

# Homework #1

Student: *Le Yang 1751894*

---

Course: *Digital Image Processing (42033501)* – Professor: *Dr. Qingjiang Shi*  
Due date: *March 28th, 2025*

---

## 1. Denosing for Astrophotography

a) To generate a single denoised image from each video, compute a running average of the frames  $f^t$  ( $t = 1, 2, \dots$ ) in the video without frame alignment, according to the following update rule:

$$f_{average}^1 = f^1$$
$$f_{average}^t = \frac{t-1}{t} f_{average}^{t-1} + \frac{1}{t} f^t$$

Display and submit  $f_{average}^t$  at  $t = 30$  for each video. Comment on how effectively the noise is reduced and how much the sharp features are blurred by the averaging operation.

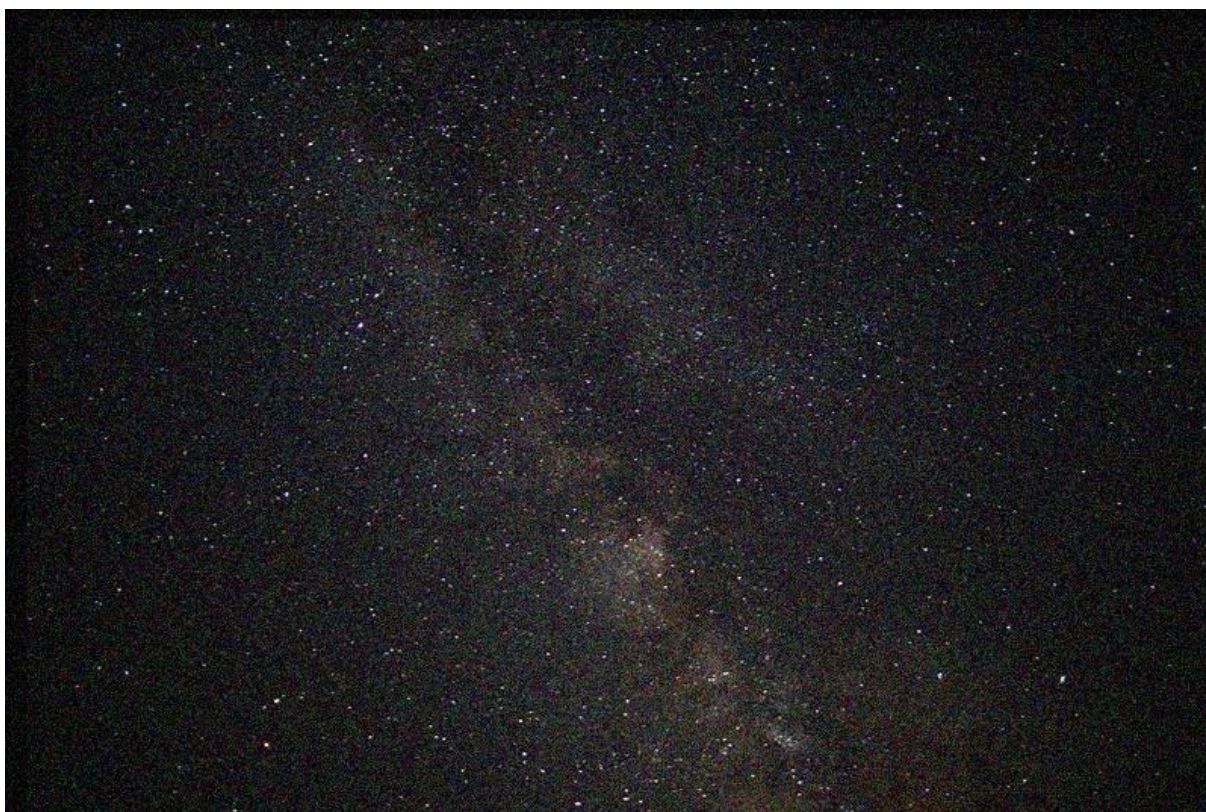


Figure 1: origin 30rd frame of sky\_1



Figure 2: origin 30rd frame of sky\_2

**Answer:** First, I generate the two origin 30rd frames of the two videos for comparison. The corresponding Matlab code is **origin.m**. This code generate two images: **sky1origin\_30.jpg**, **sky2origin\_30.jpg**. They are shown as **Figure 1** and **Figure 2**. Then I use the update rule in the question to denoise the image. My Matlab code is followed and is saved as **without\_align.m**, this code generate two  $f_{average}^t$  at 30rd frame of each video which are shown as **Figure 3** and **Figure 4** below.

```

1      %without_align.m
2      clc,clear;
3      vidobj_1=VideoReader("hw1_sky_1.avi");
4      numFrames_1=vidobj_1.NumberOfFrames;
5
6      vidobj_2=VideoReader("hw1_sky_2.avi");
7      numFrames_2=vidobj_2.NumberOfFrames;
8
9      for i=1:numFrames_1
10         frame_1=im2double(read(vidobj_1,i));
11         image_name_1=strcat('result\sky1woalign_',num2str(i));
12         image_name_1=strcat(image_name_1, '.jpg');
13
14         frame_2=im2double(read(vidobj_2,i));
15         image_name_2=strcat('result\sky2woalign_',num2str(i));
16         image_name_2=strcat(image_name_2, '.jpg');
17         if(i==1)

```



```
18         f_average_1=frame_1;
19         f_average_2=frame_2;
20     else
21         f_average_1=(i-1)/i*f_average_1+frame_1/i;
22         f_average_2=(i-1)/i*f_average_2+frame_2/i;
23     end
24
25     if(i==30)
26         woalign_1=f_average_1;
27         imwrite(woalign_1,image_name_1,'jpg');
28         woalign_2=f_average_2;
29         imwrite(woalign_2,image_name_2,'jpg');
30         break;
31     end
32 end
```

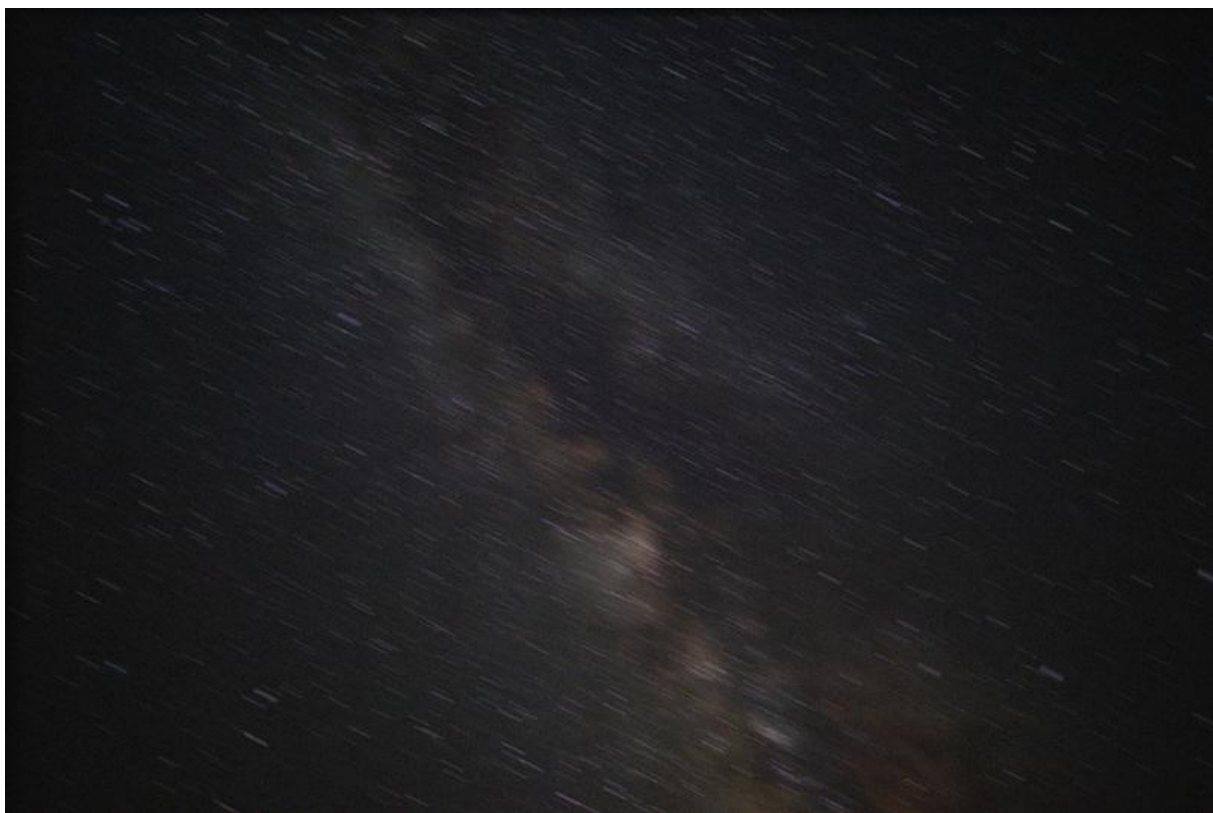


Figure 3:  $f_{average}^t$  at 30rd frame of sky\_1



Figure 4:  $f_{average}^t$  at 30rd frame of sky\_2

From the results above, we can see that we reduce the noise in the video to some extent by computing the running average of the frames. It is more easy to recognize in the sky2 video with the moon in the sky because the noise spots mix with stars in the sky1 video. Compared to **Figure 2**, we can see that in **Figure 4**, all the noise spots around the moon are removed. However, because we don't utilize frame alignment, we can see that many sharp features are blurred by the averaging operation like the edges of the moon in sky2 and stars in sky1. As a result, it is hard to see some details.

b) Now, compute a running average of the frames with frame alignment, according to the following update rule:

$$f_{average}^1 = f^1$$

$$f_{average}^t = \frac{t-1}{t} f_{average}^{t-1} + \frac{1}{t} \text{Align}(f^t, f_{average}^{t-1}), t = 2, 3, \dots$$

Display and submit  $f_{average}^t$  at  $t = 30$  for each video. Compare to the result in (a) and comment on how effectively noise is reduced while sharp features are better preserved.

**Answer:** I use the update rule in the question to denoise the image with frame alignment. My Matlab code is followed and is saved as **with\_align.m**, this code generate

two  $f_{average}^t$  at 30rd frame of each video which are shown as **Figure 5** and **Figure 6** below.

```
1      %with_align.m
2      clc,clear;
3      vidobj_1=VideoReader("hw1_sky_1.avi");
4      numFrames_1=vidobj_1.NumberOfFrames;
5
6      vidobj_2=VideoReader("hw1_sky_2.avi");
7      numFrames_2=vidobj_2.NumberOfFrames;
8
9      for i=1:numFrames_1
10         frame_1=im2double(read(vidobj_1,i));
11         image_name_1=strcat('result\sky1wialign_',num2str(i));
12         image_name_1=strcat(image_name_1, '.jpg');
13         frame_2=im2double(read(vidobj_2,i));
14         image_name_2=strcat('result\sky2wialign_',num2str(i));
15         image_name_2=strcat(image_name_2, '.jpg');
16         if(i==1)
17             f_average_1=frame_1;
18             f_average_2=frame_2;
19         else
20             f_average_1=(i-1)/i*f_average_1+Align(frame_1,f_average_1)/i;
21             f_average_2=(i-1)/i*f_average_2+Align(frame_2,f_average_2)/i;
22         end
23
24         if(i==30)
25             wialign_1=f_average_1;
26             imwrite(wialign_1,image_name_1, 'jpg');
27             wialign_2=f_average_2;
28             imwrite(wialign_2,image_name_2, 'jpg');
29             break;
30         end
31     end
```



Figure 5:  $f_{average}^t$  at 30rd frame of sky\_1



Figure 6:  $f_{average}^t$  at 30rd frame of sky\_2

From the results above, we can see that with frame alignment the bluriness is reduced and we also remove the noise effectively.

## 2. Nighttime Road Contrast Enhancement

a) Plot and submit the histogram (MATLAB function: `imhist`) of the original images grayscale values. Briefly comment on the shape of each histogram.

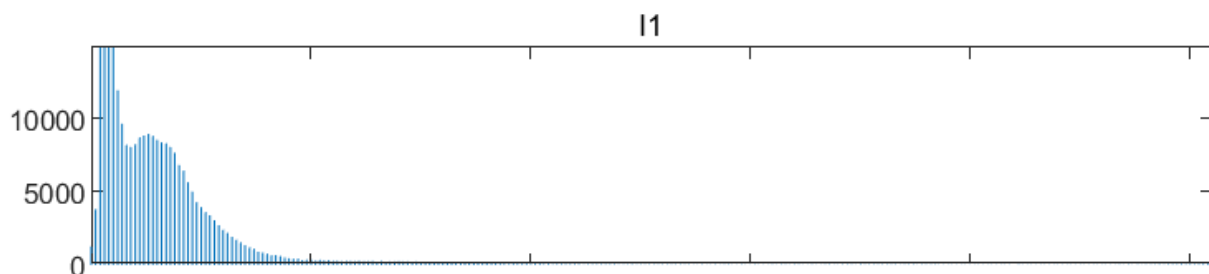


Figure 7: histogram of road1

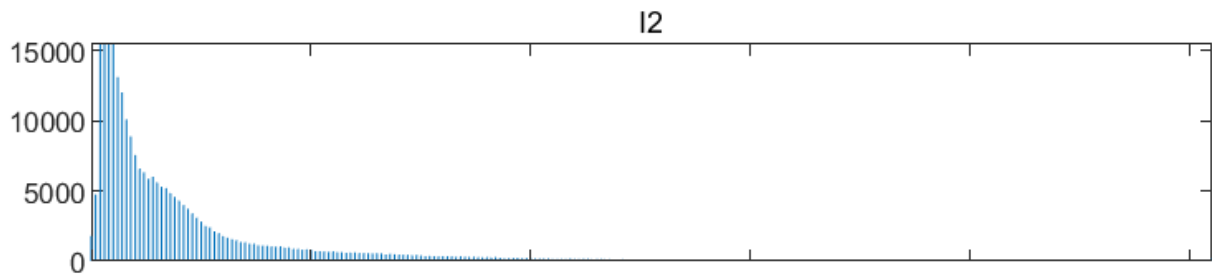


Figure 8: histogram of road2

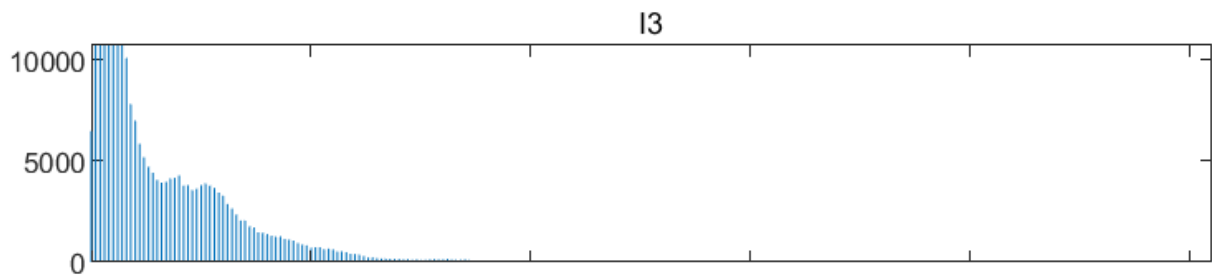


Figure 9: histogram of road3

**Answer.** The three images above are the histograms of the three origin images grayscale values. We can see that the contrast of the picture is very low, and the gray level is concentrated in the lower range. My Matlab code is followed and is saved as **a.m**

```

1  clc,clear;
2  I1=imread("hw1_dark_road_1.jpg");
3  I2=imread("hw1_dark_road_2.jpg");
4  I3=imread("hw1_dark_road_3.jpg");
5  figure('name','histogram','NumberTitle','off');
6  subplot(3,1,1);
7  imhist(I1);           %display the origin image
8  title("I1");
9  subplot(3,1,2);
10 imhist(I2);           %display the origin hist
11 title("I2");
12 subplot(3,1,3);
13 imhist(I3);           %display the origin hist
14 title("I3");

```

b) Apply global histogram equalization to the original image. Display and submit the modified image. Plot and submit the histogram of the modified images grayscale values. Comment on visually desirable/undesirable regions in the modified image.





Figure 10: image of road1 after apply global histogram equalization

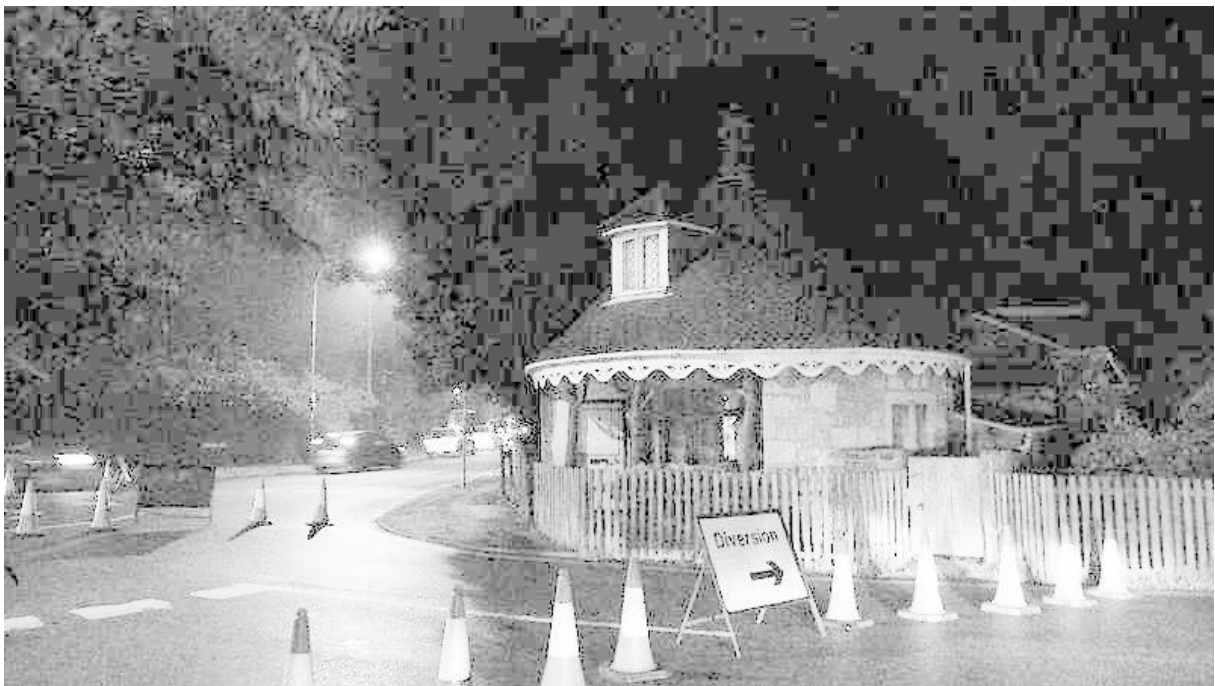


Figure 11: image of road2 after apply global histogram equalization



Figure 12: image of road3 after apply global histogram equalization

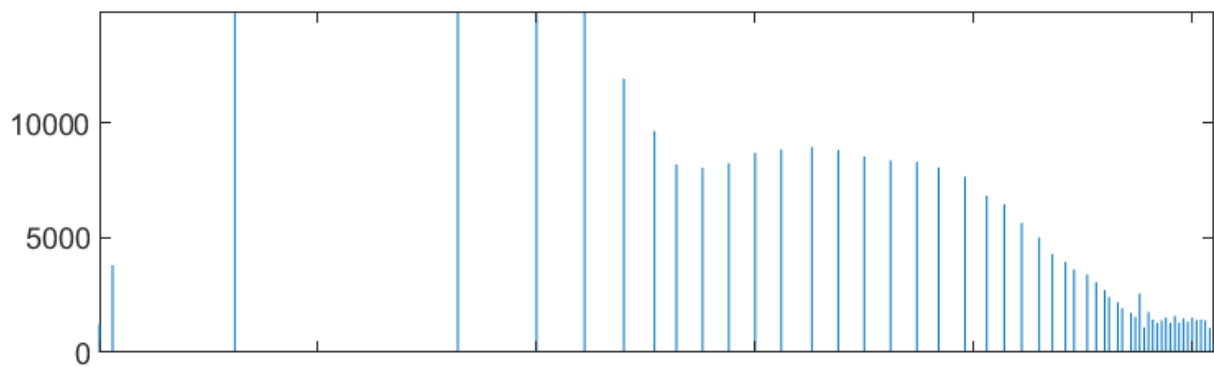


Figure 13: histogram of road1 after apply global histogram equalization

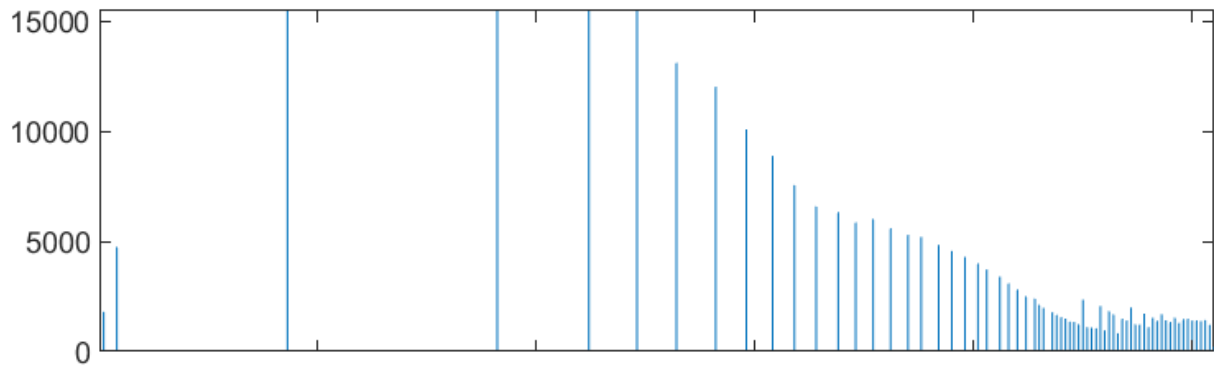


Figure 14: histogram of road2 after apply global histogram equalization

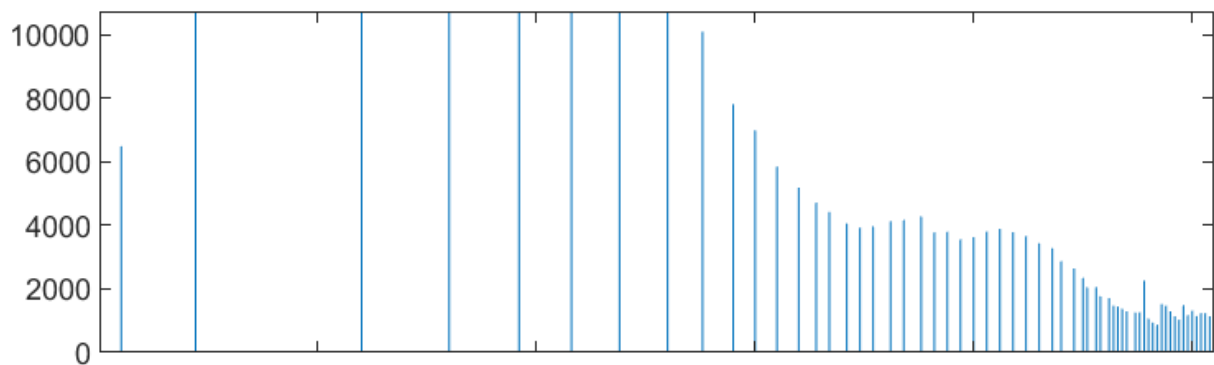


Figure 15: histogram of road3 after apply global histogram equalization

**Answer.** Figure 10-12 are the images after applying global histogram equalization to the origin images. My Matlab code is followed and is saved as **b.m**

```

1  clc,clear;
2  I1=imread("hw1_dark_road_1.jpg");
3  I2=imread("hw1_dark_road_2.jpg");
4  I3=imread("hw1_dark_road_3.jpg");
5  I1_process=myhisteq(I1);
6  I2_process=myhisteq(I2);
7  I3_process=myhisteq(I3);
8
9  figure('name','road1','NumberTitle','off');
10
11  subplot(2,1,1);
12  imshow(I1_process);           %display the MY process image
13  imwrite(I1_process,"result/I1_global.jpg","jpg");
14
15  subplot(2,1,2);
16  imhist(I1_process);           %display the MY process hist
17
18  figure('name','road2','NumberTitle','off');
19
20  subplot(2,1,1);
21  imshow(I2_process);           %display the MY process image
22  imwrite(I2_process,"result/I2_global.jpg","jpg");
23

```

```

24     subplot(2,1,2);
25     imhist(I2_process);           %display the MY process hist
26
27     figure('name','road3','NumberTitle','off');
28
29     subplot(2,1,1);
30     imshow(I3_process);           %display the MY process image
31     imwrite(I3_process,"result/I3_global.jpg","jpg");
32
33     subplot(2,1,2);
34     imhist(I3_process);           %display the MY process hist

```

c) Apply locally adaptive histogram equalization to the original image. Display and submit the modified image. Plot and submit the histogram of the modified images grayscale values. Choose and report the number of tiles and the clipping limit for attaining higher contrast while avoiding the generation of noisy regions and the amplification of nonuniform lighting effects. Comment on the subjective quality of the modified image compared to the result in (b).



Figure 16: image of road1 after apply local adaptive histogram equalization





Figure 17: image of road2 after apply local adaptive histogram equalization



Figure 18: image of road3 after apply local adaptive histogram equalization

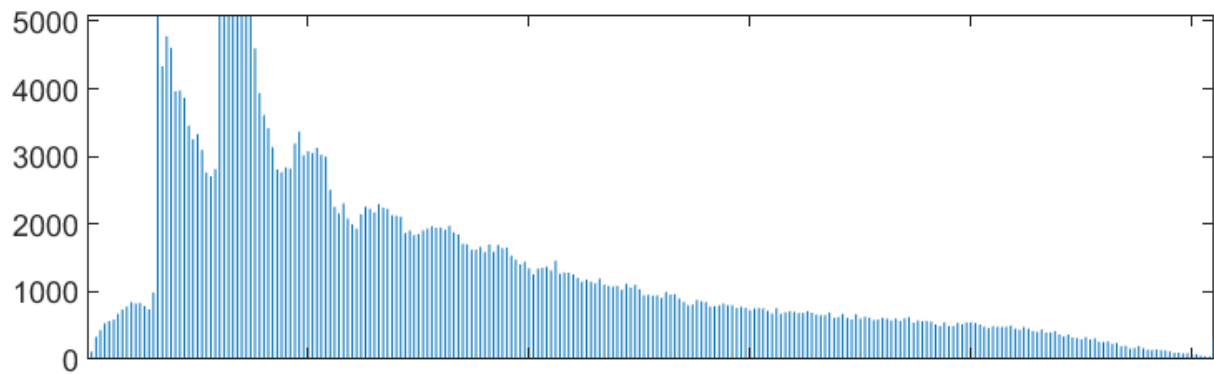


Figure 19: histogram of road1 after apply local adaptive histogram equalization

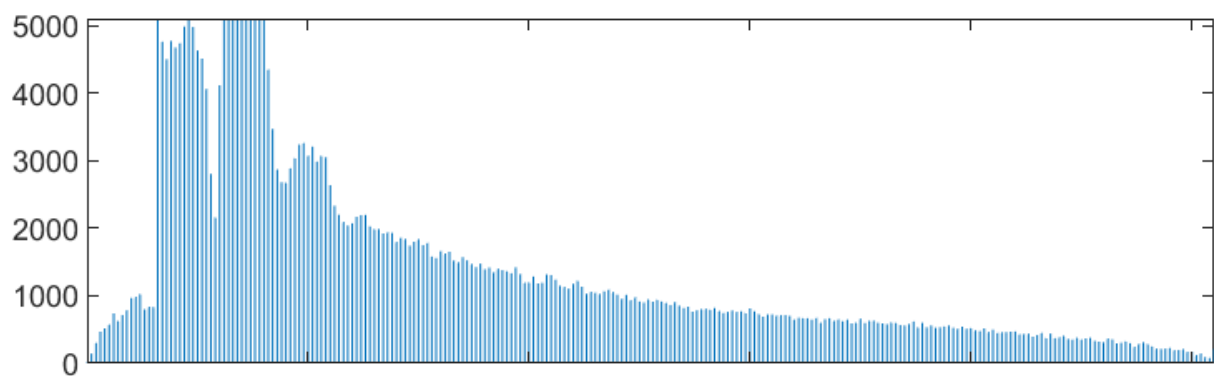


Figure 20: histogram of road2 after apply local adaptive histogram equalization

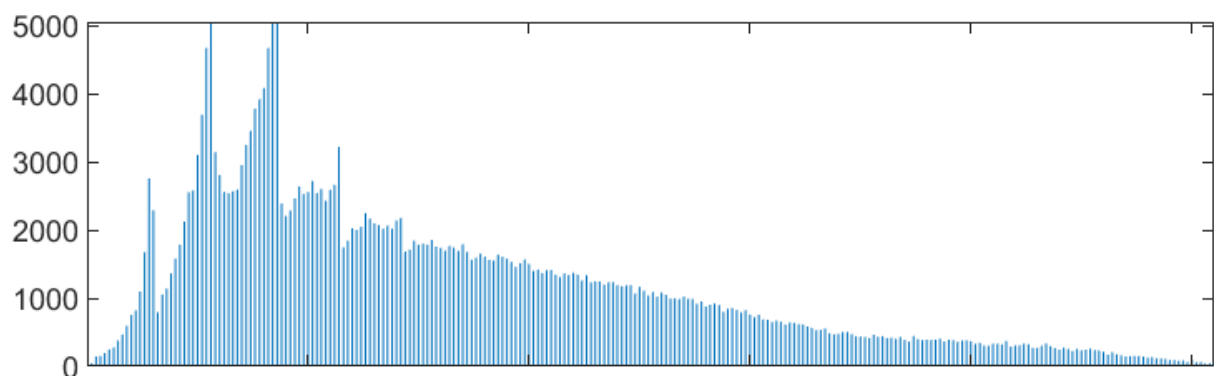


Figure 21: histogram of road3 after apply local adaptive histogram equalization

**Answer.** Figure 16-18 are the images after applying local adaptive histogram equalization to the origin images. My Matlab code is followed and is saved as **c.m**

```
1   clc,clear;
2   I1=imread("hw1_dark_road_1.jpg");
3   I2=imread("hw1_dark_road_2.jpg");
4   I3=imread("hw1_dark_road_3.jpg");
5
6   I1_process=adapthisteq(I1,'NumTiles',[25 25],'ClipLimit',0.05);
```

```
7     I2_process=adapthisteq(I2, 'NumTiles', [25 25], 'ClipLimit', 0.05);
8     I3_process=adapthisteq(I3, 'NumTiles', [25 25], 'ClipLimit', 0.05);
9
10    figure('name', 'road1', 'NumberTitle', 'off');
11
12    subplot(2,1,1);
13    imshow(I1_process);           %display the process image
14    imwrite(I1_process, "result/I1_local.jpg", "jpg");
15
16    subplot(2,1,2);
17    imhist(I1_process);           %display the process hist
18
19    figure('name', 'road2', 'NumberTitle', 'off');
20
21    subplot(2,1,1);
22    imshow(I2_process);           %display the process image
23    imwrite(I2_process, "result/I2_local.jpg", "jpg");
24
25    subplot(2,1,2);
26    imhist(I2_process);           %display the process hist
27
28    figure('name', 'road3', 'NumberTitle', 'off');
29
30    subplot(2,1,1);
31    imshow(I3_process);           %display the process image
32    imwrite(I3_process, "result/I3_local.jpg", "jpg");
33
34    subplot(2,1,2);
35    imhist(I3_process);           %display the process hist
```

d) Apply a -nonlinearity mapping to each image to perform contrast enhancement, show the new image, and submit the displayed image. For each image, find and report a value of that allows you to see more details.



Figure 22: image of road1 after apply  $\gamma$ -nonlinearity mapping



Figure 23: image of road2 after apply  $\gamma$ -nonlinearity mapping





Figure 24: image of road3 after apply  $\gamma$ -nonlinearity mapping

**Answer.** The images above are processed images after apply  $\gamma$ -nonlinearity mapping, the value of  $\gamma$  is 0.5. My Matlab code is followed and is saved as **d.m**

```
1  clc,clear;
2  I1=imread("hw1_dark_road_1.jpg");
3  I2=imread("hw1_dark_road_2.jpg");
4  I3=imread("hw1_dark_road_3.jpg");
5
6  I1_process=gama(im2double(I1),0.5);
7  figure('name','', 'NumberTitle','off');
8  imshow(I1_process);           %display the process image
9  imwrite(I1_process,"result/I1_gama.jpg","jpg");
10
11 I2_process=gama(im2double(I1),0.5);
12 figure('name','', 'NumberTitle','off');
13 imshow(I2_process);           %display the process image
14 imwrite(I2_process,"result/I2_gama.jpg","jpg");
15
16 I3_process=gama(im2double(I1),0.5);
17 figure('name','', 'NumberTitle','off');
18 imshow(I3_process);           %display the process image
19 imwrite(I3_process,"result/I3_gama.jpg","jpg");
```