

Fuzzy Logic Induced Content-Based Recommendation

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Data Preparation and Processing

In this project, we use news articles from different publishers. Each article belongs to a different category: technical, entertainment, and others. This data is a subset of the news aggregator dataset from <https://archive.ics.uci.edu/ml/datasets/News+Aggregator>.

```
library(tidyverse)

## -- Attaching core tidyverse packages ----- tidyverse 2.0.0 --
## v dplyr      1.1.2      v readr      2.1.4
## v forcats    1.0.0      v stringr   1.5.0
## v ggplot2    3.4.2      v tibble    3.2.1
## v lubridate  1.9.2      v tidyr     1.3.0
## v purrr      1.0.1
## -- Conflicts ----- tidyverse_conflicts() --
## x dplyr::filter() masks stats::filter()
## x dplyr::lag()     masks stats::lag()
## i Use the conflicted package (<http://conflicted.r-lib.org/>) to force all conflicts to become errors

library(tidytext)
library(tm)

## Loading required package: NLP
##
## Attaching package: 'NLP'
##
## The following object is masked from 'package:ggplot2':
##
##   annotate

library(slam)
library(dplyr)
library(sentimentr)

set.seed(139)

cnames <- c('ID' , 'TITLE' , 'URL' , 'PUBLISHER' , 'CATEGORY' , 'STORY' , 'HOSTNAME' , 'TIMESTAMP')

data <- read_tsv('newsCorpus.csv', col_names = cnames, col_types = cols(ID = col_integer(), TITLE = col_
head(data)

## # A tibble: 6 x 8
##   ID TITLE                                URL PUBLISHER CATEGORY STORY HOSTNAME TIMESTAMP
##   <int> <chr>                                <chr> <chr>      <chr>   <chr> <chr>      <dbl>
## 1     1 1 Fed official says wea~ "htt~ Los Ange~ b      ddUy~ www.lat~ 1.39e12
```

```
## 2      2 Fed's Charles Plosser~ "htt~ Livemint  b      ddUy~ www.liv~ 1.39e12
## 3      3 US open: Stocks fall ~ "htt~ IFA Maga~ b      ddUy~ www.ifa~ 1.39e12
## 4      4 Fed risks falling 'be~ "htt~ IFA Maga~ b      ddUy~ www.ifa~ 1.39e12
## 5      5 Fed's Plosser: Nasty ~ "htt~ Moneynews b      ddUy~ www.mon~ 1.39e12
## 6      6 Plosser: Fed May Have~ "htt~ NASDAQ   b      ddUy~ www.nas~ 1.39e12
```

Every article has the following columns: * ID: A unique identifier

* TITLE: The title of the article (free text)

* URL: The article's URL

* PUBLISHER: Publisher of the article

* CATEGORY: Some categorization under which the articles are grouped

* STORY: An ID for the group of stories the article belongs to

* HOSTNAME: Hostname of the URL

* TIMESTAMP: Timestamp published

The following are some distinct publishers and categories:

```
data %>% group_by(PUBLISHER) %>% summarise()
```

```
## # A tibble: 10,938 x 1
##   PUBLISHER
##   <chr>
## 1 100.7 WZLX Classic Rock
## 2 1011now
## 3 106 JACK fm
## 4 10News
## 5 10TV
## 6 1200 WOA1
## 7 1230 WBZT
## 8 123Jump.com
## 9 123Macmini.com
## 10 12NewsNow.Com
## # i 10,928 more rows
```

```
data %>% group_by(CATEGORY) %>% summarise()
```

```
## # A tibble: 4 x 1
##   CATEGORY
##   <chr>
## 1 b
## 2 e
## 3 m
## 4 t
```

There are around 10,900 publishers and four categories. We will randomly select a sample of 5000 publishers and get the top 100 publishers by looking at the number of articles they have published:

```
data <- sample_n(data, 5000)
publisher.count <- data.frame(data %>% group_by(PUBLISHER) %>% summarise(ct = n()))
publisher.top <- head(publisher.count[order(-publisher.count$ct),], 100)
head(publisher.top)
```

```
##           PUBLISHER ct
## 1321           Reuters 47
## 1063           NASDAQ 36
## 498       Examiner.com 27
## 711   Huffington Post 27
## 1684 TheCelebrityCafe.com 25
```

```
## 486      Entertainmentwise 24
```

We can see that Reuters tops the list. We have retained only the articles from the top 100 publishers list for our exercise. Data frame `publisher.top` has the top 100 publishers. Now we will get the top 100 publishers, their articles, and other information.

```
data.subset <- inner_join(publisher.top, data)
```

```
## Joining with `by = join_by(PUBLISHER)`
```

```
head(data.subset)
```

```
##   PUBLISHER ct      ID
## 1   Reuters 47  36286
## 2   Reuters 47 353724
## 3   Reuters 47 192591
## 4   Reuters 47 266993
## 5   Reuters 47 322252
## 6   Reuters 47  47804
##                                     TITLE
## 1 UPDATE 1-'Divergent' teen warriors defeat 'Muppets' at box office
## 2      UPDATE 3-BMW's $1 billion plant surfs Mexican investment wave
## 3      Vietnam index plummets about 6 pct on South China sea dispute
## 4 UPDATE 1-Krispy Kreme cuts adjusted earnings outlook as costs rise
## 5                                     Fed could fall behind the curve, Bullard warns
## 6      UPDATE 3-US Senate panel sets April 2 hearing on GM auto recalls
##
##                                     URL
## 1      http://in.reuters.com/article/2014/03/23/boxoffice-idINL1NOMK05H20140323
## 2      http://in.reuters.com/article/2014/07/04/bmw-mexico-plant-idINL2NOPE1MH20140704
## 3      http://www.reuters.com/article/2014/05/08/markets-vietnam-stocks-idUSL3NONU3EE20140508
## 4      http://in.reuters.com/article/2014/06/02/krispykreme-results-idINL3N00J3W320140602
## 5      http://www.reuters.com/article/2014/06/26/us-usa-fed-bullard-curve-idUSKBN0F12AI20140626
## 6      http://www.reuters.com/article/2014/03/26/gm-recall-congress-idUSL1NOMN18U20140326
##   CATEGORY      STORY      HOSTNAME      TIMESTAMP
## 1      e_d_oUk702ysXcmLMXRJeOR-XgNycCM in.reuters.com 1.395624e+12
## 2      b_deysR5eEKjCwHaMg-YORaeJFnY83M in.reuters.com 1.404455e+12
## 3      b_dNon3QbHmj9RMZBV7iFz3EK5TRM www.reuters.com 1.399562e+12
## 4      b_dVV5z8UmGUFI_-MUFIEC1yyFyYFTM in.reuters.com 1.401799e+12
## 5      b_dJela8uxiRnjVgMbiSKiq4Jv1b0cM www.reuters.com 1.403851e+12
## 6      t_dRQXqhof73-73FMusfrX031zeHRDM www.reuters.com 1.395882e+12
```

```
dim(data.subset)
```

```
## [1] 1366      9
```

We join our top 100 publishers data frame `publisher.top` with `data`, get all the details for our top 100 publishers. Our `data.subset` has a total of 1,366 articles.

Designing the content-based recommendation engine

To begin with, we separate our data into two data frames. Then We will be using the `tm` package in R to work with our text data. Next, we do some processing of the text data.

```
title.df <- data.subset[,c('ID', 'TITLE')]
colnames(title.df) <- c('doc_id', 'text')
others.df <- data.subset[,c('ID', 'PUBLISHER', 'CATEGORY')]

library(tm)
```

```
title.reader <- DataframeSource(title.df)
corpus <- Corpus(title.reader)
readerControl=list(reader=title.reader)

getTransformations()
```

```
## [1] "removeNumbers"      "removePunctuation" "removeWords"
## [4] "stemDocument"       "stripWhitespace"
```

Calling `getTransformation` shows us the list of available functions that can be used to transform the text:

```
corpus <- tm_map(corpus, removeNumbers)
corpus <- tm_map(corpus, removePunctuation)
corpus <- tm_map(corpus, stripWhitespace)
corpus <- tm_map(corpus, content_transformer(tolower))
corpus <- tm_map(corpus, removeWords, stopwords("english"))
```

We remove punctuation, numbers, unnecessary white spaces, and stop words from our articles. Finally, we convert our text to lowercase. Punctuation, numbers, and whitespace may not be a good feature to distinguish one article from another. Hence, we remove them.

Finally, we proceed to build our document term matrix

```
dtm <- DocumentTermMatrix(corpus, control=list(wordlength = c(3,10),weighting = "weightTfIdf"))
inspect(dtm[1:5,10:15])
```

```
## <<DocumentTermMatrix (documents: 5, terms: 6)>>
## Non-/sparse entries: 6/24
## Sparsity          : 80%
## Maximal term length: 10
## Sample           :
##          Terms
## Docs      bmws investment mexican plant surfs wave
## 192591     0          0          0      0      0      0
## 266993     0          0          0      0      0      0
## 322252     0          0          0      0      0      0
## 353724     1          1          1      1      1      1
## 36286      0          0          0      0      0      0
```

We use the `DocumentTermMatrix` function to create our matrix. We pass our text corpus and also pass a list to the parameter `control`. Inside the list, we say that we are interested only in words with length, so the number of characters between 3 and 10. For our cell values in our matrix, we want them to be TFIDF. Having created a document term matrix, let's create the cosine distance between the articles:

```
sim.score <- tcrossprod_simple_triplet_matrix(dtm)/(sqrt( row_sums(dtm^2) )%% t(row_sums(dtm^2)) )
```

and we get the similarity matrix

```
sim.score[1:10,1:10]
```

```
##          Docs
## Docs      36286  353724 192591  266993  322252  47804  60270
## 36286  1.000000 0.125000      0 0.117851 0.000000 0.125000 0.000000
## 353724 0.125000 1.000000      0 0.117851 0.000000 0.125000 0.000000
## 192591 0.000000 0.000000      1 0.000000 0.000000 0.000000 0.000000
## 266993 0.117851 0.117851      0 1.000000 0.000000 0.117851 0.1360828
## 322252 0.000000 0.000000      0 0.000000 1.000000 0.000000 0.000000
## 47804  0.125000 0.125000      0 0.117851 0.000000 1.000000 0.000000
```

```
## 60270 0.0000000 0.0000000 0 0.1360828 0.0000000 0.0000000 1.0000000
## 398725 0.1250000 0.2500000 0 0.1178511 0.1443376 0.1250000 0.0000000
## 101350 0.0000000 0.0000000 0 0.0000000 0.0000000 0.1581139 0.0000000
## 203598 0.0000000 0.0000000 0 0.0000000 0.0000000 0.0000000 0.0000000
## Docs
## Docs 398725 101350 203598
## 36286 0.1250000 0.0000000 0
## 353724 0.2500000 0.0000000 0
## 192591 0.0000000 0.0000000 0
## 266993 0.1178511 0.0000000 0
## 322252 0.1443376 0.0000000 0
## 47804 0.1250000 0.1581139 0
## 60270 0.0000000 0.0000000 0
## 398725 1.0000000 0.0000000 0
## 101350 0.0000000 1.0000000 0
## 203598 0.0000000 0.0000000 1
```

Searching

Having created our similarity matrix, we can leverage that matrix to find a match for any given document. We will be using the `sim.score` created in the previous step to perform the search. Let's say we want to find similar articles to article 36286:

```
match.docs <- sim.score["36286",]
match.docs
```

```
## 36286 353724 192591 266993 322252 47804 60270 398725
## 1.0000000 0.1250000 0.0000000 0.1178511 0.0000000 0.1250000 0.0000000 0.1250000
## 101350 203598 4676 181385 212332 163646 51791 267770
## 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.1336306 0.0000000 0.0000000
## 310399 260838 327205 195962 306435 230566 155784 401470
## 0.1178511 0.0000000 0.0000000 0.0000000 0.1443376 0.1250000 0.0000000 0.0000000
## 234668 402744 302682 156135 307682 377401 371053 413420
## 0.0000000 0.1250000 0.1118034 0.0000000 0.0000000 0.0000000 0.1250000 0.0000000
## 255452 304880 277559 92168 294174 179751 247177 77152
## 0.1250000 0.1118034 0.0000000 0.1443376 0.1250000 0.1336306 0.0000000 0.0000000
## 343254 317522 117017 1440 192128 165609 96179 357355
## 0.0000000 0.0000000 0.1250000 0.1178511 0.1178511 0.0000000 0.1250000 0.0000000
## 334251 197210 8689 391558 144791 150378 371743 259180
## 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.1336306 0.0000000 0.0000000
## 293817 213014 302377 188553 307753 128387 354263 30940
## 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000
## 200683 204250 393295 95977 199974 171384 315231 155957
## 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000
## 196395 176240 192149 181085 330375 308077 339457 410418
## 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000
## 149616 88391 217785 275619 333208 126701 7289 66811
## 0.1250000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000
## 118917 287724 341328 380944 39704 72120 92001 182437
## 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000
## 381531 21531 164925 150645 140107 34105 21532 45795
## 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000
## 249881 7247 343026 179101 26222 15463 215637 15793
## 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000
## 143478 358435 2805 234933 169010 55444 367332 237801
```

| | | | | | | | |
|----|-----------|-----------|-----------|-----------|-----------|-----------|-----------|
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 29214 | 58952 | 118468 | 116696 | 127716 | 196785 | 352516 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 93113 | 183175 | 211096 | 271961 | 390485 | 274149 | 421153 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 46289 | 300463 | 6458 | 19905 | 157486 | 67767 | 23001 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 365416 | 323787 | 145232 | 376350 | 329090 | 123120 | 254885 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 416731 | 168522 | 269848 | 179348 | 2926 | 14180 | 106978 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 258230 | 390092 | 320337 | 280235 | 337624 | 258125 | 293026 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 6659 | 265582 | 161411 | 251889 | 86210 | 93511 | 258085 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 303676 | 154698 | 49737 | 49410 | 363514 | 342649 | 320844 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 325201 | 270579 | 135434 | 362669 | 397149 | 15045 | 254434 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 274766 | 54316 | 293103 | 127006 | 14564 | 332209 | 58912 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.1767767 | 0.0000000 |
| ## | 408330 | 67852 | 151443 | 374057 | 313608 | 37038 | 75348 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 276770 | 191370 | 364918 | 223206 | 299352 | 397607 | 106483 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 328739 | 354568 | 247391 | 412065 | 420483 | 148063 | 363403 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 404181 | 422693 | 279147 | 75771 | 15682 | 317940 | 317769 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 77254 | 92154 | 305682 | 117406 | 57043 | 185641 | 13178 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 230511 | 3355 | 371871 | 201409 | 38698 | 86813 | 83712 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.1250000 | 0.0000000 | 0.0000000 |
| ## | 298336 | 230702 | 405397 | 50521 | 217693 | 13910 | 357327 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 180838 | 50423 | 60092 | 346145 | 231787 | 348317 | 393266 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 31304 | 378704 | 173698 | 260950 | 313179 | 369128 | 2670 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 31766 | 387068 | 273367 | 124890 | 402875 | 162458 | 186011 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 229034 | 410174 | 359562 | 242699 | 102258 | 245913 | 36925 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 222098 | 257312 | 270425 | 211133 | 205716 | 240859 | 134104 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.1178511 | 0.0000000 | 0.0000000 |
| ## | 302351 | 172110 | 180482 | 353317 | 317738 | 160768 | 31344 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 77518 | 239803 | 17804 | 302216 | 364508 | 165889 | 366573 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 302129 | 156230 | 104689 | 386499 | 241113 | 226329 | 152064 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 45370 | 55983 | 237045 | 644 | 410808 | 160366 | 391439 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 321339 | 37867 | 61074 | 231758 | 237679 | 413071 | 116840 |

| | | | | | | | |
|----|-----------|-----------|-----------|-----------|-----------|-----------|-----------|
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 226940 | 343194 | 398599 | 255510 | 184474 | 192631 | 261404 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 81028 | 168189 | 33528 | 284850 | 292557 | 259307 | 342483 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 292558 | 355045 | 321921 | 374019 | 364136 | 292794 | 22939 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 275761 | 295701 | 72812 | 140283 | 187672 | 312839 | 138700 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 292103 | 3479 | 229299 | 14993 | 376299 | 23498 | 317573 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 258487 | 222126 | 313749 | 360374 | 185423 | 343429 | 336860 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 403757 | 277316 | 31792 | 327355 | 385933 | 286194 | 68787 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 296767 | 224292 | 313613 | 16247 | 89849 | 100919 | 415584 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 265252 | 199801 | 144199 | 4888 | 202859 | 401332 | 37477 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 369718 | 46995 | 222881 | 159980 | 293010 | 124782 | 35569 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 264246 | 71833 | 159574 | 306755 | 406855 | 203949 | 237923 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 46970 | 68584 | 246699 | 413303 | 217618 | 181387 | 269296 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 419780 | 378930 | 275597 | 170538 | 413829 | 109999 | 278898 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 322113 | 270497 | 140112 | 133483 | 153647 | 106247 | 243036 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.1443376 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 244261 | 296565 | 206208 | 333498 | 34095 | 130311 | 78785 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 190644 | 125876 | 215998 | 285910 | 293158 | 206842 | 47658 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 318848 | 229996 | 371120 | 317244 | 157407 | 264617 | 410829 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 159884 | 166696 | 420968 | 284951 | 345652 | 100368 | 173609 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 389679 | 56120 | 101327 | 409952 | 338917 | 249874 | 156190 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 127901 | 420932 | 371727 | 176603 | 43446 | 55719 | 175196 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 130559 | 67293 | 370120 | 342615 | 357849 | 175870 | 334879 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 54046 | 240535 | 53254 | 248984 | 104955 | 414529 | 412710 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 156234 | 371659 | 33366 | 163191 | 238836 | 217163 | 155917 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 297449 | 212790 | 95804 | 34979 | 213169 | 237950 | 103208 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 361126 | 354848 | 39753 | 19786 | 98434 | 202955 | 366575 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 118776 | 347546 | 178633 | 10892 | 10901 | 3624 | 299168 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 265294 | 225816 | 82822 | 386398 | 203540 | 413509 | 345981 |

| | | | | | | | |
|----|-----------|-----------|-----------|-----------|-----------|-----------|-----------|
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 203280 | 204872 | 308448 | 209289 | 263234 | 40794 | 326556 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 3465 | 315356 | 290055 | 39931 | 124167 | 100564 | 362423 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 142933 | 219003 | 211943 | 198580 | 177283 | 296806 | 339551 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 8697 | 405941 | 57228 | 31230 | 414212 | 192558 | 212845 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 339538 | 87334 | 70533 | 353605 | 171331 | 35465 | 137091 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 185581 | 124401 | 405513 | 383484 | 245191 | 405334 | 310617 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 290779 | 387037 | 49838 | 390201 | 124776 | 394695 | 55313 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 380 | 244311 | 213971 | 142575 | 285966 | 262762 | 152303 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 154492 | 213703 | 112937 | 280595 | 283448 | 1530 | 391310 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 322682 | 170542 | 370939 | 189479 | 98121 | 34807 | 81339 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 343341 | 159869 | 83600 | 10047 | 289950 | 236492 | 394847 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 6406 | 202896 | 240996 | 15724 | 291120 | 152446 | 387177 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 147454 | 127447 | 340356 | 184189 | 200650 | 418086 | 321602 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 78709 | 230722 | 360712 | 392575 | 312474 | 266030 | 157453 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.2132007 | 0.0000000 | 0.0000000 |
| ## | 143601 | 291527 | 44135 | 157902 | 143538 | 414077 | 278403 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 23073 | 270913 | 354703 | 303086 | 349080 | 384139 | 66112 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 128770 | 145138 | 257078 | 223802 | 157540 | 120888 | 217096 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 298867 | 410592 | 171367 | 312216 | 235202 | 171406 | 255050 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 144720 | 255492 | 1193 | 139376 | 208703 | 5504 | 180647 |
| ## | 0.0000000 | 0.0000000 | 0.1443376 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 48662 | 272504 | 204545 | 225871 | 181139 | 87668 | 387090 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 255751 | 125754 | 359917 | 60272 | 105050 | 136788 | 156576 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 24293 | 325390 | 238757 | 192262 | 83380 | 406318 | 361640 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 336216 | 204458 | 145339 | 322921 | 120897 | 85268 | 308667 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 173560 | 80493 | 276250 | 412575 | 173854 | 307586 | 276884 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 385724 | 224306 | 368577 | 56657 | 252595 | 191432 | 21670 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 415312 | 253282 | 343318 | 65016 | 45419 | 88503 | 57596 |
| ## | 0.0000000 | 0.1250000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 17836 | 298952 | 57362 | 10833 | 291260 | 205575 | 160177 |

| | | | | | | | |
|----|-----------|-----------|-----------|-----------|-----------|-----------|-----------|
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 83986 | 389621 | 219082 | 287466 | 168549 | 202204 | 73148 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 300260 | 236901 | 42604 | 89949 | 140527 | 7683 | 268113 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 356837 | 125115 | 159201 | 226107 | 310587 | 330456 | 38041 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 97172 | 150070 | 160592 | 21735 | 94885 | 235901 | 316448 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 29268 | 277353 | 2319 | 419850 | 189303 | 269063 | 137454 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 347904 | 169998 | 420514 | 220295 | 227500 | 264163 | 419753 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 23587 | 40083 | 409544 | 42817 | 242443 | 34028 | 142363 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 26130 | 20360 | 405260 | 175675 | 361243 | 421572 | 415059 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 389072 | 85624 | 10941 | 202456 | 403558 | 376315 | 168381 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.2357023 | 0.0000000 | 0.0000000 |
| ## | 196302 | 366681 | 27335 | 130471 | 149046 | 118852 | 261415 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 153030 | 224171 | 208017 | 372552 | 12332 | 272690 | 209411 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 11125 | 208808 | 377539 | 155664 | 356064 | 307677 | 146602 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 228074 | 77327 | 157787 | 179199 | 334393 | 268545 | 417975 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 106275 | 115133 | 215697 | 141520 | 217889 | 131388 | 290803 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 310180 | 258725 | 91726 | 132331 | 90978 | 311411 | 330155 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 76141 | 352258 | 353600 | 79814 | 91683 | 80237 | 77849 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 255648 | 202634 | 276889 | 344679 | 279352 | 129859 | 233395 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 144151 | 369809 | 158829 | 6792 | 376619 | 238937 | 19032 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 19951 | 109331 | 130158 | 415100 | 178285 | 361357 | 206418 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 287952 | 386409 | 177786 | 39950 | 258163 | 381468 | 339617 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 325458 | 409802 | 27830 | 181988 | 78327 | 265118 | 355170 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 238892 | 373996 | 271596 | 72220 | 243801 | 167625 | 3764 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 342424 | 86742 | 218425 | 338402 | 112600 | 95736 | 311326 |
| ## | 0.0000000 | 0.3162278 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 371019 | 247955 | 383418 | 155821 | 263165 | 139603 | 366985 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 412637 | 301848 | 92323 | 394076 | 177341 | 85209 | 207781 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 163919 | 416802 | 209635 | 404787 | 316493 | 399274 | 141757 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.1336306 | 0.1178511 | 0.0000000 |
| ## | 166329 | 361854 | 213458 | 344191 | 56467 | 319770 | 33064 |

| | | | | | | | |
|----|-----------|-----------|-----------|-----------|-----------|-----------|-----------|
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 169551 | 58966 | 172819 | 178754 | 236869 | 11816 | 295684 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 417626 | 36230 | 187571 | 283973 | 281016 | 263590 | 20706 |
| ## | 0.0000000 | 0.4743416 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 30877 | 45094 | 33015 | 303542 | 156605 | 170968 | 172675 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 125987 | 229482 | 273590 | 312007 | 394680 | 5542 | 188992 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 291085 | 128403 | 181063 | 120575 | 212597 | 83173 | 410027 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 46705 | 20847 | 262900 | 174666 | 97169 | 415789 | 260396 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 269876 | 275767 | 71815 | 149627 | 59912 | 17853 | 60439 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 207611 | 342879 | 59613 | 238187 | 420101 | 399537 | 191471 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 270753 | 325103 | 380345 | 346581 | 10894 | 355760 | 243568 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.2500000 | 0.0000000 |
| ## | 396782 | 351447 | 317564 | 401205 | 99889 | 418724 | 32424 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 313631 | 322073 | 363587 | 388900 | 25511 | 168764 | 135285 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 249083 | 363888 | 228978 | 184406 | 346711 | 92433 | 118174 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 101696 | 243660 | 91470 | 111803 | 403229 | 404835 | 148821 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 333044 | 71239 | 87654 | 338761 | 173358 | 196346 | 357042 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 57063 | 334527 | 68368 | 403520 | 274830 | 15190 | 6587 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 255010 | 148407 | 110902 | 271762 | 153540 | 144041 | 366083 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 358552 | 372833 | 396056 | 328550 | 411528 | 269768 | 274604 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 361034 | 103667 | 242758 | 168063 | 252135 | 332337 | 67739 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 322048 | 23296 | 247453 | 6469 | 320379 | 54074 | 179176 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 131343 | 19773 | 337448 | 54652 | 247393 | 75720 | 147898 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 221992 | 284597 | 271166 | 271661 | 295604 | 401779 | 175439 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.1118034 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 137472 | 385519 | 286403 | 291992 | 207977 | 209034 | 185405 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 328823 | 103019 | 262386 | 375039 | 32458 | 304546 | 110565 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 140843 | 260210 | 322634 | 51045 | 412970 | 403604 | 29984 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 66964 | 119341 | 13317 | 371287 | 31723 | 356079 | 356178 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 |
| ## | 135579 | 93760 | 150634 | 365190 | 27589 | 218844 | 21005 |
| ## | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.0000000 | 0.2886751 | 0.0000000 |
| ## | 121026 | 278823 | 77587 | 246953 | 220173 | 365776 | 260248 |

```
## 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000
##      260921      202879      313026      206495      140992      124232      295608      222812
## 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000
##      243134      342656      10843      119342      23345      44035      138752      13055
## 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000
##      21901      404175      174252      118402      124129      247214      320876      302858
## 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000
##      369576      396682      6127      78810      189716      258483      287779      328846
## 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000
##      11642      369608      43390      285383      324759      65757      119037      300308
## 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000
##      206525      78039      271093      190382      254143      252058      351503      72370
## 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000
##      58880      165374      142282      40527      402862      168972      6487      407874
## 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000
##      137338      162372      309287      17831      335762      392896      217729      278009
## 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000
##      388226      38382      57818      338710      836      44109      334466      314743
## 0.0000000 0.0000000 0.1250000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000
##      230968      621      330332      255127      14634      365257      416106      175312
## 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000
##      361136      378786      358099      300309      254469      357441      172826      149974
## 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000
##      75190      409833      248674      29212      13920      147279      250491      252745
## 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000
##      250072      406462      245755      334532      90835      96046      29959      246849
## 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000
##      214423      421650      325501      373602      238351      382488      96399      220980
## 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000
##      119049      389695      247337      380867      261001      403992      53541      416145
## 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000
##      261715      201194      378891      129301      279137      117683      66618      347047
## 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000
##      106217      167425      301262      84499      205130      177153      15432      61365
## 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000
##      211689      71728      248440      348636      349409      383920      208382      87680
## 0.0000000 0.1250000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000
##      234637      376773      339251      208467      269596      368034      10176      412267
## 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000
##      88428      52939      155675      60080      231558      408627      147748      27055
## 0.0000000 0.1250000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000
##      78962      228642      83033      202276      258094      144183
## 0.0000000 0.0000000 0.0000000 0.2500000 0.2500000 0.0000000
```

We go to our `match.doc` similarity matrix and pick up row 36286. Now, this row has all the other articles and their similarity scores. Let's now take this row and make a data frame:

```
match.df <- data.frame(ID = names(match.docs), cosine = match.docs, stringsAsFactors=FALSE)
match.df$ID <- as.integer(match.df$ID)
head(match.df)
```

```
##      ID      cosine
## 36286 36286 1.0000000
## 353724 353724 0.1250000
## 192591 192591 0.0000000
```

```
## 266993 266993 0.1178511
## 322252 322252 0.0000000
## 47804 47804 0.1250000
```

Our `match.df` data frame now contains all the matching documents for 36286. Now, we are going to recommend only the top 30 matches:

```
match.refined<-head(match.df[order(-match.df$cosine),],30)
head(match.refined)
```

```
##          ID      cosine
## 36286 36286 1.0000000
## 36230 36230 0.4743416
## 86742 86742 0.3162278
## 218844 218844 0.2886751
## 243568 243568 0.2500000
## 202276 202276 0.2500000
```

Now that we have the matching documents, we need to present them in a ranked order. In order to rank the results, we are going to calculate some additional measures and use fuzzy logic to get the final ranking score. Before we go ahead and calculate the additional measures, let's merge `title.df` and `others.df` with `match.refined`:

```
colnames(title.df) <- c('ID','TITLE')
match.refined <- inner_join(match.refined, title.df)
```

```
## Joining with `by = join_by(ID)`
match.refined <- inner_join(match.refined, others.df)
```

```
## Joining with `by = join_by(ID)`
head(match.refined)
```

```
##          ID      cosine
## 1 36286 1.0000000
## 2 36230 0.4743416
## 3 86742 0.3162278
## 4 218844 0.2886751
## 5 243568 0.2500000
## 6 202276 0.2500000
##                                     TITLE
## 1          UPDATE 1-'Divergent' teen warriors defeat 'Muppets' at box office
## 2                                     'Divergent' tops weekend box office
## 3                                     Captain America's box office record
## 4          'Godzilla' flattens box office with monstrous debut
## 5          X Men Days of Future Past Box Office: Millions For Mutants!
## 6 'Neighbors' Crashing Spider-Man's Party at Box Office with $45 Million Opening
##          PUBLISHER CATEGORY
## 1          Reuters          e
## 2          Newsday          e
## 3  Belfast Telegraph          e
## 4  Detroit Free Press          e
## 5 The Hollywood Gossip          e
## 6          Variety          e
```

Polarity scores

We are going to leverage the `sentimentr` R package to learn the sentiments of the articles we have collected. Let's look at how to score using the `sentiment` function :

```
sentiment.score <- sentiment(match.refined$TITLE)
head(sentiment.score)
```

```
##      element_id sentence_id word_count  sentiment
## 1:           1           1           9 -0.2666667
## 2:           2           1           5  0.4472136
## 3:           3           1           5  0.0000000
## 4:           4           1           7 -0.1889822
## 5:           5           1          11  0.0000000
## 6:           6           1          11 -0.3015113
```

The `sentiment` function in `sentimentr` calculates a score between -1 and 1 for each of the articles. If a text has multiple sentences, it will calculate the score for each sentence. A score of -1 indicates that the sentence has a very negative polarity. A score of 1 means that the sentence is very positive. A score of 0 refers to the neutral nature of the sentence.

However, we need the score at an article level and not at a sentence level, so we can take an average value of the score across all the sentences in a text.

```
sentiment.score <- sentiment.score %>% group_by(element_id) %>% summarise(sentiment = mean(sentiment))
head(sentiment.score)
```

```
## # A tibble: 6 x 2
##   element_id sentiment
##       <int>     <dbl>
## 1         1    -0.267
## 2         2     0.447
## 3         3      0
## 4         4    -0.189
## 5         5      0
## 6         6    -0.302
```

Here, the `element_id` refers to the individual article. By grouping `element_id` and calculating the average, we can get the sentiment score at an article level. We now have the scores for each article. Next we update the `match.refined` data frame with the polarity scores

```
match.refined$polarity <- sentiment.score$sentiment
head(match.refined)
```

```
##      ID      cosine
## 1  36286 1.0000000
## 2  36230 0.4743416
## 3  86742 0.3162278
## 4 218844 0.2886751
## 5 243568 0.2500000
## 6 202276 0.2500000
##
##                                     TITLE
## 1      UPDATE 1-'Divergent' teen warriors defeat 'Muppets' at box office
## 2                                     'Divergent' tops weekend box office
## 3                                     Captain America's box office record
## 4                                     'Godzilla' flattens box office with monstrous debut
## 5      X Men Days of Future Past Box Office: Millions For Mutants!
## 6 'Neighbors' Crashing Spider-Man's Party at Box Office with $45 Million Opening
```

```
##          PUBLISHER CATEGORY    polarity
## 1          Reuters          e -0.2666667
## 2          Newsday          e  0.4472136
## 3    Belfast Telegraph      e  0.0000000
## 4    Detroit Free Press      e -0.1889822
## 5 The Hollywood Gossip      e  0.0000000
## 6          Variety          e -0.3015113
```

Jaccard's distance

While ranking the matched articles, we want to also include the category and publisher columns. Let's proceed to include those columns:

```
target.publisher <- match.refined[1,]$PUBLISHER
target.category <- match.refined[1,]$CATEGORY
target.polarity <- match.refined[1,]$polarity
target.title <- match.refined[1,]$TITLE
```

We need the publisher, category, and the sentiment details of the document we are searching for. Fortunately, the first row of our `match.refined` data frame stores all the details related to 36286. For the rest of the articles, we need to find out if they match the publisher and category of document 36286.

```
match.refined$is.publisher <- match.refined$PUBLISHER == target.publisher
match.refined$is.publisher <- as.numeric(match.refined$is.publisher)
match.refined$is.category <- match.refined$CATEGORY == target.category
match.refined$is.category <- as.numeric(match.refined$is.category)
```

With the two new columns, we can calculate the Jaccard's distance between document 36286 and all the other documents in the `match.refined` data frame.

```
match.refined$jaccard <- (match.refined$is.publisher + match.refined$is.category)/2
```

The Jaccard index measures the similarity between two sets, and is a ratio of the size of the intersection and the size of the union of the participating sets. Here we have only have two elements, one for publisher and one for category, so our union is 2. The numerator, by adding the two Boolean variable, we get the intersection.

Finally, we also calculate the absolute difference (Manhattan distance) in the polarity values between the articles in the search results and our search article. We do a min/max normalization of the difference score.

```
match.refined$polaritydiff <- abs(target.polarity - match.refined$polarity)
```

```
range01 <- function(x){(x-min(x))/(max(x)-min(x))}
match.refined$polaritydiff <- range01(unlist(match.refined$polaritydiff))
head(match.refined)
```

```
##          ID    cosine
## 1    36286 1.0000000
## 2    36230 0.4743416
## 3    86742 0.3162278
## 4   218844 0.2886751
## 5   243568 0.2500000
## 6   202276 0.2500000
##
##                                     TITLE
## 1          UPDATE 1-'Divergent' teen warriors defeat 'Muppets' at box office
## 2                                     'Divergent' tops weekend box office
## 3                                     Captain America's box office record
## 4                                     'Godzilla' flattens box office with monstrous debut
## 5          X Men Days of Future Past Box Office: Millions For Mutants!
```

```
## 6 'Neighbors' Crashing Spider-Man's Party at Box Office with $45 Million Opening
##          PUBLISHER CATEGORY    polarity is.publisher is.category jaccard
## 1         Reuters          e -0.2666667          1          1          1.0
## 2        Newsday          e  0.4472136          0          1          0.5
## 3  Belfast Telegraph          e  0.0000000          0          1          0.5
## 4  Detroit Free Press          e -0.1889822          0          1          0.5
## 5 The Hollywood Gossip          e  0.0000000          0          1          0.5
## 6         Variety          e -0.3015113          0          1          0.5
## polaritydiff
## 1  0.00000000
## 2  0.83159146
## 3  0.31063714
## 4  0.09049376
## 5  0.31063714
## 6  0.04059019
```

We remove some of the unwanted fields from the `match.refined` data frame. Finally, we have the ID, cosine distance, title, publisher, category, Jaccard score, and the polarity difference.

```
match.refined$is.publisher = NULL
match.refined$is.category = NULL
match.refined$polarity = NULL
match.refined$sentiment = NULL
head(match.refined)
```

```
##          ID      cosine
## 1  36286 1.0000000
## 2  36230 0.4743416
## 3  86742 0.3162278
## 4 218844 0.2886751
## 5 243568 0.2500000
## 6 202276 0.2500000
##
##                                     TITLE
## 1          UPDATE 1-'Divergent' teen warriors defeat 'Muppets' at box office
## 2                                     'Divergent' tops weekend box office
## 3                                     Captain America's box office record
## 4          'Godzilla' flattens box office with monstrous debut
## 5          X Men Days of Future Past Box Office: Millions For Mutants!
## 6 'Neighbors' Crashing Spider-Man's Party at Box Office with $45 Million Opening
##          PUBLISHER CATEGORY jaccard polaritydiff
## 1         Reuters          e          1.0  0.00000000
## 2        Newsday          e          0.5  0.83159146
## 3  Belfast Telegraph          e          0.5  0.31063714
## 4  Detroit Free Press          e          0.5  0.09049376
## 5 The Hollywood Gossip          e          0.5  0.31063714
## 6         Variety          e          0.5  0.04059019
```

Ranking search results

We need to perform our ranking based on the following metrics we have calculated: * Cosine similarity * Jaccard index * Polarity difference In this project, we will leverage fuzzy logic programming to do the search result ranking. We will be using the `sets` R package for our fuzzy logic programming:

```
library(sets)
```

```
##
```

```
## Attaching package: 'sets'

## The following objects are masked from 'package:lubridate':
##
##   as.interval, interval, is.interval

## The following object is masked from 'package:forcats':
##
##   %>%

## The following object is masked from 'package:stringr':
##
##   %>%

## The following object is masked from 'package:dplyr':
##
##   %>%

## The following object is masked from 'package:purrr':
##
##   %>%

## The following object is masked from 'package:tidyr':
##
##   %>%

## The following object is masked from 'package:tibble':
##
##   %>%
```

```
sets_options("universe", seq(from = 0, to = 1, by = 0.1))
```

The first step is to set up our universe. We define the range of values and the granularity of the values we will be dealing with in our universe. Our cosine, Jaccard, and polarity are all normalized to have a value between zero and one. Hence, the range of our universe is set between zero and one.

The first step in fuzzy logic programming is to define the linguistic variables we will be dealing with:

```
variables <- set(
  cosine = fuzzy_partition(varnames = c(vlow = 0.2, low = 0.4, medium = 0.6, high = 0.8), FUN = fuzzy_c
  jaccard = fuzzy_partition(varnames = c(close = 1.0, halfway = 0.5, far = 0.0), FUN = fuzzy_cone , rad
  polarity = fuzzy_partition(varnames = c(same = 0.0, similar = 0.3, close = 0.5, away = 0.7), FUN = fuzz
  ranking = fuzzy_partition(varnames = c(H = 1.0, MED = 0.7 , M = 0.5, L = 0.3), FUN = fuzzy_cone , rad
```

For each variable, we define the various linguistic values and the fuzzy membership function. For example, for our linguistic variable `cosine`, the linguistic values include `vlow`, `low`, `medium`, and `high`.

Based on the interaction between the linguistic variables `cosine`, `jaccard`, and `polarity`, the ranking linguistic variables are assigned different linguistic values. These interactions are defined as rules. Having defined the linguistic variables, the linguistic values, and the membership function, we proceed to write down our fuzzy rules:

```
rules <- set(
##### Low Ranking Rules #####
fuzzy_rule(cosine %is% vlow, ranking %is% L),
fuzzy_rule(cosine %is% low || jaccard %is% far || polarity %is% away, ranking %is% L),
fuzzy_rule(cosine %is% low || jaccard %is% halfway || polarity %is% away, ranking %is% L),
fuzzy_rule(cosine %is% low || jaccard %is% halfway || polarity %is% close, ranking %is% L),
fuzzy_rule(cosine %is% low || jaccard %is% halfway || polarity %is% similar, ranking %is% L),
fuzzy_rule(cosine %is% low || jaccard %is% halfway || polarity %is% same, ranking %is% L),
```

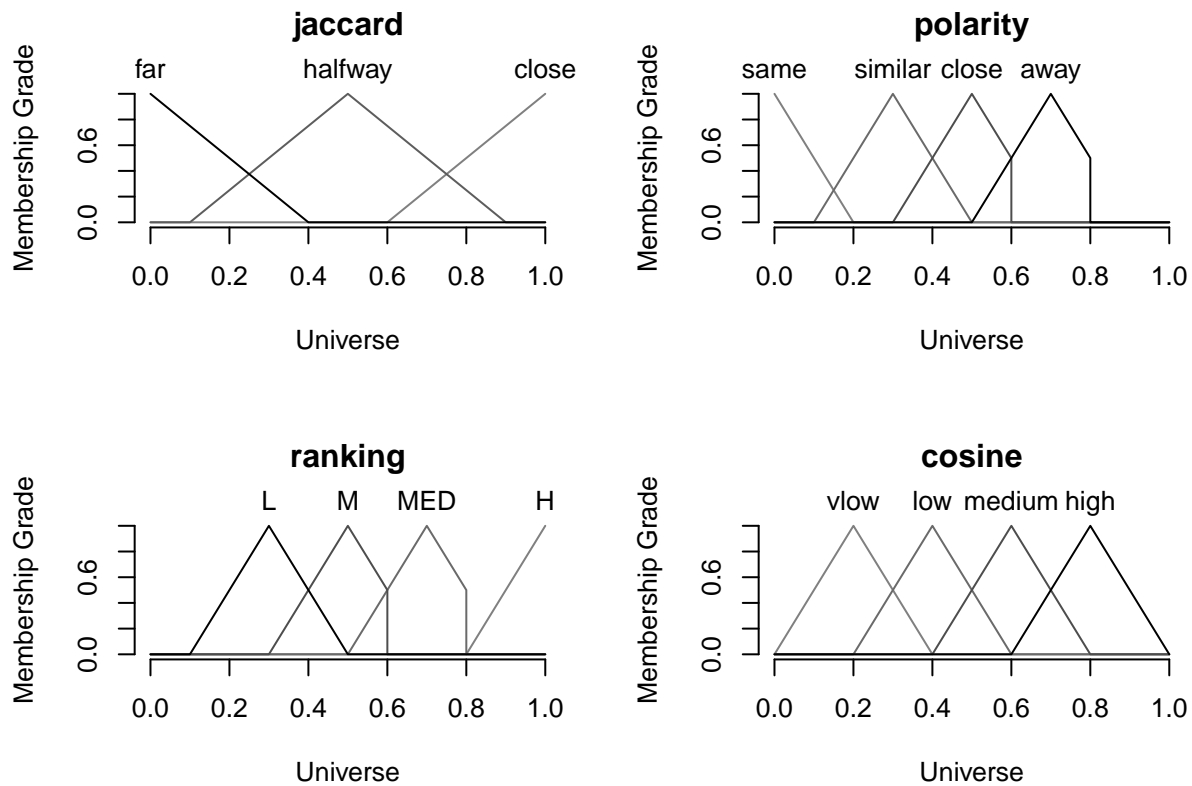


```
fuzzy_rule(cosine %is% medium || jaccard %is% far || polarity %is% away, ranking %is% L),
##### Medium Ranking Rules #####
fuzzy_rule(cosine %is% low || jaccard %is% close || polarity %is% same, ranking %is% M),
fuzzy_rule(cosine %is% low && jaccard %is% close && polarity %is% similar, ranking %is% M),
##### Median Ranking Rule #####
fuzzy_rule(cosine %is% medium && jaccard %is% close && polarity %is% same, ranking %is% MED),
fuzzy_rule(cosine %is% medium && jaccard %is% halfway && polarity %is% same, ranking %is% MED),
fuzzy_rule(cosine %is% medium && jaccard %is% close && polarity %is% similar, ranking %is% MED),
fuzzy_rule(cosine %is% medium && jaccard %is% halfway && polarity %is% similar, ranking %is% MED),
##### High Ranking Rule #####
fuzzy_rule(cosine %is% high, ranking %is% H))
```

With the rules and linguistic variables defined, we can now put our complete fuzzy system together:

```
ranking.system <- fuzzy_system(variables, rules)
print(ranking.system)
```

```
## A fuzzy system consisting of 4 variables and 14 rules.
##
## Variables:
##
## jaccard(close, halfway, far)
## polarity(same, similar, close, away)
## ranking(H, MED, M, L)
## cosine(vlow, low, medium, high)
##
## Rules:
##
## cosine %is% low && jaccard %is% close && polarity %is% similar => ranking %is% M
## cosine %is% medium && jaccard %is% close && polarity %is% same => ranking %is% MED
## cosine %is% medium && jaccard %is% close && polarity %is% similar => ranking %is% MED
## cosine %is% medium && jaccard %is% halfway && polarity %is% same => ranking %is% MED
## cosine %is% medium && jaccard %is% halfway && polarity %is% similar => ranking %is% MED
## cosine %is% low || jaccard %is% far || polarity %is% away => ranking %is% L
## cosine %is% low || jaccard %is% close || polarity %is% same => ranking %is% M
## cosine %is% low || jaccard %is% halfway || polarity %is% away => ranking %is% L
## cosine %is% low || jaccard %is% halfway || polarity %is% same => ranking %is% L
## cosine %is% low || jaccard %is% halfway || polarity %is% close => ranking %is% L
## cosine %is% low || jaccard %is% halfway || polarity %is% similar => ranking %is% L
## cosine %is% medium || jaccard %is% far || polarity %is% away => ranking %is% L
## cosine %is% high => ranking %is% H
## cosine %is% vlow => ranking %is% L
plot(ranking.system)
```



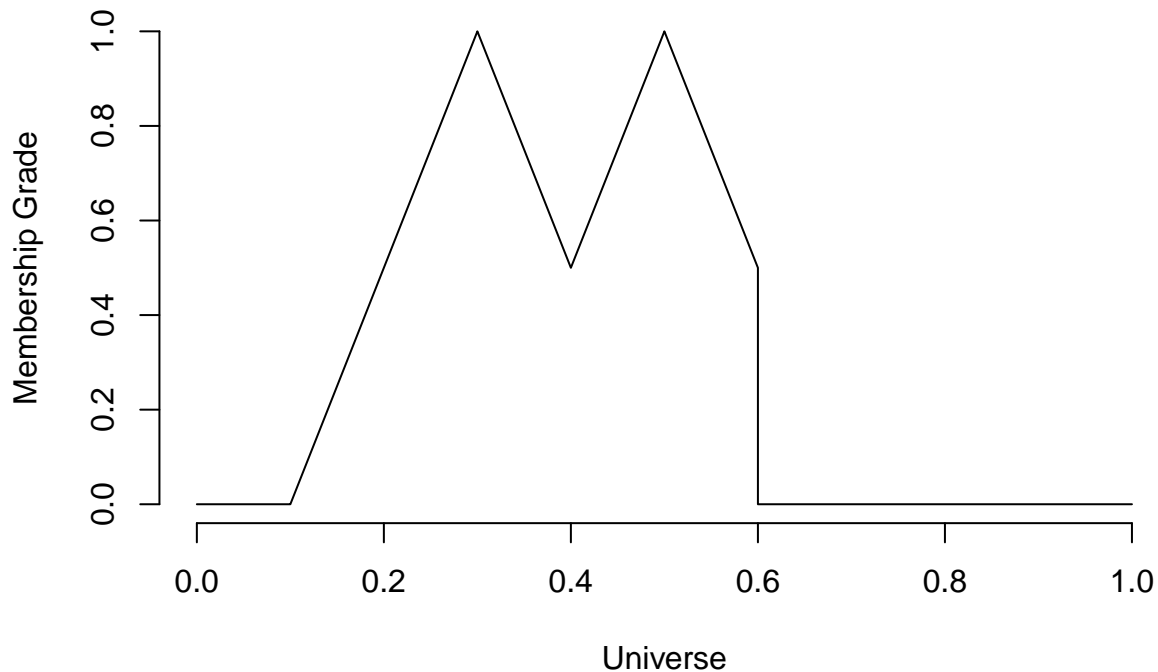
The final plot reveals the fuzziness in the boundary for different linguistic variables. Compare this with a hard-coded if-else logic system.

We can now proceed to use this system to do the ranking. Let's do the ranking on a single example:

```
fi <- fuzzy_inference(ranking.system, list(cosine = 0.5000000, jaccard = 0, polarity=0.0000000))
gset_defuzzify(fi, "centroid")
```

```
## [1] 0.4
```

```
plot(fi)
```



For given values of cosine, polarity, and Jaccard, we get a ranking score of 0.4. Now we can use this score to rank the results.

Let's generate the rankings for all the articles in `match.refined`:

```
get.ranks <- function(dataframe){
  cosine = as.numeric(dataframe['cosine'])
  jaccard = as.numeric(dataframe['jaccard'])
  polarity = as.numeric(dataframe['polaritydiff'])
  fi <- fuzzy_inference(ranking.system, list(cosine = cosine, jaccard = jaccard, polarity=polarity))
  return(gset_defuzzify(fi, "centroid"))
}
```

```
match.refined$ranking <- apply(match.refined, 1, get.ranks)
match.refined <- match.refined[order(-match.refined$ranking),]
head(match.refined)
```

```
##      ID    cosine
## 1  36286 1.0000000
## 2  36230 0.4743416
## 3  86742 0.3162278
## 4 218844 0.2886751
## 5 243568 0.2500000
## 6 202276 0.2500000
##                                     TITLE
## 1          UPDATE 1-'Divergent' teen warriors defeat 'Muppets' at box office
## 2                                     'Divergent' tops weekend box office
## 3          Captain America's box office record
```

```

## 4          'Godzilla' flattens box office with monstrous debut
## 5          X Men Days of Future Past Box Office: Millions For Mutants!
## 6 'Neighbors' Crashing Spider-Man's Party at Box Office with $45 Million Opening
##          PUBLISHER CATEGORY jaccard polaritydiff ranking
## 1          Reuters          e      1.0  0.00000000    0.4
## 2          Newsday          e      0.5  0.83159146    0.3
## 3    Belfast Telegraph      e      0.5  0.31063714    0.3
## 4    Detroit Free Press      e      0.5  0.09049376    0.3
## 5    The Hollywood Gossip      e      0.5  0.31063714    0.3
## 6          Variety          e      0.5  0.04059019    0.3

```

The `get.ranks` function is applied in each row of `match.refined` to get the fuzzy ranking. Finally, we sort the results using this ranking.