

week02 tutorial

Q1

Use quantifiers to express the statement that "There is a woman who has taken a flight on every airline in the world."

$P(x)$ = a women

$Q(x)$ = who has taken a flight on every airline in the world

$$\exists x \exists y \forall z (P(x, y) \wedge Q(y, z))$$

Q2

$$1. Q(0, 0, 0) \wedge Q(0, 1, 0)$$

$$2. Q(0, 1, 1) \vee Q(1, 1, 1) \vee Q(2, 1, 1)$$

$$3. Q(1, 0, 0) \vee Q(1, 0, 1) \vee (1, 1, 0) \vee Q(1, 1, 1) \vee$$

$$Q(2, 0, 0) \vee Q(2, 0, 1) \vee Q(2, 1, 0) \vee Q(2, 1, 1)$$

4. *more...*

Q3

$$\forall x (P(x) \wedge Q(X))$$

$$= P(x)$$

$$= R(x)$$

$$\forall x (Q(x) \wedge S(x))$$

$$= S(x)$$

$$\forall x (R(x) \wedge S(x))$$

$$Q. E. D.$$

Q4

$$\exists x \neg P(x)$$

$$= \neg \forall x P(x)$$

$$= \forall x Q(x) Q(a)$$

$$= \forall x S(x) S(a)$$

$$\forall x (R(x) \rightarrow \neg S(x))$$

$$S(c) \rightarrow \neg R(c)$$

$$= \exists x \neg R(x)$$

Q5

$$p \vee q$$

$$\neg p \vee q$$

$$p \vee \neg q$$

$$\neg p \vee \neg q$$

$$q$$

$$\neg q$$

Q. E. D