

23. An LTI system is described by the difference equation

$$y[n] = bx[n] + 0.8y[n - 1] - 0.81y[n - 2].$$

```
% Defining the LTI System
```

```
a = [1, -0.8, 0.81];  
b = [1];
```

(d) Determine analytically the response $y[n]$ to the input $x[n] = 2 \cos(\pi n/3 + 45)$.

(e) Using MATLAB compute the steady-state response to $x[n]$ above.

```
n=[0:100];
```

```
% Defining x[n]
```

```
x = 2 * cos((1/3)*pi*n + 45*(pi/180));
```

```
% Calculating the Steady State Response
```

```
y = filter(b,a,x);
```

```
figure();
```

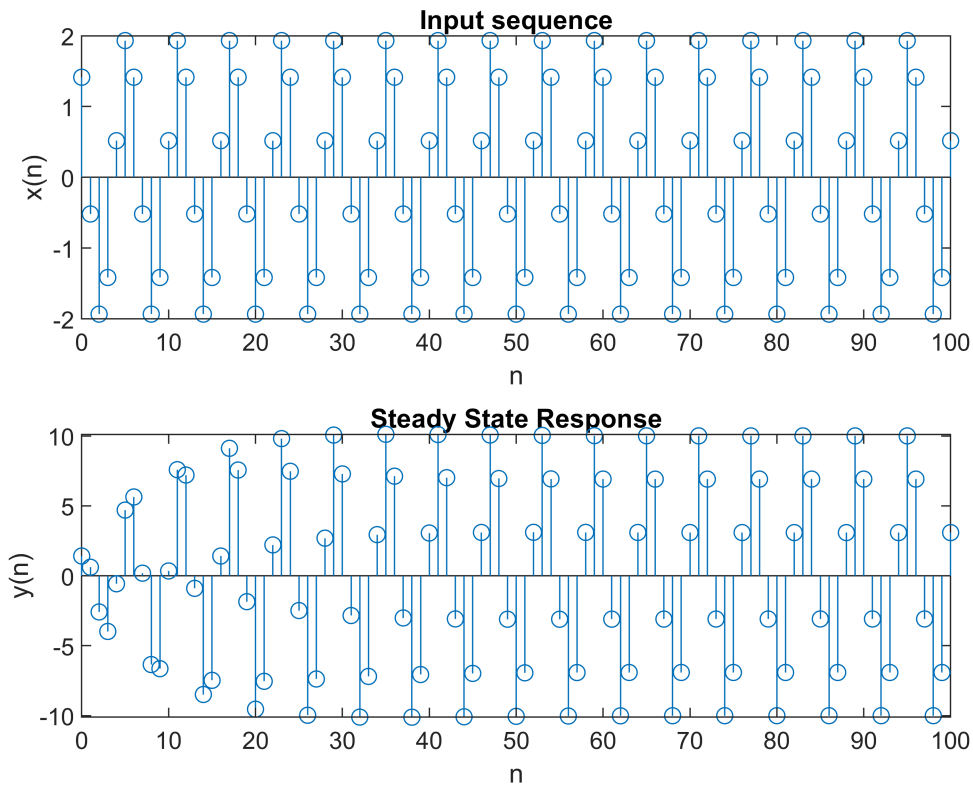
```
% Plotting the Input and Steady State Response
```

```
subplot(2,1,1); stem(n,x);
```

```
xlabel('n'); ylabel('x(n)'); title('Input sequence')
```

```
subplot(2,1,2); stem(n,y);
```

```
xlabel('n'); ylabel('y(n)'); title('Steady State Response')
```



31. A multiband ideal bandpass filter is given by

$$H(e^{j\omega}) = \begin{cases} e^{-j\omega n_d}, & \frac{\pi}{8} < |\omega| < \frac{2\pi}{8} \\ 0.5e^{-j\omega n_d}, & \frac{5\pi}{8} < |\omega| < \frac{7\pi}{8} \\ 0, & \text{otherwise} \end{cases}$$

(c) From the above truncated impulse response, compute and plot the magnitude response of the filter using MATLAB and compare it with the ideal filter response.

```
b1 = [0,1]; a1 = [1];
b2 = [0,0.5]; a2 = [1];

n=-100:1:100;

% Frequency Response

[h1,w1] = freqz(b1,a1,201,'whole');
[h2,w2] = freqz(b2,a2,201,'whole');

% Truncation based on limits

h00 = zeros(13,1);
```

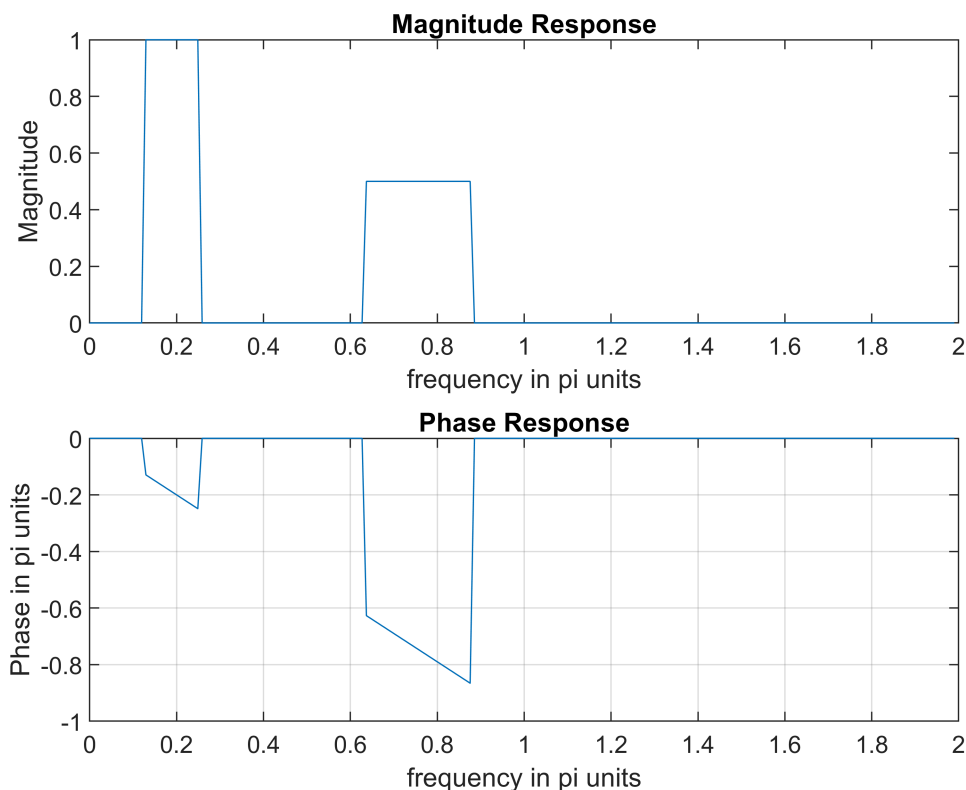
```

h11 = h1(14:26);
h110 = zeros(38,1);
h22 = h2(64:88);
h220 = zeros(200-88,1);

% Final Response
h = cat(1,h00,h11,h110,h22,h220);

% Magnitude and Phase Plot
magH = abs(h); phaH = angle(h);
figure()
subplot(2,1,1);plot(w1/pi,magH);
xlabel('frequency in pi units'); ylabel('Magnitude');
title('Magnitude Response')
subplot(2,1,2);plot(w1/pi,phaH/pi);grid
xlabel('frequency in pi units'); ylabel('Phase in pi units');
title('Phase Response')

```



46. An LTI system is described by the difference equation $y[n] = x[n] - x[n - 4] - 0.81y[n - 2] - 0.6561y[n - 4]$.

```

a = [1,0,0.81,0,0.6561];
b = [1,0,0,0,-1];

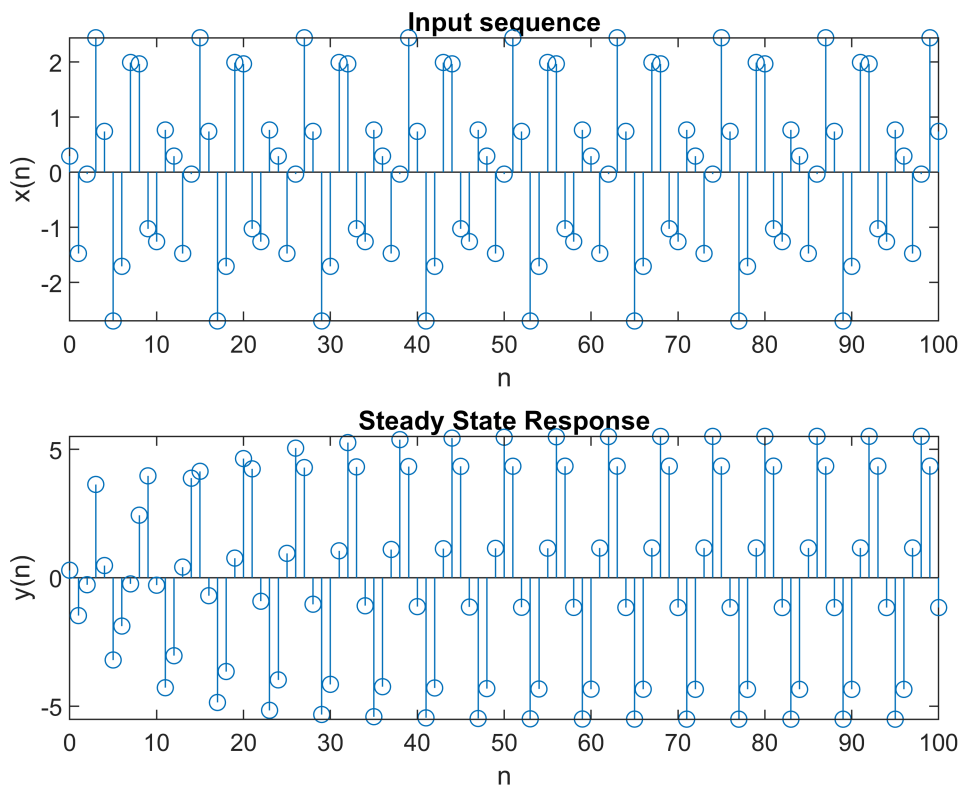
```

(d) Determine analytically the response $y[n]$ to the input $x[n] = 2 \cos(0.5\pi n + 60) + \sin(\pi n / 3 - 45)$.

(e) Using MATLAB compute the steady-state response to $x[n]$ above and verify your

result.

```
n=[0:100];  
  
% Defining x[n]  
x = 2 * cos((1/2)*pi*n + 60*(pi/180)) + sin(pi*n/3 - 45*pi/180);  
% Calculating the Steady State Response  
y = filter(b,a,x);  
  
figure();  
% Plotting the Input and Steady State Response  
subplot(2,1,1); stem(n,x);  
xlabel('n'); ylabel('x(n)'); title('Input sequence')  
subplot(2,1,2); stem(n,y);  
xlabel('n'); ylabel('y(n)'); title('Steady State Response')
```



54. A multiband ideal bandstop filter is given by

$$H(e^{j\omega}) = \begin{cases} e^{-j\omega n_d}, & 0 < |\omega| < \frac{\pi}{8} \\ \frac{2}{3}e^{-j\omega n_d}, & \frac{3\pi}{8} < |\omega| < \frac{5\pi}{8} \\ \frac{1}{3}e^{-j\omega n_d}, & \frac{7\pi}{8} < |\omega| < \pi \\ 0, & \text{otherwise} \end{cases}$$

- Determine the impulse response of the filter.
- Graph the impulse response for $n_d = 0$ for $-200 \leq n \leq 200$.
- From the above truncated impulse response, compute and plot the magnitude response of the filter using MATLAB and compare it with the ideal filter response.

```
clear;
w1=linspace(0,pi/8,401);
w2=linspace(3*pi/8,5*pi/8,401);
w3=linspace(7*pi/8,pi,401);
k=0;
% Using synthesis equation we find the impulse response
for n=-200:1:200
    k=k+1;
    h1(k)=(1/(2*pi))*trapz(w1,exp(1i*w1*n));
    h2(k)=(1/(2*pi))*(2/3)*trapz(w2,exp(1i*w2*n));
    h3(k)=(1/(2*pi))*(1/3)*trapz(w3,exp(1i*w3*n));
end

% Complete Impulse Response is given by
h=h1+h2+h3;
n=-200:1:200;
figure()
subplot(311)
stem(n,h)
```

Warning: Using only the real component of complex data.

```
title('Impulse response for nd=0')
xlabel('n')
ylabel('h(n)')

%to find magnitude and phase of truncated impulse response h(n)
w=0:(pi/1000):pi;
[H,w]=freqz(h,1,w);
subplot(312)
plot(w,abs(H))
title('Magnitude response')
xlabel('w')
ylabel('|H(w)|')
subplot(313)
```

```

plot(w,angle(H))
title('Phase response')
xlabel('w')
ylabel('<H(w)')

```

