All shocks a_{nt} , $a_{\eta t}$, a_{ct} , and a_{wt} are independent and normally distributed white noises. The vector $\Delta^2 z_t$ contain the second difference of exogenous variables such as labour productivity, terms-of-trade, and the wage share, whose measurement is explained in Section 4.

The Phillips curve (2.11) is compatible with both backward- and forward-looking expectations: with backward-looking expectations the labour cost indicator corresponds to the change in wage inflation whereas with forward-looking expectations the relevant indicator is the growth of real unit labour cost - see Section 4. No exogenous information is used in the forward-looking Phillips curve. Instead, the forward-looking assumption leads to the restriction $\beta_1 = \beta_0(\phi_{w1} - 0.99)/(0.99\phi_{w1} - 1)\phi_{c2}$, where 0.99 is the assumed discount factor.

Model (2.10)-(2.11) is estimated by maximum likelihood after casting the model equations in a state space format and launching the Kalman recursions from a diffuse initialisation; details can be found in the GAP Manual.

In a second step the NAWRU is corrected to incorporate an anchor S_t to which it is assumed to converge at some horizon T + h under the hypothesis of no-policy change; in

short it is assumed that $nawru_{T+h} = S_{T+h}$, where h is typically equal to ten years. The anchor is built using a panel regression on structural indicators of the labour market (Orlandi, 2012). Smoothing the preliminary estimates given the hypothesis $nawru_{T+h} = S_{T+h}$ yields the anchored NAWRU; details can be found in Hristov, Planas, Roeger, and Rossi (2017).

Plugging the NAWRU estimates together with the working age population and the smoothed participation rate into (2.5) yields potential labour up to T+2.

2.1.2 Capital

The net capital stock is calculated using the Perpetual Inventory Method. Capital stock grows through real gross fixed capital formation IQ and it decreases with the consumption of capital CFC. Given the investment deflator defl and a starting point in 1960, real capital stock K is measured as:

$$K_t = K_{t-1} + IQ_t - \frac{CFC_t}{defl_t}$$

$$\tag{2.12}$$

Two-year-ahead forecasts are provided by the country-desks in DG ECFIN. Capital contributes entirely to potential output and it is not subject to any transformation in the EUCAM.

2.1.3 Total Factor Productivity

TFP is calculated by exponentiating the Solow residual sr_t defined by:

$$sr_t = \log Y_t - \alpha \log L_t - (1 - \alpha) \log K_t \tag{2.13}$$

Two-year-ahead forecasts of the Solow residual are provided by the country-desks in DG ECFIN as part of the European Economic Forecasts. The Solow residual including the two-year-ahead extension is then decomposed into a trend srk_t plus a cycle c_t using the

model:

$$sr_{t} = srk_{t} + c_{t}$$

$$\Delta srk_{t} = \mu_{p} + \eta_{t-1} + a_{pt}$$

$$\eta_{t} = \rho \eta_{t-1} + a_{\eta t}$$

$$c_{t} = 2 A\cos(2\pi/\tau)c_{t-1} - A^{2}c_{t-2} + a_{ct}$$
(2.14)

The trend component srk_t follows a damped trend model with average growth μ_p . The cyclical component c_t follows instead a second-order autoregressive process which is parameterized in terms of amplitude A and periodicity τ . The productivity cycle also appears in the fluctuations of capacity utilization, $cubs_t$, so the model is completed with the measurement equation:

$$cubs_t = \mu_{cu} + \beta_{cu}c_t + e_t$$

$$e_t = \phi_{cu}e_{t-1} + a_{cut}$$
(2.15)

where e_t is an unobserved idiosyncratic component which can be autocorrelated. All shocks, namely a_{pt} , $a_{\eta t}$, a_{ct} , and a_{et} are independent and normally distributed white noises. The cubs indicator is built from capacity utilization surveys in industry and two economic sentiment indicators for construction and services - see Section 4. Contrary to the Solow residual, no T+2 forecasts are available for cubs which ends in time T or sometimes earlier. To cope with this the estimation procedure allows for missing observations.

Model (2.14)-(2.15) is estimated in the Bayesian framework given prior distributions for each EU Member State. Given the prior distributions, the Solow residual, and the capacity utilization series, the trend component srk_t is estimated by its posterior mean in a Bayesian inference as explained in the GAP Manual. The estimate of potential TFP is then obtained as:

$$POTTFP_t = \exp(srk_t) \tag{2.16}$$

Plugging potential TFP (2.16), potential labour (2.5), and capital into (2.2) yields potential GDP up to T+2 together with the output gap.

2.2 Medium-term forecasts: from T+3 to T+5

Potential output and capital are jointly forecast from T+3 to T+5 using the following system of non-linear equations:

$$YPOT_{t} = \exp(srk_{t}) LP_{t}^{\alpha} K_{t}^{1-\alpha}$$

$$K_{t} = IQ_{t} + (1 - \delta_{t}) K_{t-1}$$

$$IQ_{t} = (IYPOT_{t}/100) YPOT_{t}$$

$$Y_{t} = YPOT_{t} (1 + YGAP_{t}/100)$$
(2.17)

Given inputs from srk_t , LP_t , δ_t , $IYPOT_t$, $YGAP_t$, the model above yields medium-term projections for $YPOT_t$, IQ_t , K_t , Y_t , and sr_t , using the recursive method discussed in Juillard (1996). The output gap which is available until T+2 is extended to T+5 by assuming that it closes in three years as in:

$$YGAP_{T+3} = \frac{2}{3}YGAP_{T+2}$$

$$YGAP_{T+4} = \frac{1}{3}YGAP_{T+2}$$

$$YGAP_{T+5} = 0$$
(2.18)

Investment to potential ratio $IYPOT_t$ is extended to T+5 using an autoregressive model. The other inputs are described below.

2.2.1 Labour

Potential labour in (2.5)-(2.8) depends on the working age population, on the trend participation rate, and on the NAWRU. The working age population is available until T+2.

Predictions until T+5 are built using the long-range projections of the 15-74 population by Eurostat (POPAF) as in:

$$popw_t = popw_{t-1} \times \frac{POPAF_{t-1} + POPAF_t}{POPAF_t + POPAF_{t+1}}$$
(2.19)

The NAWRU is extended from T+3 to T+5 according to:

$$nawru_{T+3} = nawru_{T+2} + \frac{1}{2}(nawru_{T+2} - nawru_{T+1})$$

$$nawru_{T+4} = nawru_{T+3}$$

$$nawru_{T+5} = nawru_{T+4}$$

$$(2.20)$$

Both the trend of hours worked per employee in (2.6) and the trend participation rate in (2.9) are available until T+5. Plugging them together with the population forecasts (2.19) and the nawru extension (2.20) into (2.5)-(2.8) yields potential labour until T+5.

2.3 Country specificities

On 4 September 2017, the Economic and Financial Committee approved principles and governance rules for making economically justified country-specific exceptions to the EUCAM. The amendments adopted to date are described below.

2.3.1 Ireland

The capital stock series for Ireland is adjusted in order to correct an anomaly in the national accounts in this country. The anomaly is caused by a relatively small number of firms that relocated intellectual property assets to this country: it happens that the relocations increase capital stock but leave gross fixed capital formation unaffected, thus breaking the Perpetual Inventory formula (2.12). To remedy the issue, the EPC agreed on a first set of adjustments on 20 October 2016. The OGWG suggested further refinements which were adopted by the

EPC on 15 October 2018. Capital stock for Ireland K_t^{IE} is now calculated as follows:

until 2014:
$$K_t^{IE} = K_t$$

2015: $K_t^{IE} = 1.53 \times K_t$
2016: $K_t^{IE} = K_{t-1}^{IE} + IQ_t - \frac{CFC_t}{defl_t}$
2017: $K_t^{IE} = K_{t-1}^{IE} (1 - \delta)$ (2.21)

where K_t is the capital stock obtained from the Perpetual Inventory Method as described in Section 2.1.2, and δ is the implied capital depreciation rate between 2015 and 2016.

2.3.2 Latvia

A measurement issue with the consumption of fixed capital distorts the calculation of the depreciation rate for Latvia. The OGWG proposed to adjust the depreciation rate for Latvia to more closely resemble that of Estonia and Lithuania. The Economic Policy Committee (EPC) endorsed this exception on 23 January 2018. The depreciation rate for Latvia is calculated as the arithmetic mean of depreciation rate of Estonia and Lithuania.

2.3.3 Luxembourg

In Luxembourg, cross-border employment amounts to 40% of total employment, pulling the participation rate (i.e. the ratio of employment to working age population) above 100%. To address this issue, the OGWG agreed to model domestic and cross-border workers separately in the calculation of the participation rate for Luxembourg. The EPC endorsed this exception by January 2018. The measurement of labour in Luxembourg is amended as follows:

$$L_t = empl_t^n \times hpere_t^n + empl_t^{cb} \times hpere_t^{cb}$$

where the superscripts 'n' and 'cb' refer to national and cross-border respectively. Expanding employment in the two groups yields:

$$L_t = popw_t^n \times (part_t^n/100) \times (1 - lurharm_t^n/100) \times hpere_t^n + popw_t^{cb} \times (part_t^{cb}/100) \times (1 - lurharm_t^{cb}/100) \times hpere_t^{cb}$$

Contrary to the national group, for the cross-border workers no information is available on the participation rate, the unemployment rate, and on the pool of working age population. Assuming a participation rate equal to 100% and no unemployment, the cross-border working age population amounts to cross-border employment. Assuming further that the cross-borders work on average the same number of hours as the nationals, total hours worked verifies:

$$L_t = popw_t^n \times (part_t^n/100) \times (1 - lurharm_t^n/100) \times hpere_t + empl_t^{cb} \times hpere_t$$
(2.22)

Equation (2.22) measures labour for Luxembourg. Potential labour is derived similarly, except that the trend of cross-border employment is needed. Rather than calculating trend cross-border employment directly, the trend of the ratio of cross-border employment to total employment is calculated via HP-filtering with inverse signal to noise ratio set equal to 10, after extending the series with forecasts from an ARI(1,1) model. Eventually, potential labour in Luxembourg is obtained by solving:

$$LP_{t} = popw_{t}^{n} \times (parts_{t}^{n}/100) \times (1 - nawru_{t}^{n}/100) \times hperehp_{t}$$

$$+ (\frac{empl_{t}^{cb}}{empl_{t}})_{hp} \times LP_{t}$$

where the number of cross-border workers $empl_t^{cb}$ is measured as the difference between domestic and national employment:

$$empl_t^{cb} = empl_t - empl_t^n$$

= $NETD - NETN$ using AMECO labels. (2.23)

The correction implicitly yields a participation rate equal to 60% in 2017 instead of more than 100% when no distinction is made between national and cross-borders workers.

3 User manual

3.1 Installation

Installation is made by running the self-extracting executable file EUCAMv10setup.exe. By default the program is installed in the folder C:\EUCAMv10 but the users can change the location. Unless a recent version of Matlab such as 2018b is already available on the disk, users are proposed to install Matlab Runtime routines. These routines serve to visualise and to tune the prior distributions for the parameters of the TFP-CU model (2.14)-(2.15). This step can be skipped by simply answering 'No' if the user is not interested in these aspects. Once completed, the installation yields the files and sub-folders shown in Figure 2:

FIGURE 2 EUCAM Main Folder

Name	Date modified	Туре	Size
2020_AUTUMN_F	1/7/2021 9:21 AM	File folder	
2020_SPRING_F	1/7/2021 9:21 AM	File folder	
<mark>□</mark> bin	1/7/2021 9:21 AM	File folder	
<mark></mark> log	1/7/2021 9:21 AM	File folder	
src	1/7/2021 9:21 AM	File folder	
upgrades	1/4/2021 9:13 AM	File folder	
🔁 EU-CAMv10_user_manual.pdf	12/1/2020 9:25 AM	Adobe Acrobat Document	1,390 KB
🔁 GAPv50_user_manual.pdf	12/11/2020 12:48 PM	Adobe Acrobat Document	670 KB
EUCAMv1.xlsm	1/7/2021 9:06 AM	Microsoft Excel Macro-Enabled Worksheet	6,768 KB
EUCAMLicence.txt	1/7/2021 11:28 AM	Text Document	15 KB
GAPLicence.txt	1/7/2021 11:26 AM	Text Document	8 KB

The folder structure in Figure 2 is explained below:

- Year_Season_F: contains the data files, the models, and the results for final version F of data vintage Year in period Season. Season is typically Spring or Autumn, and sometimes Winter. For instance 2020_Spring_F refers to the final version of data vintage Spring 2020.

- bin: contains the Python executable EUCAMv10.exe, the files related to the graphical interface, and the dynamic link library version of Program GAP, gap50dll.dll.
- log: contains log files written during program execution.
- src: contains the Python source code.
- upgrades: EUCAM can be easily updated by importing the latest program files *.bas,
 *.dll, and *.exe that are stored in this folder see subsection 3.2.7 'Upgrades'.

The main folder contains the following files:

- The excel interface EUCAMv10.xlsm.
- The licence agreements EUCAMLicence.txt and GAPLicence.txt that the users are kindly invited to read.
- The EUCAM user-guide and the GAP manual where details about the econometric methodology implemented to estimate the NAWRU and potential TFP can be found.

The software requires that the decimal character is set to a dot as in 1.234 and not as a comma - please check your regional settings following the path Region - Additional Settings in the Windows Control Panel.

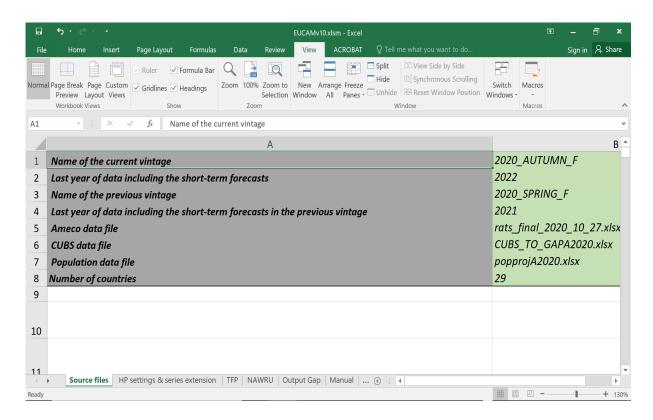
The Excel interface reads and writes namelist files (*.nml) which are given as input to GAP. Each namelist file contains model equations and all necessary statistical information in a human-readable format. To ease reading, it is recommended to associate the *.nml filetype to a preferred text editor. In Windows 10, this can be managed in the Settings area, following the path Default Apps - Choose default apps by file type.

3.2 Getting started: the file EUCAMv10.xlsm

To start the user needs to open the Excel interface EUCAMv10.xlsm. Seven worksheets are available. They are described below.

3.2.1 Worksheet Source

FIGURE 3 EUCAM Worksheet Source



In the worksheet Source, the user can set the:

- Name of the current vintage: the format is Year_Season_F, referring to the Final storage of data in Season typically Spring, Autumn, or Winter of vintage Year. All inputs and outputs related to this vintage are located in the directory named according to this name.
- Last year of data including the short-term forecasts: for instance, 2022 for

vintage Autumn 2020 since it is extended with two years of forecasts.

- Name of the previous vintage: the previous vintage to be used for comparisons, written in the same format as for current vintage. All input and output files related to this vintage are located in the directory named accordingly.
- Last year of data including the short-term forecasts in the previous vintage: for instance, 2021 for vintage Spring 2020 which is extended with two years of forecasts starting from 2019.
- Ameco data file The series in the Ameco data file are described in Section 4. A link to the equations in Section 2 is provided.
- CUBS data The capacity utilization series in the CUBS data file are described in Section 4.
- Population data The series in the Population data file are described in Section 4.

The data files in the last three items must be located in the folder corresponding to the current vintage.

3.2.2 Worksheet HP settings & series extensions

The HP-filter is used to estimate the trend of the participation rate and of hours worked until T+5. The investment to potential output ratio is instead extended to T+5 using autoregressive forecasts. The worksheet is illustrated in Figure 4.

| DCMM dem-fixed | DCMM

FIGURE 4 EUCAM Worksheet HP settings & series extensions

The worksheet is organized as follows:

- Participation rate: the user can set the autoregressive order AR Order, include a Constant or a linear time trend in the model used for forecast three additional years, and select the AR Starting year of the sample used to estimate the parameters.
 The inverse signal to noise ratio Lambda for the HP filter can be inserted in Column F, and select the HP Starting year for computing the filtered estimates.
- Hours worked: the user can set the autoregressive order AR Order, include or not a

Constant, select the AR starting year of the sample used to estimate the parameters, insert the inverse to noise ratio Lambda, and select the HP Starting year for computing the filtered estimates.

- Investment to potential output ratio: the user can set the autoregressive order AR order, include a Constant, and select the AR starting year for model estimation.
- TFP: the user can enter in columns S-X the settings for HP filtering as an alternative to the EUCAM for decomposing TFP.
- NAWRU: the user can enter in columns Z-AD the settings for HP filtering as an alternative to the EUCAM for estimating the NAWRU. This is currently used in the case of IE. The constant used for uncentering the NAWRU as discussed in Section 2.4.2 of Havik et al. (2014) appears in column AE entitled 'Adjustment factor'.

3.2.3 Worksheet TFP

The worksheet TFP sets up the estimation of potential TFP and TFP gap up to T+2.

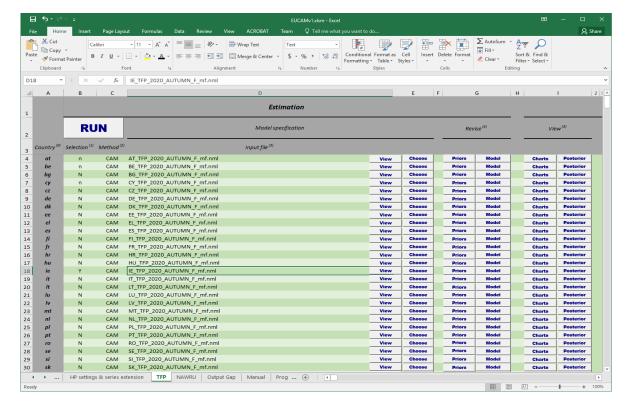


FIGURE 5 EUCAM Worksheet TFP

- Selection: the user can include or exclude a country from the TFP decomposition process by setting Selection = Y or N. If N is selected so that no TFP decomposition is performed, the TFP trend must be provided in an Excel file with the vintage information in its name, for instance tfp_2019_Autumn_F.xls in the format shown in Figure 6, otherwise no output gap calculation can be made for this country.

FIGURE 6 The data file tfp_2019_Autumn_F.xls

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	1965			-7.64749			-7.47719			-7.60882			-6.01914			Ι
Г	1966			-7.5983			-7.45879			-7.58659			-6.01762			
	1967			-7.56748			-7.42768			-7.56844			-5.96499			
T	1968			-7.52418			-7.39385			-7.52397			-5.9116			
	1969			-7.47129			-7.34866			-7.46928			-5.85939			
Т	1970			-7.39877			-7.29837			-7.43823			-5.85551			
Г	1971			-7.37141			-7.27456			-7.41481			-5.82469			
Т	1972			-7.34275			-7.22398			-7.38293			-5.79054			
)	1973			-7.32051			-7.17309			-7.34761			-5.75558			
	1974			-7.33411			-7.14494			-7.32885			-5.76621			
	1975			-7.32266			-7.1584			-7.31614			-5.75314			
,	1976			-7.29294			-7.11417			-7.27805			-5.72024			
	1977			-7.26868			-7.10764			-7.24905			-5.69996			
	1978			-7.26497			-7.08539			-7.22799			-5.68357			
,	1979			-7.24057			-7.07215			-7.20517			-5.65741			
,	1980	-7.24101		-7.24322	-7.03302		-7.03181	-7.214		-7.20437	-5.6552		-5.67029	-7.58059		
1	1981	-7.22919		-7.23086	-7.01977		-7.01992	-7.20118		-7.19959	-5.63765		-5.65618	-7.59473		
Т	1982	-7.2172		-7.21831	-7.00622		-7.00479	-7.18797		-7.20048	-5.61949		-5.62908	-7.60602		
	1983	-7.20496		-7.19372	-6.99237		-6.99852	-7.17384		-7.18035	-5.60119		-5.60476	-7.61637		
Т	1984	-7.19319		-7.19875	-6.97811		-6.98665	-7.15895		-7.15952	-5.5829		-5.57614	-7.62199		
2	1985	-7.1809		-7.18256	-6.96345	-0.02514	-6.97976	-7.14331	-0.00627	-7.14215	-5.56512		-5.55323	-7.62847	-0.0021	
	4000	7 40007		7 40057	0.04004	0.00004	0.00057	7 40000	0.000400	7 42040	E E 4044		5 50040		0.005040	
	EU-	CAMv1.0_2	020_1_F	+						1						

- Method: either CAM or HP.
- Press View to visualise the model file which contains all information about the model specification. For instance AT_TFP_2020_Autumn_F_m0.nml contains a model specification for Austria. The namelist syntax is described in the GAP manual.
- Press Choose to pick a model file located in the vintage folder: The selected file appears in column D.
- Press Priors² to revise the prior distributions. The current model is left unchanged.
 The user is first asked to choose the name of the file which will contain the new

²This facility is available if the user allowed the Matlab Runtime routines to be installed running the program setup.

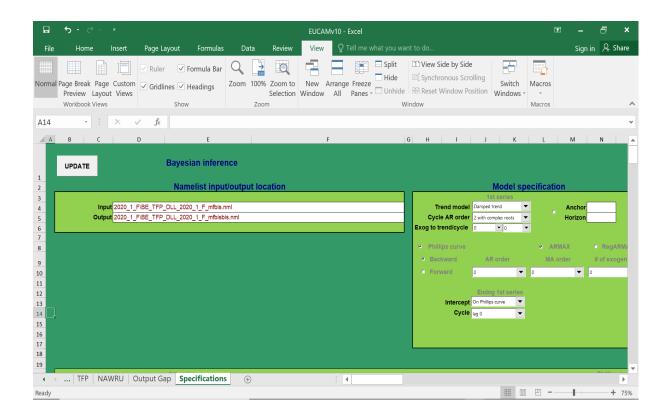
priors. Once entered, an interface where the prior distributions can be tuned through the menu-entry Priors appears as shown in Figure 7. Please notice that the interface can take several minutes to load the first time it is launched. Further details on this interface can be found in the GAP Manual.

FIGURE 7 EUCAM Worksheet TFP - Interface for updating priors



- Press Model to revise the model specification. This action opens the Specifications worksheet. The user can choose a model name, change the model specifications, update the bounds, and save the new model file by pressing Update. The interface for setting priors displayed in Figure 7 opens automatically.

FIGURE 8 EUCAM Worskheet TFP - Interface for updating the model

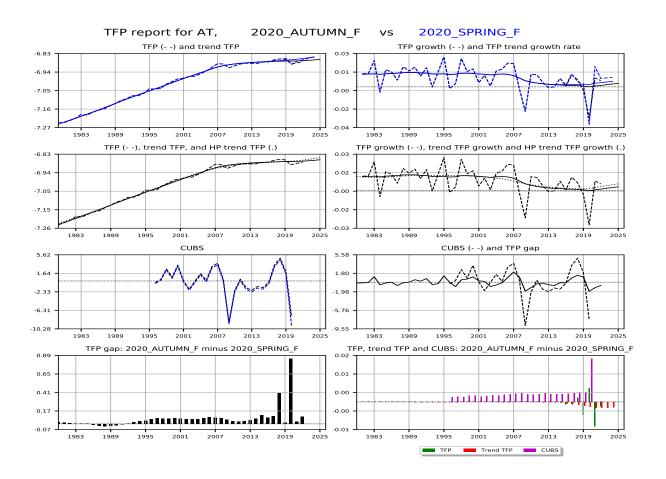


- Press RUN to estimate potential TFP for each country for which estimation is set to 'Y'.
- Press Charts to see graphics. The Chart button opens the file Country_TFP_Vintage_
 Modelname.pdf located in the vintage folder. Eight panels are displayed:
 - the TFP series in the current and previous vintage plus the respective trends;
 - the growth rate of TFP and trend TFP in the current and previous vintage;
 - as above with the addition of the HP trend;
 - the CUBS series together with its cyclical part which is commonly shared with TFP;
 - the revisions to the TFP cycle compared to the previous vintage;

– the revisions to TFP, TFP trend, and CUBS compared to the previous vintage.

The charts focus on the last fourty years. An example is given in Figure 9.

FIGURE 9 EUCAM Worskheet TFP - Charts



```
Statistics for 2020_AUTUMN_F :
Beta coef. = 1.71
Cor. TFP gap/CU : 0.84

Statistics for 2020_SPRING_F :
Beta coef. = 1.6
Cor. TFP gap/CU : 0.8
```

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 Press Posterior to see the posterior distribution of the estimated parameters, together with the relative prior distribution.

3.2.4 Worksheet NAWRU

The worksheet NAWRU controls the NAWRU estimation up to T+2.

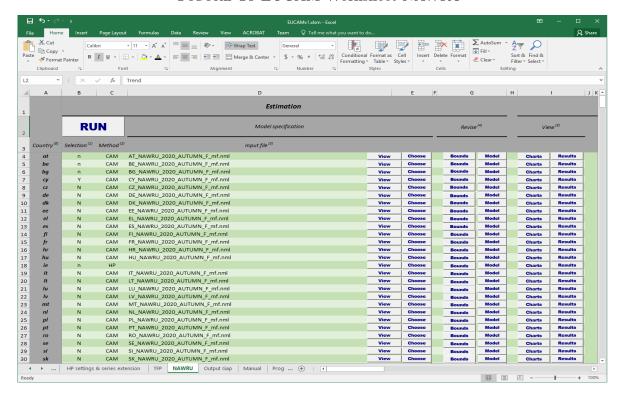
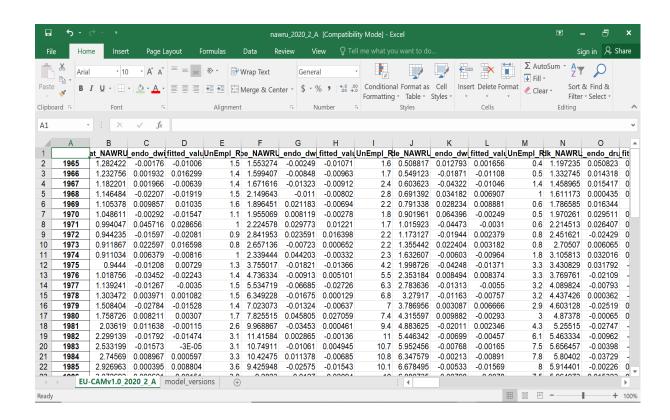


FIGURE 10 EUCAM Worksheet NAWRU

- Selection the user can include or exclude a country from the NAWRU estimation process by setting Selection=Y or N. If N is selected so that no estimation is performed, the NAWRU must be provided in an Excel file with the vintage information in its name, for instance NAWRU_2020_Autumn_F.xls in the format shown in Figure 11, otherwise no output gap calculation can be made for this country.

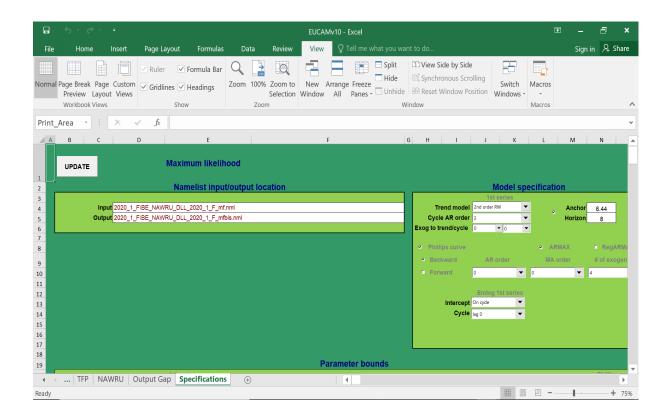
FIGURE 11 The data file NAWRU_2020_Autumn_F.xls



- Method either CAM or HP.
- Press View to visualise the model file which contains all information about the model specification.
- Press Choose to pick a model file located in the vintage folder: for instance AT_NAWRU_
 2020_Autumn_F_mf.nml contains a model specification for Austria. The selected file appears in column D as shown in Figure 10.
- Press Bounds to revise the bounds of the variance parameters see model (2.10)-(2.11).
 Use can be made of the information displayed in columns M-N, P-Q, and S-T, where the current variance bounds are reported. The user is first asked to choose the name of the model file which will contain the new bounds.

- Press Model to revise the model specification. This action opens the "Specifications" worksheet as shown in Figure 12. The user can choose a model name, change the model specifications, and save the new model file by pressing Update.

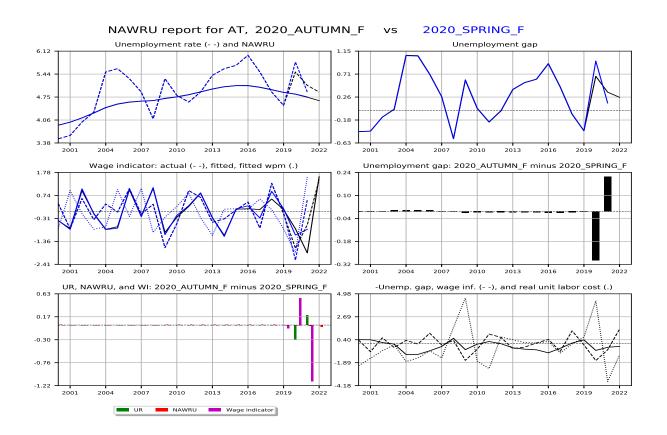
FIGURE 12 EUCAM Worskheet NAWRU - Interface for updating the model



- Press RUN to estimate the NAWRU for each country for which estimation is set to 'Y'.
- Press Charts in column View to see graphics as illustrated in Figure 13. Six panels are displayed:
 - The top-left panel displays the unemployment rate and the NAWRU in the current and previous vintage;
 - The top-right panel shows the unemployment gap in the last two vintages.

- The mid-left panel shows the labour cost indicator in the Phillips curve (2.11), change in wage inflation in the case of AT, together with its 'fitted' component which refers to its explained component, i.e. the component of the labour cost indicator which is common to unemployment. The fitted values obtained by applying the previously used model to the new vintage is also displayed in dots label 'wpm'.
- The mid-right panel shows the revisions to the unemployment gap compared to the previous vintage in the last years.
- The bottom-left panel displays the revisions to the unemployment rate, the NAWRU,
 and the wage indicator compared to the previous vintage in the last years.
- The bottom-right panel shows the unemployment gap times its coefficient ($\beta < 0$) in (2.11) together with the labour cost indicator.

FIGURE 13 EUCAM Worskheet NAWRU - Charts



```
2020_AUTUMN_F : Beta t-stat = -1.47

.LB UB

Slope var. 0.01 0.1

Trend var. 1e-08 0.05

Cycle var. 0.07 0.15

2020_SPRING_F : Beta t-stat = -1.64

.LB UB

Slope var. 0.01 0.1

Trend var. 1e-08 0.05

Cycle var. 0.07 0.15
```

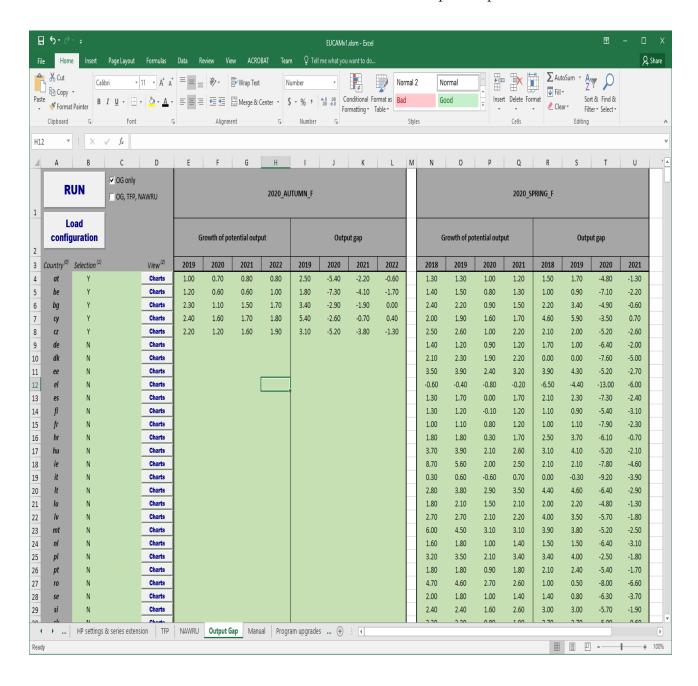
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 Press Results to see the SOL.txt file that contains the maximum likelihood parameter estimates. The estimated value of a selection of parameters is reported from columns L onward.

3.2.5 Worksheet Output Gap

The worksheet Output Gap displays the Potential Growth and Output Gap estimates.

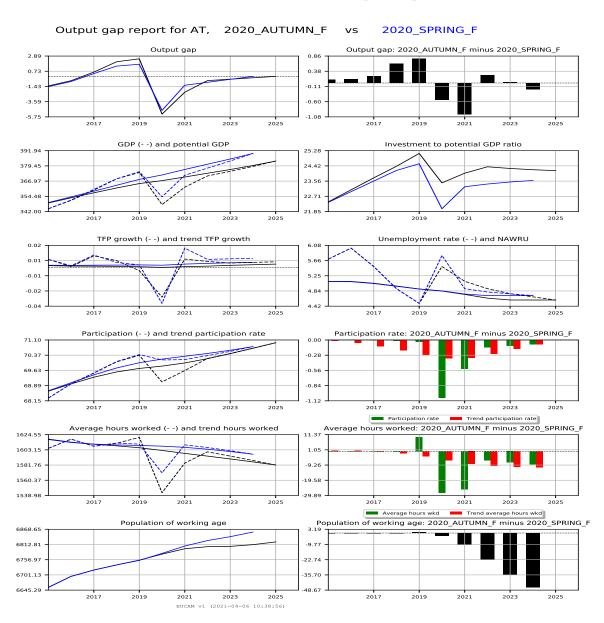
FIGURE 14 EUCAM Worskheet Output Gap



- Press RUN to build the new Output Gap estimates. Depending on which box is ticked, OG only or OG, TFP, NAWRU, also the potential TFP and the NAWRU are recalculated, otherwise used is made of the last estimates. Columns E-H displays potential growth from T-1 to T+2 and columns I-L the respective output gap estimates. Columns N to U reports the values obtained with the previous vintage.
- Press Charts to see graphics as illustrated in Figure 15. Twelve panels are displayed:
 - The first-left panel shows the output gap in the current and previous vintages.
 - The first-right panel shows the revisions in output gap between the current and the previous vintage.
 - The second-left panel shows GDP and potential GDP in the current against the previous vintage.
 - The second-right panel shows investment to potential for the current and previous vintage.
 - The third-left panel displays the current and previous vintages of TFP and trend
 TFP.
 - The third-right panel shows Unemployment and NAWRU in the current against the previous vintage.
 - The fourth-left panel shows the participation rate and its trend in the current and previous vintages.
 - The fourth-right panel shows the revisions in the current vintage of participation rate and trend participation rate.
 - The fifth-left panel shows average hours worked and its trend in the current and previous vintages.
 - The fifth-right panel shows the revisions in the current vintage of hours worked.
 - The sixth-left panel shows population of working age in the current and previous vintages.

- The sixth-right panel shows the revisions in the current current vintage of population of working age.
- Press Load configuration to load the settings saved in a previous work session, for instance with a different data vintage. The configuration is written in the file Configurationfile.nml which contains all the settings introduced in the Excel interface. The program overwrites the file Configurationfile.nml at each execution.

FIGURE 15 EUCAM Worskheet Output Gap - Charts



3.2.6 Worksheet Manual

The worksheet Manual contains the links to open the EUCAM and GAP manuals.

3.2.7 Worksheet Upgrades

The worksheet Upgrades allows users to easily upgrade the EUCAM software. The updated program files upgrades.zip or upgrades.rar must be downloaded from the CIRCA website and written in the folder C:\EUCAM\Upgrades. EUCAM is then updated by simply pressing the button Upgrades (see Figure 16). The new files (with extension *.bas, *.dll, and *.exe) overwrite the existing ones.

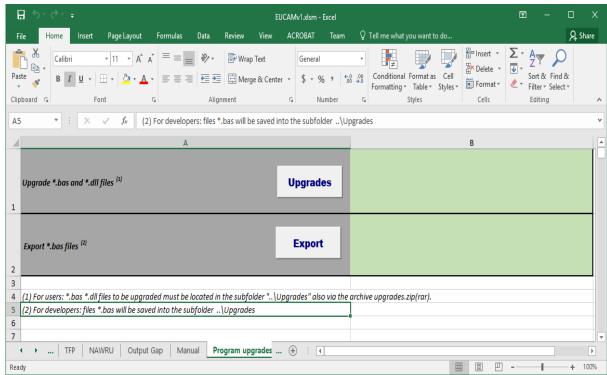


FIGURE 16 EUCAM Worksheet Program upgrades

Conversely, pressing Export saves the Visual Basic routines *.bas that are incorporated in the EUCAM Excel file into the folder C:\EUCAM\Upgrades.

4 Data description

This Section describes the data involved in the EUCAM. Three sources are used: AMECO, the DG ECFIN Business and Consumer surveys, and Eurostat.

4.1 AMECO

Most of the data come from AMECO. The AMECO database collects national accounts data from either the national institutions, Eurostat, or the OECD. The AMECO data are distributed in an Excel file together with EUCAM. A typical AMECO data file is illustrated in Figure 17. Each row starting with the label 'co_x' contains data about variable 'x' in country 'co'. The acronyms used in the data file and their correspondence with AMECO codes are displayed in Table A. Further details can be found in Appendix A.

FIGURE 17 Example of AMECO data file

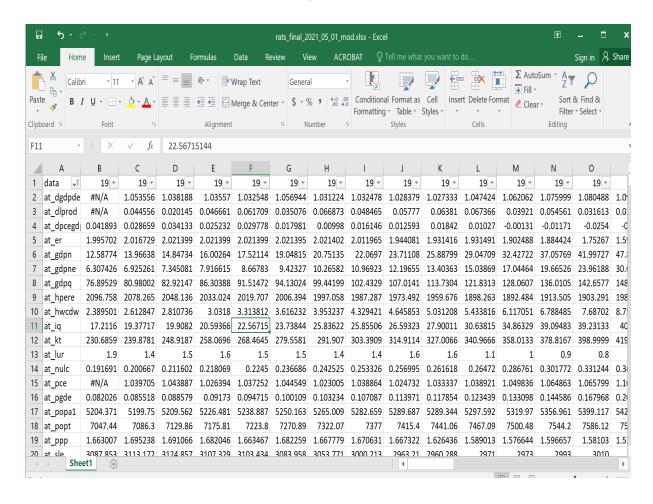


Table A List of variables with correspondences

Name in data file	AMECO	Description	Formula
dgdpdef	PVGD	GDP def. % change	(A3)
dlprod	RVGDE	Change in productivity	(2.11), (A1)
dpcegdp		log(Private consumption def/GDP def)	
er	XNE	Exchange rate	Output data
gdpn	UVGD	Nominal GDP	Output data
gdpne	UVGD	Nominal GDP in euro	Output data
gdpq	OVGD	Real GDP	(2.14)
hpere	NLHA	Hours worked per employee	(2.4), (2.6)
hwcdw	HWCDW	Nominal compensation	(A3)
		per employee	
iq	OIGT	Real gross fixed capital formation	(2.12)
kt	OKND	Capital stock	(2.12)
lur	ZUTN	Harmonised unemployment rate	(2.4), (2.10)
nulc	PLCD	Nominal unit labour cost	
pce dpce	PCPH	Private consumption	(A3)
		expenditure deflator, $\%$ change	(A3)
pgde	PVGD	GDP def. (euro)	Output data
popa1	NPAN1	Working age population (15-74)	(2.4)
popt	NPTD	Total population	Output data
ppp	KNP	Purchasing power parity	Output data
sle	NECN	Employment, civilian	Output data
sle1	NETN	Employment, national	(2.22)
sled	NETD	Employment, domestic	(2.7), (2.22)
winf	HWCDW	Wage inflation	(2.11)
ws	UWCD	Wage share	(2.11)

4.2 CUBS data

The CUBS series which are used to detrend TFP series are distributed in the CUBS file, whose format is illustrated in Figure 18. CUBS is a composite indicator of capacity utilisation calculated using DG ECFIN data from Business and Consumer surveys. A detailed description can be found in Annex 3 of Havik et al. (2014).

CUBS_TO_GAP_S2021.xlsx - Excel Sign in 🔑 Share View ACROBAT Home ∑ AutoSum → AT D - 11 Wrap Text Genera ▼ Fill • €.0 .00 Conditional Format as Cell Insert Delete Format Paste Sort & Find & \$ Clear → Formatting Table Styles Filter - Select -Clipboard 5 Alianment Styles Editina Font Number Cells fx X Spring 2021 С G F Н M NomvSReaCUBS_ST_AT CUBS_ST_BE CUBS_ST_BG CUBS_ST_CY CUBS_ST_CZ CUBS_ST_DE CUBS_ST_DK CUBS_ST_EE CUBS_ST_EL CUBS_ST_EL CUBS_ST_EL CUBS_ST_EL CUBS_ST_EL CUBS_ST_DE CUBS_ST_DE CUBS_ST_EL CUBS_ST_EL CUBS_ST_DE CUB 1 Forecast year 2 1985 Spring 2021 OVG -0.0039 -0.0010 -0.02373 1986 Spring 2021 OVG -0.0282 0.0109 0.0364 4 1987 Spring 2021 OVG -0.0379 0.0014 -0.0012 0.0369 0. 5 1988 Spring 2021 OVG -0.0160 -0.0137 0. 0.0192 0.0157 1989 Spring 2021 0. 6 OVG 0.0102 0.0561 0.0024 0.0600 0. 7 1990 Spring 2021 OVG 0.0195 0.0687 0.0141 0.0473 0. 8 1991 Spring 2021 OVG -0.0016 0.0411 -0.0015 0.0567 9 -0. 1992 Spring 2021 OVG -0.0275 -0.1190 -0.0362-0.0176 0.0524 10 1993 Spring 2021 OVG -0.1444 -0. -0.0593 -0.0942 -0.04150.0305 11 1994 Spring 2021 OVG -0.0251 -0.1075 -0.0324 0.0084 0.0205 -0. 12 1995 Spring 2021 OVG 0.0157 -0.0691 -0.0706 0.0280 0.0279 0.0460 0. 13 1996 Spring 2021 OVG 0.0010 -0.0045 -0.0637 -0.0340 0.0084 0.0071 0.0279 0. 14 1997 Spring 2021 OVG 0.0055 0.0230 -0.0561 -0.0153 0.0274 0.0273 0.0287 0. 15 1998 Spring 2021 OVG 0.0281 0.0461 -0.0870 0.0528 0.0416 0. -0.0159 0.0538 1999 Spring 2021 0. 16 OVG 0.0104 0.0340 -0.1820 -0.0103 0.0417 0.0129 0.0645 2000 Spring 2021 0. 17 OVG 0.0345 0.0473 -0.1481 -0.0220 0.0585 0.0167 0.0923 18 2001 Spring 2021 OVG 0.0009 0.0187 -0.1267 0.0181 -0.0032 0.0207 0.0473 0. 19 2002 Spring 2021 OVG -0.0164 -0.0146 0.1149 0.0374 -0.0614 0.0012 0.0589 -0.0099 0. 20 2003 Snring 2021 OVG -0 0011 -N N193 **0.0358** 0.0274 -0 0358 -0.0066 0.0503 -0.0022 ١ CUBS ST

FIGURE 18 Example of Capacity Utilisation data file

4.3 Population

Two series, namely population of working age POPAF and total population POPTF, are used to extend the population series. The format of the input file is illustrated in Figure 19

while the abbreviations are explained in Table B.

Figure 19 Example of Population data file

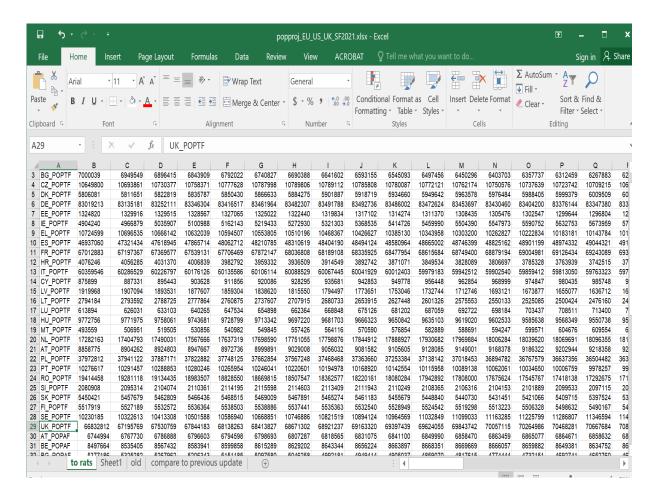


Table B Population variables with correspondences

Name in data file	Eurostat	Description	Formula
POPAF	proj_18np	Projection for working	(2.19)
POPTF	proj_18np	age population (15-74) Projection for total population	(2.19)

5 Conclusion

The EUCAM software implements the methodology commonly agreed between EU Member States to estimate potential growth and the output gap. All operations are integrated in a user-friendly environment which offers several facilities like multi-country analysis and graphical comparisons using another data vintage. The program is open-source and can be downloaded from CIRCABC together with the data files.

Appendix A AMECO data & acronyms

Compensation of employees

- UWCD: total economy.

Note: domestic concept, included are residents as well as non-residents working for resident producer units. Compensation of employees includes wages and salaries and employers' social contributions.

UWCD is used for calculating the labour cost indicator (A2) or (A3) which appears in the Phillips curve (2.11).

Consumption of fixed capital at current prices

- UKCT: total economy.

UKCT is used to measure capital.

Employment (1000 persons)

– NECN: Civilian employment.

Note: Civilian employment is equivalent to civilian labour force NLCN minus total unemployment ZUTN. Civilian employment according to the national concept includes residents who work for resident as well as non-resident producer units.

- NETN: national, total economy.
- NETD: all domestic industries, total economy.

Note: NETD is a domestic concept, included are residents as well as non-residents who work for resident producer units. Employment covers employees and self-employed persons. Annual average.

- FETD = domestic, full time equivalent, total economy.

- NWTD: all domestic industries excluding self-employed workers, total economy.
- FWTD: full-time equivalents; total economy.

NETN is used as number of employees when calculating labour in (2.4).

Gross domestic product at market prices

- UVGD: at current prices, total economy.
- OVGD: at constant prices, total economy.
- PVGD: price deflator calculated as $100 \times \text{UVGD/OVGD}$.

OVGD is used to derive the Solow residual in (2.13) and the output gap in (2.3).

Gross domestic product at market prices per hours worked

- NLHA: Average annual hours worked per person employed.
- NLHT: Total hours worked.

Hours worked per employee is one component of total labour in (2.4).

Gross domestic product at market prices per person employed

- RVGDE is calculated in constant prices either as:

$$RVGDE = 1000 \times OVGD/NETD$$

or $= 1000 \times OVGD/FETD$ (A1)

RVGDE is used for the calculation of real unit labour costs in (A2)-(2.11).

Gross fixed capital formation at constant prices

- OIGT: total economy.

- PIGT: price deflator, total economy.

Net capital stock at constant prices

- OKND: total economy (OKND_{t-1}+OIGT_t-100 × UKCT_t/PIGT_t).

Nominal unit labour cost

- PLCD: total economy.

$$PLCD_t = 100 \times \frac{(UWCD_t/NWTD_t)/(OVGD_t/NETD_t)}{(UWCD_{95}/NWTD_{95})/(OVGD_{95}/NETD_{95})}$$

Nominal compensation per employee

– HWCDW: total economy, equal to either $1000 \times \text{UWCD/NWTD}$ or to $1000 \times \text{UWCD/FWTD}$. HWCDW is involved in the calculation of real unit labour in (A2).

Population

- NPTD: total, annual average.

- NPAN1: 15-74 years.

Working age population helps calculating the participation rate in (2.7).

Private final consumption expenditures

- UCPH: current prices.

- OCPH: constant prices.
- PCPH: Price deflator (100×UCPH/OCPH)

Note: private final consumption expenditure refers to the expenditure on consumption of goods and services of households and non-profit institutions serving households. Goods and services financed by the government and supplied to households as social transfers in kind are not included.

PCPH is used in (A3) to obtain terms-of-trade which is one possible explanatory variable in the backward-looking Phillips curve (2.11).

Real unit labour cost

- The growth rate of real unit labour cost is calculated as:

$$\Delta RULC_t = (HWCDW_t/HWCDW_{t-1} - 1) - \Delta RVGDE_t - (\Delta ZCPIH_t - 1)$$
(A2)

where $ZCPIH_t$ is the harmonized consumer price index.

Real unit labour cost appears as endogenous variable in the forward-looking Phillips curve (2.11).

Terms-of-trade

- Terms-of-trade TOT_t is calculated as the difference between the harmonized consumer price index $ZCPIH_t$ and the GDP deflator $PVGD_t$, i.e. $TOT_t = ZCPIH_t - PVGD_t$. The second-order derivative involved in (2.11) is calculated as:

$$ddtot_{t} = \frac{dpce_{t} - dgdpdef_{t}}{dpce_{t-1} - dgdpdef_{t-1}}$$
(A3)

where $dpce_t$ and $dgdpdef_t$ denote the first-difference of ZCPIH and $PVGD_t$.

Unemployment

- ZUTN: percentage of civilian labour force; Member States, Source: AMECO.
Note: unemployed persons as a share of the labour force (number of people employed and unemployed, see also ESA 95, paragraph 11.21). For unemployed persons see ZUTN.

Unemployment is used to calculate the participation rate and the NAWRU in (2.7) and (2.10).

Wage inflation

- Wage inflation WINF is calculated using net compensation of employees as in:

$$WINF_t = HWCDW_t/HWCDW_{t-1} - 1 \tag{A3}$$

The change in wage inflation is the endogenous variable in the backward-looking wage Phillips curve (2.11).

Appendix B Output files

Tables B1-B3 describe the variables produced in output. Some variables which are not involved in the EUCAM are produced for internal needs. The output files are named for instance like 'EUCAM_output_2021_Spring_F.xls' (Table B1), 'NAWRU_2021_Spring_F.xls' (Table B2), and 'TFP_2021_Spring_F.xls' (Table B3), and can be found in the vintage folder.

Table B1 Variables in main output file

Y gross domestic product

Y_GAP output gap estimated using EUCAM

Y_Pot potential output
Part participation rate

Part_S trend participation rate

wSR growth of TFP

wSR_KF growth of potential TFP

NAWRU non-accelerating wage rate of unemployment

UnEmpl_Rate unemployment rate

HperE hours worked per employee

Investment investment

Pot_LF potential labour force
Pot_Empl potential employment
Pot_Tot_Hrs potential total hours

Empl employment
Tot_Hrs total hours
Capital capital

Wage_Infl wage inflation Civ_Empl civil employment

Pop_WA population of working age

Tot_Pop total population

SR TFP (solow residual)
SR_HP HP filtered TFP
SR_Kf Potential TFP

Depreciation depreciation rate Exchange rate exchange rate

PPS purchase power standard

GDP deflator GDP deflator

Nominal_GDP-e nominal GDP in euro NULC nominal unit labour cost

endo_dwinf wage indicator used in NAWRU estimation

fitted_values fitted wage Phillips curve
CUBS capacity utilisation indicator

hperehp hours worked per employee, HP-trend

whperehp growth of HP-filtered hours worked per employee

Table B2 NAWRU data file

NAWRU	non-accelerating wage inflation rate of unemployment
$endo_dwinf$	wage indicator used in NAWRU estimation
	(first difference of wage inflation)
$endo_drulc$	wage indicator used in NAWRU estimation
	(first difference of real unit labour cost)
$fitted_values$	fitted wage Phillips curve
$UnEmpl_Rate$	unemployment rate

Table B3 TFP data file

cubs	CUBS indicator used to detrend TFP
$fitted_values$	fitted CUBS
cuext	forecasted CUBS
sr	Solow residual
tfpf	forecasted Solow residual
srkf	trend of Solow residual

Appendix C The Hodrick-Prescott filter

The Hodrick-Prescott filter decomposes an observed series x_t into a trend p_t plus an independent noise u_t as in $x_t = p_t + u_t$ by minimising the loss function:

$$\min_{p_1, \dots, p_T} \sum_{t=1}^{T} u_t^2 + \lambda \sum_{t=3}^{T} (\Delta^2 p_t)^2$$

where Δ denotes first-difference and λ is the inverse signal to noise ratio, for instance 1/100 for yearly data (Hodrick and Prescott, 1997). Harvey and Jaeger (1993) show that the HP filter is a minimum mean square error filter for the I(2) plus noise model below which is thus implicit in HP-detrending:

$$x_t = p_t + u_t$$

$$\Delta^2 p_t = a_{pt} \qquad \lambda = V(a_{ut})/V(p_t)$$

Appendix D The autoregressive model

In order to mitigate end effects, the HP-filter is applied on series extended with forecasts. These forecasts are obtained fitting an autoregressive model such as:

$$x_t = \mu + \gamma_1 x_{t-1} + \dots + \gamma_p x_{t-p} + e_t$$

where e_t is a white noise. The coefficients are estimated by least-squares given the first p observations.

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