6/22/2014 Minimum distance

## **Minimum-Distance Classifiers**

Template matching can easily be expressed mathematically. Let  $\mathbf{x}$  be the feature vector for the unknown input, and let  $\mathbf{m}_1$ ,  $\mathbf{m}_2$ , ...,  $\mathbf{m}_c$  be templates (i.e., perfect, noise-free feature vectors) for the c classes. Then the error in matching  $\mathbf{x}$  against  $\mathbf{m}_k$  is given by

$$\|\mathbf{x} - \mathbf{m}_k\|$$
.

Here  $\| \mathbf{u} \|$  is called the **norm** of the vector  $\mathbf{u}$ . A minimum-error classifier computes  $\| \mathbf{x} - \mathbf{m}_k \|$  for k = 1 to c and chooses the class for which this error is minimum. Since  $\| \mathbf{x} - \mathbf{m}_k \|$  is also the distance from  $\mathbf{x}$  to  $\mathbf{m}_k$ , we call this a **minimum-distance** classifier. Clearly, a template matching system is a minimum-distance classifier.

