

Assignment 2

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February 17, 2015

Dobrow Chapter 3

3.3

If a tree has 70% chance of being infected with root rot or bark disease there is a 40% chance it has root disease. If you take the compliment of 40%, (1-.4), then the infected tree has a 60% (.6) that it is bark disease.

$$P(\text{Infected}|\text{Bark}) = (.7) * (.6) P(I|B) = 0.42$$

3.6

Lottery tickets 1 and 1000 Tickets needed to buy to get probability of winning 50%

x=tickets needed to get probability of winning to 50%

$$.5 = (1/1000) * x \quad x = 500 \text{ Tickets}$$

3.8 50-50 chance that the queen carries hemophilia and each prince has 50-50 chance of having hemophilia.

a) three princes without the disease, what the is the probability the queen is a carrier.

$$P(H|E) = P(H)P(E|H)/P(H)P(E|H) + P(H^C)P(E|H^C) \quad .5^3 * .5 / (.5^3 * .5 + .5)$$

$$=.111$$

b) If there is a four prince what is the probability $P(H|E) = P(H)P(E|H)/P(H)P(E|H) + P(H^C)P(E|H^C)$
 $.5^4 * .5 / (.5^4 * .5 + .5)$

$$=.05882353$$

3.16

$$(n/k) = n!/k!(n-k)!$$

a) Straight Flush (5 cards same suit) $P(\text{Straight Flush}) = 36/(52/5)$ $P(\text{Straight Flush}) = 36/(8.065818e + 67/(120 * 2.586232e + 59)) = 1.385169e-05$

b) Four of a Kind (four cards one face value and one other card) $P(\text{Four of a Kind}) = 624/(52/5)$
 $= 624/(8.065818e + 67/(120 * 2.586232e + 59)) = 0.000240096$

c) Full House (three cards of one face value and wo of another face value) $P(\text{Full House}) = 3744/(52/5)$
 $= 3744/(8.065818e + 67/(120 * 2.586232e + 59)) = 0.001440576$

d) Flush (five cards same suit) $P(\text{Flush}) = 5108/(52/5) = 5108/(8.065818e + 67/(120 * 2.586232e + 59)) = 0.001965401$

e) Straight (Five cards in a sequence) $P(\text{Straight}) = 10200/(52/5) = 10200/(8.065818e + 67/(120 * 2.586232e + 59)) = 0.003924646$

f) Three of a Kind (Three cards) $P(\text{Three Kind}) = 54912/(52/5) = 54912/(8.065818e + 67/(120 * 2.586232e + 59)) = 0.02085141$

g) Two Pair $P(\text{Two Pair}) = 123552/(52/5) = 123552/(8.065818e + 67/(120 * 2.586232e + 59)) = 0.04753901$

h) One Pair $P(\text{One Pair}) = 1098240/(52/5) = 1098240/(8.065818e+67/(120*2.586232e+59)) = 0.4225689$

3.22

```
p <- as.numeric(1/6)
scenarios <- c(1, 2, 3)

for (i in scenarios) {
  # Accumulate the probability that fewer than the target # of sixes occurs.
  x <- 0
  # Total number of dice.
  n <- 6 * i
  # Calculate the probability for each possible # of sixes that is less than the goal.
  for (j in 0:(i-1)) {
    x <- x + dbinom(j, n, p)
  }
  print(paste("Probability of at least", i, "six in", n, "fair dice:", 1 - x))
}
```

```
## [1] "Probability of at least 1 six in 6 fair dice: 0.665102023319616"
## [1] "Probability of at least 2 six in 12 fair dice: 0.618667373732309"
## [1] "Probability of at least 3 six in 18 fair dice: 0.597345685947723"
```