



Functions

Data

Today's Superpower

Interweaving functions and
data structures for much
goodness.



Quick Recap

```
double [] = []  
double (x:xs) = 2*x : double fn xs
```

```
Prelude> double [ 1, 2, 3 ]
```

[1, 2, 3]
 ↓ ↓ ↓
 (*2) (*2) (*2)
 ↓ ↓ ↓
[2, 4, 6]

```
sumList [] = 0  
sumList (x:xs) = x + sumList xs  
Prelude> sumList [ 1, 2, 3 ]
```

```
sumList [ 1, 2, 3 ]  
sumList 1 : 2 : 3 : []  
  
1 + sumList 2 : 3 : []  
1 + 2 + sumList 3 : []  
1 + 2 + 3 + sumList []  
1 + 2 + 3 + 0  
  
6
```

```
double [] = []  
double (x:xs) = 2*x : double xs
```

```
wordLen [] = []  
wordLen (x:xs) = length x : wordLen xs
```

```
rem7 [] = []  
rem7 (x:xs) = rem x 7 : rem7 xs
```

```
double [1,2,3]          => [2,4,6]
```

```
wordLen ["bee","deer","egret"] => [3,4,5]
```

```
rem7 [6,7,8]            => [6,0,1]
```

```
double [] = []  
double (x:xs) = 2*x : double xs  
  
wordLen [] = []  
wordLen (x:xs) = length x : wordLen xs  
  
rem7 [] = []  
rem7 (x:xs) = rem x 7 : rem7 xs
```

Three different functions

But not that different-what **two** things
differentiates each from the others?

Function name

~~double wordLen rem7~~

The function applied to each element
(***2**), **length**, (**flip rem 7**)

```
double [] = []  
double (x:xs) = 2*x : double xs  
  
wordLen [] = []  
wordLen (x:xs) = length x : wordLen xs  
  
rem7 [] = []  
rem7 (x:xs) = rem x 7 : rem7 xs
```

```
mapper _fn [] = []  
  
mapper fn (x:xs) = fn x : mapper fn xs
```

Three different functions

What differentiates each from the others?

The function applied to each element
*(*2), length, (flip rem 7)*

```
*Main> mapper (*4) [1,2,3]  
[4,8,12]
```

```
*Main> mapper length ["ant","bear"]  
[3,4]
```

```
*Main> mapper (flip rem 7) [6,7,8]  
[6,0,1]
```

```
mapper _fn []      = []  
mapper  fn (x:xs) = fn x : mapper fn xs
```

Standard Haskell library function: **map**

```
*Main> map (*4) [1,2,3]  
[4,8,12]
```

```
*Main> map length ["ant","bear"]  
[3,4]
```

```
*Main> map (flip rem 7) [6,7,8]  
[6,0,1]
```



```
double [] = []  
double (x:xs) = 2*x : double fn xs  
  
Prelude> double [ 1, 2, 3 ]
```

[1, 2, 3]

↓ ↓ ↓
(*2) (*2) (*2)

↓ ↓ ↓
[2,]

```
sumList [] = 0  
sumList (x:xs) = x + sumList xs  
Prelude> sumList [ 1, 2, 3 ]
```

sumList [1, 2, 3]

sumList 1 : 2 : 3 : []

1 + sumList 2 : 3 : []

1 + 2 + sumList 3 : []

1 + 2 + 3 + sumList []

1 + 2 + 3 + 0

6

```
sumList [] = 0
sumList (x:xs) = x + sumList xs
```

```
timesList [] = 1
timesList (x:xs) = x * timesList xs
```

```
len [] = 0
len (x:xs) = 1 + len xs
```

What **two** things differentiates each function from the others?

The function applied to each element

$(x+y)$, $(x*y)$, $(1+y)$

The initial (empty list) value

0, 1, 0

```
reduce _fn value [] = value
reduce fn value (x:xs) = reduce fn (fn value x) xs
```

```
reduce _fn value [] = value
reduce  fn value (x:xs) = reduce fn (fn value x) xs
```

```
reduce (+) 0 [1,2,3]
reduce (+) (value + x) [2, 3]
reduce (+) (0 + 1) [2, 3]
reduce (+) (1 + 2) [3]
reduce (+) (3 + 3) []
6
```

Haskell calls this function a *fold*.

Because it consumes data from the left, its name is **foldl**

Map

```
double [] = []  
double (x:xs) = 2*x : double fn xs
```

```
Prelude> double = map (*2)
```

Use **map** to transform a list into another list by applying a function to each element in turn.

Fold

```
sumList [] = 0  
sumList (x:xs) = x + sumList xs
```

```
Prelude> sumList = foldl (+) 0
```

Use **fold** to reduce a list into a single value.

(The single value might itself be a list...)

Quick lab...

Let's play with `map` and `foldl` using GHCi.

- Use `map` to convert a list of strings to a list of those strings' lengths.
- A convenient way to see if two words are anagrams is to sort the letters in each. If the sorted values are the same, then the two words contain the same letters, and are anagrams. Write a function that takes a list of words and returns a list of each word sorted. (So `["ant", "cat", "tan"]` would return `["ant", "act", "ant"]`)
- Use `reduce` to find the largest value in a list of positive numbers. The largest value in an empty list is zero.
- Use `reduce` to concatenate the values in a list of strings (the `++` operator merges two strings)

```
double [] = []  
double (x:xs) = 2*x : double fn xs
```

```
Prelude> double = map (*2)
```

```
sumList [] = 0  
sumList (x:xs) = x + sumList xs
```

```
Prelude> sumList = foldl (+) 0
```

Defining Data Types

Switch:

On

Off



In code:

```
// Boolean  
switch = true  
switch = false
```


Switch:



In code:

```
// String  
switch = "closed"  
switch = "open"
```

Switch:

On



Off



In code:

```
// Integer  
switch = 1  
switch = 0
```

Switch:



In code:

```
// Object  
switch = new Switch()  
switch.close()  
switch.open()
```

*All I wanted was a variable
that can just hold two values!*

Switch:

On

Off



In Haskell:

```
data Switch = SwitchOn | SwitchOff
```

```
switch = SwitchOn
```

```
other
```

```
data Switch = SwitchOn | SwitchOff
```

```
sw1 = SwitchOn
```

```
sw2 = SwitchOff
```

```
data Switch = SwitchOn | SwitchOff
```

```
sw1 = SwitchOn
```

```
sw2 = SwitchOff
```

```
toggle SwitchOn  = SwitchOff
```

```
toggle SwitchOff = SwitchOn
```

```
sw1' = toggle sw1
```

```
roomLights = [ SwitchOn, SwitchOn, SwitchOff ]
```

```
newScene = map toggle roomLights
```

```
data Switch = SwitchOn | SwitchOff
```

```
sw1 = SwitchOn
```

```
sw2 = SwitchOff
```

```
toggle SwitchOn  = SwitchOff
```

```
toggle SwitchOff = SwitchOn
```

```
sw1' = toggle sw1
```

```
roomLights = [ SwitchOn, SwitchOn, SwitchOff ]
```

```
newScene = map toggle roomLights
```

All you can do with type Switch is assign it and pattern match against it. You can't even do `show sw1`

```
data Switch = SwitchOn | SwitchOff
```

```
  Deriving (Show, Eq)
```

```
sw1 = SwitchOn
```

```
sw2 = SwitchOff
```

```
toggle SwitchOn  = SwitchOff
```

```
toggle SwitchOff = SwitchOn
```

```
sw1' = toggle sw1
```

```
roomLights = [ SwitchOn, SwitchOn, SwitchOff ]
```

```
newScene = map toggle roomLights
```

Deriving tells Haskell to apply some defaults for common capabilities (such as showing, equality, and ...)

100%
:
50%
:
Off



In Haskell:

```
data Dimmer = DimmerOff |  
             DimmerOn Float
```

100%
:
50%
:
Off



In Haskell:

```
data Dimmer = DimmerOff |  
              DimmerOn Float
```

```
dim1 = DimmerOn 50
```

```
dim2 = DimmerOn 80
```

```
dim3 = DimmerOff
```

100%
:
50%
:
Off



In Haskell:

```
data Dimmer = DimmerOff |  
              DimmerOn Float  
  
dim1 = DimmerOn 50  
dim2 = DimmerOn 80  
dim3 = DimmerOff  
  
isBright DimmerOff = False  
isBright (DimmerOn pc) = pc >= 75
```

100%
:
50%
:
Off



In Haskell:

```
data Dimmer = DimmerOff |  
              DimmerOn Float  
  
dim1 = DimmerOn 50  
dim2 = DimmerOn 80  
dim3 = DimmerOff  
  
isBright DimmerOff = False  
isBright (DimmerOn pc) = pc >= 75  
  
isBright dim1      -- False  
isBright dim2      -- True  
isBright dim3      -- False
```

*I think that I shall never see
A poem lovely as a tree.*

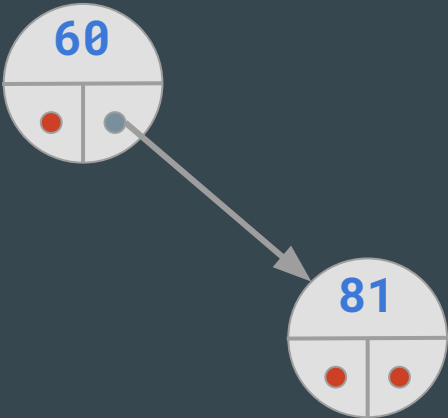
Joyce Kilmer



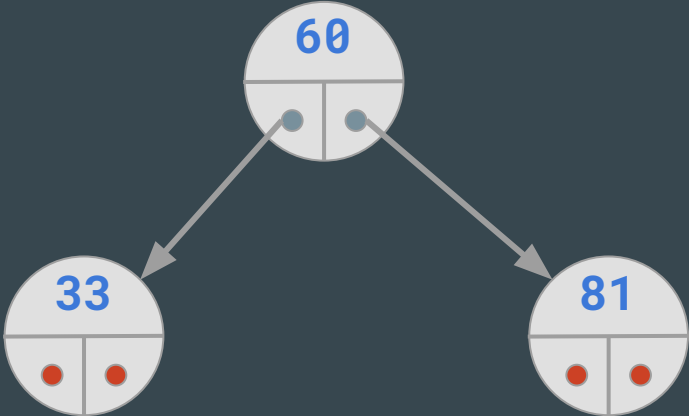
tree = Empty
Add 60



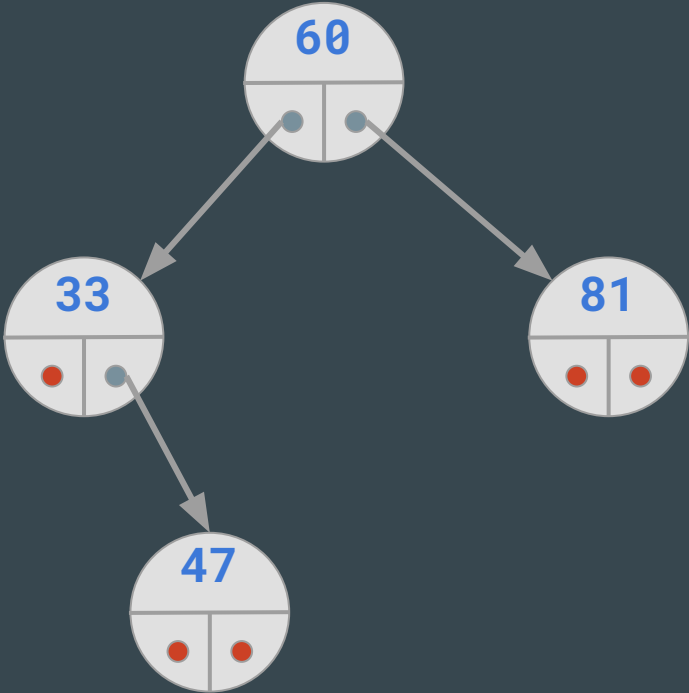
tree = Empty
Add 60
Add 81



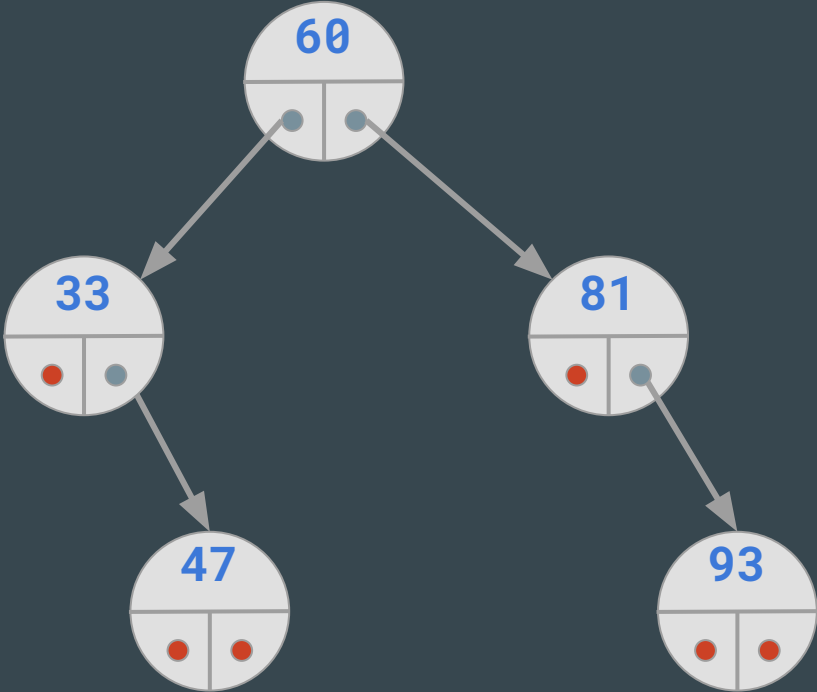
tree = Empty
Add 60
Add 81
Add 33



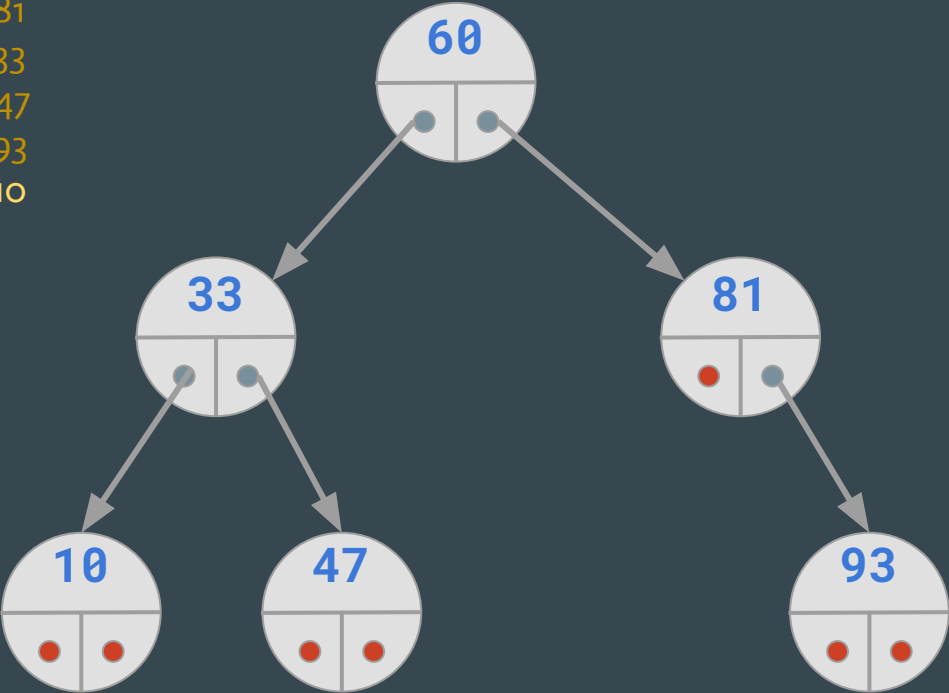
tree = Empty
Add 60
Add 81
Add 33
Add 47

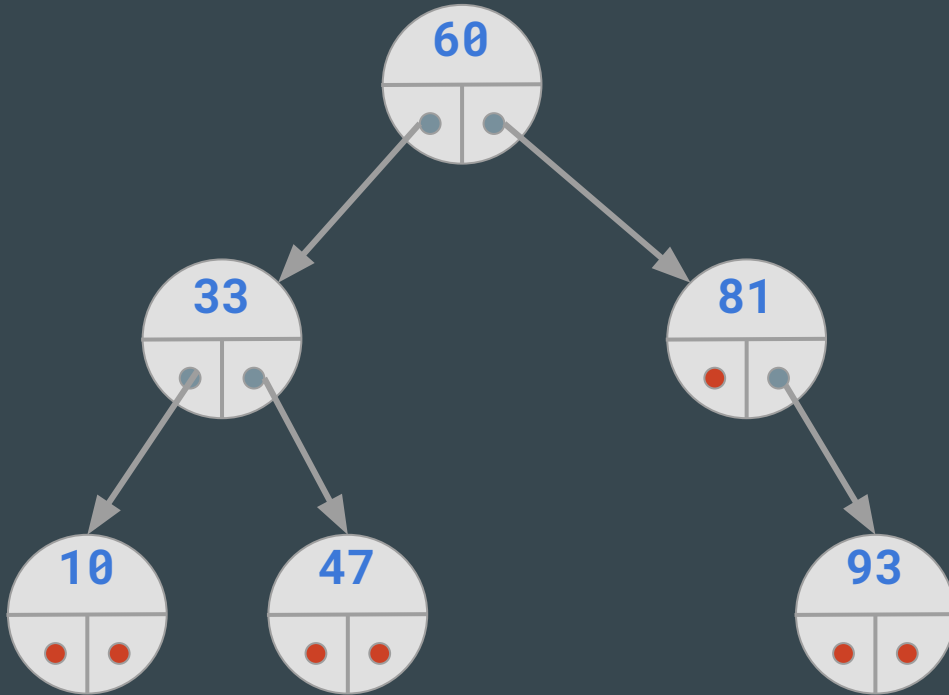


tree = Empty
Add 60
Add 81
Add 33
Add 47
Add 93



tree = Empty
Add 60
Add 81
Add 33
Add 47
Add 93
Add 10





A Tree is:

Value: (integer)

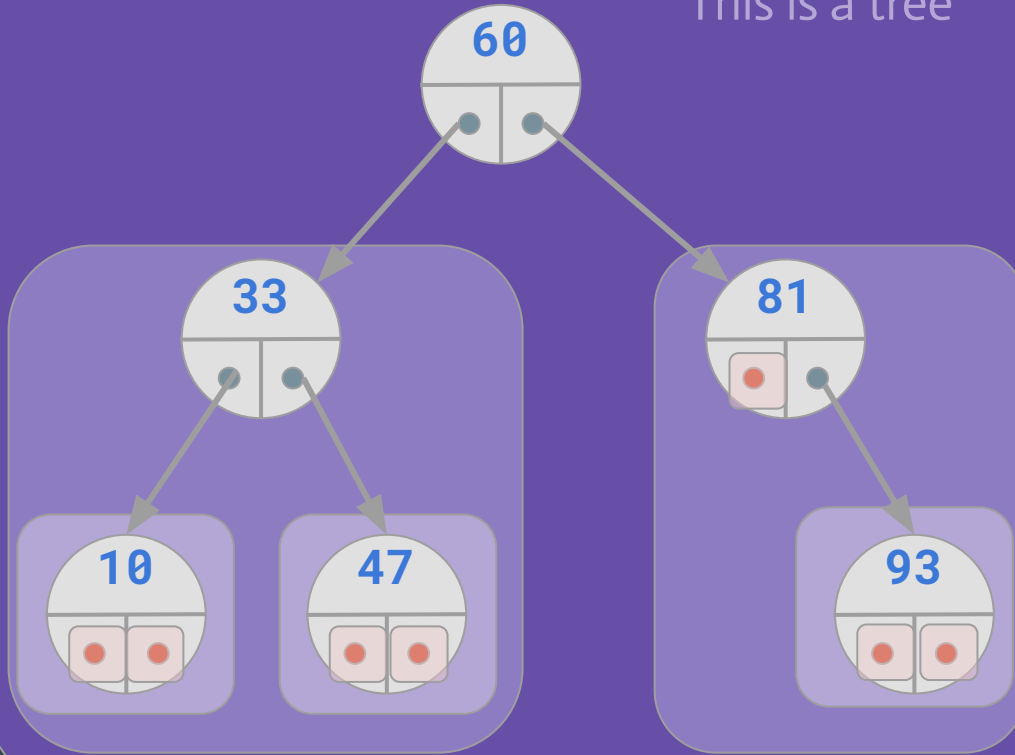
Left child: Tree

Right child: Tree

-or-

Empty

This is a tree



A Tree is:

Value: (integer)

Left child: Tree

Right child: Tree

-or-

Empty

```
data Tree = Empty
          | Branch Tree Tree Integer
          deriving (Show, Eq)
```

A Tree is:

Value:	(integer)
Left child:	Tree
Right child:	Tree

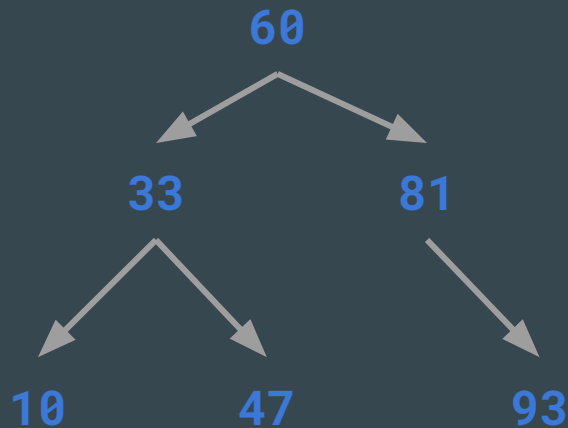
-or-

Empty

```
data Tree = Empty
          | Branch Tree Tree Integer
          deriving (Show, Eq)
```

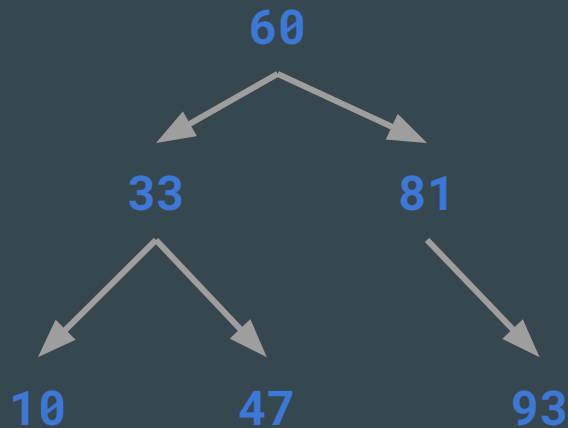
Branch

```
(Branch
  (Branch
    (Branch Empty Empty 10)
    (Branch Empty Empty 47)
    33
  )
  (Branch
    Empty
    (Branch Empty Empty 93)
    81
  )
  60
```




```
data Tree = Empty
          | Branch Tree Tree Integer
          deriving (Show, Eq)
```

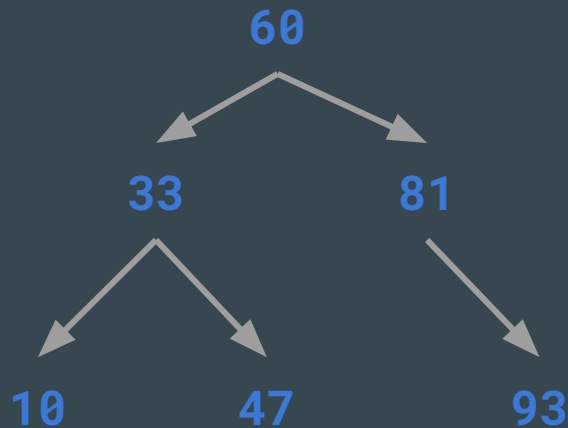
```
tsum Empty = 0
tsum (Branch left right value) =
    value + tsum left + tsum right
```



```
data Tree = Empty
          | Branch Tree Tree Integer
          deriving (Show, Eq)

tfold fn initialValue Empty = initialValue
tfold fn initialValue (Branch l r v) =
  fn v (fn foldLeftChild foldRightChild)
  where
    foldLeftChild  = doFold l
    foldRightChild = doFold r
    doFold = tfold fn initialValue

tsum :: Tree -> Integer
tsum = tfold (+) 0
```



```
tadd :: Tree -> Integer -> Tree
tadd Empty value = Branch Empty Empty value
tadd (Branch l r nodeValue) newValue
  | newValue < nodeValue = Branch (tadd l newValue) r nodeValue
  | otherwise           = Branch l (tadd r newValue) nodeValue

tbuild :: [Integer] -> Tree
tbuild = foldl tadd Empty
```

```
Prelude> tbuild [6,5,9]
```

```
Branch (Branch Empty Empty 5) (Branch Empty Empty 9) 6
```

Homework...

Due Tuesday, May 11

Fork and clone the repo <https://github.com/Eastside-FP/dayfive> You'll be working on code the the `assignment/` directory, and submitting using a pull request.

Fork and clone the repo <https://github.com/Eastside-FP/dayfive>. You'll be working on code the the `assignment/` directory, and submitting using a pull request.

In that directory, you'll find the file `assignment.hs`.

It contains placeholders for code that you'll write, along with a set of tests.

Update the placeholders to make them do what the description says, and so that the tests pass.