

A lowpass digital filter's specifications are given by: $\omega_p = 0.4$, $\omega_s = 0.25$, $\omega_p = 50$, $\omega_s = 0.25$

```
% Digital Filter Specifications:
wp = 0.25*pi; % digital Passband freq
ws = 0.4*pi; % digital Stopband freq
Ap = 0.25; % Passband ripple in dB
As = 50; % Stopband attenuation in dB

Td = 1;
```

a. Using an impulse invariance approach, find $H(z)$ that satisfies the above specifications with monotonic passband and stopband.

Design the analog lowpass filter $H_c(s)$.

```
[N,Omegac] = buttord(wp,ws,Ap,As,'s')
```

```
N = 16
Omegac = 0.8769
```

```
[C,D] = butter(N,Omegac,'s')
```

```
C = 1×17
    0         0         0         0         0         0         0         0 ...
D = 1×17
    1.0000    8.9466   40.0208   118.5757   260.0165   446.8788   622.0719   714.9710 ...
```

We obtain the desired digital filter $H(z) = B(z)/A(z)$ using the coefficients in the arrays B and A.

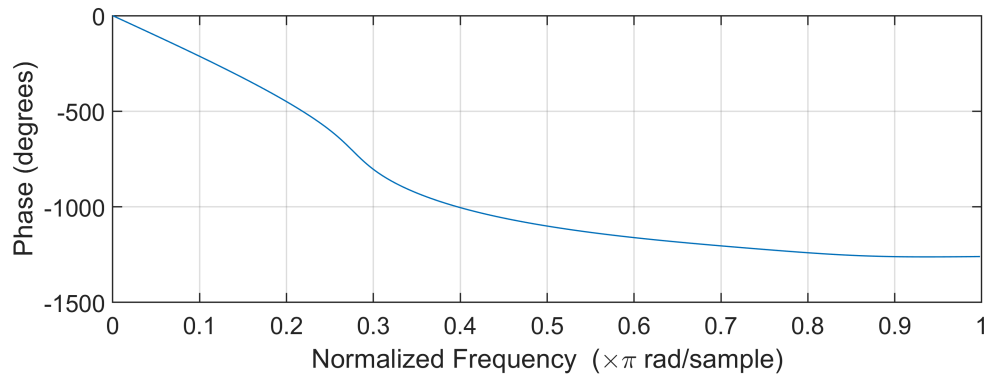
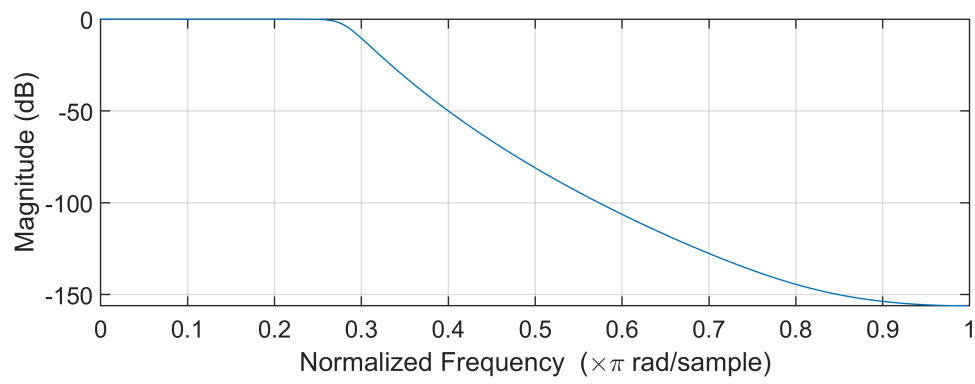
```
[B,A] =impinvar(C,D,1/Td)
```

Warning: The output is not correct/robust. Coeffs of $B(s)/A(s)$ are real, but $B(z)/A(z)$ has complex coeffs.
Probable cause is rooting of high-order repeated poles in $A(s)$.

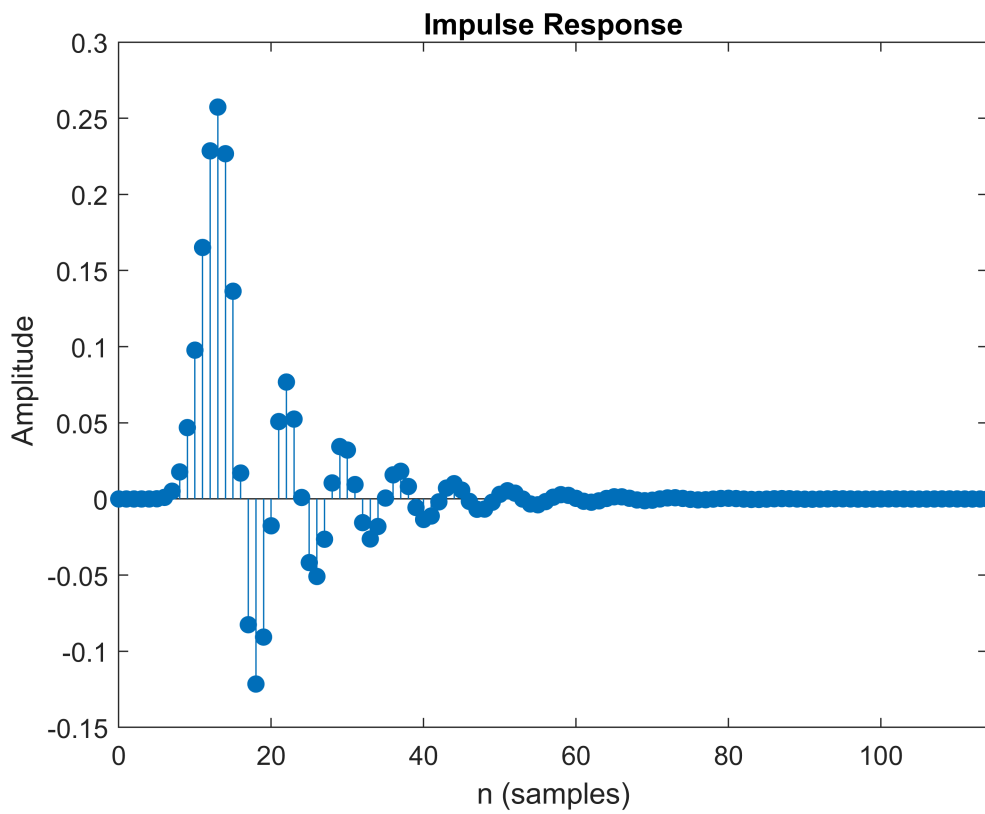
```
B = 1×17
10-3 ×
   -0.0000    0.0001   -0.0004    0.0011    0.0059    0.0743    0.2731    0.4704 ...
A = 1×17
    1.0000   -7.4315   27.1507  -64.1755  109.2091 -141.2721  143.2320 -115.7981 ...
```

b. Provide design plots in the form of log-magnitude, phase, group-delay, and impulse responses.

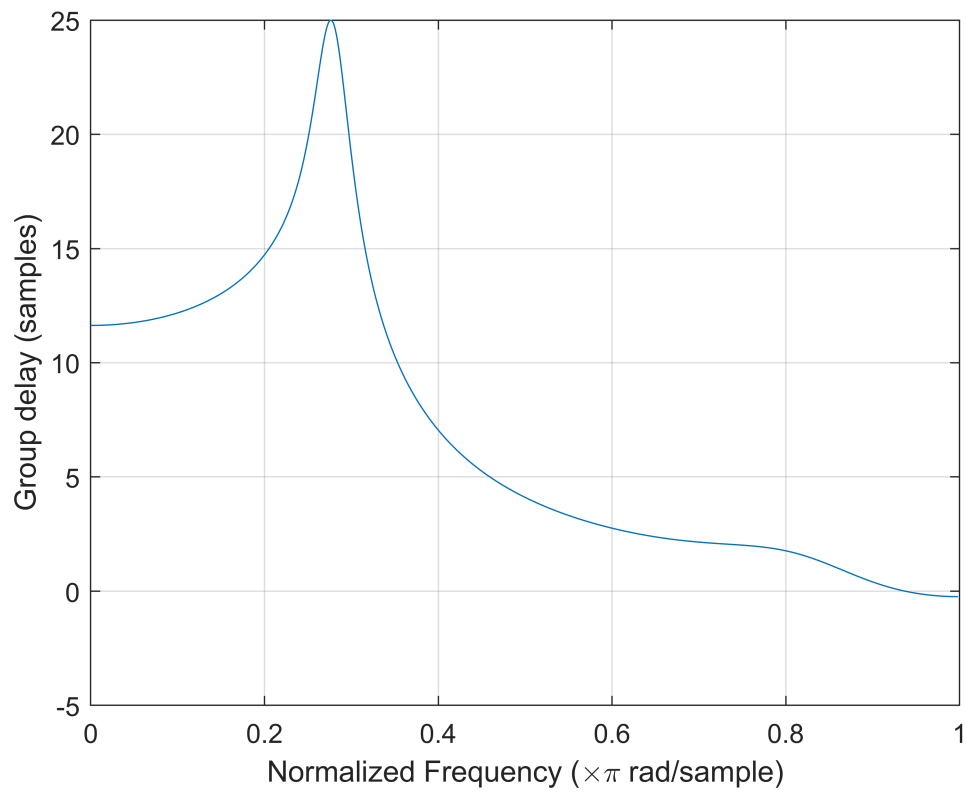
```
freqz(B,A)
```



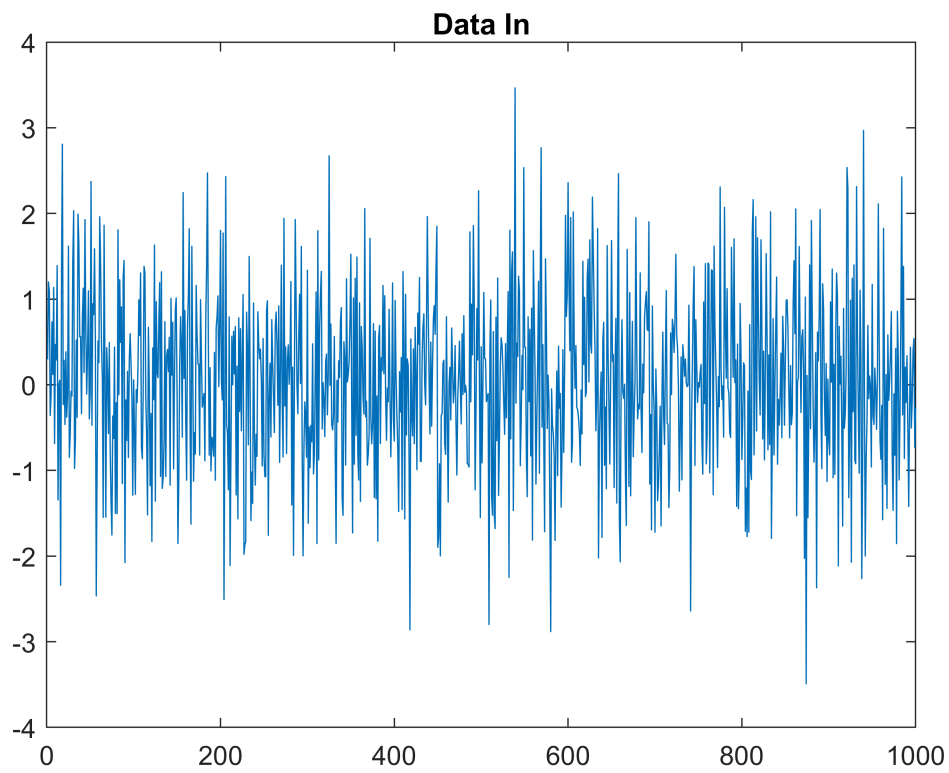
```
impz(B,A)
```



grpdelay(B,A)



```
dataIn = randn(1000,1);  
dataOut = filter(B,A,dataIn);  
plot(dataIn)  
title('Data In')
```



```
plot(dataOut)  
title("Filtered Data")
```

