INTRO TO DATA SCIENCE LECTURE 9: DECISION TREE CLASSIFIERS

I. DECISION TREES
II. BUILDING DECISION TREES
III. OPTIMIZATION FUNCTIONS
IV. PREVENTING OVERFITTING

EXERCISE:

V. IMPLEMENTING DECISION TREES WITH SCIKIT-LEARN

I. DECISION TREES

Q: What is a decision tree?

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DECISION TREE CLASSIFIERS

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non-parametric: no parameters, no distribution assumptions

hierarchical: consists of a sequence of questions which yield a class label when applied to any record

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- A: Using a configuration of nodes and edges.

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In a decision tree, the nodes represent questions (test conditions) and the edges are the answers to these questions.

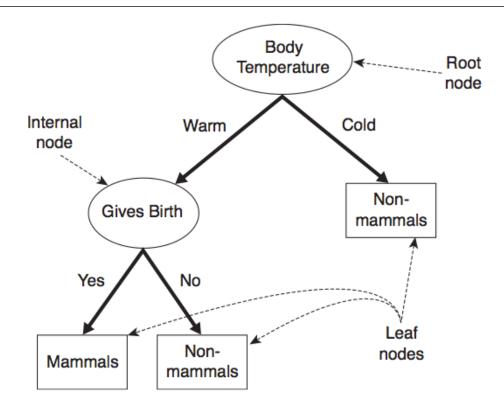


Figure 4.4. A decision tree for the mammal classification problem.

source: http://www-users.cs.umn.edu/~kumar/dmbook/ch4.pdf

TYPES OF NODES

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NOTE

The nodes in our tree are connected by directed edges.

These directed edges lead from parent nodes to child nodes.

Table 4.1. The vertebrate data set.

Name	Body	Skin	Gives	Aquatic	Aerial	Has	Hiber-	Class
	Temperature	Cover	Birth	Creature	Creature	Legs	nates	Label
human	warm-blooded	hair	yes	no	no	yes	no	mammal
python	cold-blooded	scales	no	no	no	no	yes	reptile
salmon	cold-blooded	scales	no	yes	no	no	no	fish
whale	warm-blooded	hair	yes	yes	no	no	no	mammal
frog	cold-blooded	none	no	semi	no	yes	yes	amphibian
komodo	cold-blooded	scales	no	no	no	yes	no	reptile
dragon								
bat	warm-blooded	hair	yes	no	yes	yes	yes	mammal
pigeon	warm-blooded	feathers	no	no	yes	yes	no	bird
cat	warm-blooded	fur	yes	no	no	yes	no	mammal
leopard	cold-blooded	scales	yes	yes	no	no	no	fish
shark								
turtle	cold-blooded	scales	no	semi	no	yes	no	reptile
penguin	warm-blooded	feathers	no	semi	no	yes	no	bird
porcupine	warm-blooded	quills	yes	no	no	yes	yes	mammal
eel	cold-blooded	scales	no	yes	no	no	no	fish
salamander	cold-blooded	none	no	semi	no	yes	yes	amphibian

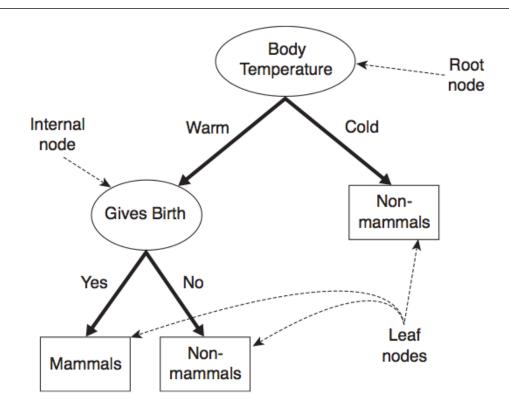


Figure 4.4. A decision tree for the mammal classification problem.

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NOTE

Internal nodes

represent test

at that node.

conditions which

partition the records

EXAMPLE — DECISION TREE

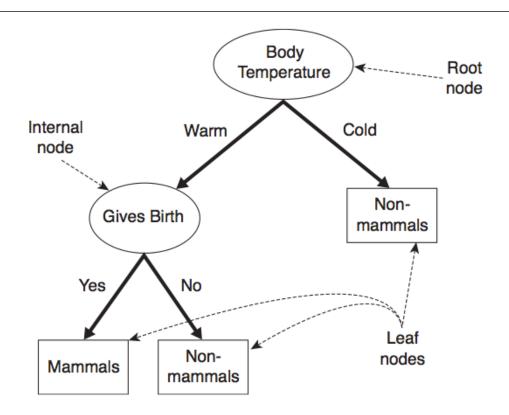


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II. BUILDING DECISION TREES

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But this is generally too complex to be practical $\rightarrow 0(2^n)$.

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A: Use a heuristic algorithm.

The basic method used to build (or "grow") a decision tree is **Hunt's** algorithm.

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greedy — algorithm makes locally optimal decision at each step recursive — splits task into subtasks, solves each the same way local optimum — solution for a given neighborhood of points

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The partitioning decision is made at each node according to a metric called purity.

A partition is 100% pure when all of its records belong to a single class.

1) If all records in D_t belong to class X, then t is a leaf node corresponding to class X.

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NOTE

This is the base case for the recursive algorithm.

2) If D_t contains records from both classes, then a test condition is created to partition the records further. In this case, t is an internal node whose outgoing edges correspond to the possible outcomes of this test condition.

Consider a binary classification problem with classes X, Y. Given a set of records D_t at node t, Hunt's algorithm proceeds as follows:

2) If D_t contains records from both classes, then a test condition is created to partition the records further. In this case, t is an internal node whose outgoing edges correspond to the possible outcomes of this test condition.

These outgoing edges terminate in **child nodes**. A record d in D_t is assigned to one of these child nodes based on the outcome of the test condition applied to d.

3) These steps are then recursively applied to each child node.

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NOTE

Decision trees are easy to interpret, but the algorithms to create them are a bit complicated.

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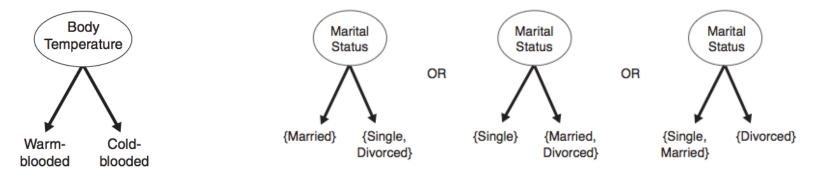
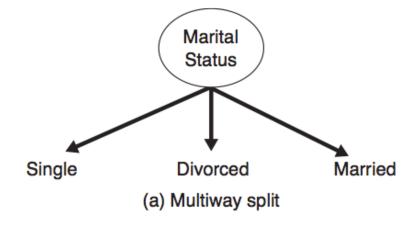


Figure 4.8. Test condition for binary attributes.

(b) Binary split {by grouping attribute values}

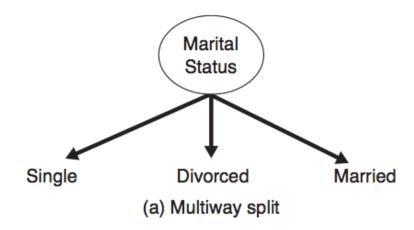
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NOTE

Multiway splits can produce purer subsets, but may lead to overfitting!

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For continuous features, we can use either method:

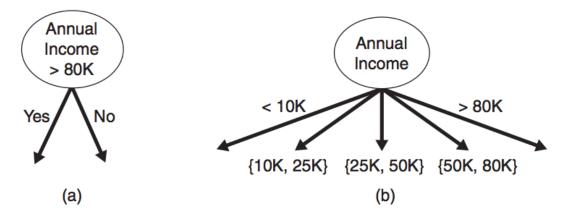


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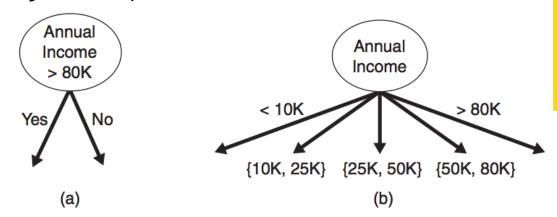


Figure 4.11. Test condition for continuous attributes.

NOTE

There are optimizations that can improve the naïve quadratic complexity of determining the optimum split point for continuous attributes.

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Therefore we want each step to create the partition with the highest possible purity.

We need an objective function to optimize!

III. OPTIMIZATION FUNCTIONS

OBJECTIVE FUNCTIONS

We want our objective function to measure the gain in purity from a particular split.

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E.G. the fraction of records labeled i at node t

OBJECTIVE FUNCTIONS

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The maximum purity partition is given (eg) by the distribution: p(0|t) = 1 - p(1|t) = 1

Some measures of impurity include:

Entropy(t) =
$$-\sum_{i=0} p(i|t) \log_2 p(i|t)$$
,

c-1

Gini(t) =
$$1 - \sum_{i=0}^{c-1} [p(i|t)]^2$$
,

Classification error(t) = $1 - \max_{i}[p(i|t)],$

Note that each measure achieves its max at 0.5, min at 0 & 1.

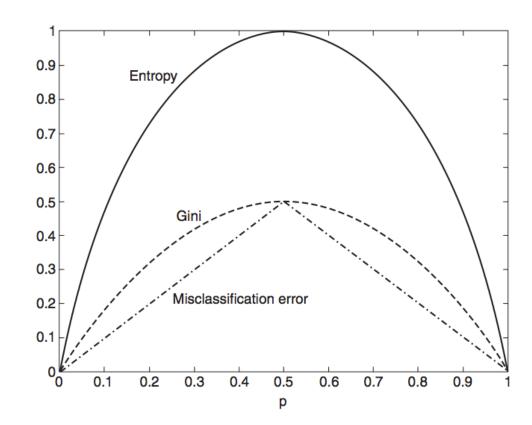


Figure 4.13. Comparison among the impurity measures for binary classification problems.

Note that each measure achieves its max at 0.5, min at 0 & 1.

NOTE

Despite consistency, different measures may create different splits.

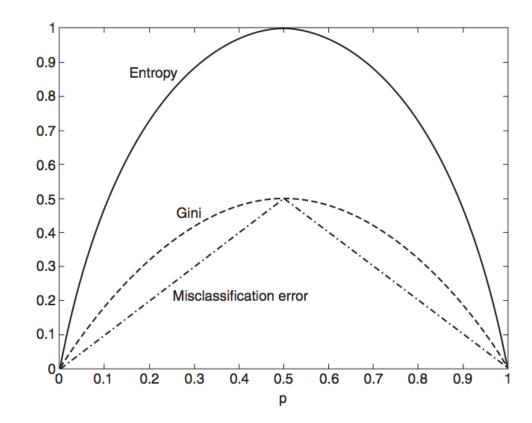


Figure 4.13. Comparison among the impurity measures for binary classification problems.

Impurity measures put us on the right track, but on their own they are not enough to tell us how our split will do.

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Q: Why is this true?

OBJECTIVE FUNCTIONS

Impurity measures put us on the right track, but on their own they are not enough to tell us how our split will do.

Q: Why is this true?

A: We still need to look at impurity before & after the split.

We can make this comparison using the gain:

$$\Delta = I(\text{parent}) - \sum_{\text{children } j} \frac{N_j}{N} I(\text{child } j)$$

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When I is the entropy, this quantity is called the information gain.

OBJECTIVE FUNCTIONS

Generally speaking, a test condition with a high number of outcomes can lead to overfitting (ex: a split with one outcome per record).

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One way of dealing with this is to restrict the algorithm to binary splits only.

Another way is to use a splitting criterion which explicitly penalizes the number of outcomes.

We can use a function of the information gain called the gain ratio to explicitly penalize high numbers of outcomes:

gain ratio =
$$\frac{\Delta_{info}}{-\sum p(v_i)log_2p(v_i)}$$

(Where $p(v_i)$ refers to the probability of label i at node v)

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regularization!

This is a form of

NOTE

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IV. PREVENTING OVERFITTING

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This is correct in principle, but would likely lead to overfitting.

PREVENTING OVERFITTING

One possibility is **pre-pruning**, which involves setting a minimum threshold on the gain, and stopping when no split achieves a gain above this threshold.

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This prevents overfitting, but is difficult to calibrate in practice (may preserve bias!)

Alternatively we could build the full tree, and then perform pruning as a post-processing step.

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To prune a tree, we examine the nodes from the bottom-up and simplify pieces of the tree (according to some criteria).

PREVENTING OVERFITTING

Complicated subtrees can be replaced either with a single node, or with a simpler (child) subtree.

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The first approach is called subtree replacement, and the second is subtree raising.

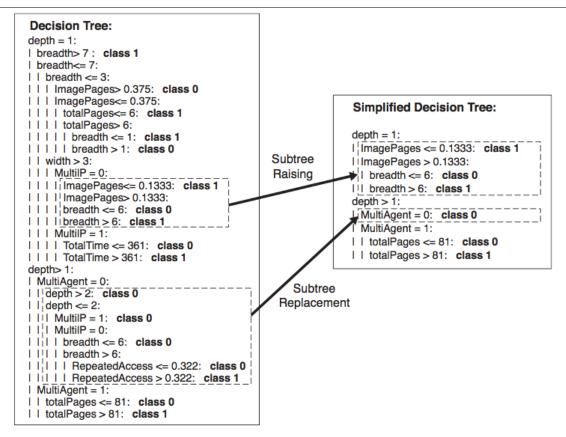


Figure 4.29. Post-pruning of the decision tree for Web robot detection.

EX: DECISION TREES IN PYTHON

V. RANDOM FORESTS

1) Select a sample of the original training set and build a tree as follows:

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- 2) Repeat (1) for N iterations
- 3) Predict based on majority vote of N trees

INTRO TO DATA SCIENCE

DISCUSSION