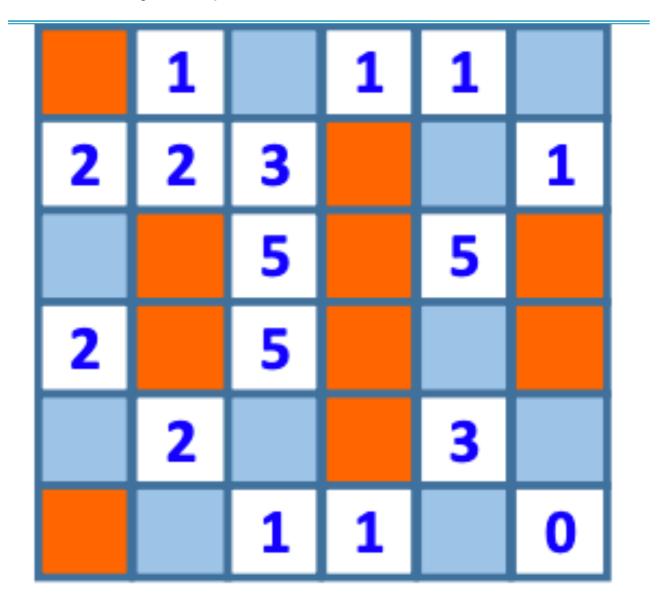
# CSP - Minesweeper

## **Introduction to Artificial Intelligence Project 2**

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## **Task Description**

Solve a classic game - "MineSweeper" by seeing it as a CSP problem.

Design a backtracking algorithm for it.

Discuss difference when applying different strategy listed below:

Forward Checking, MRV heuristic, Degree heuristic, LCV heuristic

I also proposed a cut named CUTA,

if a variable cannot be assign to any variables in the node, all siblings need not to be explored

## **Implementation Details**

Language and Tools:

- 1. Python 3
- 2. Editor: Jupyter Notebook
- 3. Version Control: git
- 4. Report: Mac OS Pages

Interactive programming and experimentations

Use flag to control usage of heuristic

An independent solver is available ("solver.py")

Usage:

- 1. python3 solver.py
- 2. Use STD in to input the constraints like in the HW spec
  - A string in one line in format "n m #mine board(n\*m)"

## **Experiments**

#### **Performance Evaluation**

For evaluation of performance of algorithms,

I choose three features described as follow:

- Node\_pushed
- Compare with node\_popped can see how heuristics do in the sense of "variable visit order"
  - Node\_popped
    - # node popped, ~ time\_elapsed

- Node cut
  - estimation of # cut tree nodes, by pow(branching factor, # unassigned VAR)
- Time\_elapsed
  - Real time elapsed during the algorithm
- Since I thought time elapsed may not be ~ node popped, the two measurement is taken at the same time

#### **Experiment Designs**

- EXP1: Compare **performance of different heuristic combination** in 6\*6 board with 18 variables
  - 100 random generated test cases corresponding to each n, m, # variables
- EXP2: Compare **growth of statistics** with all hyper params ON **respect to different board size** / # **variable**

#### **Experiment Results**

#### 1. EXP1 - Combinations of Heuristics(ALL-, and indivisual)

test data = testcase\_6\_6\_18\_100.txt generated randomly
TLE means time limit exceeds with time limit set to 2 seconds
In all, if DEG+MRV is both used, the heuristic sort consider MRV first

ALGO/(avg)	Node Popped	Node Pushed	Node Cut	Time Elapsed	TLE
Without Forward	TLE	TLE	TLE	TLE	All
MRV	42.03	247.48	890175.08	0.17	2
Degree	135.85	320.17	1242165.37	0.26	5
LCV	-	-	-	-	All
CUTA	-	-	-	-	All
ALL - MRV	141.26	326.71	861950.91	0.2375	5
ALL - Degree	44.29	251.23	836149.90	0.15	1
ALL - LCV	59.07	265.1	825385.13	0.157	1
ALL -CUTA	66.81	272.96	828476.58	0.18	2
ALL	58.05	264.3	825352.79	0.162	1

The experiment result shows that

- 1. Without Forward Checking => Doomed to TLE
- 2. Need at least one "variable choosing heuristic" (MRV or degree)
- 3. However Degree does not sync with MRV well(by node popped, ALL-degree < ALL)
  - 4. MRV better than degree with ALL- test and Individual test
  - 5. CUTA is actually a better supporting feature than LCV
- 6. Also, I would like to say CSP problems solutions are not easy to be compare, since it is extremely task/test cases dependent!

#### 2. EXP2 - #Variable (single test case for each)

BOARD/VAR/Popped			30	50
6x6	19(~0.1sec)	TLE	NOCASE	
10x10	21(0.4sec)	31(0.85sec)	~51(2sec)	
15x15	21(0.97)	31(2sec)	~51(5.48sec)	

- REALLY surprisingly, node popped ~ #VAR and is the same number with randomly generated test case!!
- And since the processing of node in my algorithm is  $O(n^2)$ , the time elapsed values' relation is no surprise
- I would guess that there is a threshold of ratio of #VAR/SIZE(GRID) that the problem become unsolvable in practical time.

## **Remaining Questions and Future Work**

- 1. Find out the "critical ratio" in this task
- 2. More experiment on various test cases
- 3. But I think solving CSP problems in this way is essentially Backtracking Search + Heuristic + Cutting Techniques, spending too much time would be a waste of time, since the result is not generalizable in the big picture :(

## Code

#### 1. LAB2-1.py

```
#!/usr/bin/env python
# coding: utf-8
# In[1]:
import os
import numpy as np
from copy import deepcopy
from time import time
from colored import fg, bg, attr
# In[2]:
# macro
UNKNOWN = -1
CONSTRAINT = -2
ASSIGNED = 1
NOMINE = 0
MINE = 1
FAIL_MSG = "leave reached but WA"
# In[3]:
#here stores hyper params
TIMELIMIT = 3 #second
FORWARD = True
# in which order should we explore variables
```

```
# MRV, domain smaller
# DEG, vertex that affect more points
MRV = True
DEG = True
# limitation added if assign this value to the variable
LCV = True
GLOBALH = False
# If a variable can not be assign, do not need to try sidlings
CUTA = True
# In[4]:
#board related
#board size
n = 0
m = \emptyset
#number of mines
n mine = 0
#maps
C = list() #constraint value
A = list() #ans
# dx, dy can use for loop 3*3 - 0.0
# In[5]:
def inrange(i, j):
    global n, m
    \#if(((i >= 0) \text{ and } (i < n) \text{ and } (j >= 0) \text{ and } (j < m))):
    # print(i, j)
    return ((i \ge 0) \text{ and } (i < n) \text{ and } (j \ge 0) \text{ and } (j < m))
def printA(A):
    global n, m
```

```
for i in range(n):
       for j in range(m):
           print(str(A[i][j]), end = " ")
       print()
# In[25]:
#input the problem
# 6 6 10 -1 -1 -1 1 1 -1 -1 3 -1 -1 -1 0 2 3 -1 3 3 2 -1 -1 2 -1 -
1 -1 -1 2 2 3 -1 3 -1 1 -1 -1 -1 1
test data = [
   "4 4 5 2 -1 -1 2 -1 3 3 -1 2 2 2 1 -1 -1 -1 0",
   "6 6 10 -1 -1 -1 1 1 -1 -1 3 -1 -1 -1 0 2 3 -1 3 3 2 -1 -1 2 -
1 -1 -1 -1 2 2 3 -1 3 -1 1 -1 -1 -1 1",
   "6 6 10 -1 -1 -1 1 1 1 3 4 -1 2 -1 -1 2 -1 -1 -1 -1 -1 -1 2
2 -1 2 1 2 -1 -1 1 -1 1 -1 1 0 -1".
   "6 6 10 -1 -1 -1 -1 -1 -1 -1 2 2 2 3 -1 -1 2 0 0 2 -1 -1 2 0 0
2 -1 -1 3 2 2 2 -1 -1 -1 -1 -1 -1 -1 ",
   "6 6 10 -1 1 -1 1 1 -1 2 2 3 -1 -1 1 -1 5 -1 5 -1 5 -1 5 -1 5 -1
-1 -1 -1 2 -1 -1 3 -1 -1 -1 1 1 -1 0",
   0 -1 2 -1 -1 1 1 1 1 1 1 -1 -1 -1 1 2 -1 3 2 -1 4 -1 -1 -1 1 -1
-1 -1 -1 -1 4 -1 5 -1 -1 2 3 -1 -1 -1 2 -1 -1 -1 2 -1 1 1 -1 2 1 3
-1 5 2 0 -1 0 -1 -1 1 2 -1 -1 2 1 -1 0 -1 1 1 1 -1 2 2 -1 -1 0",
"10 10 24 -1 1 -1 2 -1 2 -1 2 2 1 0 1 -1 3 -1 -1 -1 4 -1 -1 1 1
2 -1 -1 -1 -1 -1 2 -1 1 -1 4 4 3 2 -1 -1 -1 0 -1 4 -1 -1 -1 1 -1 0
1 4 -1 3 1 -1 -1 2 1 2 -1 3 -1 -1 0 -1 2 -1 1 1 -1 2 1 -1 0"
1
# In[7]:
class Node:
   def __init__(self, remain=None, UB=None, LB=None, VAR=None,
DOM=None):
```

```
#2D list
        self.remain = None
        self.TYPE = None
        self.VAL = None
        self.DOM = None
   # forward calculations
   # will calclulate UpperBound and LowerBound and change Domain
   def forward domain(self):
        newDOM = [[[] for j in range(m)] for i in range(n)]
        takemin = [[False for j in range(m)] for i in range(n)]
        takemax = [[False for j in range(m)] for i in range(n)]
        cnt = 0
        for x in range(n):
            for y in range(m):
                if(self.TYPE[x][y] == UNKNOWN):
                    cnt += 1
                if(self.TYPE[x][y] == CONSTRAINT):
                    lb = 0
                    rb = 0
                    for dx in range(-1, 2, 1):
                        for dy in range(-1, 2, 1):
                            nx, ny = x + dx, y + dy
                            if((dx == 0 and dy == 0) or not
inrange(nx,ny)):
                                continue
                            if (self.TYPE[nx][ny] == UNKNOWN):
                                 if(len(self.DOM[nx][ny]) == 0):
                                    #print("should not print this")
                                    return False
                                 lb += min(self.DOM[nx][ny])
                                 rb += max(self.DOM[nx][ny])
                            if (self.TYPE[nx][ny] == ASSIGNED):
                                lb += self.VAL[nx][ny]
                                 rb += self.VAL[nx][ny]
                    if(lb > C[x][y] or rb < C[x][y]):
                        \#print("bound error@" + str(x) + " " +
str(y))
                        #printA(self.TYPE)
```

```
#printA(self.VAL)
                        #print(C[x][y], lb, rb)
                         return False
                    if(lb == C[x][y]):
                        for dx in range(-1, 2, 1):
                             for dy in range(-1, 2, 1):
                                 nx, ny = x + dx, y + dy
                                 if((dx == 0 and dy == 0) or not
inrange(nx,ny)):
                                     continue
                                 if(self.TYPE[nx][ny] == UNKNOWN):
                                     takemin[nx][ny] = True
                    if(rb == C[x][y]):
                         for dx in range(-1, 2, 1):
                             for dy in range(-1, 2, 1):
                                 nx, ny = x + dx, y + dy
                                 if((dx == 0 and dy == 0) or not
inrange(nx,ny)):
                                     continue
                                 if (self.TYPE[nx][ny] == UNKNOWN):
                                     takemax[nx][ny] = True
        for i in range(n):
            for j in range(m):
                if(self.TYPE[i][j] == UNKNOWN and
len(self.DOM[i][j]) == 2):
                    if(takemin[i][j] and takemax[i][j]):
                         return False
                    elif(takemin[i][j]):
                         self.DOM[i][j] = [min(self.DOM[i][j])]
                    elif(takemax[i][j]):
                         self.DOM[i][j] = [max(self.DOM[i][j])]
                    else:
                        pass
        if(self.remain > cnt or self.remain < 0):</pre>
            return False
        return True
   # use UB-LB or can use DOM len
```

```
def calc LCV(self, x, y):
        ret = 2
        for dx in range(-2, 3, 1):
            for dy in range(-2, 3, 1):
                nx, ny = x + dx, y + dy
                if((not (dx == 0 and dy == 0)) and inrange(nx,ny)
and self.TYPE[nx][ny] == UNKNOWN):
                    ret = min(ret, len(self.DOM[nx][ny]))
        return ret
   # return - size of domain, because we want heuristic to be
bigger => better
    def calc_MRV(self, x, y):
        return -len(self.DOM[x][y])
   #how many (valuabe) constraint are besides it
    def calc_DEG(self, x, y):
        ret = 0
        for dx in range(-1, 2, 1):
            for dy in range(-1, 2, 1):
                nx, ny = x + dx, y + dy
                if((not (dx == 0 and dy == 0)) and inrange(nx,ny)
and self.TYPE[nx][ny] == CONSTRAINT):
                    ret += 1
        return ret
    def check_AC(self):
        if(self.remain != 0): # bug, mistype == 0
            return False
        for i in range(n):
            for j in range(m):
                if(self.TYPE[i][j] == UNKNOWN):
                    return False
                if(self.TYPE[i][j] == CONSTRAINT):
                    cnt = 0
                    for dx in range(-1, 2, 1):
                        for dy in range(-1, 2, 1):
                            nx, ny = i + dx, j + dy
```

```
if((not (dx == 0 and dy == 0)) and
inrange(nx,ny) and self.TYPE[nx][ny] == ASSIGNED):
                                cnt += self.VAL[nx][ny]
                    if cnt != C[i][j]:
                        return False
        return True
    # return a Node with value updated after assign
    def assign(self, xy, val):
        x, y = xy
        ret = deepcopy(self)
        ret.remain -= val
        ret.TYPE[x][y] = ASSIGNED
        ret.VAL[x][y] = val
        return ret
# In[8]:
def solve(id = 0, input_tc=None):
    global n, m, n_mine, C, A
    # input
    if id == -1:
        all_input = list(map(int,input_tc.strip().split()))
    else:
        all_input = list(map(int,test_data[id].strip().split()))
    #apply input to variables
    n, m, n_mine = all_input[:3]
    flat_constraint = all_input[3:]
    assert(len(flat constraint) == n*m)
    #print(n,m, len(flat_constraint))
    C = np.asarray([ [ flat_constraint[i*n+j] for j in range(m)]
for i in range(n)])
    A = np.asarray([[ -1 if (C[i][j] == -1) else -2 for j in
range(m)] for i in range(n)])
    #empty stack, init statistics
```

```
node popped = 0
    node pushed = 0
   node cut = 0
    start t = time()
   time elasped = 0
    fail leaf = 0
    solution = None
    stack = list()
    init_node = Node()
    init_node.remain = n_mine
    init_node.TYPE = [[ UNKNOWN if (C[i][j] == -1) else CONSTRAINT
for j in range(m)] for i in range(n)]
    init_node.VAL = [[ None for j in range(m)] for i in range(n)]
    init_node.DOM = [[[MINE, NOMINE] for j in range(m)] for i in
range(n)]
    if(FORWARD and not init_node.forward_domain()):
        return None
    stack.append(init_node)
    node pushed += 1
   while(len(stack) != 0):
        cur = stack[-1]
        stack.pop(-1)
        node_popped += 1
        # debug msg
        if(node_popped % 100 == 0):
            #print("Node pushed", node_pushed)
            #print("Node popped", node_popped)
            #printA(cur.VAL)
            time_passed = time() - start_t
            if( time_passed > TIMELIMIT):
                print("TLE with time limit {}".format(TIMELIMIT))
                break
        ## add variable todo
        todo = []
```

```
for i in range(n):
            for j in range(m):
                if(cur.TYPE[i][j] == UNKNOWN):
                    mrv = cur.calc MRV(i, j) if MRV else 0
                    deg = cur.calc_DEG(i, j) if DEG else 0
                    todo.append((mrv, deg, (i,j)))
        # done assignment
        if(len(todo) == 0):
            if(not cur.check_AC()):
                print(FAIL_MSG)
                fail leaf += 1
                continue
            else:
                solution = cur
                break
        # Start Assignments by heuristic, first MVC, then DEG
        #todo.sort(reverse=True)
        todo.sort(reverse=False)
        #False with MRV DEG is guicker =>
        #desireto too see negative MRV nigger first and degree
bigger first
        topush = []
        FAILA = False
        for mcv_h, deg_h, (nx, ny) in todo:
            # LCV heuristic
            # the one with greater dimension of freedom explore
first
            nxt = []
            for val in cur.DOM[nx][ny]: # 0, 1
                nxti = cur.assign((nx, ny), val)
                flag = nxti.forward_domain()
                if(FORWARD and not flag):
                    node cut += 1*pow(2, len(todo)-1)
                    continue
                if(LCV):
                     h = nxti.calc_LCV(nx, ny) # constant of
25cells
```

```
elif(GLOBALH):
                     h = int((val == MINE and len(todo)/2 <
cur.remain) or (val == NOMINE and len(todo)/2 >= cur.remain) )
                else :
                    h = 0
                node pushed += 1
                nxt.append((nxti, h))
            if(CUTA):
                if(len(nxt) == 0):
                    FAILA = True
                    #printA(cur.DOM)
                    #print(nx, ny)
                    break
            #nxt.sort(key=lambda x :x[1], reverse=True) # try
smaller LSV, earlier pop
            nxt.sort(key=lambda x :x[1], reverse=False) # bigger
LCV, later insertion, earlier exlporation
            for nxtnode, h_ in nxt:
                topush.append(nxtnode)
        if(CUTA and FAILA):
            node pushed -= len(topush)
            node\_cut += len(topush)*pow(2, len(todo)-1)
            continue
        else:
            stack.extend(topush)
  #end of CSP solver
   end_t = time()
   time_elasped = end_t - start_t
   #print(solution.VAR)
   #if(time elasped >= TIMELIMIT):
   # return None, 1000, 1000, 0, TIMELIMIT
    return solution, node_pushed, node_popped, node_cut,
time_elasped
```

```
def print statistics (ANS, node pushed, node popped, node cut,
time_elasped):
    global n, m,A, C
    print("Node pushed", node_pushed)
    print("Node popped", node_popped)
    print("time elasped", time_elasped)
    print("Node cut", node_cut)
    printA(C)
    print()
    if(time_elasped < TIMELIMIT):</pre>
        # combine rule and result
        final board = [
             [ str(C[i][j]) if A[i][j]==-2 else ".x"[ANS.VAL[i][j]]
for j in range(m)] for i in range(n)
        1
        # print with color
        for i in range(n):
            for j in range(m):
                print("%s"%(fg(1)) if A[i][j] != -2 else "",
final_board[i][j], "%s"%(attr(0))if A[i][j] != -2 else "", end=' ')
            print()
# In[10]:
solution, node_pushed, node_popped, node_cut, time_elasped =
solve(3)
print_statistics(solution, node_pushed, node_popped, node_cut,
time elasped)
```

# In[9]:

```
# In[11]:
tests = [
    [6, 6, 10, 100],
    [6, 6, 20, 100],
    [6, 6, 30, 100],
    [10, 10, 40, 100],
   [10, 10, 50, 100],
1
def get_file_name(wrapper):
    n, m, v, tcn = wrapper
    return "testcase_{}_{}_{}_{}.txt".format(n,m,v,tcn),
"stat_{}_{}_{}.txt".format(n,m,v,tcn)
# In[12]:
#get file name(tests[0])
# In[13]:
def exp(wrapper):
    n, m, v, tcn = wrapper
    inf, outf = get_file_name(wrapper)
    attr = ["popped", "pushed", "cut", "time_elasped"]
    stat = {}
    for s in attr:
        stat[s] = []
    with open(inf, "r") as fo:
        tcs = fo.readlines()
        #print(tcs[0])
        for i in range(tcn):
            solution, node_pushed, node_popped, node_cut,
time_elasped = solve(-1, tcs[i])
```

```
stat["pushed"].append(node pushed)
            stat["popped"].append(node_popped)
            stat["cut"].append(node cut)
            stat["time elasped"].append(time elasped)
            #print_statistics(solution, node_pushed, node_popped,
time elasped)
    for s in attr:
        stat[s].sort
   with open(outf, "w") as fo:
        for s in attr:
            fo.write("Max_{}: {}\n".format(s, sum(stat[s])/tcn))
            fo.write("MID_{{}: {}\n".format(s, stat[s][tcn//2]))
            fo.write("AVG_{\}: {\}\n".format(s, stat[s][-1]))
            print("AVG_{\}: {\}".format(s, sum(stat[s])/tcn))
            print("MID_{{}: {}".format(s, stat[s][tcn//2]))
            print("MAX_{}: {}".format(s, stat[s][-1]))
# In[14]:
#exp(tests[0])
# In[15]:
#for test in tests:
# exp(test)
# In[20]:
#here stores hyper params
TIMELIMIT = 3 #second
FORWARD = True
# in which order should we explore variables
```

```
# MRV, domain smaller
# DEG, vertex that affect more points
MRV = 1
DEG = 0
# limitation added if assign this value to the variable
LCV = 0
GLOBALH = 0
# If a variable can not be assign, do not need to try sidlings
CUTA = 0
# In[21]:
exp([6,6,18,100])
# In[26]:
solve(5)
# In[27]:
solve(-1, "15 15 19 0 0 1 -1 1 0 0 0 0 0 0 0 1 1 1 0 0 1 1 1 0 0 0
0 0 0 0 0 1 1 -1 0 0 1 -1 -1 1 0 0 0 -1 1 1 0 0 0 1 1 2 2 2 1 0 1
1 2 -1 1 1 1 0 1 -1 1 0 0 0 0 1 -1 2 1 1 -1 -1 -1 1 1 1 1 -1 1 0 1
1 1 0 0 3 3 1 0 1 1 2 -1 2 1 1 0 -1 0 0 -1 -1 1 0 1 -1 2 1 2 -1 1
0 0 0 0 2 -1 1 0 1 1 2 1 2 1 1 0 0 0 0 -1 0 0 0 0 0 1 -1 1 0 1 1 1
1 1 0 0 0 0 0 1 2 2 1 0 1 -1 2 -1 -1 0 0 0 0 0 1 -1 1 0 0 1 1 2 -1
2 0 -1 0 0 0 1 1 1 0 0 0 0 1 1 1")
# In[28]:
```

# In[30]:

# In[31]:

# In[32]:

solve(-1, "10 10 18 1 -1 1 0 1 1 1 0 0 -1 2 2 1 0 2 -1 2 0 1 1 -1 -1 1 1 3 -1 -1 2 3 -1 1 1 1 -1 2 -1 -1 -1 3 -1 -1 0 1 1 -1 2 3 -1 3 2 0 0 0 0 1 -1 1 -1 1 -1 0 0 0 -1 1 2 2 2 3 3 1 -1 0 0 -1 1 -1 2 -1 -1 -1 2 0 0 0 0 -1 2 4 4 3 -1 2 0 0 0 0 1 -1 -1 1")

# In[33]:

# In[ ]:

#### 2. testcase\_generator.py

```
# author = yt lin
# usage = python3 testcase generator.py < 6 6 10 100
import os
import numpy as np
import random
## hyper params
n = 6
m = 6
nv = 10
n mine = 0
## use input
n, m, nv, N = list(map(int,input().strip().split()))
## init all positions
all coordinate = []
for i in range(n):
    for j in range(m):
        all coordinate.append((i,j))
```

```
def inrange(i, j):
    return i \ge 0 and i < n and j \ge 0 and j < m
def gen(n, m, nv):
    n mine = 0
    ## pick variable positions
    POSV = random.sample(all coordinate, nv)
    MARK = [[ 0 for j in range(m)] for i in range(n)]
    for pos in POSV:
        MARK[pos[0]][pos[1]] = 1
    # variables
    A = [[random.choice([0,1]) if MARK[i][j] else -1 for j in
range(m)] for i in range(n)]
    for i in range(n):
        for j in range(m):
            n_{mine} += int(A[i][j] == 1)
    # constraints init
    B = [[0 \text{ for } i \text{ in } range(m)]] for i in range(n)]
    # calc constraints
    for i in range(n):
        for j in range(m):
            if A[i][j] == -1:
                 for di in range(-1, 2, 1):
                     for dj in range(-1, 2, 1):
                         if(not (di == dj and di == 0) and
inrange(i+di, j+dj)):
                             B[i][j] += int(A[i+di][j+dj] == 1)
    TC = [[B[i][j] \text{ if } A[i][j] == -1 \text{ else } -1 \text{ for } j \text{ in } range(m)]
for i in range(n)]
    SAMPLE\_ANS = [[B[i][j] if A[i][j] == -1 else "ox"[A[i][j]]]
for j in range(m)] for i in range(n)]
    return n, m, n mine, TC, SAMPLE ANS
def create_tc_file(n, m, nvar, ntc):
    with open("testcase_" + str(n) + "_" + str(m) + "_" +
str(nvar) + "_" + str(ntc) + ".txt", "w") as fo:
        for i in range(ntc):
            n, m, n_mine, TC, SAMPLE_ANS = gen(m, m, nvar)
```

```
TC_str = str(n) + " " + str(m) + " " + str(n_mine)
for i in range(n):
    for j in range(m):
        TC_str += " " + str(TC[i][j])
fo.write(TC_str)
fo.write("\n")
```

create\_tc\_file(n, m, nv, N)