



## Task 2: Tree Cutting

*Lugh Tuatha Dé* is the world's finest assassin, whom is in love with *Dia Viekone*. *Lugh* is eager to flex his financial muscle in a bid to win over *Dia's* heart. *Lugh* plans to buy an entire acre of land, carve out the shape of a **tree** with  $N$  vertices, and propose to *Dia* in front of it.

There is one problem. *Lugh* has one particular request, that **exactly** 1 edge of the tree be removed and 1 new edge added such that the **longest** path is maximised. Can you help *Lugh* impress the love of his life?

### Input

Your Program must read from standard input.

The first line contains an integer,  $N$ , the number of vertices.

In the next  $N - 1$  lines, each line contains 2 distinct integers  $u$  and  $v$ , representing an edge in the tree.

### Output

Your program must print to standard output.

The output should contain a single integer on a single line, the new longest path.

### Subtasks

The maximum execution time on each instance is 1.0s. For all testcases, the input will satisfy the following bounds:

- $1 \leq N \leq 300\,000$
- $1 \leq u, v \leq N$

Your program will be tested on input instances that satisfy the following restrictions:



Subtask	Marks	Additional Constraints
1	5	$N \leq 10$
2	10	$N \leq 100$
3	10	$N \leq 3000$
4	20	$N \leq 300\,000$ , there is at most one vertex with degree $\geq 3$
5	55	-

## Sample Testcase 1

This testcase is valid for all subtasks.

Input	Output
4 1 2 1 3 3 4	3

## Sample Testcase 1 Explanation

No matter which edge we choose to remove, we cannot increase the longest path on the tree beyond 3.

## Sample Testcase 2

This testcase is valid for all subtasks

Input	Output
6 1 2 2 3 2 5 4 5 5 6	5

## Sample Testcase 2 Explanation

We can remove edge 2 — 5, this splits the tree into 2 components containing:

1. Vertices 1, 2 and 3
2. Vertices 4, 5 and 6



Next, we can add a new edge  $3 - 4$ , the longest path will now be  $1 - 2 - 3 - 4 - 5 - 6$  with a length of 5.