

Q.1. 1. No: $\{(1, 8), (7, 10), (9, 20)\}$
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if we choose shortest, then only $(7, 10)$
but we can choose $(1, 8)$ and $(9, 20)$

2. $N_0 = \left\{ \underset{3}{(1, 1)}, \underset{4}{(1, 5)}, \underset{3}{(0, 2)}, \underset{3}{(0, 2)}, \underset{3}{(0, 2)}, \underset{2}{(4, 7)}, \underset{4}{(6, 8)}, \underset{4}{(7, 10)}, \underset{4}{(7, 10)}, \underset{4}{(7, 10)}, \underset{3}{(9, 20)} \right\}$

Follow the strategy would choose $(4, 7)$ first, but

the only solution is $\{(-1, 1), (1, 5), (6, 8), (9, 20)\}$

3. Yes. Because it is actually do the activities in the reverse order, it can obviously give an optimal solution in the same. Every time we choose the best choice.

4. No $\{(1,7), (2,3), (4,5)\}$

Follow the strategy will choose $(1, 7)$ only, but the solution is $\{(2, 3), (4, 5)\}$

Q.2. According to the fractional knapsack problem, we will choose the highest value density we can. Assume the solution is

$S = \{s_1, s_2, \dots, s_n\}$. Use greedy algorithm works by assign $s_n = \min(w_n, W)$ and then solve the subproblem with $\{v_1, v_2, \dots, v_{n-1}\}, \{w_1, w_2, \dots, w_{n-1}\}, W - w_n$

Proof by contradiction: Suppose there is solution s_1, s_2, \dots, s_n that $s_n < \min(w_n, W)$, then we can replace the smallest i ($s_i > 0$)'s s_i to $\max(0, W - w_n)$ and increase s_n to the same amount. then we get a better solution, which lead to a contradiction. Hence the problem has the greedy-choice property.