

CALIFORNIA STATE UNIVERSITY, NORTHRIDGE

Survey of Imperative Style Turing Complete proof techniques
and an application to prove Proteus Turing Complete

A thesis submitted in partial fulfillment of the requirements
for the degree of Master of Science in
Computer Science

By

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1 Acknowledgements

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2 List of Figures

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3 List of Tables

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4 List of Illustrations

This list must reference the figure/table/illustration, page it appears, and subject matter.

5 Abstract

Abstract which will cover the contents of the entire paper in less than 350 words or so. 1.5 pgs
double spaced

state research problem briefly describe methods and procedures used in gathering data or studying the problem give a condensed summary of the findings of the study

6 Introduction

Background on the topic

6.1 Turing Machines

What is a TM?

6.2 Turing Complete

What does TC mean?

How is it different from TMs?

6.2.1 Example of Turing Complete Systems

Link some funny/interesting examples of TC that have been proven.

7 Different Proof Techniques for demonstrating Turing Completeness

7.1 Turing Complete Proofs Overview

All proofs are equivalent in goal. The difference lies in their usability for specific domains.

7.2 Computer Engineering

7.2.1 Gates & Wiring

NOR, ADDER, OR, NOT gates

7.3 Computer Science

7.3.1 State Machines

Formal Technical Writing

$\lambda\gamma\tau$ etc. being used to describe TC

Gamified Writing

$\lambda\gamma\tau$ etc. being used to describe TC, but based on a very verbose and interactive style

7.3.2 Software Implementation

Demonstrate an example of a problem/scenario which shows TC.

Conway's Game of Life

Classic example to implement

Rule 110

Simpler example to implement

Calculator with Store Value

More challenging to implement than the previous two.

7.3.3 Interpreter for TC lang

Implement an interpreter for a known TC language in a given language.

Brainfuck

Describe Brainfuck

C

Is C TC?

Show how this

7.4 Mathematics

7.4.1 Lambda Calculus

Whatever the fuck this is, is TC

8 Proteus is Turing Complete

This section will describe how we will construct 1+ proofs for showing that Proteus is TC.

8.1 The Proteus Grammar

List out the grammar and describe how it can be read, line by line. Probably have a small example of a program that shows most of (maybe all) of the functionality with Proteus

8.2 Initial Thoughts based off of the grammar

List out some ideas that led to the idea that Proteus could be TC

8.3 Proof Outline

Theorems that would be used Steps for proof outline

8.4 Proof v1

Formal proof that follows the outline

8.5 Implementing Rule 110

Implementation of Rule 110 that is a demonstration of TC.

9 Conclusion

Succinctly describe what was the several techniques. Compare and constrast them? Perhaps a discussion section?

References

- [1] Baker, N. 1966, in *Stellar Evolution*, ed. R. F. Stein & A. G. W. Cameron (Plenum, New York)

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