

Abstract Interpretation

Software Quality Assurance - Static Code Analysis, II | Florian Sihler | December 9, 2024

The Why

```
public static void main(String[] args) {  
    int a = 1;  
    double r = Math.random() * 10;  
    if (r > 5) {  
        a = 2;  
    }  
    System.out.println(a);  
}
```

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public static void main(String[] args) {  
    int a = 1; { a ∈ {1} }  
    double r = Math.random() * 10;  
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The Why

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public static void main(String[] args) {  
    int a = 1;           { a ∈ {1} }  
    double r = Math.random() * 10; { r ∈ [0..10) }  
    if (r > 5) {  
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        a = 2;           { a ∈ {2} }  
    }  
    System.out.println(a); { a ∈ {1,2} }  
}
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The Why

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public static void main(String[] args) {  
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- We want to proof, that a program satisfies certain properties

Origins

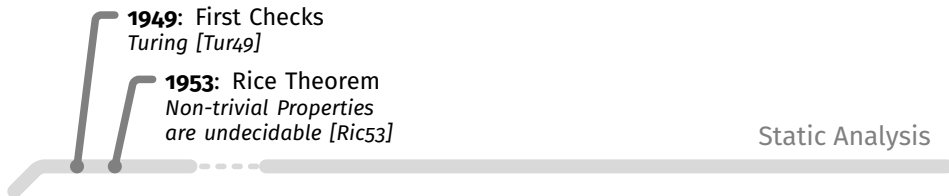
Static Analysis

A horizontal line with a bracket on the left and a dashed segment in the middle.

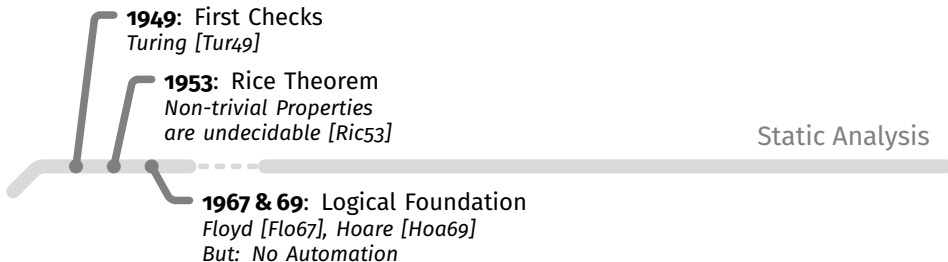
Origins



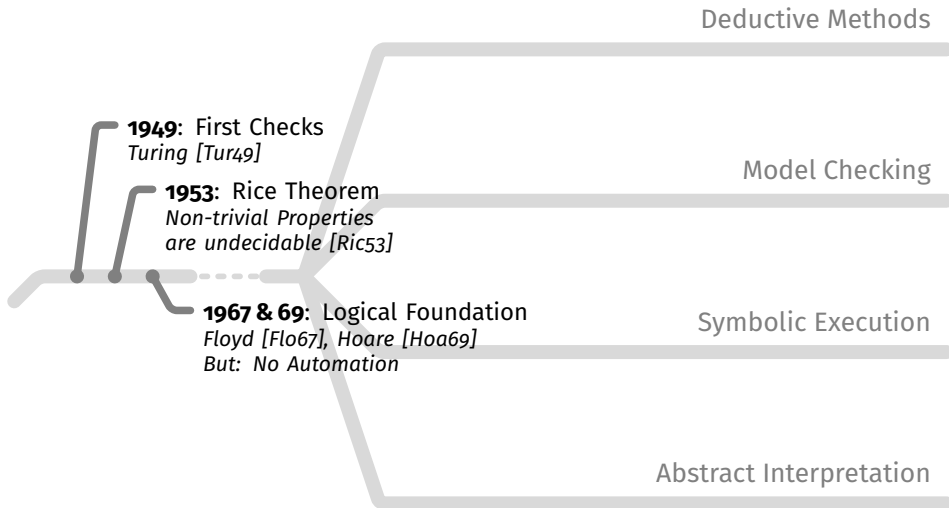
Origins



Origins

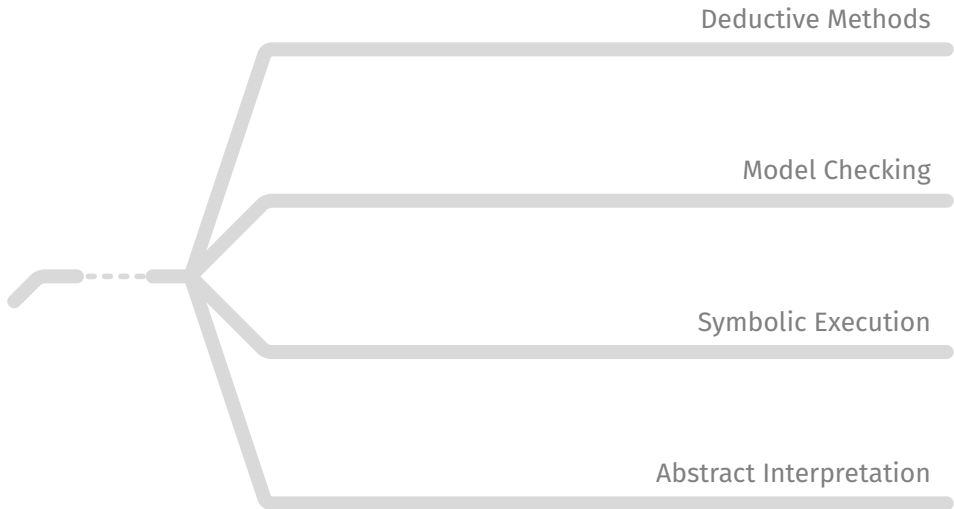


Origins



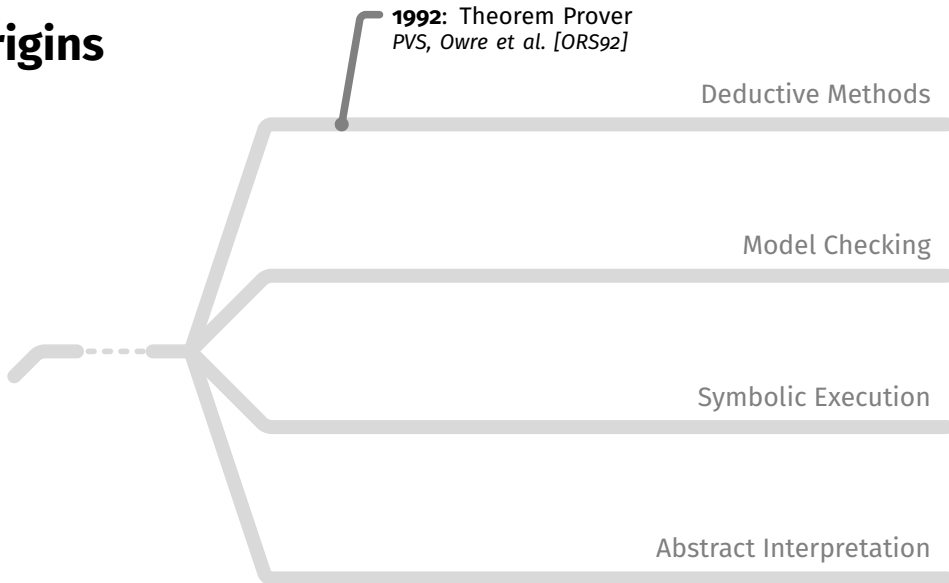
Based on the amazing "Tutorial on Static Inference of Numeric Invariants by Abstract Interpretation" by Miné [Min17] and <https://www.di.ens.fr/~cousot/AI/>

Origins



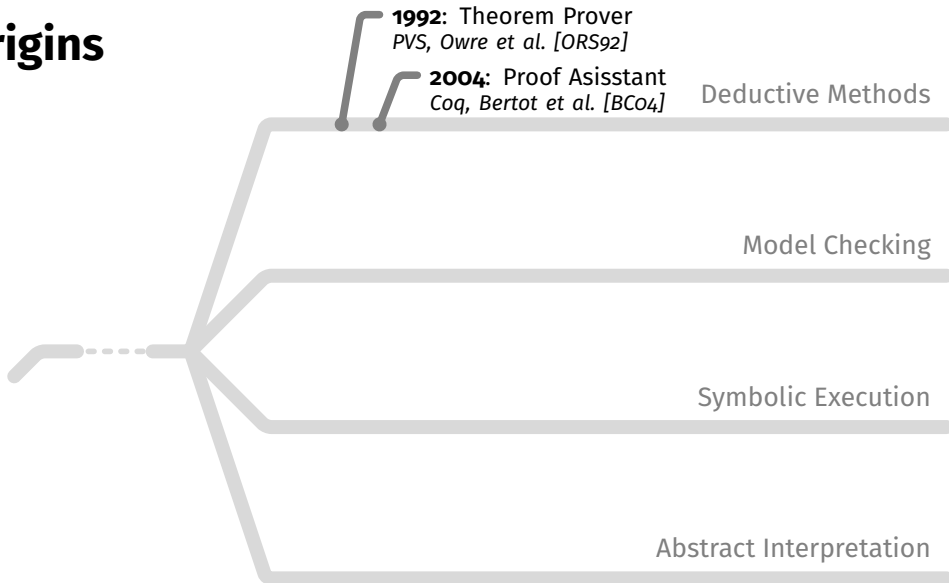
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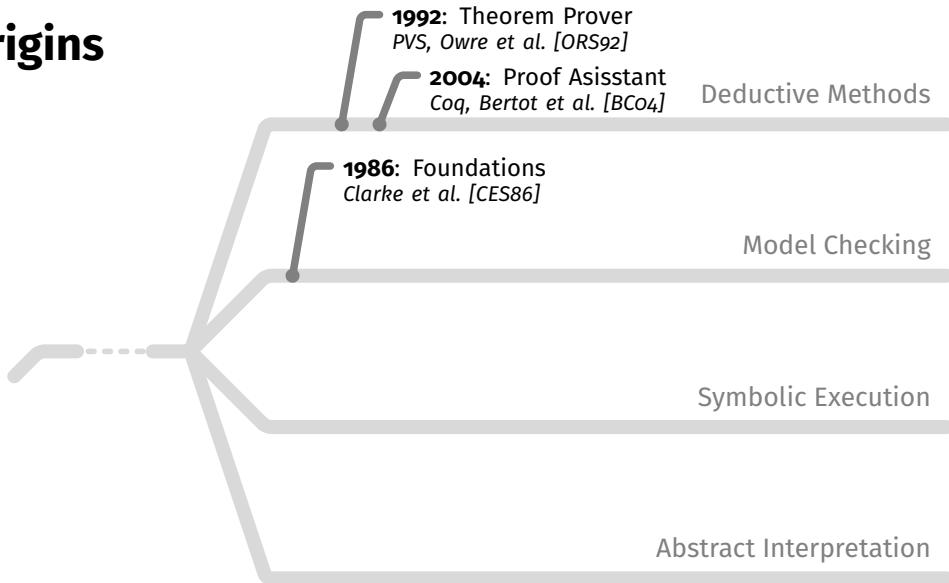
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Origins



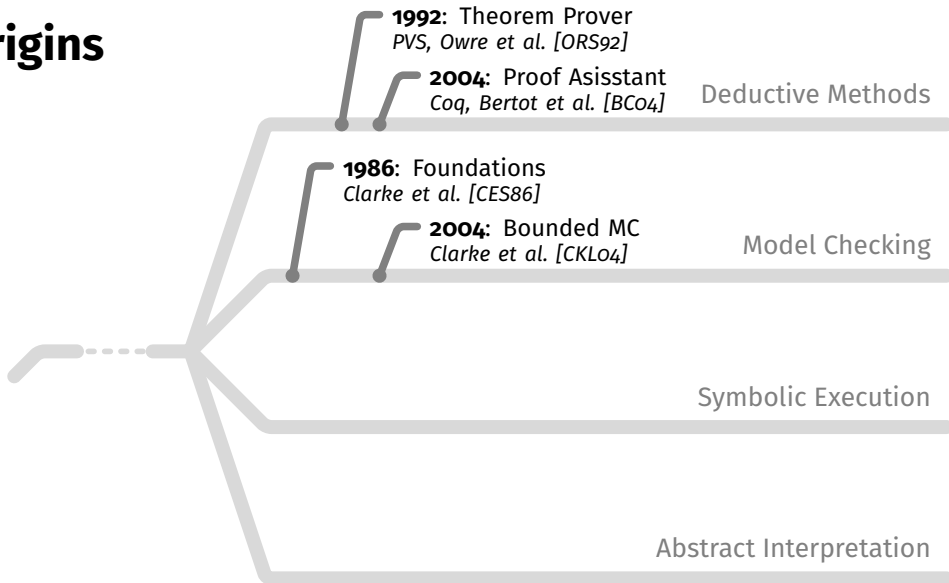
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Origins

Content of first slide [TODO: timeline]

What is a Property? Set basis Poset etc. I have to abstract! Galois, Semantics Principles of Abstract Interpretation book

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References III

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