

Correlation

Cross Correlation

Auto Correlation

Circular Correlation

▢ Cross correlation:

$$X(n) = \{1, 1, 2, 2\}, \quad Y(n) = \{1, 3, 1\}$$

First step:

$$Y(-n) = \{1, 3, 1\}$$

$$Y(-n) \rightarrow$$

		1	3	1
1	1	1	3	1
1	1	1	3	1
2	2	2	6	2
2	2	2	6	2

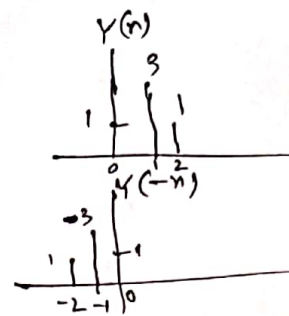
$$\rightarrow 1, 4, 6, 9, 8, 2$$

$$\{1, 4, 6, 9, 8, 2\}$$

$$\text{Highest} = +3$$

$$\text{Lowest} = -2$$

$$\therefore r_{xy} = \{1, 4, 6, 9, 8, 2\} \quad \underline{\text{Ans}}$$



▢ Auto correlation:

$$X(n) = \{1, 2, 3, 4\}$$

$$\therefore X(-n) = \{4, 3, 2, 1\}$$

$$X(-n) \rightarrow$$

		4	3	2	1
1	1	4	3	2	1
2	2	8	6	4	2
3	3	12	9	6	3
4	4	16	12	8	4

$$\{4, 11, 20, 30, 20, 11, 4\}$$

$$\text{Highest} = +3$$

$$\text{Lowest} = -3$$

$$\therefore r_{xx} = \{4, 11, 20, 30, 20, 11, 4\} \quad \underline{\text{Ans}}$$

▢ Circular Correlation:

$$X(n) = \{1, 1, 2, 1\}, \quad Y(n) = \{2, 3, 1, 1\}$$

$$\overline{r}_{xy} = \begin{bmatrix} 2 & 3 & 1 & 1 \\ 1 & 2 & 3 & 1 \\ 1 & 1 & 2 & 3 \\ 3 & 1 & 1 & 2 \end{bmatrix} \begin{bmatrix} 1 \\ 1 \\ 2 \\ 1 \end{bmatrix} = \begin{bmatrix} 8 \\ 10 \\ 9 \\ 8 \end{bmatrix}$$

$$\overline{r}_{xy} = \{8, 10, 9, 8\}$$