Problem 1: Decision Trees for Spam Classification

1.1

```
In [31]: import math
def binary_entropy(p):
    if p == 0.0 or p == 1.0:
        return 0

    return (-p) * math.log(p,2.0) - (1.0 - p) * math.log(1.0 - p, 2.0)
hy = binary_entropy(0.6)
print "Entropy H(y) of this binary class variable y: " + str(hy)
```

Entropy H(y) of this binary class variable y: 0.970950594455

1.2

```
In [35]: def binary_information_gain(hy,x_true,x_true_y_true,x_false_y_true):
    return hy - x_true * binary_entropy(x_true_y_true) - (1 - x_true) * binary_entropy(x_false_y_true)
print "Information gain for feature x1 is: " + str(binary_information_gain(hy,0.6,0.5,0.25))
print "Information gain for feature x2 is: " + str(binary_information_gain(hy,0.5,0.0,0.8))
print "Information gain for feature x3 is: " + str(binary_information_gain(hy,0.7,3.0 / 7.0,1.0 / 3.0))
print "Information gain for feature x4 is: " + str(binary_information_gain(hy,0.7,2.0 / 7.0,2.0 / 3.0))
print "Information gain for feature x5 is: " + str(binary_information_gain(hy,0.3,1.0 / 3.0,3.0 / 7.0))
print "We should choose feature 2 as root"
```

Information gain for feature x1 is: 0.046439344671
Information gain for feature x2 is: 0.609986547011
Information gain for feature x3 is: 0.00580214901435
Information gain for feature x4 is: 0.0912774462417
Information gain for feature x5 is: 0.00580214901435
We should choose feature 2 as root

```
In [44]: def decision_tree(x1,x2,x3,x4,x5):
             y = None
              if x2 == 1:
                 y = -1
              else:
                  if x4 == 0:
                      y = 1
                  else:
                      if x1 == 1:
                          y = 1
                      else:
                          if x3 == 1:
                              y = -1
                          else:
                              y = 1
              return y
         print(decision_tree(0,0,1,1,0))
         print(decision_tree(1,1,0,1,0))
         print(decision tree(0,1,1,1,1))
         print(decision_tree(1,1,1,1,0))
         print(decision_tree(0,1,0,0,0))
         print(decision_tree(1,0,1,1,1))
         print(decision_tree(0,0,1,0,0))
         print(decision_tree(1,0,0,0,0))
         print(decision_tree(1,0,1,1,0))
         print(decision tree(1,1,1,1,1))
         print "As we can see my decision tree splits all data perfectly"
         -1
          _1
          -1
          -1
         _1
         1
```

Problem 2: Decision Trees in Python

As we can see my decision tree split all data perfectly

```
In [2]: import numpy as np
    import mltools as ml

X = np.genfromtxt('data/X_train.txt', delimiter=None)
Y = np.genfromtxt('data/Y_train.txt', delimiter=None)
X,Y = ml.shuffleData(X,Y)
# and simlarly for test data features and target values
```

2.1

```
In [86]: for i in range(1,15):
             print "Feature " + str(i) + " Max: " + str(max(X[:,i - 1])) + " Min: " + str(min(X[:,i-1])) + \
             " Mean: " + str(np.mean(X[:,i-1])) + " var: " + str(np.var(X[:,i-1]))
         Feature 1 Max: 253.0 Min: 197.0 Mean: 241.8989735 var: 81.1988159813
         Feature 2 Max: 248.0 Min: 190.0 Mean: 228.381307 var: 89.1502653418
         Feature 3 Max: 252.02 Min: 214.97 Mean: 241.9059345 var: 34.5577443467
         Feature 4 Max: 252.02 Min: 205.42 Mean: 233.8253765 var: 94.5072114082
         Feature 5 Max: 17130.0 Min: 10.0 Mean: 2849.0465 var: 10505588.3006
         Feature 6 Max: 12338.0 Min: 0.0 Mean: 862.8611 var: 3090415.20751
         Feature 7 Max: 9238.0 Min: 0.0 Mean: 163.65265 var: 698073.355698
         Feature 8 Max: 27.419 Min: 0.0 Mean: 3.0557549345 var: 7.27689094671
         Feature 9 Max: 18.107 Min: 1.2189 Mean: 6.311441945 var: 6.18300320297
         Feature 10 Max: 11.368 Min: 0.0 Mean: 1.89391480435 var: 4.15093181021
         Feature 11 Max: 18.771 Min: 0.0 Mean: 4.289551351 var: 3.94461529254
         Feature 12 Max: 14.745 Min: 0.0 Mean: 2.7977508345 var: 1.93234397277
         Feature 13 Max: 278.71 Min: 1.0271 Mean: 10.452536635 var: 170.00184292
         Feature 14 Max: 769.2 Min: -999.9 Mean: 7.65813 var: 1528.9473589
```

2.2

```
In [21]: print Y.shape
    Xtr = X[:10000,:]
    Ytr = Y[:10000]
    Xva = X[10000:,:]
    Yva = Y[10000:]
    learner = ml.dtree.treeClassify(Xtr, Ytr, maxDepth=50)
(20000,)
```

```
Training err: 0.0119
Validation err: 0.3744

2.3

In [34]: maxDepth = range(0,16)
    train_err = []
    validation_err = []
    for depth in maxDepth:
        learner = ml.dtree.treeClassify(Xtr, Ytr, maxDepth=depth)
        train_err.append(learner.err(Xtr,Ytr))
```

In [22]: print "Training err: " + str(learner.err(Xtr,Ytr))

print "Validation err: " + str(learner.err(Xva,Yva))

validation err.append(learner.err(Xva,Yva))

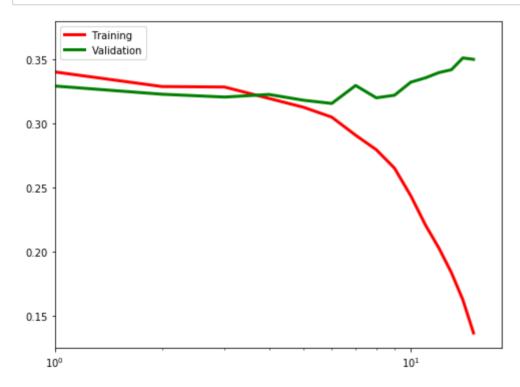
```
In [39]: import matplotlib.pyplot as plt
fig, ax = plt.subplots(1, 1, figsize=(8, 6))

# I added lw (line width) and the label.
ax.semilogx(maxDepth, train_err, 'r-', lw=3, label='Training')
ax.semilogx(maxDepth, validation_err, 'g-', lw=3, label='Validation')

# Adding a legend to the plot that will use the labels from the 'label'.
ax.legend()

# Controlling the axis.
ax.set_xlim(0, 18)

# And still doing this to clean the canvas.
plt.show()
```



According to the plot above, we can conlude that model with higher maxdepth has higher complexity. MaxDepth = 6 can provide best model

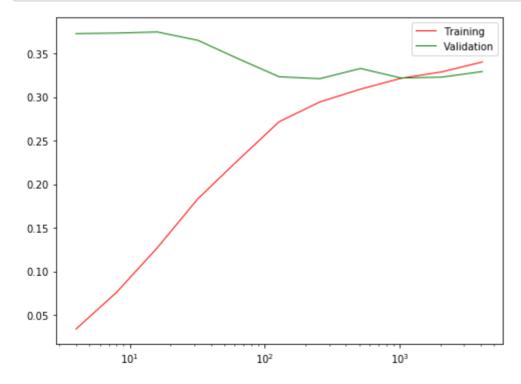
```
In [50]: minParent = [2**x for x in range(2,13)]
    train_err = []
    validation_err = []
    for parent in minParent:
        learner = ml.dtree.treeClassify(Xtr, Ytr, maxDepth=50,minParent=parent)
        train_err.append(learner.err(Xtr,Ytr))
        validation_err.append(learner.err(Xva,Yva))
```

```
In [56]: fig, ax = plt.subplots(1, 1, figsize=(8, 6))

# I added lw (line width) and the label.
ax.semilogx(minParent, train_err, 'r-', lw=1, label='Training')
ax.semilogx(minParent, validation_err, 'g-', lw=1, label='Validation')

# Adding a legend to the plot that will use the labels from the 'label'.
ax.legend()

# And still doing this to clean the canvas.
plt.show()
minParent[np.argmin(validation_err)]
```



According to the plot, we can conlude that higher minParent model has lower complexity, The best choice of minParent is 256

2.5

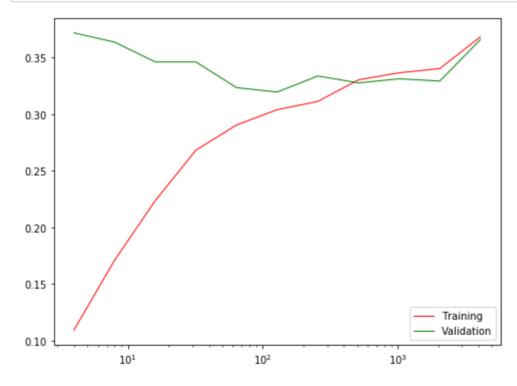
```
In [59]: minLeaves = [2**x for x in range(2,13)]
    train_err = []
    validation_err = []
    for leaf in minLeaves:
        learner = ml.dtree.treeClassify(Xtr, Ytr, maxDepth=50,minLeaf = leaf)
        train_err.append(learner.err(Xtr,Ytr))
        validation_err.append(learner.err(Xva,Yva))
```

```
In [60]: fig, ax = plt.subplots(1, 1, figsize=(8, 6))

# I added lw (line width) and the label.
ax.semilogx(minLeaves, train_err, 'r-', lw=1, label='Training')
ax.semilogx(minLeaves, validation_err, 'g-', lw=1, label='Validation')

# Adding a legend to the plot that will use the labels from the 'label'.
ax.legend()

# And still doing this to clean the canvas.
plt.show()
```



Out[60]: 128

Controling minLeaf and controling minParent might have the same effect.

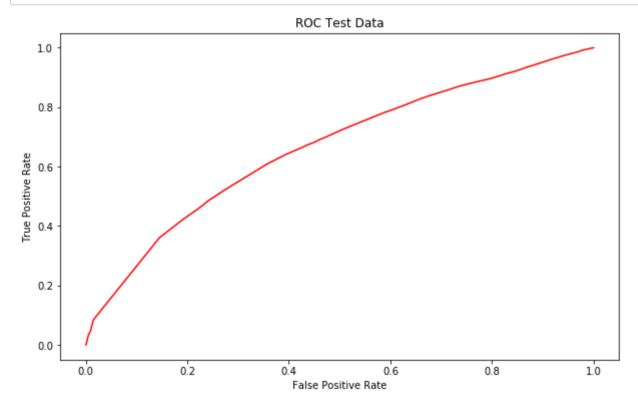


The AUC score of training data is: 0.71260139096
The AUC score of validation data is: 0.672140967409

```
In [84]: X_test = np.genfromtxt('data/X_test.txt', delimiter=None)
    Y_test = np.genfromtxt('data/Y_test.txt', delimiter=None)
    my_model = ml.dtree.treeClassify(X,Y,maxDepth=7,minParent=256)
    fprTest, tprTest, tnrTest = my_model.roc(X_test, Y_test)

from matplotlib.pyplot import figure
    figure(num=None, figsize=(10, 6), facecolor='w', edgecolor='k')
    plt.plot(fprTest, tprTest, 'r')
    plt.title('ROC Test Data')
    plt.xlabel('ratle Positive Rate')
    plt.ylabel('True Positive Rate')
    plt.legend(loc='upper right')
    plt.show()

print "The error of my model on test data is: " + str(my_model.err(X_test,Y_test))
    print "The AUC score of my model on test data is: " + str(my_model.auc(X_test,Y_test))
```



The error of my model on test data is: 0.32135
The AUC score of my model on test data is: 0.667994512393

Problem 3 Ensemble Methods (Option 1)

```
In [97]: bags = [1,5,10,25,45]
         bagTrainError = []
         bagValidationError = []
         ensembles = []
         def random forest predict(ensemble, X,Y):
             Yhat = np.zeros((X.shape[0],len(ensemble)))
             for i in range(len(ensemble)):
                 Yhat[:,i] = ensemble[i].predict(X)
             Yhat = np.mean(Yhat,axis=1)
             Yhat[Yhat > 0.5] = 1
             Yhat[Yhat <= 0.5] = 0
             return Yhat
         for bag in bags:
             print bag
             decisionTrees = bag * [None]
             for i in range(bag):
                 Xi, Yi = ml.bootstrapData(X=Xtr,Y=Ytr,n boot=10000)
                 decisionTree = ml.dtree.treeClassify(X=Xi,Y=Yi,maxDepth=16,minLeaf=4)
                 decisionTrees[i] = decisionTree
             YHatTrain = random forest predict(decisionTrees, Xtr, Ytr)
             YHatVal = random forest predict(decisionTrees, Xva, Yva)
             bagTrainError.append(np.mean(YHatTrain != Ytr))
             bagValidationError.append(np.mean(YHatVal != Yva))
             ensembles.append(decisionTrees)
         plt.plot(bags, bagTrainError, 'r', label='Training Error')
         plt.plot(bags, bagValidationError, 'q', label='Validation Error')
         plt.legend(loc='upper right')
         plt.title('Error vs number of Learners in Bag')
         plt.show()
         index = np.argmin(bagValidationError)
         print "Minimum Error on an Ensemble of Learners = ", bagValidationError[index]
         print "Number of Learners in Ensemble = ", bags[index]
```

0.35 - Training Error Validation Error 0.30 - Validation Error 0.20 - 0.15 - 0.20 - 0.15 - 0.20 - 0.15 - 0.20 - 0.15 - 0.20 - 0.15 - 0.20 - 0.15 - 0.20 -

Minimum Error on an Ensemble of Learners = 0.3034 Number of Learners in Ensemble = 25

3.2

ensemble = []

error_rate: 0.29925

In [98]:

```
for i in range(25):
    Xi, Yi = ml.bootstrapData(X=X,Y=Y,n_boot=10000)
    decisionTree = ml.dtree.treeClassify(X=Xi,Y=Yi,maxDepth=16,minLeaf=4)
    ensemble.append(decisionTree)

In [100]: test_predict = random_forest_predict(ensemble,X_test,Y_test)
    print "error rate: " + str(np.mean(test predict != Y test))
```

I choose the ensemble size = 25, and get an error rate of 0.29925 on test data set, which is an obvious improvement to my best single decision tree model

Statement of Collaboration

I obeyed the UCI Academic Honesty Policy. During my work on this assignment, I didn't discuss anything with anybody about the homework that's to say I finished all things above on my own.